# Hypothesis-Driven Specialization-based Analysis of Gene Expression Association Rules

by

Dharmesh Thakkar

A Thesis

Submitted to the Faculty

of the

#### WORCESTER POLYTECHNIC INSTITUTE

In partial fulfillment of the requirements for the

Degree of Master of Science

in

Computer Science

by

May 2007

APPROVED:	
Professor Carolina Ruiz, Thesis Advisor	
Professor Elizabeth Ryder, Co-Advisor	
Professor Murali Mani, Thesis Reader	
Professor Michael Gennert, Head of Departr	nent

#### Abstract

During the development of many diseases such as cancer and diabetes, the pattern of gene expression within certain cells changes. A vital part of understanding these diseases will come from understanding the factors governing gene expression. This thesis work focused on mining association rules in the context of gene expression. We designed and developed a tool that enables domain experts to interactively analyze association rules that describe relationships in genetic data. Association rules in their native form deal with sets of items and associations among them. But domain experts hypothesize that additional factors like relative ordering and spacing of these items are important aspects governing gene expression.

We proposed hypothesis-based specializations of association rules to identify biologically significant relationships. Our approach also alleviates the limitations inherent in the conventional association rule mining that uses a support-confidence framework by providing filtering and reordering of association rules according to other measures of interestingness in addition to support and confidence. Our tool supports visualization of genetic data in the context of a rule, which facilitates rule analysis and rule specialization. The improvement in different measures of interestingness (e.g., confidence, lift, and p-value) enabled by our approach is used to evaluate the significance of the specialized rules.

#### Acknowledgments

I would like to express my gratitude to my advisor, Prof. Carolina Ruiz for her guidance and support throughout the course of this thesis which has helped me grow and be better prepared for the professional challenges I would encounter. But for her constant encouragement, patience and availability it would have been impossible for me to go on. I would like to thank my co-advisor Prof. Liz Ryder who did not get bugged by all the biology questions I had but instead went to great lengths to ensure that even a computer science student could understand them. Their (both my advisor's and co-advisor's) enthusiasm in the 8 a.m. meetings forced upon them by my schedule always kept me motivated. I thank Prof. Murali Mani for agreeing to be my reader and also for reading the thesis at such short notice. Last but not the least, I would like to thank my family, that is, my folks back home in India and my wife Vandna. Their confidence in me inspires me to scale new heights and they form a strong support system whenever I need it.

# Contents

1	Intr	roduction	1
	1.1	Biological Motivation	2
	1.2	Computational Motivation	4
	1.3	Problem Statement	7
	1.4	Summary of the contributions of this work	11
<b>2</b>	Bac	kground	12
	2.1	Gene Expression	12
	2.2	Association rules	13
	2.3	Prior work at WPI	14
3	Dat	a: Motif Elicitation and Sequence Annotation	16
	3.1	Data Collection	16
	3.2	Motif Elicitation	20
	3.3	Sequence annotation	21
	3.4	ARFF Generation	25
4	Dat	a Visualization and Mining	26
	4.1	Mining Process	26
	4.2	Visualization and Specialization Module	28

		4.2.1	Analysis Frame	28
		4.2.2	Inter-Motif Distance Plot	31
		4.2.3	Sequence Plot	35
		4.2.4	Order of occurrence of motifs	39
		4.2.5	Adding Rules Manually	41
		4.2.6	Hybrid Rule	42
		4.2.7	Aliases	45
5	Sys	tem A	rchitecture	48
	5.1	Comp	onent Interaction	48
	5.2	Syster	n Design	51
	5.3	Imple	mentation Details	54
6	Exp	erime	ntal Evaluation	55
	6.1	Exper	imental Protocol and Parameters to be measured	55
	6.2	Exper	imental Results and Analysis	57
		6.2.1	Order of motif occurrence specialization of Rules (6.1) and (6.2)	) 59
		6.2.2	Inter-motif distance specialization of Rules (6.3) and (6.4) $$	63
		6.2.3	Distance from SoT specialization of Rules (6.5) and (6.6)	67
		6.2.4	Experimental results	72
7	Cor	nclusio	ns and Future Work	<b>7</b> 5
$\mathbf{A}$	San	nple A	RFF File	80
В	Per	l scrip	t to convert probability matrix to log odds matrix.	116
$\mathbf{C}$	Use	r Guid	le	119
	C.1	Analy	sis Frame	119

C.2	Inter-N	Motif Distance Plot
	C.2.1	Sequence Plot
	C.2.2	Order of occurrence of motifs
	C.2.3	Add Rule
	C.2.4	Hybrid Rule
	C.2.5	Aliases
	C.2.6	Delete Rule
	C.2.7	Export Rules
	C.2.8	Import Rules
	C.2.9	Hide Current Column
	C.2.10	Sorting in Analysis Frame

# List of Figures

1.1	Structure of a DNA molecule and corresponding linear simplification.	2
1.2	Central dogma of biology: DNA $\rightarrow$ RNA $\rightarrow$ Protein	3
1.3	Hypothetical dataset of 15 genes and 10 motifs	7
1.4	Syntax description of order of occurrence based specialized rules	10
3.1	List of high density cell types with the associated identified genes	
	that are expressed in the worm's adult life stage	18
3.2	Overview of the process from data collection to the ARFF generation.	19
3.3	Sample promoter sequence from the data collected	20
3.4	Sample motif represented as a position probability matrix	22
3.5	MAST annotated sequence sample	23
3.6	Sample motif represented as a Log-odds matrix	24
4.1	Sample Analysis Frame	29
4.2	A sample gene expression information file	29
4.3	Sample Inter-Motif Distance Frame	32
4.4	Visualize change command from the inter-motif distance plot	34
4.5	A row representing the addition of a specialization to the Analysis	
	Frame	35
4.6	Sample Sequence Plot Frame.	36

4.7	Visualize change command from the sequence plot	37
4.8	Analysis Frame with two distance from SoT based specializations	38
4.9	Inter-Motif Distance Plot for Motifs M5 and M6	39
4.10	Sequence Plot for Motifs M5 and M6. Observe that in the rule sup-	
	porting sequences (upper part) a red-dot is usually followed by a blue	
	dot scanning the gene sequence from right end (SoT) to left	40
4.11	Add Rule option in the Analysis Frame provides for free text option	
	to add rules	41
4.12	Grammar to parse rules	43
4.13	Grammar based parsing helps identify user errors in typing the rule	44
4.14	Hybrid rules help specify multiple constraints (based on different hy-	
	potheses) within a single specialization	45
4.15	Aliases let user define specializations with inter-related constraints	46
5.1	Process depicting the flow of data (interactions) between the WPI-	
	Weka system and the VSM	49
5.2	CSV interface to transfer rule sets between WPI-Weka system and	
	VSM	50
5.3	VSM System Design	52
5.4	Hierarchical internal data structure - Hash of hashes	53
6.1	Experimental Setup	56
6.2	List of motifs from the base rules under consideration along with their	
	consensus sequences	58
6.3	Inter-motif distance plot for the base rule M6 && M52 $\Rightarrow$ expr=HSN.	60
6.3 6.4	Inter-motif distance plot for the base rule $M6 \&\& M52 \Rightarrow expr=HSN$ .  Analysis frame providing a comparison of the interestingness of the	60

6.5	Inter-motif distance plot for the base rule $M54 \&\& M80 \Rightarrow \exp r = HSN$ .	62
6.6	Analysis frame providing a comparison of the interestingness of the	
	specialized rule, Rule (6.8), with the base rule, Rule (6.2). $\dots$	62
6.7	Inter-motif distance plot for the base rule M47 && M53 $\Rightarrow$ expr=ADL.	64
6.8	Analysis frame providing a comparison of the interestingness of the	
	specialized rule, Rule (6.9), with the base rule, Rule (6.3). $\dots$	64
6.9	Inter-motif distance plot for the base rule $M77\ [rp0-rp1]\ M48[rp2-rp3]$	
	$\Rightarrow expr=ALM.$	66
6.10	Analysis frame providing a comparison of the interestingness of the	
	specialized rule, Rule (6.10), with the base rule, Rule (6.4)	67
6.11	Sequence plot for the base rule $M69 \Rightarrow expr=HSN.$	69
6.12	Analysis frame providing a comparison of the interestingness of the	
	specialized rule, Rule (6.11), with the base rule, Rule (6.5)	70
6.13	Sequence plot for the base rule $M6 \Rightarrow expr=HSN$	71
6.14	Analysis frame providing a comparison of the interestingness of the	
	specialized rule, Rule (6.12), with the base rule, Rule (6.6)	71
6.15	Statistical measures over training data	73
6.16	Specializations and various measures of interestingness evaluated over	
	the <b>test data</b>	74
C.1	Sample Analysis Frame	120
C.2	Sample Inter-Motif Distance Frame - The numeric pointers refer to	
	the enumerated text explaining Inter-Motif Distance Plot	.22
C.3	Inter-Motif Distance Frame depicting an inter-motif range of 0-500	
	bp for Motif pair M10 and M16	ւ25
C.4	Visualize command invoked inter-Motif distance plot displaying data	
	in the context of the specialised rule M10 (0-500) M16 $\Rightarrow$ expr = ALM.1	126

C.5	A row representing the addition of a specialization to the Analysis
	Frame
C.6	Multiple pairwise inter-motif distance plots for a base rule with more
	than two motifs. For instance the base rule for this plot is M10 &&
	M12 && M16 $\Rightarrow$ expr = ALM
C.7	Sample Sequence Plot Frame - The numeric pointers refer to the
	enumerated text explaining the Sequence Plot
C.8	Sequence Plot Frame depicting a distance of $500~\mathrm{bp}$ from SoT for M10.132
C.9	Analysis Frame depicting a couple of newly added distance from SoT
	based specializations
C.10	Inter-Motif Distance Plot for Motifs M5 and M6. Observe the lack of
	magenta (dark) dots in the right half of the frame
C.11	Sequence Plot for Motifs M5 and M6. Observe that in the rule sup-
	porting sequences (upper part) a red dot is usually followed by a blue
	dot scanning the gene sequence from right end (SoT) to left 135
C.12	Add Rule option in the Analysis Frame provides for free text option
	to add rules
C.13	Grammar based parsing helps identify user-errors in typing the rule $137$
C.14	Hybrid rules help specify multiple constraints (based on different hy-
	pothesis) within a single specialization
C.15	Aliases let user define specializations with inter-related constraints 140

# Chapter 1

# Introduction

During the development of many diseases such as cancer and diabetes, the pattern of gene expression within certain cells changes. A vital part of understanding these diseases will come from understanding the factors governing gene expression. This thesis work focused on association rules mined in the context of gene expression. We designed and developed a tool that enables domain experts to interactively analyze association rules that describe relationships in genetic data. Association rules in their native form deal with sets of items and associations among them. But domain experts hypothesize that additional factors like relative ordering and spacing of these items are important aspects governing gene expression.

We proposed hypothesis-based specializations of association rules to identify biologically significant relationships. Our approach also alleviates the limitations inherent in the conventional association rule mining that uses a support-confidence framework by providing filtering and reordering of association rules according to other measures of interestingness in addition to support and confidence. Our tool supports visualization of genetic data in the context of a rule, which facilitates rule analysis and rule specialization. The improvement in different measures of interestingness (e.g., confidence, lift, and p-value) enabled by our approach is used to evaluate the significance of the specialized rules.

### 1.1 Biological Motivation

One of the central questions in modern biology today is what controls gene expression. Deoxyribonucleic acid (DNA) is a complex molecule which encodes genetic information unique to an organism. Every cell in an organism contains the same set of instructions encoded in the DNA, and this information is arranged into regions called genes. Still, a brain cell is very different from a heart cell and performs an

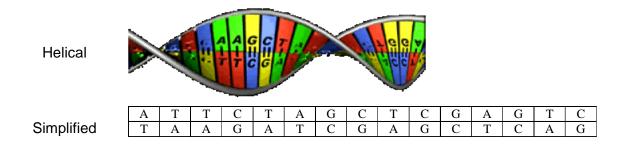


Figure 1.1: Structure of a DNA molecule and corresponding linear simplification.

Gene expression is the process by which the information encoded in a gene is copied (transcribed) into RNA which may further be translated into a protein. The promoter region of a gene is the portion of the DNA sequence upstream of the gene. The process of making an RNA copy of the relevant portion of the genes DNA is called transcription, and the point where the promoter region ends and the gene begins is called the start of transcription (SoT). RNA is chemically slightly different from DNA, but contains the relevant information for a particular gene, and it can move to a part of the cell where that information can be translated into protein.

Proteins are the basic chemicals that make up the structure of cells and direct their activities. Each protein has a specific function that is determined by the blueprint stored in DNA, specifically the gene.

Deeper understanding of gene expression would not only help in the functional classification of genes but would also be instrumental for developing cures to diseases where the gene expression patterns within a cell change. With technological advances more genetic data is being collected today than ever before. This is creating an increasing gap between the rate of data collection and the rate of data analysis.

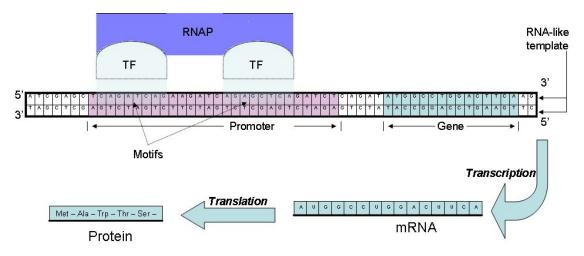


Figure 1.2: Central dogma of biology: DNA→RNA→Protein. During transcription, RNA polymerase (RNAP) copies DNA to RNA using the template strand. The RNA transcribed is identical to the RNA-like strand except that U's are substituted for T's. A transcription protein (TP) binds to either enhance or repress transcription of a gene by assisting or blocking RNAP binding. During translation, the RNA encodes proteins.

Domain experts attribute the selective activation of genes in any cell to:

- 1. The presence of a particular set of proteins controlling transcription called Transcription Proteins (TP) in a given cell.
- 2. The presence of certain repeated sequences of DNA (motifs) in the promoter

region, which is the section of the DNA sequence upstream of the gene. These motifs are bound by transcription proteins during transcription.

Throughout this thesis we focus on identifying control patterns, defined in terms of the presence of a motif, to model gene expression. Motifs control gene expression, as they are putative binding sites which bind the transcriptional proteins. Expression of each gene may require the presence of a combination of motifs. Domain experts also hypothesize that inter-motif distances and order of occurrence of motifs in the promoter region are additional factors that control this regulatory interplay of motifs and thus also influence gene expression.

### 1.2 Computational Motivation

Computational processes to identify and shortlist interesting relationships (associations) between motifs and gene expression, which could then be analyzed biologically in detail, are gaining importance, as these would help reduce the growing gap between data collection and analysis. Associations that are statistically significant may yield biologically valid connections between associated variables. Association rule mining, introduced in [AIS93], provides a useful mechanism for discovering relationships between variables in a dataset. Relationships are represented in an if-then format with statistical measures to indicate the strength of the relationship. Association rules are of the form:

 $Antecedent \Rightarrow Consequent[Support = S, Confidence = C]$  such that  $S, C \in [0, 1]$ 

A rule of this form in a market basket analysis of customer purchases could be:

$$Bread, Butter \Rightarrow Eggs[Support = 0.45, Confidence = 0.80]$$
 (1.1)

The **Support** of the rule is the probability of finding both the antecedent (the *if* part) and consequent (the *then* part) of the rule in a data instance (i.e., a row in the dataset). For instance, in rule 1.1, the Support of the rule signifies that 45% of the customers in the database bought all three items, that is, Bread, Butter, and Eggs.

The **Confidence** of the rule is the conditional probability of the consequent given the antecedent. Again, in the context of sample rule 1.1, the Confidence of the rule signifies that 80% of the customers who bought Bread and Butter bought Eggs as well.

Previous work at WPI ([MPPT01], [BLT02], [BFG<sup>+</sup>03], [Ice03], [IRR03]) has provided the foundation for gene expression association rule mining. [BLT02] focused on creating a computational biology tool, CAGE, that built association rule based models to predict gene expression. [BFG<sup>+</sup>03] implemented a more elaborate methodology for discovering potential motifs and concentrated on improving the predictive accuracy of the models. However, none of these systems provide an interface that enhances the ability of a domain expert to analyze the resulting rules. This work focuses on facilitating visualization of the mined rules with respect to location of motifs on promoter regions of interest, since this is essential to interpretation of the rules by domain experts.

Besides setting the base methodology, [MPPT01] also attempted to address the biological hypothesis - "Does distance between motifs matter?". [Ice03], [IRR03]

extended the idea and focused on incorporating distance information in the mining process itself. But they do not provide a way to verify alternative biological hypotheses. Consider the following scenario, which brings forth one of the shortcomings of incorporating more constraints in the mining process, and suggests why it might not be the best approach in an environment where we intend to perform exploratory analysis. A batch of gene sequences was mined for gene expression related association rules with a support and confidence of 0.5 or greater. If the user now wants to find out rules with support and confidence of 0.4 or greater, the only way to achieve this is to mine again, which is a very time consuming process. From an exploratory analysis perspective, it is imperative to facilitate visualization of data in the context of a rule in real-time. So one could mine for association rules with lowest bounds of support and confidence. Then this work lets the user visualize the data which may allow the user to quickly perceive a pattern in the data, suggesting a specialization that would greatly increase the confidence (or other measures of interestingness). This work also computes the different measures of interestingness of the specialization over the training data for each such identified specialization and thereby provides an instantaneous estimate on the statistical strength of the rule. This work provides the ability to test a few biological hypotheses, as such a provision is instrumental in the development of an effective data-mining algorithm for gene expression.

Moreover all the above mentioned efforts were based on the basic supportconfidence framework of rule generation. Several other measures of interestingness have been proposed to measure the relative importance of association rules (e.g., gain [Mor98], chi-squared value [Alv03], and lift [BMS97]). But there is no one good measure that is applicable to all domains. This work provides a way to analyze important rules according to several measures and thereby observe the applicability of each of these measures to this problem domain.

[PR05] introduced an algorithm to mine expressive positional relationships from complex sequential data. We adapted the data to define motifs as events and then utilized this algorithmic approach to mine for statistically significant association rules with positional relationships. This work also provides a facility to visualize genetic data in the context of such positional specializations.

### 1.3 Problem Statement

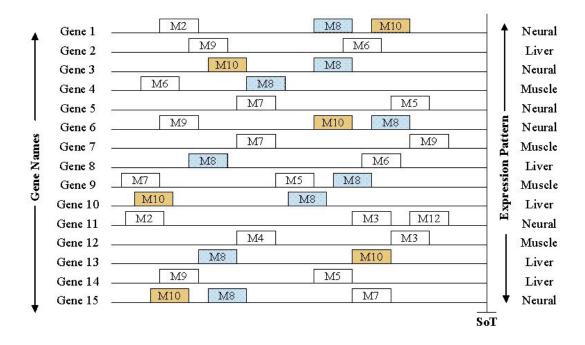


Figure 1.3: Hypothetical dataset of 15 genes and 10 motifs.

We designed and developed a tool to facilitate the post-mining analysis of rules for verifying biological hypotheses and also to aid the visualization of the rules generated. The tool has been integrated with the WPI-Weka system, a local version of the open source data mining tool. Mining of a hypothetical gene expression dataset as shown in Figure 1.3 would produce association rules of the form:

M8 && M10 
$$\Rightarrow$$
 neural [Support = 0.27, Confidence = 0.67] (1.2)

which states that the presence of Motif M8 and Motif M10 in the promoter region of a gene implies that there is a 67% likelihood that the gene is expressed in cells of type neural. Also, 27% of our data instances contain M8, M10 and are expressed in cells of type neural. The support and confidence statistics are computed from the hypothetical data in Figure 1.3.

This work will provide the necessary functionality for a domain expert to interactively analyze genetic data in the context of the following biological hypotheses:

1. Inter-motif distance is important in characterizing gene expression. DNA consists of linearly linked nucleotides. Subsequences of the DNA sequence, like a gene or a promoter region, can be represented for example as ATTTCC-CGGT. By representing DNA as a sequence, the number of bases could be used to imply a notion of distance between motifs. In the sample sequence ATTCGGGGGGTAT we could say that the Motif ATT is at a distance of 7 bases from the Motif TAT. Now consider the following specialized form of rule 1.3:

$$M8 (0-250) M10 \Rightarrow neural [Support = 0.20, Confidence = 1.0]$$
 (1.3)

That is, the presence of Motif M8 within a distance of 250 bases from Motif M10 implies that the gene is likely to be expressed in cells of type neural. Again the support and confidence statistics are computed from the hypothetical data in Figure 1.3. Notice the change in the statistical measures with respect to (1.2). Every time a rule is specialized, it may be applicable to fewer data-

instances (genes) in the dataset. This explains the reduction in the Support value. The increase in Confidence is indicative of the classification accuracy. A value of 1.0 signifies that of the data instances (genes) to which the rule could be applied (i.e., those that match the antecedent of the rule), the expression type predicted by the consequent of the rule is correct(i.e., it matches the known expression type of the data instance.

2. Distance of a motif from the start of transcription (SoT) affects gene expression.

Since many of the known putative regulatory elements are found close to the Start of Transcription (SoT), we want to find out if the distance of the occurrence of a motif to the start of transcription has any effect on gene expression. This work facilitates visualization of gene sequences, along with the motifs involved and the start of transcription, in the context of the generic rule of the form (1.2). This enables the user to form and visualize specializations of the form:

M8 (0-500) SoT && M10 
$$\Rightarrow$$
 neural [ $Supp = 0.13, Conf = 1.0$ ] (1.4)

where the presence of Motif M8 within a distance of 500 bases or less from the Start of Transcription (SoT) and presence of motif M10 anywhere in the promoter region imply that the gene is likely to be expressed in cells of type neural. Again the support and confidence statistics are computed from the hypothetical data in Figure 1.3. Observe again the alteration in support and confidence as compared to (1.2).

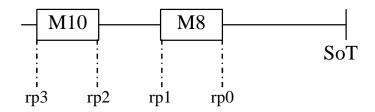


Figure 1.4: Syntax description of order of occurrence based specialized rules.

3. The order of occurrence of motifs affects gene expression. Knowledge of gene expression regulation is not complete. Domain experts hypothesize that the order of occurrence of motifs in the regulatory regions could also affect gene expression. This work provides the facility to visualize the gene sequences in the context of specializations of the following form which were either mined directly using the approach in [PR05] or visually observed and enhanced as a part of the exploratory analysis.

M8 (rp0-rp1) M10 (rp2-rp3) 
$$\Rightarrow$$
 neural [Supp = 0.20, Conf = 0.75] (1.5)

This rule states that the presence of an occurrence of Motif M8 in the promoter region of a gene in between an occurrence of Motif M10 and the Start of Transcription (SoT) implies that the gene is likely to be expressed in cells of type neural. rp in the rule above refers to the relative position of the motif with respect to the Start of Transcription (Figure 1.4). Each motif has a begin point and an end point and hence requires both a begin index and an end index to capture the relative positioning of the motifs on the gene sequence. The support and confidence statistics are computed from the hypothetical data in Figure 1.3. Here again we notice that the specialization process produces an improvement in the confidence of the rule.

For each of the form of specializations discussed above, different measures of interestingness are computed to estimate if the hypothesis-based specialized rule better explains the underlying regulatory mechanism as compared to its generic counterpart.

## 1.4 Summary of the contributions of this work

This work focused on the development of a computational tool for exploratory specialization of association rules predicting gene expression in the context of the above mentioned biological hypotheses. Also it provides for filtering/sorting association rules based on measures of interestingness beyond the conventional measures of confidence and support.

The main contributions of this work are a framework and a tool that can:

- 1. Facilitate exploratory rule analysis (specialization) by providing a user-interface for rule visualization in the context of different biological hypotheses.
- 2. Select and present rules according to different interestingness metrics.
- 3. Test hypotheses relating the order of motifs, inter-motif distance and the distance of motifs from the start of transcription to gene expression control.
- 4. Provide updated genetic data, an important resource for any further research in the domain.
- 5. Be integrated seamlessly with the WPI Weka system. That is, gene expression association rules mined with the WPI-Weka system can be visualized and specialized using this work. Also, a model consisting of interesting rules and their specializations could be used by the WPI Weka to measure the model's classification accuracy over novel data.

# Chapter 2

# Background

### 2.1 Gene Expression

Simply put, a gene is a segment of DNA and is the physical and functional unit of heredity information. Gene expression is the process of using the information encoded in a gene to manufacture protein in the cell. Each cell of an organism, for instance neural or muscle, has the same DNA, but still performs completely different functions. This phenomenon is often referred to as the "The central dogma of biology" and is described in more detail in Section 1.1.

With technical advances in all fields, more and more data is being generated today than ever before, and the field of gene expression is no exception. Thus there is an imperative need for methods to analyze data at an equivalent rate.

The focus of this work was to design and develop a tool that helps a biologist to visualize genetic data to explore interesting regulatory patterns governing gene expression. As discussed in Section 1.1, motifs (repeating DNA segments) control gene expression, as they are putative binding sites which bind the transcriptional proteins. Hence, it is central to our work to determine groups of motifs that are likely

to be real binding sites collectively controlling expression, which in turn is contingent upon the quality of the data used to discover (elicit) motifs. This was one of the prime reasons why we decided to collect data from scratch. We compiled a database using the Wormbase database [Wor] and RSA database [RSA] that consists of 164 genes, from nine different cell types with at least 30 genes known to be expressed in each cell type. Furthermore, we conducted a pilot experiment that elicited motifs from these sequences using both MEME [MEM] and GIBBS [JAC95] to observe the cost vs quality analysis of both algorithms. Since there was no perceived benefit in terms of quality of motifs we opted for lower cost (less time-consuming) elicitation algorithm MotifSampler (GIBBS). The data collection as well as the motif elicitation process is covered in detail in Section 3.

#### 2.2 Association rules

Association rules were introduced in [AIS93]. Consider a database (D) in relational format where each record (data instance) consists of n boolean attributes. Association rules model relationships of the form: presence of a set A ( $A \subset D$ ) implies the presence of the another set C ( $C \subset D$ ) where the two sets A and C are disjoint (i.e.,  $A \cap C = \emptyset$ ). The most common statistical measures to estimate the strength of the rule are support and confidence and these have been covered in depth in Section 1.2.

Apriori is the traditional algorithm used to mine association rules [AS94]. Even a small dataset could yield a large number of rules and so the support-confidence framework is utilized to identify relationships which are statistically interesting. It follows an inductive approach to find *itemsets* (i.e., sets of items belonging to the data) that occur together *frequently*, within a dataset. An itemset is frequent if the

support of the itemset is greater than the minimum support, a threshold provided as an input parameter. The apriori principle basically states that an itemset is frequent only if all its subsets are frequent and this principle is utilized in the inductive approach to search for frequent itemset.

Even with the popularity of the support-confidence framework in the association rule mining literature there is no one good measure that is applicable to all domains. Several other measures of interestingness have been proposed to measure the relative importance of association rules. The lift value of an association rule is another measure to try to quantify the interestingness of the rule. It is defined as the ratio of the confidence of the rule and the support of the consequent of the rule. The p-value of the rule is the probability that the correlation between the antecedent and the consequent is due to chance by using the chi-square test.

### 2.3 Prior work at WPI

As discussed in Section 1.2 previous work at WPI has provided the foundation for gene expression association rule mining. AprioriSetsAndSequences [PR05] introduced an algorithm to mine expressive temporal relationships from complex sequential data in addition to the regular association rule mining and provides enhanced pruning mechanism, which is of significant value especially when mining large sequence databases. It takes preprocessed sequences, that is sequences of events (e.g., the price of a company's stock recorded every hour or the repeating patterns in a gene sequence) as input with a minimum support and confidence threshold and produces association rules with temporal relationships between events. [MPPT01] attempted to address the biological hypothesis - "Inter-motif distance influences gene expression". [Ice03], [IRR03] extended the idea and focused on incorporating

distance information in the mining process itself. Integrating this work with the WPI-Weka system has been a shared goal with [Rudss], a work in progress.

Chapter 3

Data: Motif Elicitation and

Sequence Annotation

The data in the domain of interest (genetics) is sequential in nature. In this section

we present the process followed in order to transform sequential genetic data to a

relational format. That is, a format similar to the conventional database format that

enables the use of existing data-mining algorithms to identify patterns of interest

from a gene regulation perspective.

3.1 **Data Collection** 

It cannot be stressed enough that no matter how good a mining algorithm may be,

the information retrieved/discovered is only as good as the data. Adhering to this

thought, we found an imperative need to collect genetic data from scratch.

C. elegans was our choice of organism. It is a well-studied organism often used as

a model for genetic research because it is genetically tractable, that is, the entire C.

elegans genome has been sequenced and the expression patterns of many genes are

16

known. More than 60% of human genes have homologs in the *C. elegans* genome. The facts that it is small and easy to culture are some of the secondary reasons why this nematode is popular amongst biologists.

As a first step we identified cell types to include in our study. The primary intent was to identify cell types in which there were at least 30 genes known to be expressed. We require them to be "high-density" cell types, because the data sample should be large enough to derive statistically significant information. Also, this would provide us with substantial data to break down into a training set and a test set.

We used the WormBase [Wor] database and the RSA Database [RSA] for identifying the cell types based on the conditions delineated above. The next step was to gather the actual data, that is, the promoter regions for each of the 30 or more genes per cell type. This data was downloaded from the sources listed above and manually cross verified using BLAST [BLA]. At the end we were able to identify nine cell types of interest to us, each of which had at least 30 known genes. We created nine batches of promoter sequences, one per cell type (Figure 3.1). These nine batches of gene sequences or promoter subgroups were also the initial input for the data transformation process as depicted in Figure 3.2, which provides the graphical overview of the contents of this chapter. Each subsequent step in the data transformation process corresponds to a subsequent section of this chapter.

Another important decision was with regard to the length of the promoter region for the data collected. Based on expert opinion, the length of promoter region included in the data was 5000 base pairs (bp) upstream (5' to the gene) of the gene. This choice was influenced by the fact that although the regulatory elements critical to gene expression are usually proximal to the initiation site, another type of regulatory elements called enhancers, that may influence expression, can be located

Cell Type	Genes Expressed
ASK	bra-1, cam-1, che-3, daf-11, eat-4, egl-4, gpa-14, gpa-15, gpa-3, ida-1, kin-29, kvs-1, nlp-10, nlp-14, nlp-8, odr-1, opt-3, osm-3, osm-6, osm-9, sra-7, sra-9, srg-2, srg-8, tax-2, tax-4, tax-6, unc-103, zig-4, zig-5
ASE	ceh-23, che-1, che-3, cog-1, csk-1, egl-2, egl-4, gcy-5, gcy-6, gcy-7, gpa-3, hen-1, kvs-1, lim-6, mps-1, ncs-1, nlp-14, nlp-3, nlp-7, npr-1, osm-3, osm-6, osm-9, src-1, tax-2, tax-4, tax-6, unc-5, nlp-1, flp-6
ASI	bra-1, cam-1, ceh-23, che-3, daf-11, daf-28, daf-7, gpa-1, gpa-10, gpa-14, gpa-3, gpa-4, gpa-5, gpa-6, gpc-1, ida-1, kal-1, kin-29, nlp-1, nlp-14, nlp-18, nlp-24, nlp-27, nlp-5, nlp-6, nlp-7, nlp-9, odr-1, opt-3, osm-10, osm-3, osm-6, osm-9, sra-6, srd-1, str-2, str-3, tax-2, tax-4, tax-6, ttx-3, unc-3, zig-3, zig-4
CAN	acy-1, acy-2, cam-1, ced-10, ceh-10, ceh-23, ceh-43, cle-1, ctl-2, dbl-1, ggr-2, goa-1, gpa-10, gpa-14, gpb-2, gsa-1, hbl-1, jkk-1, jnk-1, kal-1, lin-14, mig-2, nlp-10, nlp-15, pak-1, unc-129, unc-73, unc-76, vab-8, cat-1
HSN	cam-1, cdh-3, cha-1, clh-3, ctl-2, eat-16, egl-21, egl-3, egl-43, egl-44, egl-5, flt-1, gar-2, ggr-2, glr-5, goa-1, gpb-2, grd-6, gsa-1, ham-2, hbl-1, ida-1, inx-4, jkk-1, jnk-1, kal-1, mab-23, mec-6, mig-1, mig-2, nhx-5, nid-1, nlp-15, nlp-3, sax-3, sem-4, syg-1, tph-1, unc-103, unc-14, unc-17, unc-40, unc-51, unc-53, unc-73, unc-76, unc-8, unc-86, cat-1, lin-4
PHA	bra-1, ceh-14, che-2, che-3, egl-43, gcy-12, goa-1, gpa-1, gpa-13, gpa-14, gpa-15, gpa-2, gpa-3, ida-1, lin-11, ncs-1, nlp-14, nlp-7, npr-1, ocr-2, osm-10, osm-3, osm-6, osm-9, pkc-1, srg-13, tax-6, unc-103, flp-15, srb-6, tax-2
ADL	cam-1, ceh-23, ceh-32, che-3, cog-1, gpa-1, gpa-11, gpa-15, gpa-3, gpc-1, hlh-2, kvs-1, lin-11, nhr-79, nlp-10, nlp-7, nlp-8, ocr-1, ocr-2, opt-3, osm-3, osm-6, osm-9, qui-1, srb-6, sre-1, sro-1, tax-6, ttx-3, unc-103, ver-2
ASH	cam-1, ceh-23, che-1, che-3, eat-4, egl-3, egl-4, gpa-1, gpa-11, gpa-13, gpa-14, gpa-15, gpa-3, gpc-1, hlh-2, kin-29, kvs-1, mps-1, nhr-79, nlp-15, nlp-3, npr-1, ocr-2, odr-3, opt-3, osm-10, osm-3, osm-6, osm-9, qui-1, sra-6, srb-6, tax-6, unc-42, unc-8
ALM	cam-1, daf-1, deg-3, dyn-1, eat-4, egl-2, egl-21, egl-3, glr-8, goa-1, jkk-1, jnk-1, lin-14, mec-10, mec-2, mec-3, mec-4, mec-6, mec-7, mec-8, mig-2, mps-1, mtd-1, nid-1, pag-3, pat-4, pkc-1, ptl-1, tba-1, tol-1, unc-32, unc-73, unc-86, unc-97

Figure 3.1: List of high density cell types with the associated identified genes that are expressed in the worm's adult life stage.

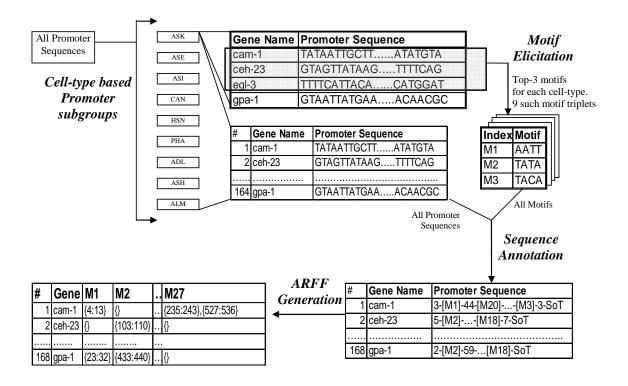


Figure 3.2: Overview of the process from data collection to the ARFF generation. Promoter regions were grouped based on the cell type in which their associated genes were expressed. DNA motifs common to promoters within a group were elicited for each group. All sequences were then annotated with all the elicited motifs. The gene expression information and the annotated sequences, that is, the sequences overlaid with the positional information of each motif, are transformed to ARFF format, Weka's input format.

#### Sample Promoter Sequence in FASTA format

Figure 3.3: Sample promoter sequence from the data collected.

several thousand base-pairs from the gene. In case another gene was found within the 5000 bp upstream sequence of the promoter sequence, the length of the promoter being considered was truncated at the start of this gene.

The data collected consists of 164 promoter sequences and is a valuable resource for future work. The collected sequences were represented in the FASTA format for further processing by motif discovery and annotation tools. A sample sequence is shown in Figure 3.3.

### 3.2 Motif Elicitation

The next step in the data transformation process is motif elicitation (Figure 3.2). A motif is a sequence pattern that occurs repeatedly (ideally at least once per gene) in a group of related promoter sequences. Motif elicitation is the process of discovering significant motifs from a group of sequences. There are several tools available that use different statistical modeling techniques to discover significant motifs. The basic premise governing the elicitation process is that the regulatory controls governing the expression of genes in the cells of the same cell type might be in common to at

least few of these sequences. The idea was to use motif search programs to identify cell type specific motifs. To avoid over fitting we decided to include only 90% of the sequences as input to motif elicitation programs and the remaining 10% of the sequence for testing.

Two different motif elicitation programs (algorithms), MotifSampler [Mot] and MEME [MEM] were used in the preliminary tests on the same dataset. Motif-Sampler is a motif finding algorithm that uses GIBBS sampling [JAC95] to find the position probability matrix that represents the motif. MEME discovers one or more motifs in a collection of sequences by using the technique of expectation maximization [BE94]. Based on the similarity of the outputs from both algorithms and considerably less computational time exhibited by MotifSampler, GIBBS was our choice of algorithm to be used for the motif elicitation stage. It is worth noting, however, that the preliminary tests were in no way a detailed comparative study of the two methods.

Based on the input from the domain expert it was decided to look for motifs of size 8, 10, or 12 base pairs. Thus, motif elicitation was performed by executing MotifSampler individually on each of the nine batches of promoter sequences (Figure 3.2), once for each size. The output of this process was in the form of a set of position probability matrices (Figure 3.4) each representing a motif. For each combination of a size and batch, the three best scoring matrices (motifs) were selected for future use. As a result we ended up with 81 motifs; nine motifs for each cell type.

### 3.3 Sequence annotation

Motifs identified by MotifSampler are in the form of a probability-matrix. The next step was to annotate all promoter sequences with the elicited motifs. Annotation

#### Sample motif represented as a position probability matrix

```
# Width = 8
 Consensus = ATAACTAG
                   С
                             G
                                       Т
        Α
    0.996545
              0.000890
                         0.000840
                                    0.001726
    0.001520
              0.000890
                         0.000840
                                    0.996750
    0.499033
              0.000890
                         0.000840
                                    0.499238
    0.499033
              0.000890
                         0.000840
                                   0.499238
    0.001520
              0.498402
                         0.498352
                                   0.001726
    0.001520
              0.000890
                         0.000840
                                    0.996750
    0.996545
              0.000890
                         0.000840
                                    0.001726
    0.001520
              0.000890
                         0.498352
                                    0.499238
```

Figure 3.4: Sample motif represented as a position probability matrix. The commented row titled width provides the length of the motif. The consensus sequence of the motif is a sample occurrence of the motif built by using the most common base at each position. Each column of the position probability matrix corresponds to the bases A, C, G and T respectively. Each row corresponds to a position of a base within the motif. For instance a position probability matrix for a motif with width 8 would consist of 8 rows. The value at row i column j in the matrix is the probability of finding the base j at position i in the motif.

is the process of finding matches of a given motif(s) in a given set of sequences and also quantifies how good each match is. We used Motif Alignment and Search Tool (MAST) [MAS] for the annotation process. A PERL script (Appendix B) was developed to convert probability-matrices from MotifSampler output to corresponding MAST friendly format(log-odds matrices as shown in Figure 3.6). A master motif file was created which consisted of all 81 identified motifs irrespective of the cell type. A master gene sequences file was created which consisted of promoter sequences for all high-density genes listed in Figure 3.1. The master gene sequences file and the master motif file were fed to MAST as input to annotate all promoter sequences with all elicited motifs. The MAST output file is a HTML file consisting

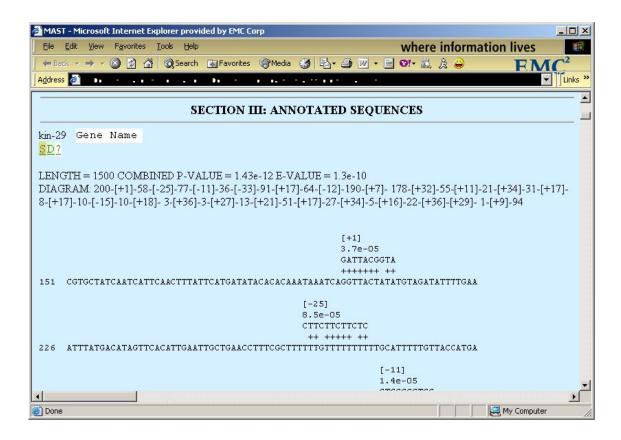


Figure 3.5: MAST annotated sequence sample.

During annotation each supplied sequence is searched for matches with each supplied motif. The four lines above each motif occurrence contain, respectively, the motif number of the occurrence, the position p-value (i.e., a measure of the match quality, lower is better) of the occurrence, the consensus sequence of the motif, and a plus sign ('+') above each letter in the occurrence that has a positive match score to the motif. MAST can automatically generate the reverse complement strand for each supplied sequence and search for motif occurrences on either the given strand or its reverse complement. The ('+') or ('-') sign alongside the motif number is used to distinguish whether the match occurred on the given strand or the reverse complement respectively.

```
Sample motif represented as a log odds matrix
# Width = 8
# Consensus = ATAACTAG
          С
                   G
                          Τ
        -766
                 -757
                         -764
166
-770
        -766
                -757
                         154
66
        -766
                -757
                         54
        -766
                         54
66
                -757
-770
        146
                164
                         -764
-770
        -766
                -757
                         154
166
        -766
                -757
                         -764
-770
        -766
                 164
                         54
```

Figure 3.6: Sample motif represented as a Log-odds matrix. This matrix is a log-odds matrix calculated by taking the log (base 2) of the ratio

p/f at each position in the motif where p is the probability of a particular letter at that position in the motif, and f is the average frequency of that letter in the training set.

of all annotated gene sequences. A relevant section of the output file is shown in Figure 3.5.

### 3.4 ARFF Generation

A Java module was developed to transform the union of annotated promoter sequences from the MAST output and the known gene expression information, that is, all of the cells in which the gene is expressed, to Attribute-Relation File Format (ARFF) format dataset. The ARFF format is a format similar to the relational database format. Each gene occurs as a tuple in the relation. Each motif is an attribute of the gene tuple. A set-value consisting of the known gene expression pattern is also an attribute of the gene. A sample of the same has been included in Appendix A. As mentioned in section 3.2, to avoid mining and exploring relationships that overfit the data, the sequences were divided into a training set (90% of the sequences) and a test set (10% of the sequence). Thus the ARFF generation was performed twice, one to create a training set ARFF file and the other for a test set ARFF file.

# Chapter 4

# Data Visualization and Mining

## 4.1 Mining Process

The sequence annotation process described in Chapter 3, transformed the gene sequences into a relational format. This provides us the ability to utilize algorithms from the WPI-Weka system to discover relationships or patterns that describe gene expression. These relationships are rules like "Genes whose promoter regions contain the motifs M10 and M16 are often expressed in Neural cells". The ability to uncover such relationships in an automated fashion is of prime importance, as they provide the domain experts with a relevant view of the data that demands further exploration.

[Ice03] investigated the problem of incorporating hypothesis based information into the mining process. We instead decided to follow a post mining exploratory approach for hypothesis testing, that is, to specialize (post-process) *interesting* rules produced by conventional association rule mining algorithms. The reasons that influenced this choice were:

1. It is very difficult, if not impossible, to determine in advance the right distance-

related and position-related mining parameters so that the mined rules will capture the desired patterns. This is due to the fact that the appropriate distance and position values vary for each subset of motifs in the context of each cell type under consideration. For instance, the appropriate values for the distance and relative position of motifs M10 and M16 in neural cells might be very different to those in muscle cells. Furthermore, these values might vary in the presence of other motifs. That is, the distance and relative position of motifs M10 and M16 in neural cells might vary even for the same cell type once that say motif M20 is added to the mix. Since mining association rules is expensive in terms of execution time, a trial and error approach in which possible values of the input parameters are guessed would require multiple executions of the mining algorithm, which would be too time consuming. Another alternative is to perform an automatic search for the right values of those parameters within the mining algorithm, but the time complexity of an exhaustive search is exponential in the size of the input data and would make the runtime of the mining algorithm prohibitive. It is unclear that good heuristics to prune the search are possible. Our selected post mining exploratory analysis approach is much faster since it is performed on one rule (i.e., one subset of motifs under one cell type) at a time, and only on such rules that are deemed interesting by the domain expert user.

2. Exploratory analysis often combines visualization with data mining tools that provides a *simple* sequence of steps(work flows) to identify and isolate *relevant* information. *Simplicity* is important because we need to bridge the gap between the domain experts and the tools usage. Equipped with an easy to use tool, the domain experts could utilize their knowledge to analyze and define the data patterns displayed by the tool in an intuitive manner. The tool is

not limiting but instead banks on the experts, and it could easily evolve to accommodate newer hypotheses.

The association rule mining modules ([Sho01] and [PR05]) of the WPI-Weka system [WPI] were used to mine for basic gene expression patterns in the annotated sequences. The visualization system that we develop here facilitates exploratory analysis to specialize these mined patterns. [Rudss] contributions to WPI Weka helped integrate the visualization modules into the WPI Weka in a transparent fashion. The user now has the choice to either save the results of the mining for perusal at a later point in time or could directly invoke the visualization modules from the mining modules.

## 4.2 Visualization and Specialization Module

Some of the prime contributions of this work are the Visualization and Specialization Module (VSM) which is an extension to the WPI Weka system. This module enables visualization of the annotated promoter sequences in the context of a specific rule or a set of motifs. The primary interface of the VSM is the Analysis frame, which is the first screen to be displayed when VSM is invoked is depicted in Figure 4.1. We explain the Analysis frame below.

## 4.2.1 Analysis Frame

The analysis frame is the focal point for using visualization extensions to WPI Weka. The analysis frame loads with two sections, the **Rules** area and the **Commands** area (Figure 4.1). We explain the Rules area below and we explain each of the options in the Commands area in subsequent subsections. The Rules area is used to display base association rules along with the corresponding values for certain

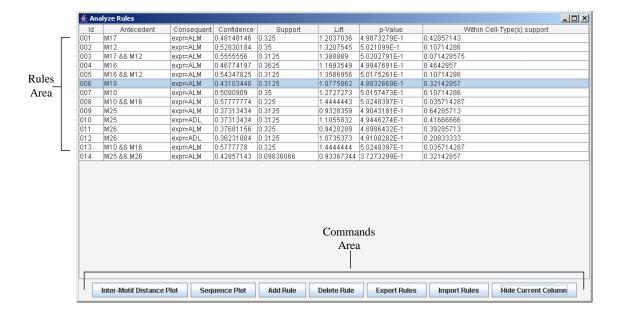


Figure 4.1: Sample Analysis Frame.

Analysis Frame can either be invoked from the mining interface of the WPI-Weka system or could be invoked as a standalone application using an exported set of mined association rules, the associated MAST results (HTML format), and a list of gene names alongside the known expression patterns. A sample of the gene expression information file is presented in Figure 4.2.

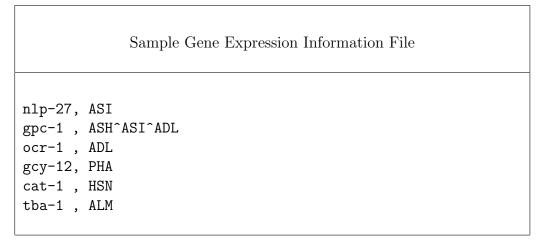


Figure 4.2: A sample gene expression information file.

The file is in CSV (Comma Separated Value) format. First value in each row is the gene name (e.g., nlp-27). The next value contains a set of cell-types the gene is known to be expressed in. Elements of the set are separated using the ^ symbol.

measures of interestingness. The design is extensible; that is, new measures of interest could be added in the future with minimal code changes. In the current state, a Rule tuple consists of the following items:

- Id this is a unique id assigned to the rule. The usability of this field increases once the user starts to generate specializations from the rule, as the Id column helps us trace the history or the specialization path of new rules.
- Antecedent The left-hand side of the rule. It contains the motifs present in the rule.
- Consequent The right-hand side of the rule. It contains the cell-types predicted by the rule.
- Support As discussed in Section 1.2, the support of a rule is the relative frequency with which the antecedent and consequent appear together in the data. That is, P(Antecedent & Consequent).
- Confidence As discussed in Section 1.2, the confidence is the likelihood that the consequent appears in a data instance that contains the antecedent. That is, P(Consequent|Antecedent).
- Lift The lift value of an association rule is another measure to try to quantify the interestingness of the rule. It is defined as the ratio of the confidence of the rule and the support of the consequent of the rule [BMS97]. In other words

$$lift(rule) = p(consequent|antecedent)/p(consequent)$$

• **p-Value** - The p-value of the rule is the probability that the antecedent and the consequent would be as highly correlated as they are, just by chance according

to a Chi square test of independence. We calculate the p-value of an association rule using the approach in [Alv03].

• Within Cell-Type Support - Provides the support of the rule among only those instances of the data that contain the consequent of the rule. This metric is very important in the context of this work because we expect to see different motifs and rules for different cell types, so we are primarily interested in the support of the rule within each cell type.

The Commands area of the Analysis frame provides buttons to perform a range of functions. The following subsections describe each of these functions provided by the visualization extensions via the analysis frame. It is important to note that most of these functions are invoked in the context of a specific rule and so it is necessary to select a rule in the rules area of the analysis frame before invoking a command.

### 4.2.2 Inter-Motif Distance Plot

Selecting a Rule in the rules area and then invoking the inter-motif distance plot via the button with the same label lets a user visualize the data in the context of the rule from an inter-motif distance perspective (Figure 4.3). This action enables a user to perform exploratory analysis in the context of the hypothesis - "Inter-motif distance influences gene expression".

On invoking this command a new frame with the pairwise inter-motif distance plot(s) is displayed. It displays one graph for each pair of motifs in the rule (selected in the Analysis Frame). For the sake of simplicity we start with a rule with only two motifs. We revisit plots originating from rules consisting of more than two motifs later in the section.

Notice that an inter-motif distance plot (Figure 4.3) is sliced into 2 parts by a

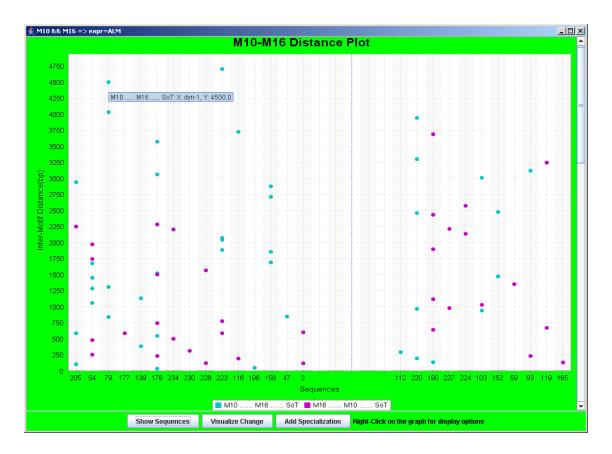


Figure 4.3: Sample Inter-Motif Distance Frame.

Each graph is displayed with the rule used to establish the context as the title of the frame. Each graph displays the pairwise inter-motif distance plots(M10 && M16  $\Rightarrow$  expr=ALM, in this case). Along the x-axis of the plot are the id's of the genes in question and along the y-axis are the inter-motif distances between the pair of motifs. For each pair (a,b) of motifs, inter motif distances of all occurrences of motif a from all occurrences of motif b are plotted. The color of each point is indicative of the order of occurrence of motifs a and b relative to the SoT. In this graph, aqua (light) denotes points in which the occurrence of M16 appears in between the occurrence of M10 and SoT; and magenta (dark) denotes points in which the occurrence of M10 appears in between the occurrence of M16 and SoT. Each graph lists only those genes on the x-axis, that support the antecedent of the rule. That is, genes whose promoter regions contain at least one occurrence of each motif. Genes on the left of the dotted line also support the consequent of the rule.

dotted line. The genes on the left of this dividing line are the ones that support the antecedent and the consequent of the rule and hence support the rule. The ones on the right are the genes that support only the antecedents of the rule. This provides the user with an easy mechanism to discover inter-motif distance based patterns on the left-hand side of the plot that are not as frequent on the right hand side, as this would let us explore specializations with improved classification accuracy(and/or confidence). Once the user has utilized the dotted separation and inter-motif distance plots to define a range of interest, for instance a range of (0-500) between motifs M10 and M16, the user can invoke the "Visualize Change" command to visualize the data in the context of the specialization as depicted in Figure 4.4. Subsequently the specialized rule could be added to the Analysis Frame using the "Add Specialization" command on the inter-motif distance plot. This causes a new entry to be inserted in the Analysis Frame (Figure 4.5) with the following specialization

$$M10(0 - 500)M16 \Rightarrow expr = ALM \tag{4.1}$$

Note that the Id field is auto-generated in a fashion that always lets a user trace back the steps in case we want to later recall which rule was used to derive the specialization.

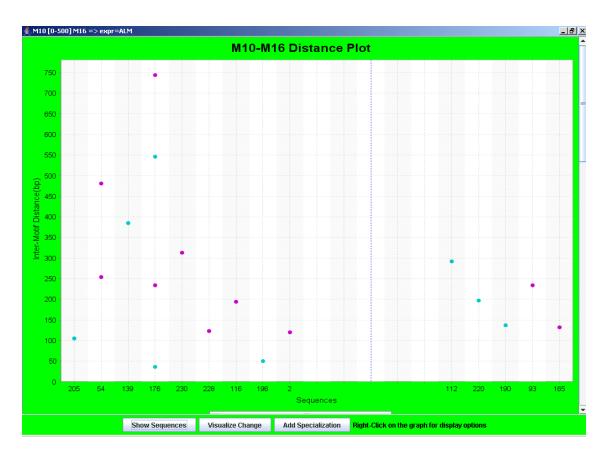


Figure 4.4: Visualize change command from the inter-motif distance plot. The Visualize Change command from the inter-motif distance plot enables the user to visualize the data in the context of the specialization. This plot depicts the specialization M10 [0-500]  $M16 \Rightarrow expr=ALM$  of the original rule M10 &&  $M16 \Rightarrow expr=ALM$  from Figure 4.3.

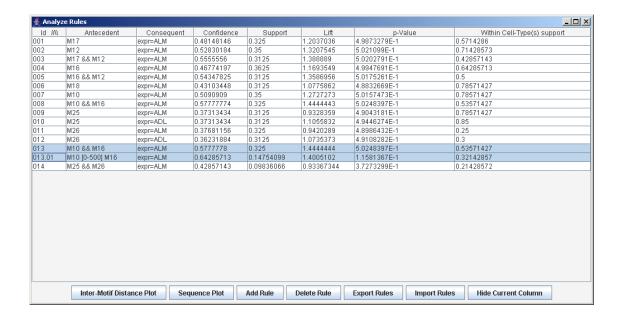


Figure 4.5: A row representing the addition of a specialization to the Analysis Frame.

## 4.2.3 Sequence Plot

Selecting a Rule in the rules area and then clicking the sequence plot button displays a visualization all the qualifying gene sequences in the context of the rule. This action enables a user to perform exploratory analysis in the context of the hypothesis - "Distance of motifs from the SoT influences gene expression". A qualifying gene sequence is one that has at least one occurrence of each motif that appears in the rule (selected in the Analysis Frame). Invoking this command causes a new frame with the sequence plot overlaid with the motif information to be displayed.

This sequence plot graph provides the user with an easy mechanism to discover "Distance from SoT" based patterns in the upper part of the plot that are not as frequent in the lower part as this would let us explore specializations with improved classification accuracy(and/or confidence). Once the user has utilized the dotted separation of the plot (into rule supporting and antecedent supporting) and the

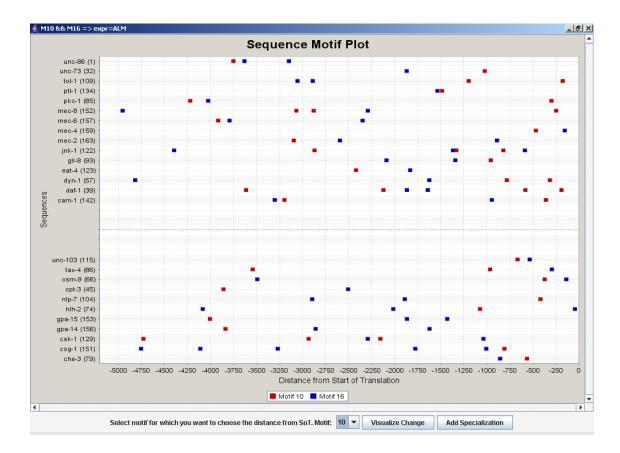


Figure 4.6: Sample Sequence Plot Frame.

Each graph is displayed with the rule used to establish the context as the title of the frame (M10 && M16  $\Rightarrow$  expr=ALM, in this case). This sequence plot displays all gene sequences that contain occurrences of the participating motifs (i.e., motifs M10 and M16). Along the y-axis is the list of gene promoters, that support the antecedent of the rule. That is, the gene promoters that contain at least one occurrence of each of the rule motifs. The x-coordinate of each point in the plot is the distance of the motif from the SoT, which is the far right end of the plot. The color of the point is used to identify the motif. The graph is sliced into two parts by a dotted line. The genes in the upper part of this dividing line are the ones that support the consequent of the rule and hence support the rule. The ones in the lower part are the genes that support only the antecedents of the rule.

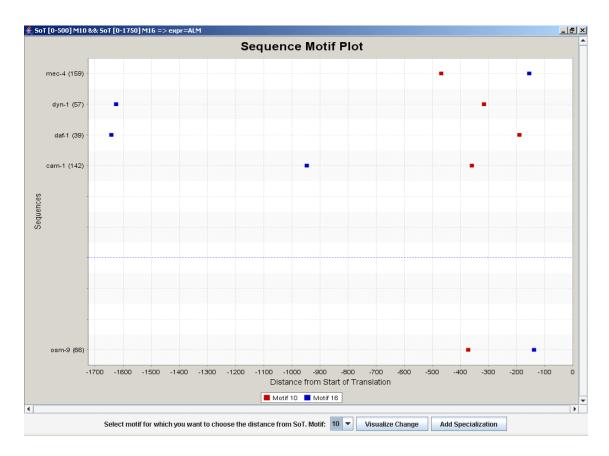


Figure 4.7: Visualize change command from the sequence plot. The Visualize Change command from the sequence plot enables the user to visualize the data in the context of the specialization. This plot depicts the specialization  $SoT \ [0-500] \ M10 \ \&\& \ SoT \ [0-1750] \ M16 \Rightarrow expr=ALM$  of the original rule  $M10 \ \&\& \ M16 \Rightarrow expr=ALM$  from Figure 4.6.

rule specific sequence plots to identify a "distance from SoT" clause of interest, the "Visualize Change" command could be invoked to visualize the data in the context of the specialization rather than the original rule as depicted in Figure 4.7. Again the title of the new window is indicating the context setting rule/specialization. If the user finds the specialization of interest, it can be added to the Analysis Frame using the "Add Specialization" command on the new sequence plot. Again this causes the specialization to appear as a new entry in the Analysis Frame with an auto-generated Id that again lets a user trace back the steps in case the user wants to later recall which rule was used to derive a specialization (Figure 4.8). In case

the base rule consisted of more than 1 motif and multiple "distances from SoT" relationships are defined (one for each motif) each such relationship is represented as a term and a collection of independent terms constitutes the specialized rule. For instance see Figure 4.8 for the following specialization, which is interpreted as: "An occurrence of Motif 10 within 500 bp from the SoT and the presence of an occurrence of Motif 16 within 1750 bp from the SoT implies that the gene is expressed in cells of type ALM".

$$SoT [0 - 500] M10$$
 &&  $SoT [0 - 1750] M16 \Rightarrow expr = ALM$  (4.2)

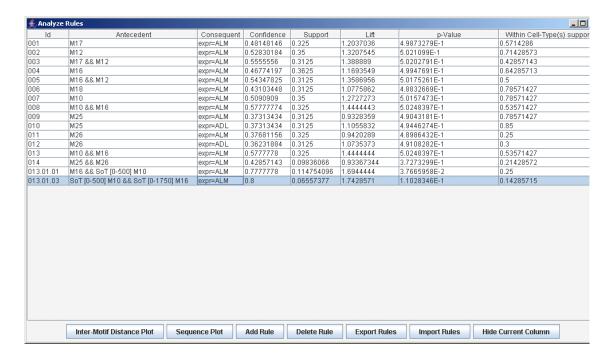


Figure 4.8: Analysis Frame with two distance from SoT based specializations.

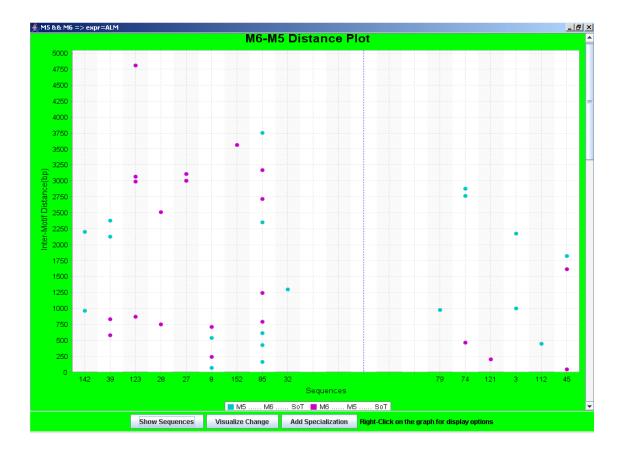


Figure 4.9: Inter-Motif Distance Plot for Motifs M5 and M6. Observe the lack of magenta (dark) dots in the right part of the frame.

### 4.2.4 Order of occurrence of motifs

We wanted the visual extensions to also accommodate exploratory analysis based on the hypothesis "The order of occurrence of motifs influences gene expression." But during the system design and the system use by the team(including the domain expert) it was observed that we already had a few ways to visualize gene sequence data in the context of the "order of the occurrence" of motifs and hence a new plot was not created. If order of occurrence of motifs was important it could be easily identified by one of three ways: the color of the points in inter-motif distance plot, a repeating sequence of color in the sequence plot, or through the operation of the ASAS mining algorithm itself.

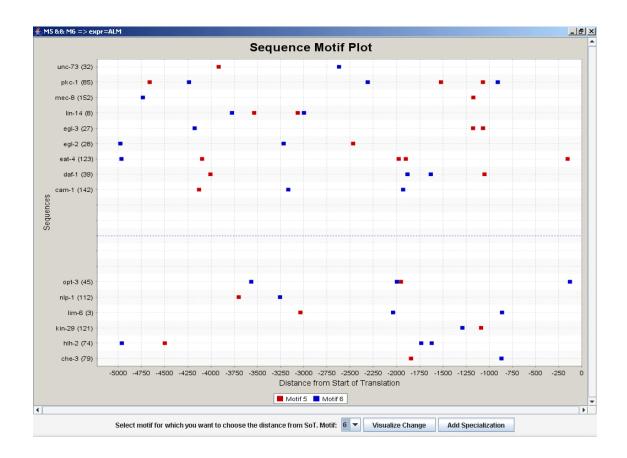


Figure 4.10: Sequence Plot for Motifs M5 and M6. Observe that in the rule supporting sequences (upper part) a red-dot is usually followed by a blue dot scanning the gene sequence from right end (SoT) to left.

Color of the points in an inter-motif distance plot. The order of the motifs in the inter-motif distance plot is represented by color. For instance in Figure 4.3, M10 to the right of M16 (i.e., M16..M10..SoT) is represented by a magenta (dark) dot, while M16 to the right of M10 is represented by a aqua (light) dot. Thus, color provides a quick visual clue whether the order of occurrence of motifs affects gene expression. If that is the case, the left part of the plot should have more points of one color than the other part.

Repeated sequence of color in the sequence plot. As mentioned in Section 4.2.3, the sequence plot displays all instances of participating motifs for qualifying

sequences as they occur on the gene relative to the SoT. Since each motif appears in its own color and the data is being visualized in the context of a single rule, one can often see a repetitive pattern of color in the upper part and a lack of the same in the lower part of the plot. Such a display could also indicate an influence of order of occurrence on gene expression.

ASAS mining algorithm. The association rule mining module from the WPI-Weka System [PR05] is capable of mining association rules with order/position based information and hence it is possible to have some of these rules with order of occurrence of motifs available already at the beginning of the exploratory analysis. Either of the two means mentioned above could be used to visually confirm/observe the order of occurrence relationship.

## 4.2.5 Adding Rules Manually

01 M17	Id	Antecedent	Consequent	Confidence	Support	Lift	p-Value	Within Cell-Type(s) support
M17 & M12	01	M17	expr=ALM	0.48148146		1.2037036	4.9873279E-1	0.5714286
M16	12	M12	expr=ALM	0.52830184	0.35	1.3207545	5.021099E-1	0.71428573
5         M16 && M12         expr=ALM         0.54347825         0.3125         1.3586956         5.0175261E-1         0.5           6         M18         expr=ALM         0.43103448         0.3125         1.0775862         4.8832669E-1         0.78671427           7         M10         expr=ALM         0.5090909         0.35         1.2727273         5.0157473E-1         0.78671427           8         M10 && M16         expr=ALM         0.57777774         0.325         1.4444443         5.0248397E-1         0.53571427           9         M25         expr=ALM         0.37313434         0.3125         0.9320359         4.9043181E-1         0.78671427           0         M25         expr=ALM         0.37681156         0.325         0.9420289         4.986432E-1         0.25           1         M26         expr=ALM         0.37681156         0.325         0.9420289         4.986432E-1         0.25           2         M26         expr=ADL         0.36231884         0.3125         1.0735373         4.910829E-1         0.3571427           3         M10 && M16         expr=ALM         0.5777778         0.325         0.9430373-3         4.910829E-1         0.36571427           4         M25 && M26	3	M17 && M12	expr=ALM	0.5555556	0.3125	1.388889	5.0202791E-1	0.42857143
6 M18 expr=ALM 0.43103448 0.3125 1.0775862 4.8832669E-1 0.78571427 7 M10 expr=ALM 0.5090909 0.35 1.2727273 5.0157473E-1 0.78571427 8 M10 & expr=ALM 0.57777774 0.325 1.4444443 5.0248397E-1 0.53571427 9 M25 expr=ALM 0.37313434 0.3125 0.3228359 4.9043181E-1 0.78571427 0 M25 expr=ALM 0.37881156 0.325 1.1055832 4.9446274E-1 0.85 1 M26 expr=ALM 0.37681156 0.325 0.9420289 4.9896432E-1 0.25 2 M26 expr=ALM 0.36231884 0.3125 1.0735373 4.9108282E-1 0.3 3 M10 & M26 expr=ALM 0.36231884 0.3125 1.0735373 4.9108282E-1 0.3 3 M10 & M26 expr=ALM 0.36231884 0.3125 1.0735373 4.9108282E-1 0.35371427 4 M25 & M26 expr=ALM 0.5777778 0.325 1.4444444 5.0248397E-1 0.53571427	4	M16	expr=ALM	0.46774197	0.3625	1.1693549	4.9947691E-1	0.64285713
M10	5	M16 && M12	expr=ALM	0.54347825	0.3125	1.3586956	5.0175261E-1	0.5
M10 && M16   expr=ALM   0.57777774   0.325   1.4444443   5.0248397E-1   0.53571427	ì	M18	expr=ALM	0.43103448	0.3125	1.0775862	4.8832669E-1	0.78571427
M25	,	M10	expr=ALM	0.5090909	0.35	1.2727273	5.0157473E-1	0.78571427
0         M25         expr=ADL         0.37313434         0.3125         1.1055832         4.9446274E-1         0.85           1         M26         expr=ALM         0.37681156         0.325         0.9420289         4.9896432E-1         0.25           2         M26         expr=ADL         0.36231884         0.3125         1.0735373         4.9108282E-1         0.36           3         M10.8.8.M16         expr=ALM         0.5777778         0.325         1.4444444         5.0248397E-1         0.53571427           4         M25.8.8.M26         expr=ALM         0.42957143         0.09836066         0.93367344         3.7273299E-1         0.21428572	3	M10 && M16	expr=ALM	0.57777774	0.325	1.4444443	5.0248397E-1	0.53571427
M26         expr=ALM         0.37681156         0.325         0.9420289         4.8986432E-1         0.25           2         M26         expr=ADL         0.36231884         0.3125         1.0753737         4.9108282E-1         0.3           3         M10 & M10 & M16         expr=ALM         0.5777778         0.325         1.4444444         5.0248397E-1         0.53671427           4         M25 & M26         expr=ALM         0.42857143         0.09836066         0.93367344         3.7273299E-1         0.21428572	3	M25	expr=ALM	0.37313434	0.3125	0.9328359	4.9043181E-1	0.78571427
2         M26         expr=ADL         0.36231884         0.3125         1.0735373         4.9108282E-1         0.3           3         M10 & M10 & M16         expr=ALM         0.5777778         0.325         1.4444444         5.0248397E-1         0.53571427           4         M25 & M26         expr=ALM         0.42857143         0.09836066         0.93367344         3.7273299E-1         0.21428572	0	M25	expr=ADL	0.37313434	0.3125	1.1055832	4.9446274E-1	0.85
3         M10 & M16         expr=ALM         0.5777778         0.325         1.4444444         5.0248397E-1         0.53571427           4         M25 & M26         expr=ALM         0.42857143         0.09836066         0.93367344         3.7273299E-1         0.21428572		M26	expr=ALM	0.37681156	0.325	0.9420289	4.8986432E-1	0.25
4 M25 & M26 expr=ALM 0.42857143 0.09836066 0.93367344 3.7273299E-1 0.21428572	2	M26	expr=ADL	0.36231884	0.3125	1.0735373	4.9108282E-1	0.3
	3	M10 && M16	expr=ALM	0.5777778	0.325	1.4444444	5.0248397E-1	0.53571427
5 M5 [rp0-rp1] M6 [rp2-rp3] expr=ALM 0.7 0.114754096 1.525 9.4429519E-2 0.25	4	M25 && M26	expr=ALM	0.42857143	0.09836066	0.93367344	3.7273299E-1	0.21428572
	5	M5 [rp0-rp1] M6 [rp2-rp3]	expr=ALM	0.7	0.114754096	1.525	9.4429519E-2	0.25

Figure 4.11: Add Rule option in the Analysis Frame provides for free text option to add rules.

We wanted to allow users to type in specialized rules manually, particularly in the cases of rules involving order, as well as certain more complex 'hybrid' rules discussed in detail below. To allow this option, we needed to write a grammar (Figure 4.12) to parse the rules. JavaCC [JCC], Java equivalent of LEX and YACC, was used to code the grammar and auto-generate the rule parser. The user can then simply type in the Antecedents and the Consequent of the rule to calculate the different statistics indicating the interestingness metrics of the rule as shown in Figure 4.11. Simply typing a complete rule computes the statistics indicating the interestingness of the rule. The user could also visualize the new rule using either the sequence plot or the inter-motif distance plot.

A rule keyed in by the user which does not adhere to this grammar results in an error as shown in Figure 4.13

## 4.2.6 Hybrid Rule

As described in the grammar governing rule definitions, each rule consists of an antecedent and a consequent. Antecedents in turn consist of terms. A rule could also include specialized term, extra hypothesis-based information(constraints) that the instances of the participating motifs must satisfy in order for a gene sequence to support the rule.

The system also supports hybrid rules, rules that consist of specialized terms based on different hypotheses and a gene sequence must satisfy all constraints in order to support the rule. In Figure 4.10 note that there exists an occurrence of M5 (the red dot) usually within the first 1600 bp from the SoT (far right end of the plot). Also note that there is an occurrence of Motif M5 between an occurrence of Motif M6 (blue dot) and the SoT. It is interesting to combine the two observations into a rule as follows and visualize it or calculate its interestingness. As we see in Figure 4.14 that this hybrid specialization:

#### Grammar

```
The grammar is defined as a 4-tuple: (SIGMA, N, P, S):
    SIGMA is an alphabet of terminal symbols
    N is an alphabet of non-terminal symbols
    P is a set of production rules
    S in N is the start symbol
Sigma := \{SoT, Mn, Mn(rp i - rp i+1), \k\k, (x-y)\}
        := {S, L1, L2, C1, C2, CL1, CL2, CL3, CL4, S}
P := {
        S = Term | (Term C1 Term) | (T C1 Term)
        C1 = &&
                                       # And
        Term = CL1 | CL2 | CL3 | CL4
        CL1 = L1 C1 L1 | CL1 C1 L1
                                       # Covers rules based on presence.
        CL2 = L1 C2 T
                                       # Covers literals of the form distance from SoT.
        CL3 = L1 C2 L1 | CL3 C2 L1
                                       # Covers literals of the form Mi at a distance of
                                       # x-y from Mj
        {\it CL4} = {\it L2} {\it C1} {\it L2} | {\it CL4} {\it C1} {\it L2}  # Covers literals of the form Mi occurs before Mj
        L1 = Mn
                                       # Motif n
        T = SoT
                                       # Start of Translation
        C2 = (x-y)
                                       # Where x and y are integers such that y > x
        L2 = Mn (rp i - rp i+1)
                                       \# Motif n exists from Relative position i to i+1
                                       # on the gene sequence.
    }
```

A sample derivation of an antecedent from the grammar is shown below:

```
S:= Term
CL1
CL1 C1 L1
CL1 && M3
L1 C1 L1 && M3
M1 && M2 && M3
This antecedent is interpreted as:
If Motif 1 is present and Motif 2 is present and Motif 3 is present.
```

Figure 4.12: Grammar to parse rules.

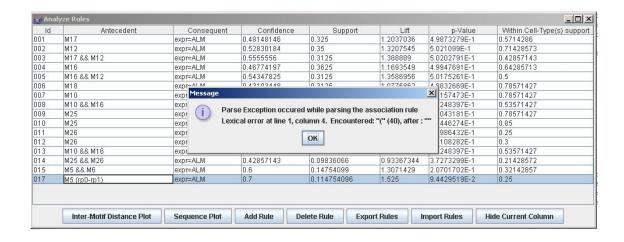


Figure 4.13: Grammar based parsing helps identify user errors in typing the rule.

M5 [rp0-rp1] M6 [rp2-rp3] && SoT [0-1600] M5 
$$\Rightarrow$$
 expr=ALM 
$$[Confidence = 0.8333333, Support = 0.08196721] \quad (4.3)$$

has a higher confidence as compared to the following simpler "order of occurrence" specialization

M5 [rp0-rp1] M6 [rp2-rp3] 
$$\Rightarrow$$
 expr=ALM 
$$[Confidence=0.8333333, Support=0.08196721] \quad (4.4)$$

As seen above hybrid specialization could have multiple specialized terms that relate to a single motif. A hybrid specialization could post multiple constraints on the same motif like Distance from SoT and Order of occurrence relative to another motif. It is important to note that although the rule may have multiple constraints for the same motif, it is not required that the same instance of the motif satisfies each of them. In the context of the 4.3 above, it is not required that the instance

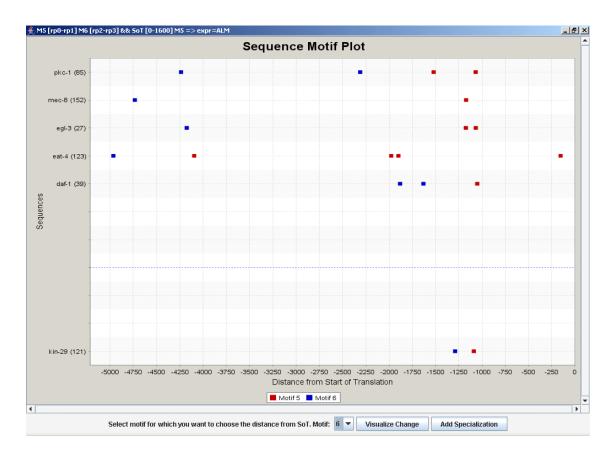


Figure 4.14: Hybrid rules help specify multiple constraints (based on different hypotheses) within a single specialization.

of Motif 5 that satisfies the order of occurrence condition is the same M5(instance) that lies within 1600 base pairs of the SoT. However, there might be a need for the user to actually specify constraints which are inter-related, aliases are supported by our rule grammar for exactly this reason.

#### 4.2.7 Aliases

Aliases were included in the grammar to provide the user with an option of defining inter-related constraints or specialization terms. Consider the following Inter-Motif

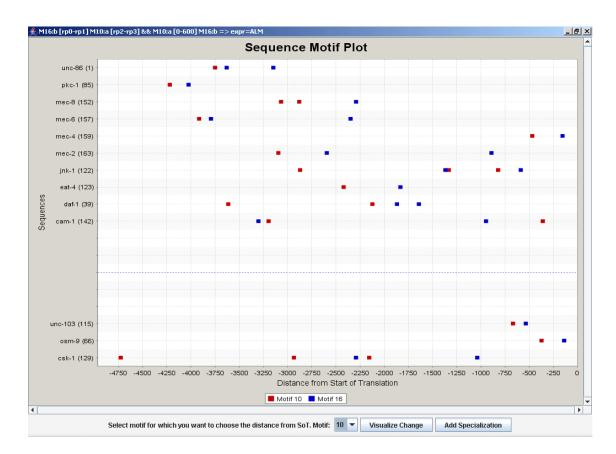


Figure 4.15: Aliases let user define specializations with inter-related constraints.

Distance based specialization from Figure 4.5:

$$M10[0 - 500]M16 \Rightarrow expr = ALM \tag{4.5}$$

Visualizing this specialization using a sequence plot (Figure 4.6), one can see distinctly that not only do motifs M10 (red dot) and M16(blue dot) occur close together but they also occur in a pattern such that the same instances of M10 and M16 that are involved in the distance-based relationship also occur in the same order relative to the SoT. Aliases enable the user to specify such complex relationships in the rule as follows (Figure 4.15):

$$M10:a [0-500] M16:b \&\& M16:b [rp0-rp1] M10:a [rp2-rp3] \Rightarrow expr=ALM (4.6)$$

For details of system operation, see User Guide.

## Chapter 5

## System Architecture

This tool was conceptualized as an extension to the WPI-Weka system and hence is also referred to as the "Visualization and Specialization Modules(VSM)". This chapter describes the interaction of this tool with the WPI-Weka system and a high level design overview.

## 5.1 Component Interaction

Figure 5.1 illustrates how VSM interacts with the WPI-Weka system, to let the user perform hypothesis-driven exploratory analysis of genetic data in order to create specialized association rules that predict gene expression. The enumerated arrows with italicized text denote the different steps that constitute the process of exploratory analysis to discover specializations predicting gene expression. Each of the steps along with the inputs and outputs to the process are listed below:

1. Mine association rules. One of the contributions of [Rudss] was to integrate into a single classifier (AssociateClassifier) within the WPI-Weka system([WPI]), contributions of previous work at WPI in the field of association rule mining.

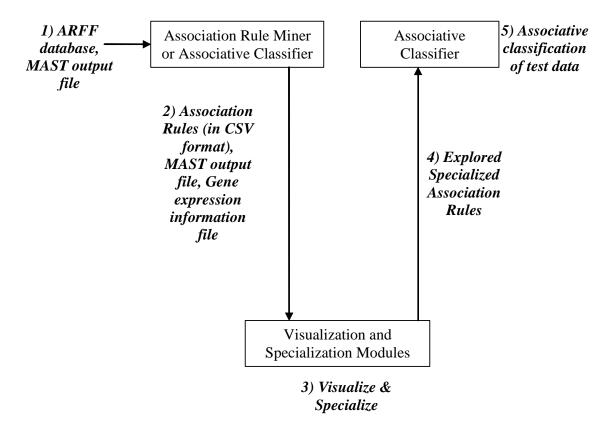


Figure 5.1: Process depicting the flow of data (interactions) between the WPI-Weka system and the VSM.

The data exchange between the WPI-Weka system and the VSM is in a comma separated value format which is explained in detail in Figure 5.2.

This classifier or the association rule miner (ARMiner) module of the WPI-Weka system, takes as input an ARFF file consisting of genetic data and a MAST output file (Section 3.3) and mines for association rules predicting gene expression.

2. Transfer mined association rules to VSM. As a part of the integration plan it was decided that both [Rudss] and this work would support import/export of rules in a predefined comma-separated values (CSV) format. So as a first step to analyzing gene expression association rules, [Rudss] could be used to invoke the VSM with the set of mined rules (Figure 5.2), the MAST output file and

#### CSV interface to transfer rule sets between WPI-Weka and VSM

```
HEADER
Id, Antecedent, Consequent, Confidence, Support, Lift, p-Value, Event Wt., Within Cell-Type(s) support

DATA
001, M17, expr=ALM, 0.48148146, 0.325, 1.2037036, 4.9873279E-1, 0, 0.42857143
002, M12, expr=ALM, 0.52830184, 0.35, 1.3207545, 5.021099E-1, 0, 0.10714286
```

Figure 5.2: CSV interface to transfer rule sets between WPI-Weka system and VSM. The header section defines a comma separated list of the headers describing the attributes contained in each data instance. The Data section consists of the actual set of rules being exported or imported.

the gene expression information.

- 3. Visualize and Specialize. The implementation of this work, that is the VSM, would let the user perform hypothesis-driven visualization of data that helps specialize a set of association rules. See Section 4.2.
- 4. Transfer the set of specialized rules to the AssociativeClassifier. Again the VSM as well as [Rudss] support the transfer of set of specialized rules explored using the VSM to the AssociativeClassifier using the predefined CSV format.
- 5. Use the classifier to predict gene expression for a novel set of genes. The classifier can be used to calculate the classification accuracy of the imported specializations over a test set consisting of novel genes (i.e., genes that have not been used during mining or specialization) in order to determine the predictive power of the relationships identified.

## 5.2 System Design

This section describes the high level design of the VSM tool from a functional perspective that is also illustrated in Figure 5.3. We describe the different modules within the VSM subsystem implementation:

- 1. MAST Parser. The VSM could be invoked from within the WPI-Weka System or as a standalone application. Irrespective of the invocation mechanism (i.e., as a standalone application or from within WPI-Weka) it requires as input the gene expression information (Figure 4.2) and a MAST output file (Figure 3.5). The information from the MAST output file and the gene expression information is parsed using this module to populate a multi-level internal data structure (Figure 5.4) and subsequently the analysis frame (Figure 4.1) is displayed.
- 2. Rule Parser. Each base rule, either belonging to the set of rules mined using the WPI-Weka system or by using the "Add Rule" (Section 4.2.5) command from the analysis frame is parsed by using this module, that is, an implementation of the grammar defined in Figure 4.12.
- 3. Charting Extensions. The parsed information from rule parser and the internal data structure are used as input to the charting infrastructure to generate hypothesis-specific plots for data visualization. The charting infrastructure is created by extending the open source charting library JFreeChart. JFreeChart separates its data from its presentation layers which means the system could be extended to add new features to plots with minimal changes. The user's exploratory analysis using these plots (data visualization) subsequently produces specialized rules which in combination to the internal data structure can be

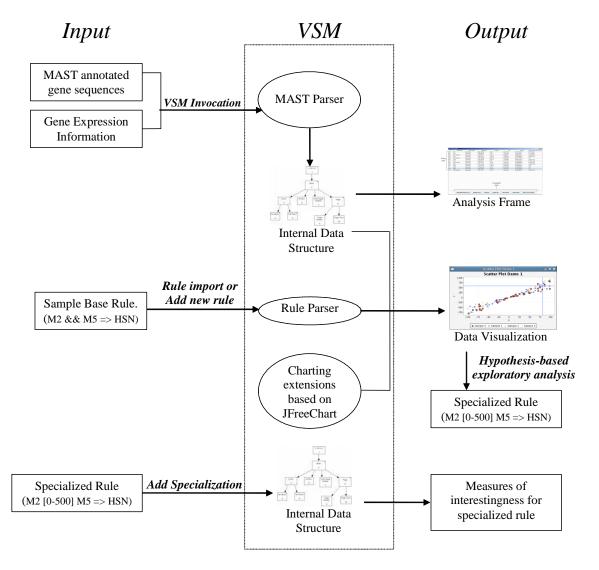


Figure 5.3: VSM System Design.

Functional design of the VSM. Each step in the exploratory analysis process is described in terms of the input(s) to the VSM subsystem, corresponding modules within the VSM invoked, and the output. The vertical rectangle represents the VSM subsystem with each oval representing a module within the VSM subsystem implementation. As delineated, the entities to the left of the VSM subsystem are the input(s) provided to each module and the entities to the right are the output(s) from the VSM at each step.

Key (Gene Name)	Value	
ceh-43	Expression Pattern	Neural
	Gene Name	ceh-43
	Length	993
	Motif-based location info	M1 250, 523
		M2 944
nlp-5	Expression Pattern	Muscle
	Gene Name	nlp-5
	Length	5000
	Motif-based location info	M1 3555
		M2 45, 856

Figure 5.4: Hierarchical internal data structure - Hash of hashes.

The top level hash has the gene name as the key attribute. The value element corresponding to each gene is also a hash consisting of sequence information which, besides gene specific information like length and expression pattern, contains location information organized on a per motif basis. The location information for each motif (key) consists of all occurrences of the motif on the gene sequence relative to the SoT. The sample here illustrates the organization of information for two sample sequences, ceh-43 and nlp-5, each of which contains one or more occurrences of motif M1 and M2.

used to calculate the different measures of interestingness for each specialized rule.

## 5.3 Implementation Details

Since the WPI-Weka system, which is an extensive collaborative effort within the KDD Research Group at WPI, is Java based, Java was chosen to implement VSM.

It was during the course of this project and [Rudss] that the WPI-Weka system was hosted in the WPI sourceforge server. As a part of this project an ant-script (Java equivalent of a makefile) was also developed that enables users to build the system from the source with minimal instructions. Eclipse was our choice of the IDE used as it provides a easy to use interface for both Java based development as well as CVS based version control.

Elements of good design were extensively applied throughout the development process. For instance, the support for import/export of CSV file containing the rules is implemented as a Java interface called the Analyzable interface which makes it easy for a new implementation to support a certain functionality without restricting a specific type of implementation. For instance if a new mining algorithm that mines gene expression rules is added to the WPI-Weka System, it could invoke VSM as long as it implements the Analyzable interface.

## Chapter 6

## **Experimental Evaluation**

Chapter 3 (Figure 3.2) describes in detail the process to create a dataset in a mining compatible format (ARFF) starting with data collection. As mentioned in Section 3.2 and again in Section 3.4, to avoid mining and exploring relationships that over fit the data, the sequences were divided into a training set (90% of the sequences) and a test set (10% of the sequences). Figure 6.1 illustrates the experimental setup.

# 6.1 Experimental Protocol and Parameters to be measured

Mining the training dataset using the WPI-Weka Association Rule Miner produces gene expression association rules. Different measures of interestingness, including the traditional measures of support and confidence, are calculated to estimate the statistical significance of the rules. Once the domain user identifies an interesting base rule (e.g., based on the values of different measures of interestingness), VSM could be used to perform hypothesis-driven exploratory analysis of the selected rule

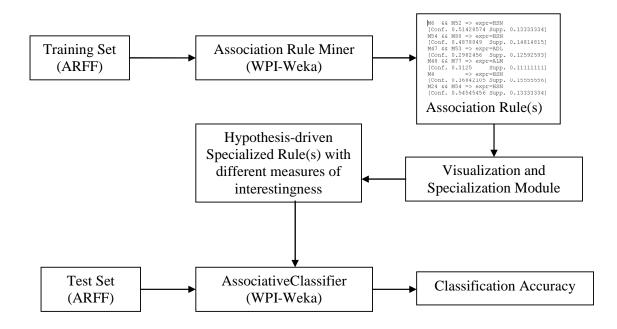


Figure 6.1: Experimental Setup.

Starting with mining of rules over the training data to the classification of the test dataset using the explored specialized rules.

to derive a specialized association rule such that the antecedent of the rule consists of additional constraints based on positional information of the motif(s). This process is repeated a few times with different base rules to derive a set of specialized rules that, at least statistically, seem to provide a more accurate representation of the underlying regulatory mechanism governing gene expression. This set of specialized rules is then tested for accuracy over a dataset consisting of novel genes (i.e., genes which were not used to elicit motifs and were also not involved in the mining or the specialization processes). The classification accuracy is a measure of predictive power. An improved classification accuracy as compared to the set of base rules translates to an increase in the confidence of the specialized rule with a reasonable decrease in the support of the rule and is used to estimate the potential biological validity of the relationship. Other measures of interestingness like the p-value and the lift also help to estimate the effectiveness of the rule. The system is extensible

from the measures of interestingness perspective; that is, it would require minimal changes for another measure of interestingness to be added to the system.

## 6.2 Experimental Results and Analysis

The target audience for the tool developed are domain experts trying to identify biologically interesting relationships. We present a walk through of a small scale experiment using real genetic data that helps establish the work flow for the process of performing hypothesis-driven specializations.

As discussed in Section 3.1, the training set consists of 151 gene sequences in ARFF format. In the experiment reported here, these sequences were mined for presence based association rule mining with a minimum support of 0.1 and a minimum confidence of 0.3. It is important to understand the reason for choosing the relatively low values for support and confidence. The choice of the low value for the minimum support is based on the way the dataset is put together. Since we tried to identify gene sequences for 9 different cell types, each cell type has approximately 11% representation in the dataset, then the motif elicitation and annotation process were performed with an intent to find cell-type specific motifs. So if a biologically valid cell-type specific regulatory mechanism was found during the mining process it is reasonable to expect that it should have low support (i.e., 11\% or less). Since we intend to explore specializations that represent the biological relationship more effectively as compared to the base rules from which they are derived, we can select base rules with low confidence measure. The mining process resulted in a total of 269 rules, out of which the following 6 rules were chosen to illustrate effectively all forms of hypothesis-driven specializations. So we intend to visualize and specialize 2 rules per hypothesis type to illustrate the work flow.

Motif	Consensus sequence
M6	GGAAGAAGAG
M47	GAGAAGAG
M48	TGAGAAAA
M52	GAAGAAGAA
M53	GAAGAAGAAGGA
M54	GAGTGAGAGGG
M69	GGGGGGAGG
M77	GAGACGAAGA
M80	GAGAAGAAG

Figure 6.2: List of motifs from the base rules under consideration along with their consensus sequences.

M6 && M52 
$$\Rightarrow$$
 expr=HSN [Conf. = 0.51428574, Supp. = 0.13333334] (6.1)

$$M54 \&\& M80 \Rightarrow expr=HSN [Conf. = 0.4878049, Supp. = 0.14814815]$$
 (6.2)

$$M47 \&\& M53 \Rightarrow expr=ADL [Conf. = 0.2982456, Supp. = 0.12592593]$$
 (6.3)

M48 && M77 
$$\Rightarrow$$
 expr=ALM [Conf. = 0.3125, Supp. = 0.11111111] (6.4)

$$M69 \Rightarrow expr=HSN [Conf. = 0.46341464, Supp. = 0.14074074]$$
 (6.5)

$$M6 \Rightarrow expr=HSN [Conf. = 0.13636364, Supp. = 0.044444446]$$
 (6.6)

## 6.2.1 Order of motif occurrence specialization of Rules (6.1) and (6.2)

In this section we specialize Rules (6.1) and (6.2) based on the hypothesis "The order of occurrence of motifs influences gene expression". Figures 6.3 and 6.5 depict the process followed to specialize the base rules from an order of occurrence of motifs perspective.

An inter-motif distance plot, for instance Figure 6.3, is split into two parts: the left part containing the sequences that support the rule and the right part containing the sequences that support the antecedent only. This provides the user with an easy mechanism to discover order of occurrence based patterns in the left part that are not as frequent in the right part, as this would let us explore specializations with improved classification accuracy(and/or confidence). For instance, in Figure 6.3, many genes on the right-hand side lack magenta (dark) dots. This implies that the occurrence of Motif 6 in between Motif 52 and the SoT (i.e., M52-M6-SoT) may positively influence a gene to be expressed in cells of type HSN. Once a user has identified such an order based relationship that is of interest, the following corresponding specialized rule can be added to the analysis frame:

M6 [rp0-rp1] M52 [rp2-rp3] 
$$\Rightarrow$$
 expr=HSN [Conf. = 0.6363636, Supp. = 0.1037037] (6.7)

The analysis frame enables the user to estimate the significance of the rule using the different measures of interestingness computed for the specialized rule. The user can also compare the interestingness of the specialized rule with that of the base rule (Figure 6.4).

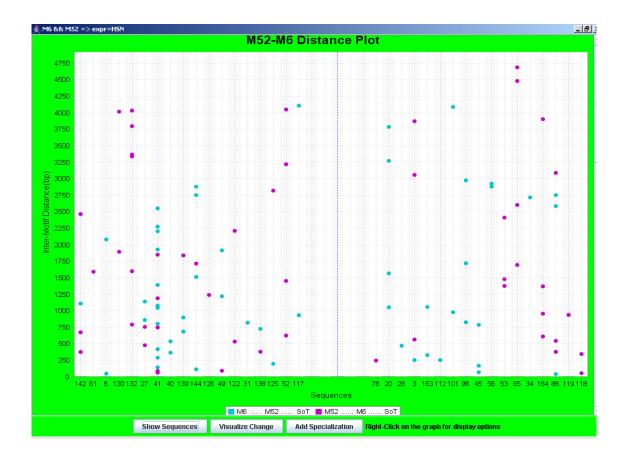


Figure 6.3: Inter-motif distance plot for the base rule  $M6 \&\& M52 \Rightarrow expr=HSN$ . Along the x-axis are the Id's corresponding to the genes. Along the y-axis is the inter-motif distance. Each point in the plot, irrespective of the color, represents the distance between an occurrence of Motif 6 from an occurrence of Motif 52. Also notice the division of the graph into two parts. Each colored dot is representative of the relative ordering of the occurrence of the motifs relative to the Start of Transcription. A magenta (dark) dot represents the inter-motif distance between an occurrence of Motif 6 and Motif 52 such that the occurrence of Motif 6 lies between the occurrence of Motif 52 and the SoT (i.e., M52-M6-SoT). A aqua (light) dot represents an intermotif distance such that the order of occurrence of motifs is M6-M52-SoT. The left-side part consists of gene sequences which support the rule and the right-side part consists of the gene sequences that support the antecedent of the rule only.

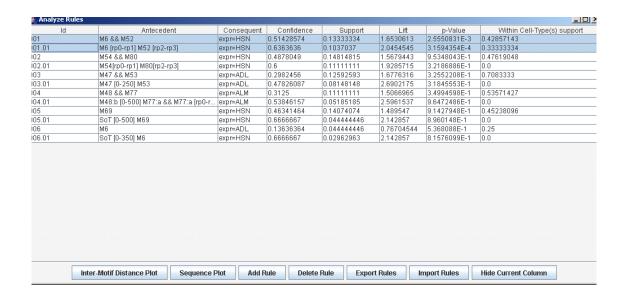


Figure 6.4: Analysis frame providing a comparison of the interestingness of the specialized rule, Rule (6.7), with the base rule, Rule (6.1).

Similarly in Figure 6.5, observe that many genes in the right part of the plot lack magenta (dark) points. This again indicates that the occurrence of motif 54 between an occurrence of Motif 80 and the SoT (i.e., SoT-M54-M80) may positively influence gene expression. Again the user could add the following corresponding specialization to the analysis frame and compare its interestingness to that of the base rule.

$$M54[rp0-rp1] M80[rp2-rp3] \Rightarrow expr=HSN [Conf. = 0.6, Supp. = 0.11111]$$
 (6.8)

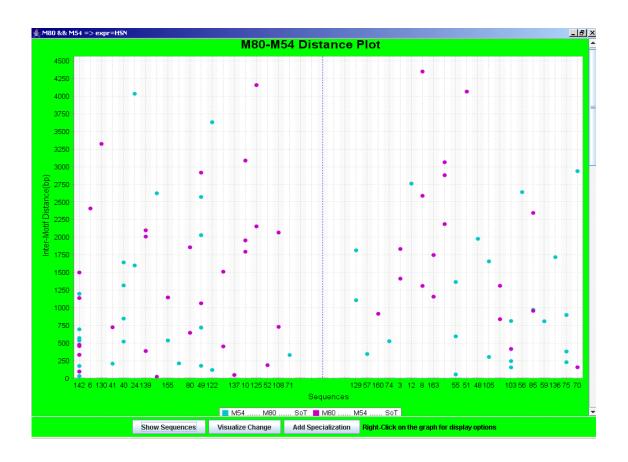


Figure 6.5: Inter-motif distance plot for the base rule  $M54 \&\& M80 \Rightarrow \exp=HSN$ .

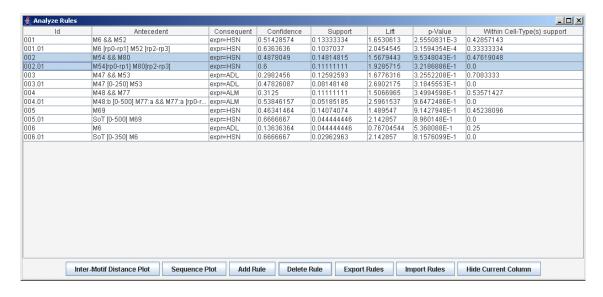


Figure 6.6: Analysis frame providing a comparison of the interestingness of the specialized rule, Rule (6.8), with the base rule, Rule (6.2).

# 6.2.2 Inter-motif distance specialization of Rules (6.3) and (6.4)

In this section we specialize Rules (6.3) and (6.4) based on the hypothesis "Intermotif distance influences gene expression". Figures 6.7 and 6.9 depict the process followed to specialize the base rules from an inter-motif distance perspective.

An inter-motif distance plot, for instance Figure 6.7, displays for qualifying gene the inter-motif distances between each occurrence of Motif 47 from each occurrence of Motif 53. A qualifying gene is one that contains at least one occurrence of each motif in the base rule. The splitting of the plot into two parts (as described in Section 6.2.1), provides the user with an easy mechanism to discover inter-motif distance pattern in the left part that are not as frequent in the right part, as this would let us explore specializations with improved classification accuracy(and/or confidence). For instance, in Figure 6.7, many genes on the right-side part lack dots in the shaded area of the plot, that is, an inter-motif distance range of 0-250 bp which implies that the occurrence of motifs 47 and 53 within 250 bp from each other may be positively related to the gene being expressed in cell type ADL. Once a user has defined an inter-motif distance relationship that is of interest the relevant region of the plot gets shaded as illustrated in Figure 6.7. Subsequently the following corresponding specialization can be added to the analysis frame.

$$M47 [0-250] M53 \Rightarrow expr=ADL [Conf. = 0.47826087, Supp. = 0.08148148] (6.9)$$

Again the user can estimate the significance of the rule by using the different measures of interestingness computed for the specialized rule. The user can also compare the interestingness of the specialized rule as compared with that of the base rule (Figure 6.8).



Figure 6.7: Inter-motif distance plot for the base rule  $M47 \&\& M53 \Rightarrow \exp(-ADL)$ .

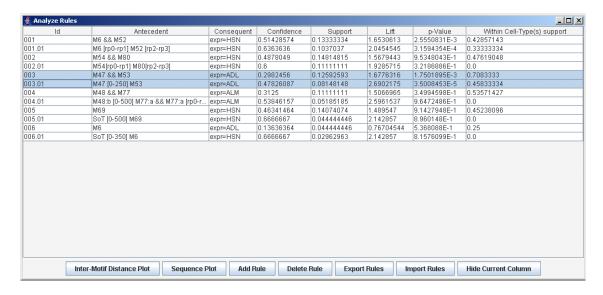


Figure 6.8: Analysis frame providing a comparison of the interestingness of the specialized rule, Rule (6.9), with the base rule, Rule (6.3).

Similarly in Figure 6.9, observe that many genes lack magenta (dark) points in the right-side part of the shaded area of the plot, that is, an inter-motif distance range of 0-500 bp. This implies that the occurrence of motif 77 and 48 within 250 bp from each other and in the order SoT-M77-M48 may positively influence gene expression in cell type ALM. Subsequent addition of the following corresponding specialization to the analysis frame enables the user to compare the interestingness of the specialized rule to that of the base rule (Figure 6.10).

M48:b [0-500] M77:a && M77:a [rp0-rp1] M48:b[rp2-rp3] 
$$\Rightarrow$$
 expr=ALM [Conf. = 0.53846157, Supp. = 0.05185185] (6.10)

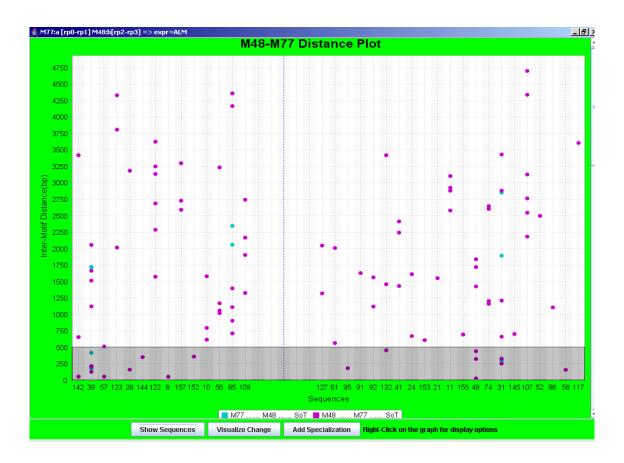


Figure 6.9: Inter-motif distance plot for the base rule M77 [rp0-rp1] M48[rp2-rp3]  $\Rightarrow$  expr=ALM.

Notice that the base rule selected is already an "order of occurrence of motifs" specialization. This was one of the rules generated by the ASAS algorithm as mentioned in Section 4.2.4.

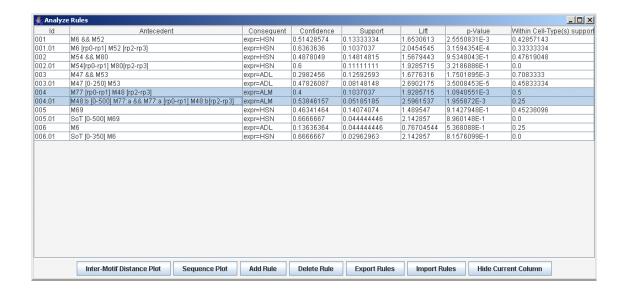


Figure 6.10: Analysis frame providing a comparison of the interestingness of the specialized rule, Rule (6.10), with the base rule, Rule (6.4).

# 6.2.3 Distance from SoT specialization of Rules (6.5) and (6.6)

In this section we specialize Rules (6.5) and (6.6) based on the hypothesis "Distance of motif occurrence from SoT influences gene expression". Figures 6.11 and 6.13 depict the process followed to specialize the base rules from a distance from SoT perspective.

A sequence plot, for instance Figure 6.11, displays qualifying genes with the motifs overlaid such that a point on the plot represents the distance of that occurrence of the motif from the SoT. A qualifying gene is one that contains at least one occurrence of each motif in the base rule. The color of the point in the plot is indicative of the motif in question. The splitting of the plot into two parts (as described in Section 6.2.1), provides the user with an easy mechanism to discover distance from SoT based pattern in the top part that are not as frequent in the bottom part, as this would let us explore specializations with improved classifica-

tion accuracy(and/or confidence). For instance, in Figure 6.11, many genes in the bottom part lack dots in the area delineated by the SoT (far right end of the plot) and the vertical line representing the 500 bp from SoT cutoff. This indicates that an occurrence of Motif 69 within a distance of 500 bp from the SoT may positively influence gene expression in cell type ADL. Once a user has defined such a "Distance from SoT" relationship it is indicated in the plot as the vertical line, in the same color as the one reserved for the motif, as illustrated in Figure 6.11 is added to the plot. Subsequently the following corresponding specialization can be added to the analysis frame.

SoT [0-500] M69 
$$\Rightarrow$$
 expr=HSN [Conf. = 0.6666667, Supp. = 0.044444446] (6.11)

Again the analysis frame with the specialized rule enables the user to compare the interestingness of the specialized rule with that of the base rule (Figure 6.12).

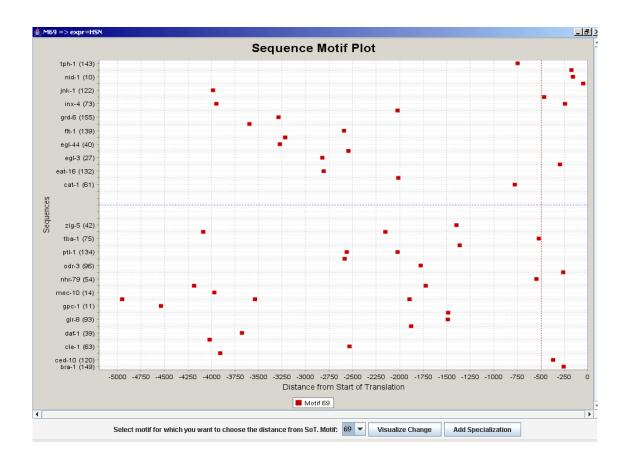


Figure 6.11: Sequence plot for the base rule  $M69 \Rightarrow expr=HSN$ .

The sequence plot lists the genes along the y-axis and the distance from SoT along the x-axis. Each colored dot represents an occurrence of a specific motif. Notice the division of the graph into two parts using a horizontal line through the plot. The top part consists of gene sequences which support the rule and the bottom part consists of the gene sequences that support the antecedent of the rule. A user introduced vertical line marks the 500 bp distance from SoT.

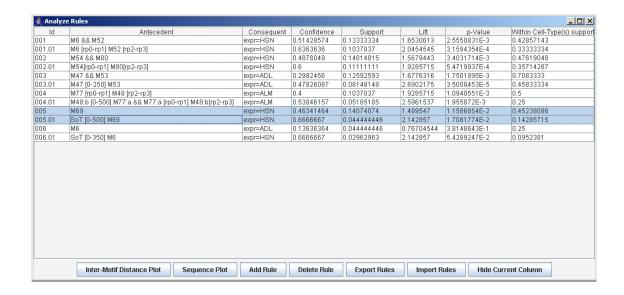


Figure 6.12: Analysis frame providing a comparison of the interestingness of the specialized rule, Rule (6.11), with the base rule, Rule (6.5).

Similarly in Figure 6.13, observe that many genes lack points in the top part in the 0-350 bp region of the plot, that is, a distance from SoT of 0-350 bp. This implies that the occurrence of motif 6 within 350 bp from the SoT may positively influence gene expression in cell HSN. Subsequent addition of the following corresponding specialization to the analysis frame enables the user to compare the interestingness of the rule to that of the base rule (Figure 6.14).

SoT 
$$[0-350]$$
 M6  $\Rightarrow$  expr=HSN[Conf. = 0.6666667, Supp. = 0.02962963] (6.12)

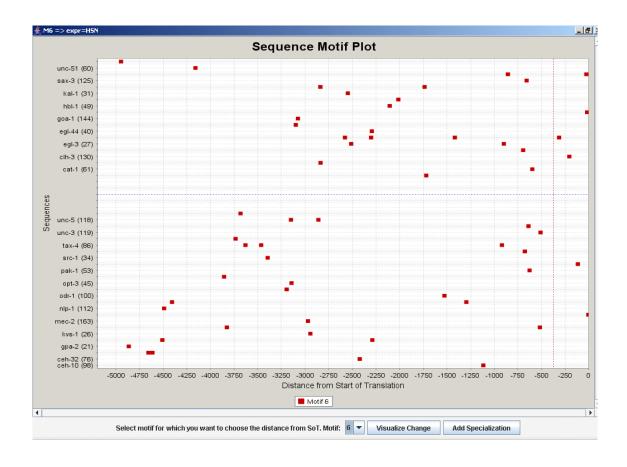


Figure 6.13: Sequence plot for the base rule  $M6 \Rightarrow \exp r = HSN$ .

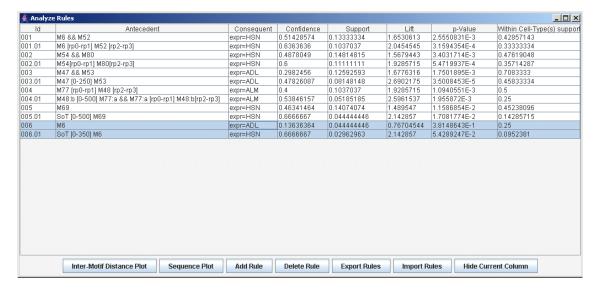


Figure 6.14: Analysis frame providing a comparison of the interestingness of the specialized rule, Rule (6.12), with the base rule, Rule (6.6).

# 6.2.4 Experimental results

As mentioned all along the analysis phase, an important feature which aids the exploratory analysis is that as soon as a specialization is added to the analysis frame using any of the visualization plots the different measures of interestingness of the newly added specialization are calculated. Thus, the domain user can instantly observe whether the specialized rule is better or worse on a specific metric and by how much. For instance, Figure 6.15 lists all the base rules and their corresponding specializations as they would appear in the analysis frame with the different measures of interestingness computed over the **training data**. At this point the user could save the rule set using the 'Export Rules' option from the analysis frame. This saved rule set can later be imported into the 'Associative Classifier' within the WPI-Weka system to test the classification accuracy over a set of novel gene sequences (test dataset) to estimate the predictive power of the specializations discovered. It is worth noting that at this point we have established the process which can be used to identify relationships which are interesting at least over the training data. Subsequently the user might want to evaluate the quality of the relationships discovered by using a test set either via the associative classifier which would provide the classification accuracy of the specialized rules or evaluate the different measures of interestingness using the VSM. Since the functionality to support associative classification is currently work under progress as a part of another effort here at WPI [Rudss], we decided to use the VSM to evaluate the strength of the relationship. Figure 6.16 lists the different measures of interestingness over the **test dataset** by using the VSM. This helps to determine if the specializations are really interesting, or if they are a case of overfit to the training data. Observe specifically the various measures for rules 1.01, both of which have a positive lift and has all the measures of interestingness as good as the base rule. Given that no extensive process was

Id	Antecedent	Consequent	Confidence	Support	Lift	p-Value	Within Cell-
							Type(s) sup-
							port
001	M6 && M52	expr=HSN	0.51428574	0.13333334	1.6530613	2.5550831E-3	0.42857143
001.01	M6 [rp0-rp1] M52 [rp2-rp3]	expr=HSN	0.6363636	0.1037037	2.0454545	3.1594354E-4	0.33333334
002	M54 && M80	expr=HSN	0.4878049	0.14814815	1.5679443	3.4031714E-3	0.47619048
002.01	M54[rp0-rp1] M80[rp2-rp3]	expr=HSN	0.6	0.11111111	1.9285715	5.4719937E-4	0.35714287
003	M47 && M53	expr=ADL	0.2982456	0.12592593	1.6776316	1.7501895E-3	0.7083333
003.01	M47 [0-250] M53	expr=ADL	0.47826087	0.08148148	2.6902175	3.5008453E-5	0.45833334
004	M77 [rp0-rp1] M48 [rp2-rp3]	expr=ALM	0.4	0.1037037	1.9285715	1.0940551E-3	0.5
004.01	M48:b [0-500] M77:a &&	expr=ALM	0.53846157	0.05185185	2.5961537	1.955872E-3	0.25
	M77:a [rp0-rp1] M48:b[rp2-						
	rp3]						
005	M69	expr=HSN	0.46341464	0.14074074	1.489547	1.1586854E-2	0.45238096
005.01	SoT [0-500] M69	expr=HSN	0.6666667	0.04444446	2.142857	1.7081774E-2	0.14285715
006	M6	expr=ADL	0.13636364	0.04444446	0.76704544	3.8148643E-1	0.25
006.01	SoT [0-350] M6	expr=HSN	0.6666667	0.02962963	2.142857	5.4289247E-2	0.0952381

Figure 6.15: Statistical measures over training data.

Base rules alongside their corresponding specializations and various measures of interestingness calculated over the training data, which help identify which specializations are interesting, and how much more interesting.

followed to divide the instances between the test set and the training set we believe this rule still might be an interesting discovery. Also we have hereby established the process that domain users might follow to verify the strength of a relationship which seems to be interesting based on the training data. It is important to understand at this point that this implementation equips the domain user with a tool and a work flow to identify potential relationships. The actual quality of the specializations is again contingent on many other things. For instance, the quality of the motifs elicited as well as the mining process both of which are outside the scope of this project. It is worth noting that both these areas are being researched in separate efforts here at WPI.

Id	Antecedent	Consequent	Confidence	Support	Lift	p-Value	Within Cell-
							Type(s) sup-
							port
001	M6 && M52	expr=HSN	0.6666667	0.16666667	2.0	1.5729921E-1	0.5
001.01	M6 [rp0-rp1] M52 [rp2-rp3]	expr=HSN	0.6666667	0.16666667	2.0	1.5729921E-1	0.5
002	M54 && M80	expr=HSN	0.2	0.083333336	0.6	4.0762594E-1	0.25
002.01	M54[rp0-rp1] M80[rp2-rp3]	expr=HSN	0.33333334	0.083333336	1.0	1E0	0.25
003	M47 && M53	expr=ADL	0.5	0.25	1.2	5.5818464E-1	0.6
003.01	M47 [0-250] M53	expr=ADL	0.33333334	0.083333336	0.8	7.3531669E-1	0.2
004	M77 [rp0-rp1] M48 [rp2-rp3]	expr=ALM	0.6666667	0.16666667	2.0	1.5729921E-1	0.5
004.01	M48:b [0-500] M77:a &&	expr=ALM	0.0	0.0	0.0	1E0	0.0
	M77:a [rp0-rp1] M48:b[rp2-						
	rp3]						
005	M69	expr=HSN	1.0	0.16666667	3.0	2.8459734E-2	0.5
005.01	SoT [0-500] M69	expr=HSN	1.0	0.083333336	3.0	1.3964939E-1	0.25
006	M6	expr=ADL	0.0	0.0	0.0	1E0	0.0
006.01	SoT [0-350] M6	expr=HSN	0.0	0.0	0.0	1E0	0.0

Figure 6.16: Specializations and various measures of interestingness evaluated over the  ${f test}$  data.

# Chapter 7

# Conclusions and Future Work

The goal of this thesis was to computationally enable the discovery of gene expression association rules based on several biological hypotheses. We designed and implemented a tool that helps domain experts visualize genetic data in the context of various biological hypotheses and perform exploratory analysis of data to discover specialized gene expression association rules. This process of exploratory analysis allows for post mining specialization of association rules, which alleviates some of the shortcomings of incorporating hypothesis-driven information into the mining process.

This work sketched out a process work flow for exploratory analysis of genetic data to discover interesting association rules. This work facilitates the process of identifying interesting rules beyond the conventional support-confidence framework by adding other measures of interestingness to the analysis process. We established via the experimental evaluation (Section 6) that the data visualization capabilities provided by our tool helps human experts in identifying hypothesis-driven specialized rules that score better than their generic counterparts in terms of different measures of interestingness. In addition to the visual mining tool, this work pro-

vides an updated genetic dataset which is an important resource for future research.

Future work would involve verifying the scalability of the tool to ensure that the tool performs well with a substantially larger dataset (e.g., so as to support a genetic database from micro array experiments). Another potential area worth investigating is to provide the functionality wherein the tool suggests patterns to the user based on the data being visualized. For instance, the approach proposed in [Ice03] could be used in an inter-motif distance plot to suggest specialization tips (visual or textual) to the domain user based only on the section of the data relevant in the context of the rule being visualized.

# Bibliography

- [AIS93] R. Agrawal, T. Imielinski, and A. Swami. Mining association rules between sets of items in large databases. In *Proc. of the ACM SIGMOD Conference on Management of Data*, pages 207–216, Washington, D.C., May 1993. ACM.
- [Alv03] Sergio A. Alvarez. Chi-squared computation for association rules: Preliminary results. Technical Report BC-CS-2003-01, Computer Science Department, Boston College, July 2003.
- [AS94] Rakesh Agrawal and Ramakrishnan Srikant. Fast algorithms for mining association rules. In *Proc. of the 20th International Conference on Very Large Databases*, Sep 1994.
- [BE94] Timothy Bailey and Charles Elkan. Fitting a mixture model by expectation maximization to discover motifs in biopolymers. In *Proc. of the Second International Conference on Intelligent Systems for Molecular Biology*, pages 28–36. AAAI Press, August 1994.
- [BFG+03] John Baird, Jay Farmer, Rebecca Gougian, Ken Monterio, and Paul Young. Motif analysis of gene expression. Undergraduate Graduation Project (MQP), 2003.

- [BLA] Wormbase sequence search. BLAST search Homepage: http://www.wormbase.org/db/searches/blat.
- [BLT02] Kristin Blitsch, Ben Lucas, and Sarah Towey. Computational analysis of gene expression. Undergraduate Graduation Project (MQP), 2002.
- [BMS97] Sergey Brin, Rajeev Motwani, and Craig Silverstein. Beyond market baskets: Generalizing association rules to correlations. In Joan Peckham, editor, SIGMOD 1997, Proceedings ACM SIGMOD International Conference on Management of Data, May 13-15, 1997, Tucson, Arizona, USA, pages 265–276. ACM Press, 1997.
- [Ice03] Aleksandar Icev. DARM: Distance-based association rule mining. Master's thesis, Worcester Polytechnic Institute, May 2003.
- [IRR03] A. Icev, C. Ruiz, and E. Ryder. Distance-enhanced association rules for gene expression. In Proc. 3rd ACM SIGKDD Workshop on Data Mining in Bioinformatics (BIOKDD2003). Held in conjunction with the 9th Intl. Conf. on Knowledge Discovery and Data Mining (KDD2003), pages 34–40, Washington DC, USA, Aug. 2003.
- [JAC95] Liu JS, Neuwald AF, and Lawrence CE. Bayesian models for multiple local sequence alignment and Gibbs sampling strategies. *Journal of the American Statistical Association*, 90(432):1156–1169, Dec 1995.
- [JCC] Javacc. JavaCC Homepage: https://javacc.dev.java.net/.
- [JFr] Jfreechart. JFreeChart Homepage: http://www.jfree.org/jfreechart/.
- $[MAS] \qquad MAST \qquad online. \qquad MAST \qquad Homepage: \\ http://meme.sdsc.edu/meme/website/mast-intro.html.$

- [MEM] MEME online. MEME Homepage: http://meme.sdsc.edu/meme/website/intro.html.
- [Mor98] S. Morishita. On classification and regression. In Proc. of the First Intl Conf on Discovery Science – Lecture Notes in Artificial Intelligence, pages 40–57. Discovery Science, 1998.
- [Mot] MotifSampler online. MotifSampler Homepage: http://homes.esat.kuleuven.be/~thijs/Work/MotifSampler.html.
- [MPPT01] B. Murphy, D. Phu, I. Pushee, and F. Tan. Motif-and expression-based classification of DNA. Undergraduate Graduation Project (MQP), 2001.
- [PR05] K.A. Pray and C. Ruiz. Mining expressive temporal associations from complex data. In Proc. of the International Conference on Machine Learning and Data Mining, pages 384–394, Leipzig, Germany, July 2005. MLDM.
- [RSA] RSA: Regulatory sequence analysis tools. RSA Homepage: http://rsat.ulb.ac.be/rsat/.
- [Rudss] Jonathon Rudolph. Gene expression rule modeling. Undergraduate Graduation Project (MQP), In progress.
- [Sho01] Christopher Shoemaker. Mining association rules over set-valued data.

  Master's thesis, Worcester Polytechnic Institute, May 2001.
- [Wor] Wormbase release ws119. WormBase Homepage: http://www.wormbase.org.
- [WPI] WPI-Weka system http://sourceforge.wpi.edu.
  Project@Repository: Bioinformatics@wekacode.

# Appendix A

# Sample ARFF File

```
Orelation test_ASAS
Cattribute gene string
@attribute M1 string
%Width = 8
%Consensus = CCGGCAAT
%Log-Odds Matrix:
%-689 217
               -684
                      -91
%-689
       246
               -684
                      -690
%-689
       -685
               264
                      -690
%-689
       -685
               264
                      -690
%-21
       200
               -684
                      -690
%165
       -685
               -684
                      -690
%165
       -685
               -684
                       -690
%-689
       -685
               -684
                      153
@attribute M2 string
%Width = 8
%Consensus = GGAAAACG
%Log-Odds Matrix:
%-736 -731
               264
                      -737
%-736 -731
               264
                      -737
%151
               -729
       -89
                      -737
%166
       -731
               -729
                      -737
%166
       -731
               -729
                      -737
%166
```

-731

-729

-737

%-736 232 -729 -181 %-736 -731 221 -41

@attribute M3 string

%Width = 8

%Consensus = GAGAGAGA

%Log-Odds Matrix:

%-689 -685 264 -690 %128 -685 50 -690 %-21 -685 218 -690 %165 -685 -684 -690 %-689 -685 264 -690 %128 -685 50 -690 %-689 -685 264 -690 %165 -685 -684 -690

@attribute M4 string

%Width = 10

%Consensus = GAGArAGAGA

%Log-Odds Matrix:

%-683 -679 263 -683 %143 -679 -16 -683 %-683 -679 263 -683 %158 -679 -172 -683 %44 -91 157 -683 %135 -679 -678 -84 %-683 -679 263 -683 %107 -679 -678 -4 %-683 -679 263 -683 %126 -679 57 -683

@attribute M5 string

%Width = 10

%Consensus = GAGAGrsAGn

%Log-Odds Matrix:

%-727 -722 264 -728 %150 -722 -62 -728 %-727 -235 259 -728 %166 -722 -720 -728

%-216	42	210	-728
%89	-722	137	-728
%-727	131	178	-728
%112	-722	59	-228
%-727	-722	264	-728
%80	-39	95	-728

@attribute M6 string

%Width = 10

%Consensus = rGAAGAAGAn

%Log-Odds Matrix:

%85	-679	125	-278
%-683	-679	263	-683
%135	-679	-16	-278
%165	-679	-678	-683
%-683	-679	263	-683
%165	-679	-678	-683
%143	-679	-678	-125
%-683	-679	263	-683
%151	-91	-678	-683
<b>%</b> 85	-679	105	-182

@attribute M7 string

%Width = 12

%Consensus = AAwTTGCCGGAA

%152	-685	-80	-690
%152	-685	-80	-690
%52	-685	-684	66
%-689	-685	-684	153
%-689	-685	-23	132
%-120	1	208	-690
%-689	246	-684	-690
%-120	200	-23	-690
%-689	-685	257	-284
%-689	-685	264	-690
%165	-685	-684	-690
%152	-98	-684	-690

@attribute M8 string

%Width = 12

%Consensus = rAGAAGArGAAr

%Log-Odds Matrix:

<b>%</b> 46	-691	181	-696
%130	-691	44	-696
%-695	-691	264	-696
%166	-691	-690	-696
%159	-691	-185	-696
%-126	-691	243	-696
%166	-691	-690	-696
%83	-691	129	-291
<b>%</b> -5	-691	211	-696
%122	-691	70	-696
%166	-691	-690	-696
%60	-691	170	-696

@attribute M9 string

%Width = 12

%Consensus = GrGAGAGwGAGm

%Log-Odds Matrix:

%-91	-658	237	-662
<b>%</b> 49	-658	179	-662
%-91	-658	237	-662
%139	-658	6	-662
%-18	-658	216	-662
%148	-658	-657	-160
%-50	-658	227	-662
%81	-658	-150	18
%-662	-167	255	-662
%139	-658	-657	-103
%-662	-658	263	-662
%49	161	-657	-662

@attribute M10 string

%Width = 8

%Consensus = GGGnGGnG

%Log-Odds Matrix:

%-748 -742 264 -749

%-313	-742	259	-749
%-748	-742	264	-749
%-19	151	37	-749
%-748	-742	264	-749
%-748	-742	264	-749
%105	-138	78	-749
%-748	-742	264	-749

@attribute M11 string

%Width = 8

%Consensus = GGGAGrAG

%Log-Odds Matrix:

%-716	-711	264	-717
%-716	-711	264	-717
%-716	-711	264	-717
%122	-711	70	-717
%-716	-711	264	-717
%31	-711	192	-717
%113	-711	92	-717
%-716	-711	264	-717

@attribute M12 string

%Width = 8

%Consensus = GGGnGGAG

%Log-Odds Matrix:

%0	-777	209	-785
%-784	-777	264	-785
%-784	-777	264	-785
%0	147	-774	-90
%-784	-777	264	-785
%-784	-777	264	-785
%141	-19	-774	-785
%-784	-777	264	-785

@attribute M13 string

%Width = 10

%Consensus = rnGGGnGGAG

%Log-Odds Matrix:

%94 -711 129 -717

%-27	-711	157	-40
%-27	-711	220	-717
%-716	-711	264	-717
%-716	-711	264	-717
%-27	140	-710	-40
%-716	-711	264	-717
%-716	-711	264	-717
%138	-5	-710	-717
%-716	-711	264	-717

# @attribute M14 string

%Width = 10

%Consensus = GGGnGGnGnn

# %Log-Odds Matrix:

%-781	-773	264	-781
%-348	-773	260	-781
%-781	-773	264	-781
%-22	134	-24	-134
%-781	-773	264	-781
%-781	-773	264	-781
%104	-42	43	-781
%-781	-773	260	-360
%-781	72	76	33
%-22	43	60	-50

# @attribute M15 string

%Width = 10

%Consensus = AnnGGmGGAG

%115	-773	89	-781
%-37	-773	152	-21
%4	-773	202	-360
%-73	-773	234	-781
%-781	-773	264	-781
%15	143	2	-781
%-781	-773	264	-781
%-781	-773	264	-781
%121	-773	76	-781
%-781	-773	264	-781

@attribute M16 string

%Width = 12

%Consensus = GGnGGrnGrGGr

%Log-Odds Matrix:

%-614	-612	263	-615
%-614	-612	263	-615
%-78	-612	198	-90
%-175	-612	217	-90
%-614	-612	234	-90
%20	-612	198	-615
%-21	-612	198	-186
%-614	59	217	-615
%78	-612	149	-615
%-614	-612	217	-33
%-614	-612	249	-186
%20	-612	198	-615

@attribute M17 string

%Width = 12

%Consensus = AwrkGGGmGGAG

%Log-Odds Matrix:

%112	-742	-62	-73
%26	-742	11	38
%97	-235	111	-749
%-217	-39	148	0
%-748	-742	264	-749
%-748	-742	264	-749
%-748	-742	264	-749
<b>%</b> 89	119	-740	-749
%-217	-742	254	-749
%-61	-742	230	-749
%144	-742	-21	-749
%-748	-742	264	-749

@attribute M18 string

%Width = 12

%Consensus = kGrGkrrGkGkG

%-657	-141	190	-4
%-657	-654	219	-36
%75	-654	154	-658
%-657	-654	263	-658
%-657	-654	190	22
%56	-654	131	-134
%56	-654	173	-658
%-657	-43	243	-658
%-657	-654	173	44
%-657	-654	263	-658
%-657	-654	131	80
%-657	-654	263	-658

# @attribute M19 string

%Width = 8

%Consensus = GGGsGGrG

# %Log-Odds Matrix:

%-836	-825	264	-837
%-836	-825	264	-837
%-63	-825	228	-414
%-836	110	193	-837
%-836	-825	264	-837
%-92	-825	238	-837
%43	-825	184	-837
%-836	-825	264	-837

# @attribute M20 string

%Width = 8

%Consensus = GGGGGnGG

%-834	-823	264	-835
%-36	-823	224	-835
%-834	-823	264	-835
%-74	-823	234	-835
%-106	-823	241	-835
%-60	74	162	-835
%-834	-823	264	-835
%-834	-823	264	-835

@attribute M21 string

%Width = 8

%Consensus = GGGnGGrG

%Log-Odds Matrix:

%-52	-836	228	-849
%-848	-836	264	-849
%-848	-836	264	-849
%-22	111	101	-427
%-848	-836	264	-849
%-848	-836	264	-849
%64	-836	167	-849
%-848	-836	264	-849

@attribute M22 string

%Width = 10

%Consensus = GAArAAGAAG

%Log-Odds Matrix:

%-763	-756	264	-764
%129	-756	50	-764
%166	-756	-754	-764
%41	-756	186	-764
%116	-756	86	-764
%166	-756	-754	-764
%-763	-756	264	-764
%166	-756	-754	-764
%161	-756	-754	-335
%-763	-756	264	-764

@attribute M23 string

%Width = 10

%Consensus = GAAGAAGAAn

%-797	-789	264	-798
%166	-789	-786	-798
%166	-789	-786	-798
%-797	-789	264	-798
%166	-789	-786	-798
%151	-85	-786	-798
%-797	-789	264	-798

%134	-789	32	-798
%129	-789	49	-798
%-49	-53	202	-798

@attribute M24 string

%Width = 10

%Consensus = GnGrGsGrGG

%Log-Odds Matrix:

%-854	-842	264	-855
%-20	-842	190	-141
%-38	-842	224	-855
%23	-842	197	-855
%-4	-842	211	-855
%-854	104	197	-855
%-422	-842	262	-855
%29	-842	194	-855
%3	-842	208	-855
%-854	-842	264	-855

@attribute M25 string

%Width = 12

%Consensus = TGTGTrTGTGTG

%Log-Odds Matrix:

%-245	-685	-684	145
%-689	-685	264	-689
%-50	-685	-684	117
%-689	-685	264	-689
%-689	30	-684	117
%30	-685	193	-689
%-50	-685	-684	117
%-689	-685	264	-689
<b>%</b> 8	-685	-684	95
%-245	-685	255	-689
%-148	-685	-684	136
%-689	-685	264	-689

@attribute M26 string

%Width = 12

%Consensus = AAGAAGAAGAAG

#### %Log-Odds Matrix:

%138	-768	14	-776
%153	-103	-766	-776
%-775	-768	264	-776
%166	-768	-766	-776
%148	-768	-44	-776
%4	-768	208	-776
%116	-61	14	-776
%116 %133	-61 -103	14 -44	-776 -776
,,	01		
%133	-103	-44	-776
%133 %-775	-103 -768	-44 264	-776 -776

#### @attribute M27 string

%Width = 12

%Consensus = TGTGTGTGTGTG

# %Log-Odds Matrix:

%-50	-685	-684	117
%-689	-685	264	-689
%-148	-11	-684	106
%-18	-685	217	-689
%-689	-685	-684	153
%-689	-685	264	-689
%8	-685	-684	95
%8 %-50	-685 -685	-684 227	95 -689
70-		001	
% <b>-</b> 50	-685	227	-689
%-50 %-91	-685 -685	227 -684	-689 127

# @attribute M28 string

%Width = 8

%Consensus = nGGmGGAG

%-2	20	159	-738
%-737	-732	264	-738
%-737	-732	264	-738
<b>%</b> 50	107	-730	-99

%-737	-732	264	-738
%-737	-732	264	-738
%166	-732	-730	-738
%-737	-732	264	-738

@attribute M29 string

%Width = 8

%Consensus = GAAGAAGA

%Log-Odds Matrix:

%-664	-661	263	-664
%165	-661	-660	-664
%165	-661	-660	-664
%-664	-661	263	-664
%165	-661	-660	-664
%165	-661	-660	-664
%-664	-661	263	-664
%165	-661	-660	-664

@attribute M30 string

%Width = 8

%Consensus = GAGAGAGA

%Log-Odds Matrix:

%-679	-676	263	-680
%149	-676	-59	-680
%-679	-676	263	-680
%111	-676	-675	-12
%-679	-676	263	-680
%165	-676	-675	-680
%-679	-676	263	-680
%165	-676	-675	-680

Qattribute M31 string

%Width = 10

%Consensus = GATTTACGrG

%Log-Odds Matrix:

%-723 -717 258 -309 %166 -717 -716 -723 %-723 -219 -716 148 %-297 -717 -716 148

%-723	-717	-716	153
%166	-717	-716	-723
%-723	240	-716	-309
%-201	-717	252	-723
<b>%</b> 54	-717	175	-723
%-297	-717	258	-723

@attribute M32 string

%Width = 10

%Consensus = AGAAGAAGAw

 $\verb|`Log-Odds Matrix:|\\$ 

%166	-741	-739	-747
%-746	-741	264	-747
%166	-741	-739	-747
%166	-741	-739	-747
%-746	-741	264	-747
%166	-741	-739	-747
%110	-741	101	-747
%-746	-741	264	-747
%135	10	-739	-747
%29	-741	69	4

@attribute M33 string

%Width = 10

%Consensus = nAAGAAGAAG

%Log-Odds Matrix:

%-11	-707	186	-144
%116	-707	86	-712
%166	-707	-706	-712
%-712	-707	264	-712
%166	-707	-706	-712
%166	-707	-706	-712
%-712	-707	264	-712
%166	-707	-706	-712
%116	-707	-35	-103
%-712	-707	264	-712

@attribute M34 string

%Width = 12

#### %Consensus = AAGAnGAAGAAG

#### %Log-Odds Matrix:

%146	-653	-652	-143
%146	-150	-133	-656
%-228	-653	254	-656
%165	-653	-652	-656
%98	-653	64	-143
%-131	-653	233	-239
%165	-653	-652	-656
%165	-653	-652	-656
%-656	-653	263	-656
%135	-52	-133	-656
%146	-52	-652	-656
%-656	-653	263	-656

# @attribute M35 string

#### %Width = 12

#### %Consensus = ATGATGATGATG

#### %Log-Odds Matrix:

%117	-131	42	-637
%-637	-634	-634	153
%-637	-634	263	-637
%165	-634	-634	-637
%-112	-634	-634	131
%-637	24	228	-637
%154	-634	-634	-220
%-637	-634	-114	142
%-209	-634	252	-637
%165	-634	-634	-637
%-637	-634	-114	142
%-637	-33	241	-637

#### @attribute M36 string

#### %Width = 12

#### %Consensus = GAArAAGAAGAr

%-656	-653	263	-656
%165	-653	-652	-656
%124	-653	64	-656

%47	-653	180	-656
%165	-653	-652	-656
%146	-653	-652	-143
%-656	-653	233	-86
%146	-653	-35	-656
%165	-653	-652	-656
%-656	-653	263	-656
%111	-52	23	-656
%98	-653	122	-656

# @attribute M37 string

%Width = 8

%Consensus = GGGmGGnG

%Log-Odds Matrix:

%-570	-569	262	-571
%-570	-569	262	-571
%-570	-569	262	-571
%65	145	-568	-571
%-570	-83	247	-571
%-570	-569	262	-571
%91	14	32	-571
%-570	-569	262	-571

# @attribute M38 string

%Width = 8

%Consensus = AGGTAGGC

%Log-Odds Matrix:

%124	-633	64	-636
%-636	-633	263	-636
%-636	-633	263	-636
%-636	-633	-632	153
%124	-633	-632	-45
%-636	-633	263	-636
%-636	-633	263	-636
%-636	245	-632	-636

@attribute M39 string

%Width = 8

%Consensus = GAAGAAGA

#### %Log-Odds Matrix:

%-607	-605	263	-607
%165	-605	-604	-607
%165	-605	-604	-607
%-607	-605	263	-607
%165	-605	-604	-607
%165	-605	-604	-607
%-607	-605	263	-607
%165	-605	-604	-607

# @attribute M40 string

%Width = 10

%Consensus = GAAGAAGAAG

# %Log-Odds Matrix:

%-570	-569	262	-571
%132	-569	32	-571
%113	72	-568	-571
%-7	-569	211	-571
%164	-569	-568	-571
%164	-569	-568	-571
%-570	-569	262	-571
%164	-569	-568	-571
%164	-569	-568	-571
%-570	-569	262	-571

# @attribute M41 string

%Width = 10

%Consensus = GrAGmAGAAG

%-596	-594	263	-596
<b>%</b> 8	-594	204	-596
%165	-594	-593	-596
%-596	-594	250	-197
%65	119	-92	-596
%165	-594	-593	-596
%-596	-594	250	-197
%139	-11	-593	-596
%165	-594	-593	-596
%-596	-594	263	-596

@attribute M42 string

%Width = 10

%Consensus = GnAGGCAGGC

%Log-Odds Matrix:

%-644	-641	263	-644
%-235	-158	55	90
%165	-641	-640	-644
%-644	-641	263	-644
%-644	-641	263	-644
%-644	195	-640	-22
%127	-641	-141	-95
%-644	-641	245	-152
%-235	-3	225	-644
%-644	218	-640	-95

# @attribute M43 string

%Width = 12

%Consensus = AAGAArrAGAAG

%Log-Odds Matrix:

%145	-538	-34	-539
%164	-538	-537	-539
%-539	-538	262	-539
%145	-538	-34	-539
%164	-538	-537	-539
%97	-538	121	-539
%97	-538	121	-539
%164	-538	-537	-539
%-539	-538	262	-539
%164	-538	-537	-539
%164	-538	-537	-539
%-539	-538	262	-539

@attribute M44 string

%Width = 12

%Consensus = AGAAGAAGrAGA

%Log-Odds Matrix:

%164 -519 -519 -521 %-521 -519 261 -521

%164	-519	-519	-521
%164	-519	-519	-521
%-521	-519	261	-521
%164	-519	-519	-521
%116	-33	-16	-521
%-521	-519	261	-521
%84	-519	140	-521
%116	65	-519	-521
%-521	-33	239	-521
%116	65	-519	-521

@attribute M45 string

%Width = 12

%Consensus = GACGACGACGnC

%Log-Odds Matrix:

%-176	-195	242	-680
%137	-676	18	-680
%-21	191	-675	-284
%-680	-195	257	-680
%152	-676	-80	-680
%-680	217	-23	-284
%-79	-676	235	-680
%137	-195	-23	-680
%-680	246	-675	-680
%-21	-676	208	-284
%52	-676	99	-59
%-680	246	-675	-680

@attribute M46 string

%Width = 8

%Consensus = GnrGGnGG

%-722	-717	264	-723
%-43	-717	74	54
%21	-717	198	-723
%-164	-717	249	-723
%-722	-717	264	-723
%-43	146	-716	-36
%-722	-717	264	-723

%-722 -717 264 -723

@attribute M47 string

%Width = 8

%Consensus = GAGAArAG

%Log-Odds Matrix:

%-718 -713 264 -718 %119 -713 -711 -32 %-718 -713 264 -718 %166 -713 -711 -718 %166 -713 -711 -718 %89 -713 137 -718 %166 -713 -711 -718 %-718 -713 264 -718

@attribute M48 string

%Width = 8

%Consensus = TGAGAAAA

%Log-Odds Matrix:

%-743 -738 -736 153 -744 %-743 -738 264 %148 -738 -48 -744 %-743 -738 264 -744 %153 -107 -736 -744 %166 -738 -736 -744 %166 -738 -736 -744 %166 -738 -744 -736

@attribute M49 string

%Width = 10

%Consensus = ArAGrAnGAG

%Log-Odds Matrix:

%120 -676 77 -680 %20 -676 198 -680 %165 -676 -675 -680 %-680 -676 263 -680 %78 -676 150 -680 %128 -676 50 -680 %78 -676 77 -91

%-680	-676	263	-680
%165	-676	-675	-680
%-272	-676	257	-680

@attribute M50 string

%Width = 10

%Consensus = rGAArAAGA

%Log-Odds Matrix:

%28	-698	174	-212
%-703	-698	264	-703
%113	-698	94	-703
%142	-698	-5	-703
<b>%</b> 54	-698	174	-703
%166	-698	-697	-703
%166	-698	-697	-703
%135	-698	27	-703
%-703	-698	264	-703
%166	-698	-697	-703

@attribute M51 string

%Width = 10

%Consensus = GAGArnAAGA

%Log-Odds Matrix:

%-123	-717	243	-723
%107	-717	106	-723
%-722	-717	264	-723
%166	-717	-716	-723
%21	-717	198	-723
%100	-717	32	-103
%114	-717	90	-723
%134	-717	32	-723
%-722	-717	264	-723
%166	-717	-716	-723

@attribute M52 string

%Width = 12

%Consensus = GAAnAnGAAGAA

%Log-Odds Matrix:

%-33 -663 212 -270

%165	-663	-662	-667
%142	-663	-9	-667
%103	-663	112	-667
%165	-663	-662	-667
%92	-663	90	-175
%-667	-26	240	-667
%142	-663	-662	-118
%165	-663	-662	-667
%-667	-663	263	-667
%158	-663	-164	-667
%165	-663	-662	-667

## @attribute M53 string

%Width = 12

%Consensus = GAArAAGAAnrA

%Log-Odds Matrix:

%8	-688	205	-692
%166	-688	-687	-692
%166	-688	-687	-692
%25	-688	196	-692
%124	-688	64	-692
%159	-688	-687	-296
%-11	-688	205	-296
%166	-688	-687	-692
%166	-688	-687	-692
%-692	-208	196	-4
%98	-688	122	-692
%166	-688	-687	-692

# @attribute M54 string

%Width = 12

%Consensus = GArwGAGArrnG

%-713	-708	264	-714
%137	-708	16	-714
%44	-708	174	-318
%31	-708	-16	43
%-713	-708	264	-714
%117	-708	83	-714

%-154	-708	247	-714
%110	-34	16	-714
%102	-708	115	-714
%66	-34	115	-714
%76	-2	83	-714
%-713	-708	264	-714

@attribute M55 string

%Width = 8

%Consensus = rGGCGGnG

 $\verb|\label{log-Odds} Matrix:$ 

%83	-687	144	-691
%-691	-687	264	-691
%-126	-687	243	-691
%-53	194	-87	-691
%-691	-687	264	-691
%-691	-687	264	-691
%104	94	-686	-691
%-691	-687	264	-691

@attribute M56 string

%Width = 8

%Consensus = GGGmGGAG

%Log-Odds Matrix:

%-708	-703	258	-308
%-103	-703	240	-708
%-708	-703	264	-708
%77	135	-702	-708
%-200	-703	252	-708
%-4	-703	211	-708
%113	-23	-5	-708
%-708	-703	264	-708

@attribute M57 string

%Width = 8

%Consensus = GGnGnsGG

%Log-Odds Matrix:

%-678 -675 263 -679 %-678 -675 241 -125

%-113	88	170	-679
%-40	-675	224	-679
%8	8	157	-679
%-678	177	125	-679
%-678	-675	263	-679
%-678	-675	263	-679

@attribute M58 string

%Width = 10

%Consensus = nnnGGnGGnG

 $\verb|\Log-Odds Matrix|:$ 

%14	-202	192	-691
<b>%-</b> 85	-104	181	-97
%83	-5	70	-691
%-691	-687	264	-691
%-691	-104	250	-691
%-691	174	-87	-17
%-691	-687	264	-691
%-691	-687	257	-290
%60	53	70	-691
%-691	-687	264	-691

@attribute M59 string

%Width = 10

%Consensus = GrnnnGGCGG

 $\verb|\Log-Odds Matrix|:$ 

%-159	-718	203	-51
%39	-718	187	-723
%-60	-718	187	-73
%-723	42	195	-130
%-60	-39	78	14
%-159	-718	248	-723
%-723	-718	264	-723
%-723	185	110	-723
%-723	-718	264	-723
%-723	-718	264	-723

@attribute M60 string

%Width = 10

### %Consensus = rGnGGGGGkG

### %Log-Odds Matrix:

%25	-693	196	-697
%-33	-693	222	-697
%-285	88	-35	54
%-697	-693	264	-697
%-132	-693	222	-144
%-697	88	205	-697
%-697	-208	205	-24
%-697	-693	264	-697
%-59	-693	122	27
%-697	-693	264	-697

# @attribute M61 string

### %Width = 12

%Consensus = nGTGTGTGTGTG

# %Log-Odds Matrix:

%88	-599	6	-45
%-601	-599	263	-601
%-90	-599	-598	126
%-90	-599	236	-601
%-601	-599	-598	153
%-601	-599	236	-102
%-186	-599	64	94
%-33	-599	221	-601
%-601	-599	-92	140
%-601	-599	263	-601
%-601	-599	-92	140
%-601	-599	263	-601

## @attribute M62 string

### %Width = 12

%Consensus = wGTGnGknkGTG

%46	-687	-184	60
%-691	<b>-</b> 5	236	-691
%-279	-687	-686	147
%-691	-202	257	-691
%1/1	-697	70	10

%-691	-687	243	-138
%-691	-104	128	60
%14	-687	202	-691
%-691	-687	144	71
%-126	-687	243	-691
%-691	-687	44	118
%-691	-687	264	-691

@attribute M63 string

%Width = 12

%Consensus = GArAAGArrnnG

%Log-Odds Matrix:

%-45	-64	202	-708
%154	-122	-702	-708
%86	-703	140	-708
%154	-703	-104	-708
%166	-703	-702	-708
%-708	-703	264	-708
%166	-703	-702	-708
%96	-703	126	-708
%86	-703	140	-708
%54	-703	111	-83
%86	-703	94	-155
%-708	-703	264	-708

@attribute M64 string

%Width = 8

%Consensus = GGGmGGAG

%Log-Odds Matrix:

%-644	-641	263	-644
%-644	-641	263	-644
%-644	-641	263	-644
%16	118	55	-644
%-644	-158	254	-644
%-644	-641	263	-644
%165	-641	-640	-644
%-644	-641	263	-644

@attribute M65 string

### %Width = 8

%Consensus = GGGrGGrG

%Log-Odds Matrix:

%-667	-663	263	-667
%-667	-663	256	-270
%-667	-663	263	-667
%15	-663	148	-77
%-667	-663	263	-667
%-259	-663	256	-667
%103	-663	112	-667
%-667	-663	263	-667

## @attribute M66 string

%Width = 8

%Consensus = GkGkGrGG

%Log-Odds Matrix:

%-739	-734	264	-740
%-739	-734	201	4
%-25	-734	220	-740
%-739	-734	187	26
%-739	-734	264	-740
%82	-734	146	-740
%-739	-734	264	-740
%-739	-734	264	-740

# @attribute M67 string

%Width = 10

%Consensus = GAAGnAGAnG

%-680	-676	263	-680
%159	-676	-178	-680
%165	-676	-675	-680
%-680	-676	235	-91
%100	59	-80	-680
%144	-676	-23	-680
%-680	-676	263	-680
%165	-676	-675	-680
%100	-195	-80	-59
%-680	-676	263	-680

@attribute M68 string

%Width = 10

%Consensus = GAAGAAGAnG

%Log-Odds Matrix:

%-718	-713	264	-718
%166	-713	-711	-718
%166	-713	-711	-718
%-718	-713	264	-718
%161	-713	-217	-718
%119	-713	59	-323
%-159	-713	242	-323
%105	-713	110	-718
%61	-137	59	-73
%-718	-235	259	-718

@attribute M69 string

%Width = 10

%Consensus = GrGnGrGAGr

%Log-Odds Matrix:

%-735	-730	264	-736
%70	-730	160	-736
%-735	-730	264	-736
%32	-730	77	-4
%-137	-730	245	-736
%79	-730	130	-246
%-57	-730	229	-736
%142	-730	-8	-736
%-735	-730	264	-736
%52	-730	176	-736

@attribute M70 string

%Width = 12

%Consensus = CGATGCACCATG

%-686	226	-681	-138
%-126	-682	243	-686
%159	-682	-681	-290
%-686	-201	-681	147

%-686	-682	264	-686
%-686	239	-681	-290
%165	-682	-681	-686
%-686	226	-681	-138
%-686	239	-681	-290
%159	-682	-184	-686
%-686	-682	-681	153
%-53	-682	228	-686

@attribute M71 string

%Width = 12

%Consensus = AAGAAGAAGAnG

%Log-Odds Matrix:

%165	-649	-648	-652
%129	30	-648	-652
%-91	-649	227	-255
%165	-649	-648	-652
%139	-649	-52	-255
%-652	-649	263	-652
%148	-166	-149	-652
%139	-166	-52	-652
%-652	-649	263	-652
%165	-649	-648	-652
%30	62	47	-160
%-652	-649	263	-652

@attribute M72 string

%Width = 12

%Consensus = GAAGAAGAnGAA

%-652	-649	263	-652
%165	-649	-648	-652
%129	-649	47	-652
%-50	-649	227	-652
%165	-649	-648	-652
%165	-649	-648	-652
%-50	-649	227	-652
%148	-166	-149	-652
%95	-69	-648	-30

%-652	-649	263	-652
%129	-649	47	-652
%139	-166	-52	-652

@attribute M73 string

%Width = 8

%Consensus = GrkGGGGG

%Log-Odds Matrix:

%-718	-713	264	-718
%102	-713	115	-718
%-718	-713	164	54
%-718	-713	264	-718
%-718	-713	235	-94
%-718	-34	208	-94
%-718	-713	264	-718
%-718	-713	264	-718

@attribute M74 string

%Width = 8

%Consensus = GrAGAGAG

%Log-Odds Matrix:

%-697	-693	264	-697
%77	-693	151	-697
%146	-53	-691	-697
%-697	-693	264	-697
%139	-693	-691	-103
%-697	-693	264	-697
%159	-693	-191	-697
%-697	-693	264	-697

Qattribute M75 string

%Width = 8

%Consensus = kGnkGGGG

%Log-Odds Matrix:

%-198 -753 164 29 %-759 -753 -760 264 %94 -753 20 -70 %-759 -753 185 29 %-125 -753 244 -760

%-759	-176	256	-760
%-759	-753	264	-760
%-759	-753	264	-760

@attribute M76 string

%Width = 10

%Consensus = GGrGrnGGAG

%Log-Odds Matrix:

%13	-718	203	-723
%-216	-718	253	-723
%71	-718	159	-723
%-312	-718	259	-723
%39	-718	187	-723
%13	61	124	-723
%13	-718	203	-723
%-723	-718	264	-723
%155	-718	-120	-723
%-723	-718	264	-723

@attribute M77 string

%Width = 10

%Consensus = nAGAnGAAGA

%Log-Odds Matrix:

%8	-693	196	-296
%166	-693	-691	-697
%-697	-693	264	-697
%159	-208	-691	-697
%66	88	6	-697
%-697	-693	264	-697
%116	69	-691	-697
%166	-693	-691	-697
%-697	-693	264	-697
%139	-693	6	-697

@attribute M78 string

%Width = 10

%Consensus = GGnGGnGGAG

%Log-Odds Matrix:

%-38 -735 224 -741

%-740	-735	264	-741
%-57	-735	150	-4
%-740	42	224	-741
%-79	-25	205	-741
%-38	74	150	-741
%-740	-25	240	-741
%-330	-735	259	-741
%107	-735	19	-117
%-740	-735	264	-741

## @attribute M79 string

%Width = 12

%Consensus = TGnsTGTGyGnG

%Log-Odds Matrix:

%-702	-698	100	98
%-291	-698	258	-703
%-702	-58	100	70
%-65	114	132	-703
%-702	-698	-196	147
%-702	-698	264	-703
%-291	-698	-697	147
%-97	-213	231	-703
%-702	99	-697	89
%-702	-698	264	-703
%-291	-698	100	89
%-702	82	208	-703

# @attribute M80 string

%Width = 12

%Consensus = rAGAAGAAGAAG

%85	-675	142	-679
%165	-675	-674	-679
%-678	-675	241	-125
%165	-675	-674	-679
%117	-33	-674	-125
%-678	-189	256	-679
%126	-675	25	-277
%143	-675	-16	-679

```
%-72
               224
                       -277
       -675
%158
       -189
               -674
                       -679
%135
       -33
               -674
                       -277
%-678
       -675
               263
                       -679
```

@attribute M81 string

%Width = 12

%Consensus = GGGnGnrGAnnG

%Log-Odds Matrix:

%-718	-713	264	-718
%-14	-713	215	-718
%-33	-713	222	-718
%-33	-75	200	-718
%-718	-713	264	-718
%3	98	100	-718
%44	-713	183	-718
%-718	-2	235	-718
%131	-713	42	-718
<b>%</b> 3	-75	174	-318
%-81	83	129	-166
%-718	-2	235	-718

### @attribute expr string

#### @data

osm-6, '\forall', '\forall', '\forall 28:35\rangle', '\forall', '\

unc-97, '{}', '{2158:2165^1927:1934}', '{}', '{474:483}', '{}', '{2124:2133}', '
{}', '{2087:2098^349:360^331:342^90:101}', '{1149:1160}', '{}', '{}', '{}', '{}', '{}',
, '{}', '{}

'{}', '{}', '{}', '{571:578}', '{}', '{1544:1553^416:425^141:150}', '{1106:1115}', '{313:322}', '{}', '{160:171}', '{1022:1033}', '{}', '{}', '{991:998}', '{}', '

unc-32, '{}', '{}', '{155:162}', '{}', '{1255:1264}', '{}', '{18:29}', '{1061:10}'
72}', '{}', '

unc-86, '{4936:4943^4428:4435}', '{68:75}', '{}', '{1543:1552^1020:1029}', '{}',
 '{1824:1833^1172:1181}', '{}', '{754:765}', '{1838:1849}', '{}', '{}', '{}', '{}',
 ';', '{4694:4703}', '{}',

', '{}', '{}', '{}', '{4461:4472^1733:1744^730:741}', '{3670:3677^695:702}', '{}', '{4439:4446}', '{}', '{3750:3759^866:875}', '{}', '{}', '{}', '{}', '{4597:4608}', 'ALM^HSN'

unc-103, '{2159:2166}', '{}', '{3055:3062}', '{1165:1174}', '{4626:4635^669:678} ', '{}', '{3910:3921^3694:3705^1213:1224}', '{575:586}', '{3637:3648^3093:3104}' , `{}', `{}', `{}', `{}', `{}', `{3393:3402^1451:1460^369:378^75:84}', `{2045:20 56^1856:1867^904:915}', '{}', '{}', '{}', '{3489:3496}', '{2721:2728}', '{2969:2 978}', '{2461:2470^265:274}', '{}', '{761:772^11:22}', '{2772:2783^2638:2649^91: 102}', '{}', '{}', '{}', '{3252:3259^3220:3227^857:864}', '{2194:2203}', '{2979: 2988^1364:1373}', '{}', '{}', '{2064:2075^938:949^282:293}', '{2104:2115}', '{}' , `{}`, `{}`, `{}`, `{4706:4715^2789:2798}`, `{4953:4962^2218:2227^1135:1144^104 5:1054}', '{2923:2934^125:136}', '{3679:3690^3518:3529^2748:2759^2558:2569}', '{ 4531:4542^4507:4518^4393:4404^3110:3121^2606:2617}', '{}', '{3042:3049}', '{3983 ^700:709}', '{2007:2016^1277:1286}', '{}', '{3063:3074^2026:2037^1073:1084^839:8 50}', '{3781:3792^3354:3365^3145:3156^3010:3021}', '{4231:4242^3764:3775^387:398} }', '{4378:4385}', '{235:242}', '{4315:4322^3806:3813^2096:2103}', '{4466:4475^4 454:4463^187:196}', '{4117:4126}', '{684:693}', '{145:156}', '{503:514}', '{3960} :3971^2544:2555^2495:2506^1352:1363}', '{}', '{}', '{}', '{2626:2635^829:838}', '{2711:2720}', '{419:428}', '{}', '{}', '{2863:2874}', '{4486:4493^1945:1952}', '{}', '{}', '{199:208}', '{}', '{}', '{488:499}', '{}', '{}', 'HSN^PHA^ADL^ASK'

unc-129, '{1022:1029^523:530^277:284}', '{3597:3604^1177:1184}', '{}', '{2711:27
20^1954:1963}', '{2758:2767}', '{654:663}', '{3216:3227^18:29}', '{1707:1718^565}
:576}', '{3525:3536}', '{}', '{}', '{}', '{99:108}', '{}',

tax-6, '{}', '{749:756^337:344}', '{}', '{262:271}', '{419:428}', '{}', '{658:66}
9}', '{703:714}', '{}', '{}', '{}', '{120:127}', '{}', '{}', '{}', '{}', '{}', '{}', '

{}', '{}', '{}', '{786:793}', '{}', '{}', '{}', '{}', '{83:94}', '{372:383}', '{}', '{1283:1290}', '{200:207}', '{}', '{}', '{}', '{}', '{}', '{1041:1052}', '{630:641}', '418^287:298}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{167:178}', '{}', '{771}:782}', '{470:477}', '{497:504}', '{}', '{214:223}', '{}',

unc-76, '{1201:1208}', '{910:917}', '{}', '{439:448^159:168}', '{}', '{}', '{167 3:1684^1159:1170^953:964^921:932}', '{2049:2060^1837:1848^510:521}', '{693:704^5 98:609^423:434}', '{}', '{}', '{}', '{}', '{724:733}', '{}', '{}', '{}', '{}', '{}', ' {}', '{}', '{}', '{}', '{}', '{}', '{1055:1064}', '{681:692^410:421}', '{}', '{}', '{} ', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{1875:1886}', '{}', ' }', '{}', '{}', '{1719:1730}', '{2134:2145^586:597}', '{934:945^225:236^73:84}', '{}', '{1646:1653}', '{}', '{}', '{102:111}', '{}', '{}', '{1983:1994}', '{1783 :1794^52:63^22:33}', '{}', '{}', '{1932:1939}', '{179:188}', '{876:885}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{114 :125}', '{}', '{818:825^272:279}', '{493:500}', '{547:556}', '{333:342^143:152}' , '{480:489}', '{641:652}', '{312:323^240:251}', '{}', 'HSN^CAN' ttx-3, '{}', '{1646:1653}', '{}', '{1803:1812^51:60}', '{}', '{1313:1324}' , '{2352:2363^1450:1461}', '{}', '{}', '{}', '{4419:4426}', '{}', '{3890:3899}', '{3977:3986^3128:3137^1996:2005}', '{}', ' }', '{4394:4403}', '{}', '{2322:2333}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}' , '{}', '{}', '{1528:1539}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{3643:3654}', '{}', '{}', '{1517:1524}', '{4525:4532}', '{3287:3294}', '{1205:1214}', '{452:46 1}', '{}', '{1486:1497}', '{3556:3567}', '{1172:1183}', '{}', '{}', '{}', '{1499 :1508}', '{}', '{2525:2534^701:710}', '{1558:1569}', '{143:150}', '{3268:3275}', '{4483:4490}' , '{}', '{1573:1582^1112:1121}', '{}', '{}', '{}', '{4428:4439}', 'ASI^ADL'

unc-73, '{3306:3313^922:929^459:466}', '{}', '{}', '{}', '{}', '{1003:1012}', '{1250:1}
259}', '{1548:1559^1491:1502}', '{4088:4099}', '{4164:4175^3751:3762^3504:3515}'
, '{}', '{}', '{3819:3826}', '{}', '{}', '{}', '{}', '{}', '{3958:3969}', '{}',
'{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{3909:39}
20}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}', '{}',
'{}', '{}'

'{}', '{}', '{854:865^192:203}', '{}', '{}', '{}', '{}', '{}', '{}', '{4209:4218}', '{
2074:2085}', '{}', '{442:453}', '{4111:4118^1153:1160^907:914}', '{}', '{}', '{}', '{}', '{}', '{1025:1034}', '{}', '{69:80}', '{}', '{4008:4019}', 'ALM^HSN^CAN'

osm-9, '{3944:3951^2699:2706^1460:1467}', '{3545:3552^2368:2375}', '{}', '{203:2}

12}', '{4121:4130}', '{}', '{4836:4847^2925:2936}', '{}

# Appendix B

# Perl script to convert probability matrix to log odds matrix.

```
#!/usr/local/bin/perl -w
use strict;
use Math::Complex;

#

#

my @args = @ARGV;

if(scalar(@args) != 3){
        print "\n The # of command line arguments supplied not correct";
        print "\nUsage: convert <Prob Matrix motif file> <background Probability File> <output file name>\n";
        exit(0);
}

my $probMatrix = shift @args;
my $percentage is shift @args;
my $percentage is shift @args;
my $percentage is shift @args;
my $outputFile= shift @args;
sub slurp {
        local $/ = undef;
```

```
open my $fh, $_[0] or die "Can't open $_[0]: $!";
      my $slurp = <$fh>;
      return \$slurp;
}
# Open Gene Names file
open(PROB, $probMatrix) || &return_error("File Error", "Unable to open " . $probMatrix . ". Reason $!");
# Open Sequence File
#open(BG, $bgFrequencyFile) || &return_error("File Error", "Unable to open " . $bgFrequencyFile . ". Reason $!");
# Open Gene Names file
open(FD, "> $outputFile") || &return_error("File Error", "Unable to open " . $outputFile . ". Reason $!");
my @bg;
my $bgline = slurp($bgFrequencyFile);
#foreach $bgline (<BG>){
 #print $bgline;
#last;
#}
print join(@bg);
my @parts;
foreach my $line(<PROB>){
      #if($line =~ /^#/){
             print FD $line;
             next;
      #}
      for(my $i=0; $i<4; $i++){
                   print FD round(logn( $parts[$i]/$bg[$i], 2) * 100);
                   print FD "\t";
             }
             print FD "\n";
      }else{
```

```
print FD $line;
               next;
       }
}
sub trim {
        my @out = @_;
         for (@out) {
                s/^\s+//;
                s/\s+$//;
         }
         return wantarray ? @out : $out[0];
}
sub round {
   my($number) = shift;
   return int($number + .5 * ($number <=> 0));
}
```

# Appendix C

# User Guide

# C.1 Analysis Frame

The visualization and specialization modules (VSM) could either be invoked from the mining interface of WPI-Weka system or could be invoked as a standalone application using exported set of mined association rules, the associated MAST results (HTML format) and a list of gene names alongside the known expression patterns. The primary interface of the VSM is the Analysis frame, that is the first screen to be displayed when VSM is invoked. See Figure C.1. We explain the Analysis frame below.

The analysis frame loads with two sections, the **Rules** area and the **Commands** area as shown in Figure C.1. We explain the Rules area below and we explain each of the options in the Commands area in subsequent subsections. The Rules area is used to display base association rules along with the corresponding values for certain measures of interestingness. The design is extensible, that is, new measures of interestingness could be added in the future with minimal code changes. In the current state, a rule tuple consists of the following items:

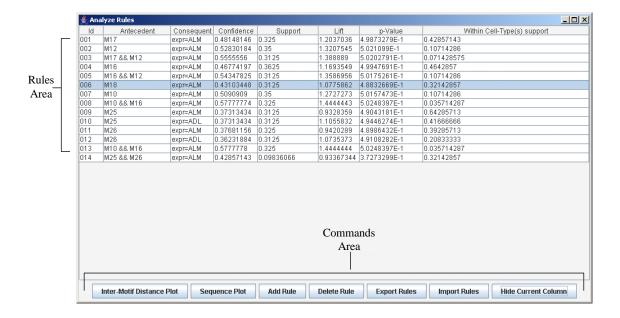


Figure C.1: Sample Analysis Frame.

- Id this is a unique id assigned to the rule. The usability of this field increases once the user starts to generate specializations from the rule, as the Id column helps us trace the history or the specialization path of new rules.
- Antecedent The left-hand side of the rule. It contains the motifs present in the rule.
- Consequent The right-hand side of the rule. It contains the cell-types predicted by the rule.
- Support As discussed in Section 1.2, Rule 1.1; the support of the rule is one of the popular scales to measure the interestingness of the rule
- Confidence Confidence is the other popular metric to measure the interestingness of the rule.
- Lift The lift value of an association rule is another measure to try to quantify the interestingness of the rule. It is defined as the ratio of the confidence of the

rule and the support of the consequent of the rule [BMS97]. In other words

$$lift(rule) = p(consequent|antecedent)/p(consequent)$$

- **p-Value** The p-value of the rule is the probability that the correlation between the antecedent and the consequent is due to chance by using the chi square test.
- Within Cell-Type Support Provides the support of the rule among only those instances of the data that contain the consequent of the rule.

The Commands area of the Analysis frame provides buttons to perform a range of functions. Each of the following subsections describe each of these functions provided by the visualization extensions via the analysis frame. It is important to note that most of these functions are invoked in the context of a specific rule and so it is necessary to select a rule in the rules area of the analysis frame before we invoke a command.

# C.2 Inter-Motif Distance Plot

Selecting a Rule in the rules area and then invoking the inter-motif distance plot via the button with the same label, lets a user visualize the data in the context of the rule from a inter-motif distance perspective. This action enables a user to perform exploratory analysis in the context of the hypothesis - "Inter-motif distance influences gene expression".

On invoking this command a new frame with the pairwise inter-motif distance plot(s) is displayed. It displays one graph for each pair of motifs in the rule (selected

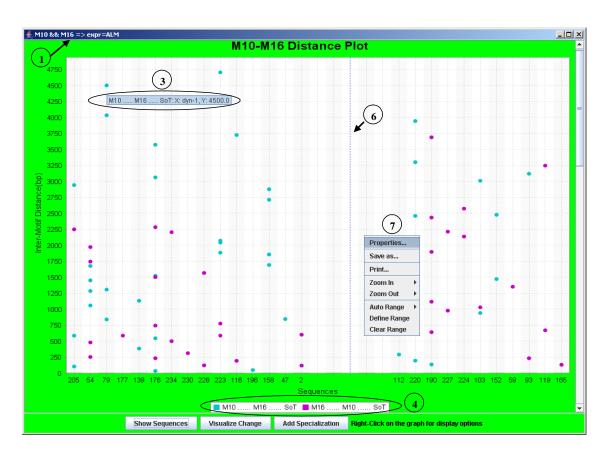


Figure C.2: Sample Inter-Motif Distance Frame - The numeric pointers refer to the enumerated text explaining Inter-Motif Distance Plot.

in the Analysis Frame). For sake of simplicity we start with a rule with only two motifs and we revisit plots originating from rules consisting of more than two motifs in item later in the section. We enlist below the highlights of the information displayed in an inter-motif distance plot and the numeric annotations in Figure C.2 are references to the information in the following enumeration.

- 1. Each graph is displayed with the rule used to establish the context as the title of the frame.
- 2. Each graph displays the pairwise inter-motif distance plots. For instance, in Figure C.2 the rule consists of motifs M10 and M16. So for each instance of M10 on a gene, a distance value from every instance of M16 is computed. Each

- such value corresponds to a point on the graph with distance being plotted on the y-axis and the x-axis is an id for the gene in question.
- 3. Rolling your mouse over any such data point displays the relevant gene name and the distance computed.
- 4. Each graph could potentially contain points in two colours. The legend explains the difference. Each point is a distance of an instance of M10 from an instance of M16 but the color helps identify the order in which these motif instances occur in the gene sequence relative to the Start of Transcription(SoT).
- 5. Each graph lists only those genes on the X-axis, that support the antecedent of the rule. That is, genes whose promoter regions contain at least one instance of both motifs.
- 6. Another mechanism to aid visual exploration is that each graph is sliced into two parts by a dotted line. The genes in the left part are the ones that support the consequent of the rule and hence support the rule. The ones on the right are the genes that only support the antecedent of the rule. This provides the user with an easy mechanism to discover inter-motif distance based patterns on the left part of the plot that are not as frequent on the right part as this would let us explore specializations with improved classification accuracy(and/or confidence).
- 7. We used the charting library, JFreeChart [JFr], as the charting infrastructure for the visualization extensions. This was an obvious choice because it was an open source, well-documented API, supporting a wide range of chart types with a flexible design that is easy to extend. A right-click on the graph area displays a popup menu with the following options:

- **Zoom** Lets you zoom in or out on the graph.
- Range Lets the user change the scale of either axis.
- Save Lets the user save an interesting graph as an image.
- Define Range This is an important extension we made to the charting infrastructure that lets the user define, in a graphical fashion, the intermotif distance to be used in the specialization. An inter-motif distance based specialization places conditions on the distance between instances of the motifs involved. For instance, it could be worth noting that there are significantly more data points with an inter-motif distance value between 0 and 500 in the left part of the Figure C.2 as compared to the same distance range in the right-hand side. The definition of this distance condition is in the form of a range, for instance, (0-500). Selecting this option from the menu changes the graph to a range define mode and a subsequent click and drag can be used to define the range.
- Clear Range Another extension to the charting infrastructure which lets a user clear a currently defined range providing an option to redefine a range.
- 8. Once the user has utilized the dotted separation and inter-motif distance plots to identify a range of interest, for instance a range of (0-500) between motifs M10 and M16, the "Define Range" option from the pop-up menu can be used to graphically define this range. Once a range has been defined for a plot, it is highlighted on the graph in a shade of gray. For instance, refer to Figure C.3 numerical annotation 8.
- 9. Even after a range has been defined the data being visualized is in the context of the original rule. At this point the user can invoke the "Visualize Change"

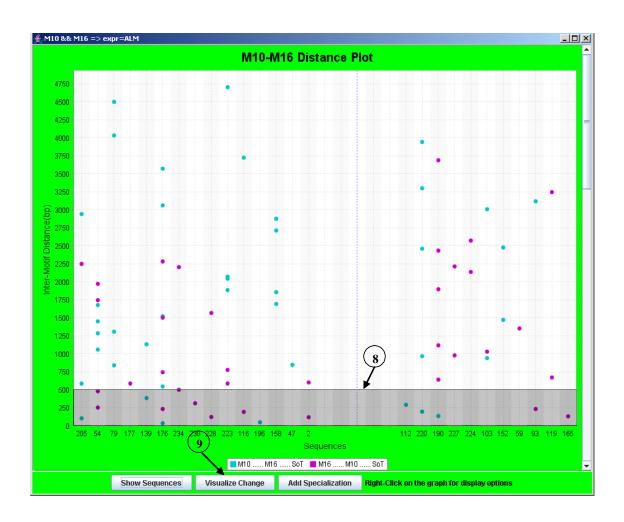


Figure C.3: Inter-Motif Distance Frame depicting an inter-motif range of 0-500 bp for Motif pair M10 and M16.

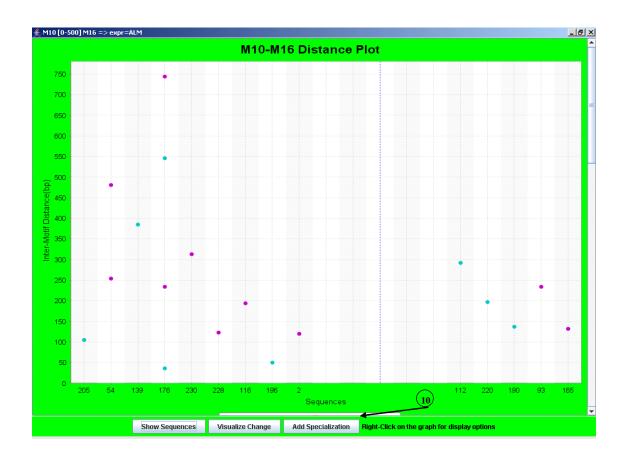


Figure C.4: Visualize command invoked inter-Motif distance plot displaying data in the context of the specialised rule M10 (0-500) M16  $\Rightarrow$  expr = ALM.

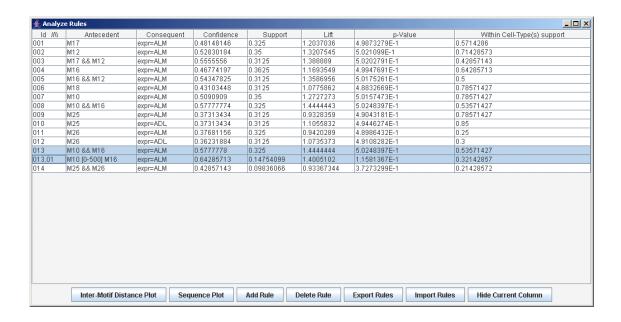


Figure C.5: A row representing the addition of a specialization to the Analysis Frame.

(Figure C.3 numerical annotation 9) command to visualize the data in the context of the specialization rather than in the context of the original rule. For instance Figure C.4. It is worth noting that the title of the new window is indicating the new context.

10. If the user finds this specialization (Figure C.4) of interest, the specialized rule can be added to the Analysis Frame using the "Add Specialization" command on the Inter-Motif distance plot. This causes a new entry to be inserted in the Analysis Frame with the following specialization

$$M10(0 - 500)M16 \Rightarrow expr = ALM \tag{C.1}$$

as shown in Figure C.5. Note that the Id field is auto-generated in a fashion that always lets a user trace back the steps in case we want to later recall which rule was used to derive the specialization. Also note the different measures of interestingness are computed for the specialized rule.

11. If the base rule consisted of more than two motifs, an inter-motif distance plot for each pair of motifs is displayed in the same frame (Figure C.6). Each chart or plot individually provides for defining relationships between a pair of motifs. In case multiple relationships are defined for more than one pair of motifs each motif is represented as a term and a collection of independent terms constitutes the specialized rule. Mechanism to define advanced relationship's between each term is also provided and we would revisit the topic later.

# C.2.1 Sequence Plot

Select a Rule in the rules area and then click the sequence plot button to visualize all the qualifying gene sequences in the context of the rule. This action enables a user to perform exploratory analysis in the context of the hypothesis - "Distance of motifs from the SoT influence gene expression". A qualifying gene sequence is one that has that has at least one instance of each motif that appears in the rule (selected in the Analysis Frame). Invoking this command causes a new frame with the sequence plot overlaid with the motif information to be displayed. We enlist below the highlights of the information displayed in an inter-motif distance plot and the numeric annotations in Figure C.7 are references to the information in the following enumeration.

- 1. Each graph is displayed with the rule used to establish the context as the title of the frame.
- 2. Displays the gene sequence plots with motif instances in the context of the rule. For example, in Figure C.7 the sequence plot displays all relevant gene

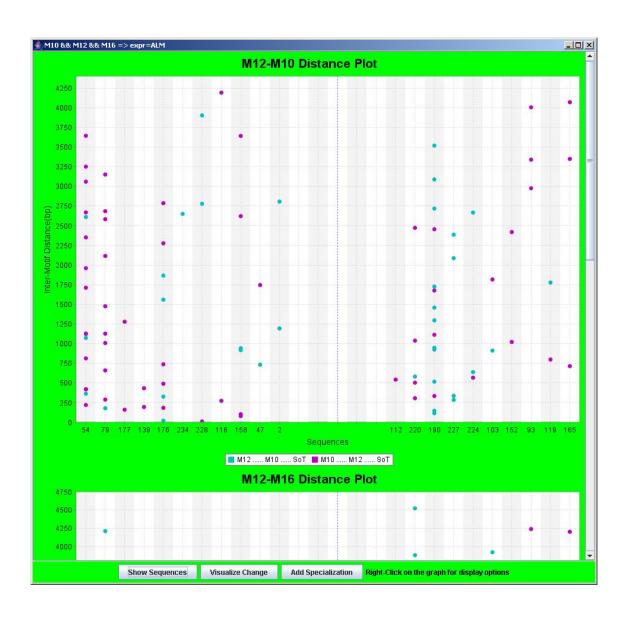


Figure C.6: Multiple pairwise inter-motif distance plots for a base rule with more than two motifs. For instance the base rule for this plot is M10 && M12 && M16  $\Rightarrow$  expr = ALM.

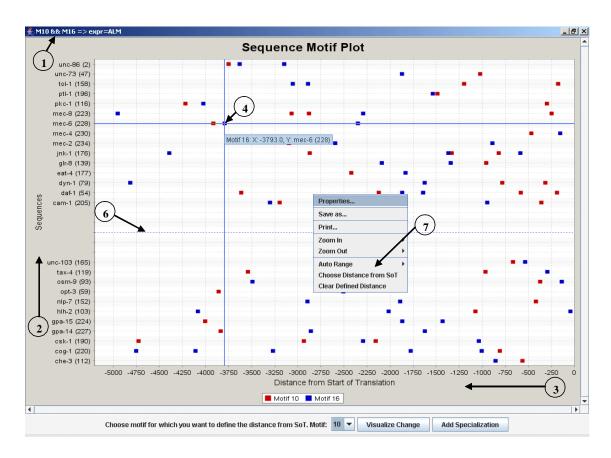


Figure C.7: Sample Sequence Plot Frame - The numeric pointers refer to the enumerated text explaining the Sequence Plot.

sequences with the instances of participating motifs (i.e., motifs M10 and M16). So along the y-axis is the list of qualifying gene promoters.

- 3. For each such gene sequence we plot all the instances of the participating motifs as they exist on the gene sequence relative to the Start of Transcription(SoT), which is the far right end of the plot. This makes the x-coordinate of each point in the plot the distance of the motif from the SoT and the color of the point is used to identify the motif.
- 4. Rolling your mouse over any such point displays the relevant gene name and the distance of the instance of the motif from the SoT.
- 5. Lists only qualifying genes on the Y-axis, that support the antecedent of the

- rule. That is, the gene sequence has at least one instance of both motifs.
- 6. Another mechanism to aid visual exploration is that each graph is sliced into two parts by a horizontal dotted line. The genes in the upper part are the ones that support the consequent of the rule and hence support the rule. The ones in the lower part are the genes that support only the antecedents of the rule. This provides the user with an easy mechanism to discover "Distance from SoT" based patterns in the upper part of the plot that are not as frequent in the lower part as this would let us explore specializations with improved classification accuracy(and/or confidence).
- 7. The following context-specific options were added to the graph right-click popup menu in the charting infrastructure:
  - Choose Distance from SoT This extension lets the user choose the "distance of a motif from the SoT" clause-based specialization in a graphical fashion. Selecting this option from the menu changes the graph to a distance selection mode. A subsequent click can be used to define the chosen value for the "distance from the SoT" and a visual confirmation of the defined distance clause is provided in the form of a vertical dotted line in the same color as the one reserved for the motif. One such distance can be defined for each participating motif. For example, in Figure C.8 a distance term of SoT [0-500] M10 is chosen.
  - Clear Distance from SoT This option lets a user clear all currently defined distances from SoT.
- 8. Once the user has utilized the dotted separation of the plot (into rule supporting and antecedent supporting) and the rule specific sequence plots to identify

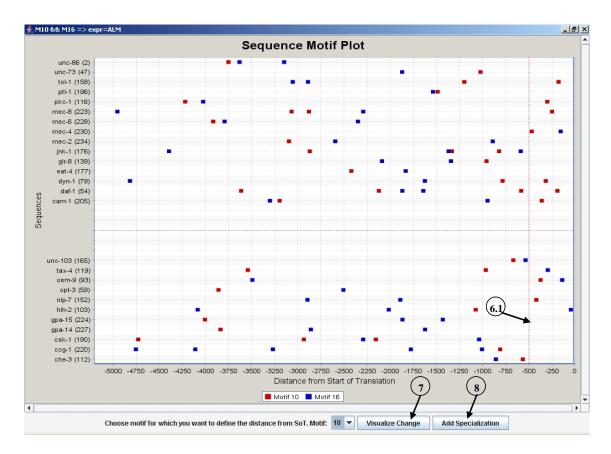


Figure C.8: Sequence Plot Frame depicting a distance of 500 bp from SoT for M10.

- a "distance from SoT" clause of interest, the "Visualize Change" command could be invoked to visualize the data in the context of the specialization rather than the original rule. Again the title of the new window is indicating the context setting rule/specialization.
- 9. If the user finds the specialization of interest, it can be added to the Analysis Frame using the "Add Specialization" command on the new sequence plot. Again this causes the specialization to appear as a new entry in the Analysis Frame with an auto-generated Id that again lets a user trace back the steps in case the user wants to later recall which rule was used to derive a specialization (Figure C.9).

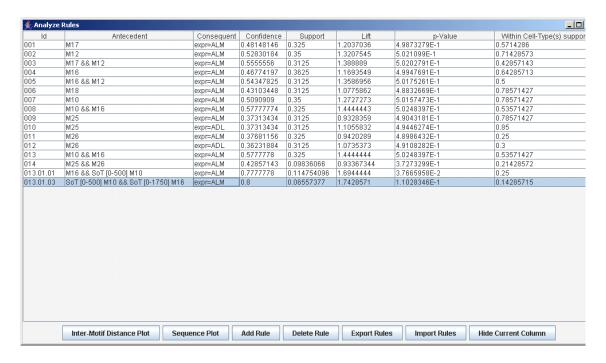


Figure C.9: Analysis Frame depicting a couple of newly added distance from SoT based specializations.

10. In case the base rule consisted of more than one motif and multiple "distances from SoT" relationships are defined (one for each motif) each such relationship is represented as a term and a collection of independent terms constitutes the specialized rule. For instance see Figure C.9 for the following specialization.

$$SoT [0 - 500] M10$$
 &&  $SoT [0 - 1750] M16 \Rightarrow expr = ALM$  (C.2)

# C.2.2 Order of occurrence of motifs

We wanted the VSM to facilitate exploratory analysis based on the hypothesis "Order of occurrence of motifs influences gene expression". But during the system design and the system use by the team(including the domain expert) it was observed that we already had a few ways to visualize gene sequence data in the context of the "order of the occurrence" of motifs. If order of occurrence of motifs was important

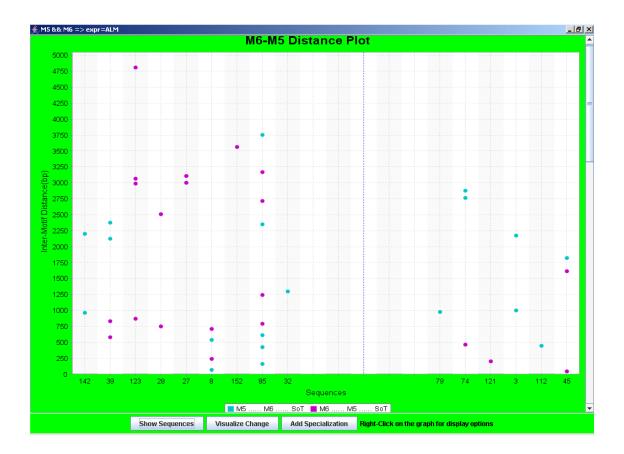


Figure C.10: Inter-Motif Distance Plot for Motifs M5 and M6. Observe the lack of magenta (dark) dots in the right half of the frame.

it could be easily identified by one of the following ways:

- 1. Color of the points in inter-motif distance plot. The order of the motifs in the inter-motif distance plot is represented by color. For instance in Figure C.2, M10 to the right of M16 (i.e., M16..M10..SoT) is represented by a magenta (dark) dot, while M16 to the right of M10 is represented by a aqua (light) dot. Thus, color provides a quick visual clue whether the order of occurrence of motifs affects gene expression; the left half of the plot should have more point of one color than the other in this case.
- 2. Repeating sequence of color in the sequence plot As mentioned in

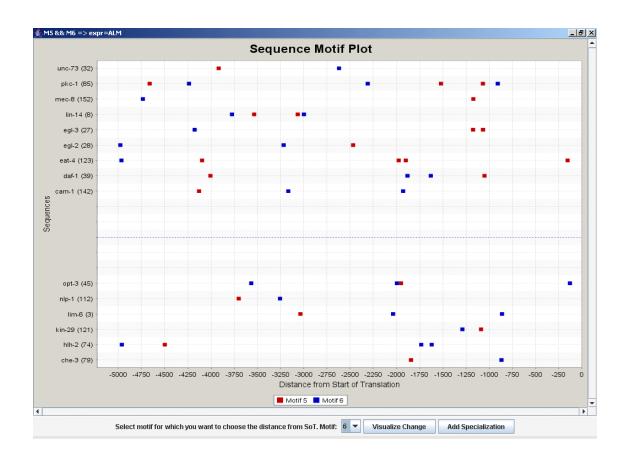


Figure C.11: Sequence Plot for Motifs M5 and M6. Observe that in the rule supporting sequences (upper part) a red dot is usually followed by a blue dot scanning the gene sequence from right end (SoT) to left.

Section C.2.1, enumeration item 2, the sequence plot displays all instances of participating motifs for qualifying sequences as they occur on the gene relative to the SoT. Since each motif appears in its own color and the data is being visualized in the context of a single rule, one can often see a repetitive pattern of color in the upper half and a lack of the same in the lower half of the plot. Such a display could also indicate an influence of order of occurrence on gene expression. In Figure C.11 one can observe that most sequences in the upper half have an occurrence of M5 (light point in the graph) closer to the SoT (the far right end of the plot) that is followed by a dark dot somewhere on the gene sequence. Also that this pattern is not so frequent in the lower part. Such pattern observation could indicate order of occurrence type relationship.

3. ASAS mining algorithm - The WPI implementation of association rule mining [PR05] used by us is capable of mining association rules with order based information and hence it is possible to have some of these rules being available already at the beginning of the exploratory analysis. Any of the two means mentioned above could be used to visually confirm/observe the order of occurrence relationship.

# C.2.3 Add Rule

Irrespective of the method used to identify a potential order of occurrence relationship between participating motifs the following option from the Analysis Frame could be used to add order-based rules. Once a user has identified an order-based (or any other) relationship between motifs, it can use the "Add Rule" option in the Analysis Frame to add a blank row for the new rule. The user can then simply type in the Antecedents and the Consequent of the rule to calculate the different

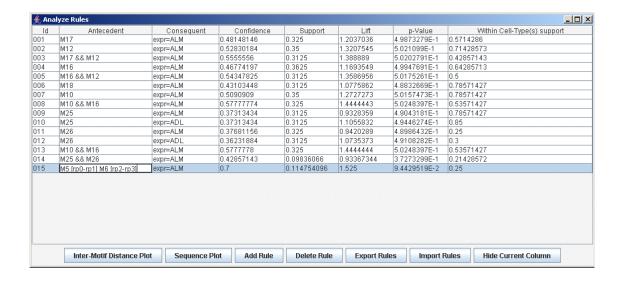


Figure C.12: Add Rule option in the Analysis Frame provides for free text option to add rules.

statistics indicating the interestingness metrics of the rule as shown in Figure C.12. Simply typing a complete rule computes the statistics indicating the interestingness of the rule. The user could also visualize the new rule using either the sequence plot or the inter-motif distance plot.

A rule keyed in by the user which does not have a valid syntax results in an error as shown in Figure C.13

Id	Antecedent	Consequent	Confidence	Support	Lift	p-Value	Within Cell-Type(s) support				
01	M17	expr=ALM	0.48148146	0.325	1.2037036	4.9873279E-1	0.5714286				
02	M12	expr=ALM	0.52830184	0.35	1.3207545	5.021099E-1	0.71428573				
03	M17 && M12	expr=ALM	0.5555556	0.3125	1.388889	5.0202791E-1	0.42857143				
04	M16	expr=ALM	0.46774197	0.3625	1.1693549	4.9947691E-1	0.64285713				
05	M16 && M12	expr=ALM	0.54347825	0.3125	1.3586956	5.0175261E-1	0.5				
06	M18	expr=ALM	U 404U0440	0.2126	1 0776060	4 9832669E-1	0.78571427				
07	M10	expr Message	expr Message x 157473E-1								
08	M10 && M16	expr				248397E-1	0.53571427				
09	M25	expr (i) Pars	expr (i) Parse Exception occurred while parsing the association rule 043181E-1 0.78571427								
10	M25	expr Lexi	Laving Larger of time 4, ashows 4, Europetersch 1991 (40), after 1991								
11	M26	expr				986432E-1	0.25				
12	M26	expr		OK		108282E-1	0.3				
13	M10 && M16	expr				248397E-1	0.53571427				
14	M25 && M26	expr=ALM	0.42857143	0.09836066	0.93367344	3.7273299E-1	0.21428572				
15	M5 && M6	expr=ALM	0.6	0.14754099	1.3071429	2.0701702E-1	0.32142857				
17	M5 (rp0-rp1)	expr=ALM	0.7	0.114754096	1.525	9.4429519E-2	0.25				
	Inter-Motif Distance Plot	Sequence Plot	Add Rule Do	elete Rule Expo	ort Rules	mport Rules	Hide Current Column				

Figure C.13: Grammar based parsing helps identify user-errors in typing the rule.

# C.2.4 Hybrid Rule

As described in the grammar governing rule definitions, each rule consists of an antecedent and a consequent. Antecedents in turn consists of terms. A rule could also include specialized term, extra hypothesis-based information(constraints) that the instances of the participating motifs must satisfy in order for a gene sequence to support the rule.

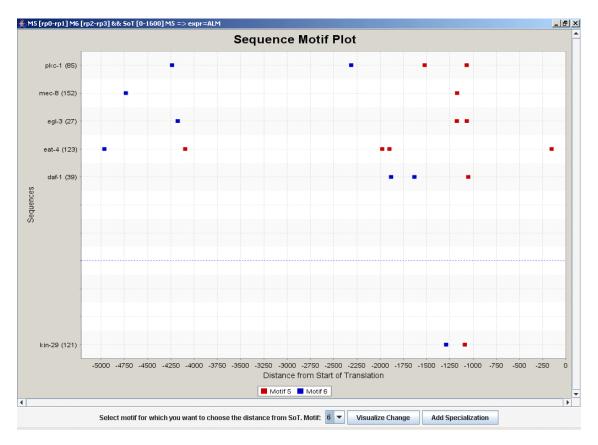


Figure C.14: Hybrid rules help specify multiple constraints (based on different hypothesis) within a single specialization.

The system also supports hybrid rules, rules that consists of specialized terms based on different hypothesis and a gene sequence must satisfy all constraints in order to support the rule. E.g. With reference to Figure C.11 note that there exists an instance of M5 (the red dot) usually within the first 1600 bp from the SoT (Far

right end of the plot). It is interesting to combine the two observations into a rule as follows and visualize it or calculate its interestingness. As we see in the figure C.14 that this hybrid specialization:

$$M5[rp0 - rp1]M6[rp2 - rp3]\&\&SoT[0 - 1600]M5 \Rightarrow expr = ALM$$
 (C.3)

has a higher confidence as compared to the following simpler "order of occurrence" specialization

$$M5[rp0 - rp1]M6[rp2 - rp3] \Rightarrow expr = ALM \tag{C.4}$$

As seen above hybrid specialization could have multiple specialized terms that relate to a single motif. A hybrid specialization could post multiple constraints on the same motif like Distance from SoT and Order of occurrence relative to another motif. It is important to note that although the rule may have multiple constraints for the same motif, it is not required that the same instance of the motif satisfies each of them. In the context of the C.3 above, it is not required that the instance of Motif 5 that satisfies the order of occurrence condition is the same M5(instance) that lies within 1600 base pairs of the SoT. Although there might be a need for the user to actually specify constraints which are inter-related and aliases are supported by the rule grammar for exactly this reason.

# C.2.5 Aliases

Aliases were included in the grammar to provide the user with an option of defining inter-related constraints or specialization terms. Consider the following Inter-Motif Distance based specialization from Figure C.5:

$$M10[0 - 500]M16 \Rightarrow expr = ALM \tag{C.5}$$

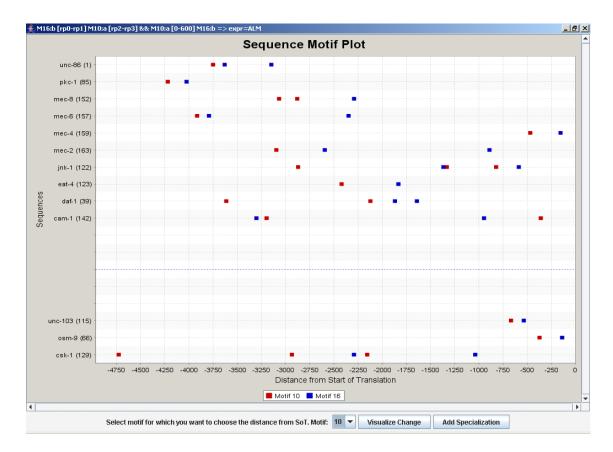


Figure C.15: Aliases let user define specializations with inter-related constraints.

Visualizing this specialization using a sequence plot (Figure C.7, one can see distinctly that not only do motifs M10 (red dot) and M16(blue dot) occur close together but they also occur in pattern such that the same instances of M10 and M16 that are involved in the distance-based relationship also occur in the same order relative to the SoT. Aliases enable the user to specify such complex relationships in the rule as follows (Figure C.15:

$$M10: a[0-600]M16: b\&\&M16: b[rp0-rp1]M10: a[rp2-rp3] \Rightarrow expr = ALM$$
 (C.6)

## C.2.6 Delete Rule

A user (usually a domain expert) can often identify rules which are of little biological significance and may want to delete such rules from the rule set. Simply selecting a rule from the Analysis frame and then clicking on the "Delete Rule" button could be used to accomplish exactly this.

# C.2.7 Export Rules

This option enables a user to save a copy of the rule set currently in the Analysis Frame to a text file. This provides the user the facility to resume working on the rule set at a later point in time or maintain motif based rule sets. The extensions to WPI-Weka rule-miner [Rudss] ensured that the rule model can also be imported into the rule mining interface.

# C.2.8 Import Rules

This option enables to import a rule model to be imported from a text-file. It could be either from a previous session of the analysis-frame or could be a rule set exported from the rule-mining interface. (Thanks Jon)

## C.2.9 Hide Current Column

If a user thinks, that one of the columns in the analysis frame is not of use in the current context the user has the option of removing a column from the display. Simply select a cell in the column that the user wants to delete and click the "Hide Current Column" button.

# C.2.10 Sorting in Analysis Frame

The Analysis Frame also provides the option of sorting the rule model in the analysis frame by simply clicking on the header of the column by which the rule model needs to be sorted. The order of sorting could also be reversed by simply clicking on the header column once more.