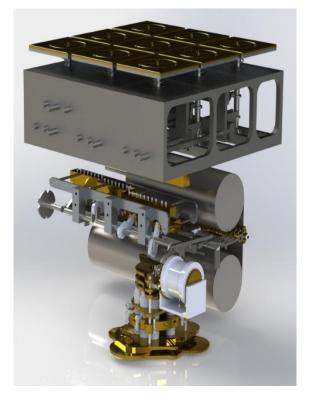


## **Mechanical Tic-Tac-Toe Board**



A Major Qualifying Project Report submitted to the Faculty of the WORCESTER POLYTECHNIC INSTITUTE in partial fulfilment of the requirements for the Degree of Bachelor of Science.

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Spring 2018
Submitted to:
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## **Abstract**

The goal of this MQP was to design, test and build a fully mechanical computer capable of playing tic-tac-toe against a human being. There is no question that modern computers could solve this problem more efficiently. However, our team aims to prove that old school technology still has a place in society today. Our design includes numerous methods of mechanical motion that are found in many designs today such as an escapement, gears, racks and pinions, and hydraulics. The machine was built almost entirely in the Higgins machine shop, except for a couple parts that were either cut with a water-jet or purchased. Our design uses an indexing module to detect position and data stored on a physical punch card to produce the best strategic answer. If the user makes the first move, the computer will never lose, only win or tie.

## Acknowledgements

Our group would like that thank our advisor Robert Daniello for his guidance and support throughout the duration of our project, Thomas Kouttron and Michael Cooke for their positive attitudes and constant aid in manufacturing, and Dane Kouttron for allowing access to machines not available within WPI facilities. We would also like to thank James Loiselle, Ian Anderson, Karl Ehlers, and Cam Collins for their good hearted aid, teaching our team the ins and outs of computer aided manufacturing and helping to figure out machining problems that we could not.

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## 1.0 Introduction

At our most animalistic level, games serve an important role in society to let humans behave in a competitive manner against one another in a confined, safe way. Games, both of the physical and mental variety, teach the importance of strategy, patience, and taking turns from an early age. Playing games provides an important developmental aspect to a child's upbringing. It is also thought that playing board games regularly reduces the likelihood of dementia in the elderly population.

The Worcester Polytechnic Institute (WPI) motto is the German phrase "Lehr und Kunst," meaning "Theory and Practice." The Institute has embraced this phrase and built aspects of theory and practice into the curriculum. One of WPI's founders, Ichabod Washburn, envisioned the school as "a formal education for tradesmen." [8] Originally, WPI students worked in the machine shops on campus to pay off their tuition fee. With the WPI spirit in mind, we aimed to integrate both theory and practice by designing, testing, and building a fully mechanical computer to play tic-tac-toe. Our design uses an indexing module to detect position and data stored on a physical punch card to produce the best strategic response. This punch card design was based off a machine invented in 1801, the Jacquard Loom. The loom allows for intricate patterns to be woven into cloth through the use of punch cards. Each punch card creates a different pattern on textile by moving the threads and hooks. Before Jacquard's version of the loom, the machine would need two people to operate [6]. If the user makes the first move, the computer will never lose; it will only win or tie. Reverse engineering was used to exhibit that, although tic-tac-toe may seem like a simple game, programming a machine to perform as well if not better than the human brain without the presence of electronics brings a new level of appreciation to a seemingly not complex game.

In order to have a successful major qualifying project, the team saw the project through the idea and concept phase to design and eventually building. A series of design options were considered before one was settled on. In order to hold true to the concept of both theory and practice, most parts that were used in the building of the project were manufactured in the shops of WPI.

## 2.0 Background

## 2.1 The Start of Computers

The definition of a computer has changed over the centuries. Before the 1930s, those who performed calculations were called computers. Charles Babbage, an English mathematician, is hailed for creating the first mechanical computer that has similar functions to the modern day computer [4]. In 1834, Babbage conceived the Analytical Engine, a mechanical computer driven by a crank that was programmable by the use of punched cards and could add, subtract, multiply, and divide numbers. Much like modern computers, the machine had a memory where the numbers and intermediate results could be held a central processor where the arithmetic was performed. A more thorough explanation of this can be found in Appendix I [2].

The Analytical Engine has long since been replaced by the modern computer. The mechanical complexity of Babbage's machine intrigued our group and we set out to prove that this technology still has a place in society today. Originally, the team set out to design a machine that would play chess with a user. After deliberation, we decided that this was not feasible because of the complexity of the game given that after three moves there is approximately 121 million ways to play the game. Tic-Tac-Toe was chosen because it could also be played but with a much more reasonable amount of data compression.

## 2.2 Tic-Tac-Toe

The classic game of tic-tac-toe involves two players and a 3x3 grid. One player is assigned to be "X" and the other "O." The game is played by taking turns marking a spot in the grid with your assigned letter. To win the game one player must have three of their letters in a row touching in any direction (vertical, horizontal, diagonal).

There are 255,168 possible games in tic-tac-toe. The different ways to play tic-tac-toe consist of the sum of possible ways to win after five, six, seven, eight, and nine moves. The lowest number of moves to win is five because one wins the game by having three marks in a row, meaning the winner played three times and the other player had two turns. In total there are eight different ways a player can get three moves in a row: three lines horizontally, three lines vertically, and two vertical lines. The math to solve the number of games possible with five moves is: (possible ways to get 3 in a row)\*(3 in a row)!\*(number of squares other player could have used)\*(number of moves to win). This can be written as:

To win after six moves, the equation used is:

The reason for the subtraction in this equation is because now both players have three moves on the board so all of the other possible outcomes where player one could have gotten three in a row must be excluded considering player two won the game on their third move.

To win after seven moves, the equation used is:

Again, as seen with winning after six moves, the possible combinations of three in a row for the player that did not win had to be removed. The winner of this game already had three moves on the board which were not all in a row before the winning mark was played. A similar technique was used for calculating the number of ways to win after eight moves, resulting in the equation:

To calculate the amount of games that can be played to the ninth square, math must be done to calculate both a win, or three moves in a row, along with all of the possible draws. This math can be simply done as 9!-4!(wins in five moves)-3!(wins in six moves)-2!(wins in seven moves)-1!(wins in eight moves). The math to solve the possible ways to win was more complex and not necessary because only the total number of games were of interest. The written out equation for this is:

$$9!-[4!(1440)]-[3!(5328)]-[2!(47952)]-[1!(72576)]=127872$$

To find the total number of games possible, the totals per moves needed for a game to end are summed together resulting in:

When played correctly, it is possible to never lose tic-tac-toe and only have the game either conclude with a draw or a win in your favor. It is easier to win if you are the player that played first. However, it is still possible to never lose the game even if you are the second to play. The figures below outline the optimal strategy to win the game if you are the first person to play or the

second, respectively. The figures are broken into the nine main grids of a regular game of tic-tactoe, and within each grid are all of the possible ways to play a game based off of the grid where the first move was made. In the figures shown below it is assumed that the greyed box is the current best strategic move at that point in the game. Based off of the sheer magnitude of marks in the second figure, it can be seen that there are many more ways to play a game as the second player trying to block the first player from winning rather than playing with the intention of beating the other player.

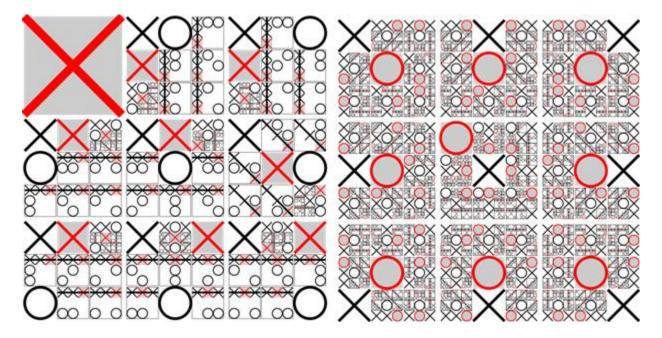


Figure 1: Optimal solution for offensive and defensive game respectively

An example game using Figure 1 above will be used given its simplicity compared to a defensive game.

## 2.2.1. Move 1:

The first move is the large red "X" in square one. It will be assumed that the player chooses to respond with the fifth square.

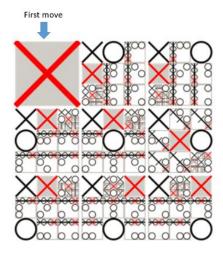


Figure 2: First Move

## 2.2.2. Move 2:

The second move is assumed to be put in tile five. Looking within tile 5 of the original grid, it can be seen that the "O" is played.

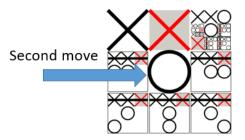


Figure 3: Second Move

## 2.2.3. Move 3:

The red "X" in this square denotes the current best strategic move.

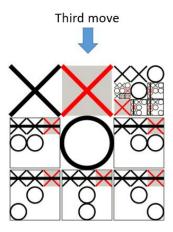


Figure 4: Third Move

#### 2.2.4. Move 4:

We will assume that the player chooses to play an "O" in tile 3. To see this move, the user must look at the third tile within the most recent board shown in move 3. For each move to see the next best move after the other player makes a move, you essentially zoom in on the grid in which the player has made their move, thus, move five will be a zoomed in version of the third square in the fifth tile of the main board.

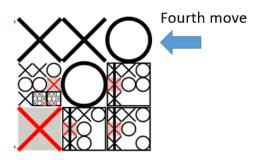


Figure 5: Fourth Move

#### 2.2.5. Move 5:

The red "X" shows the best strategic move, blocking the "O" team from diagonally getting three in a row to win the game.

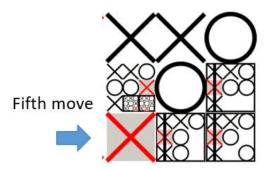


Figure 6: Fifth Move

#### 2.2.6. Move 6:

We will assume that the player chooses to place their next move, an "O" in square 7.

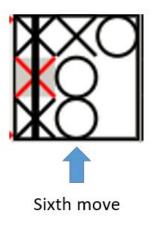


Figure 7: Sixth Move

#### 2.2.7. Move 7:

The game ends with the seventh move where it can be seen by the red "X" that there are three marks in a row.

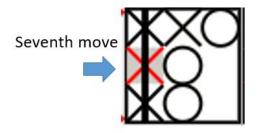


Figure 8: Seventh Move

Making a machine that never loses Tic-Tac-Toe is a simple task. Any modern computer could be programmed to solve the problem with ease. However, once electricity is removed from the solution the problem becomes much more complex. The problem then needs to be solved using an assortment of mechanical devices that have been around for centuries and are still in use today.

## 3.0 Methodology

The following methodology, developed from background research on current computing machines, was designed to most accurately guide the project to the most robust possible outcome. Inspired by Charles Babbage's Analytical Engine, our team used aspects from his design such as a crank driven machine and physical storage in the form of a punch card to create our own mechanical computer. This project is not aiming to replace computers; they are without question more efficient. Instead we aim to prove that the mechanics behind this seemingly easy task are impressive and still have a place in society today. The goal was to create a design that could be

manufactured within the time constraints of the MQP while also creating a working, functional product. To do so, the following objectives were made:

- 1. Design, with the use of computer aided design (CAD), a 3D model of a computational machine capable of storing and reading possible inputs and outputs for a game of tic-tactoe in the smallest size feasible.
- 2. Machine and assemble the mechanical computer.
- 3. Determine the accuracy and repeatability of the machine from stopping a player from winning a game.

## 3.1 Objective 1: Design a Compact 3D Model

The process that we took to create our final design is just as important as the design itself. Many aspects of previous designs were used to create one final collaborative device. While in the initial stages of the design process, the team determined a physical library would be the most effective way to store the board's optimal game responses. A physical library is a way of tangibly storing information. The library can be a card that has holes punched in specific locations that, when read, produce an output. A common machine that uses a physical library is a music box. Whether the music box uses a card with holes or a roller with bumps on it, the result is the same. The physical library rolls over metal fingers that vibrate and create a noise when moved by the punch card create music which is the response in a music box. Instead of outputting a melody, our machine would output a game of tic-tac toe.

#### 3.1.1 Preliminary Designs

We exhausted the potential design options to produce the most compact and simple machine that we could. This section will outline the process that we went through to produce our final design. Each design leading up to the final iteration is important to document because concepts and elements of past designs have been implemented in the final design. We determined that the ideal size for the machine is one cubic foot and used this information during the design process to restrict our models.

## 3.1.1.1 Cam System

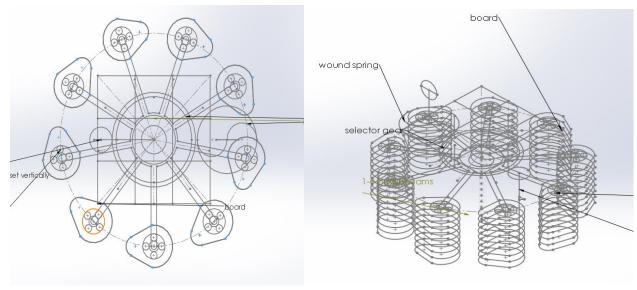


Figure 9: Cam System Partial View

Figure 10: Cam System Full System

The first design utilizes 9 drums with multiple cams working on a geared system. The user inputs onto the board by pressing on a tile. That vertical motion would rotate a carousel that would select varying cams to create the machine's response and output a response on the corresponding section of the board. The major issue with this design is the sheer number of cams needed to play through every possible iteration of the game would be too large which would cause the game board to be too big to be feasible. The design of the user-interface board has proved difficult. Originally the "X" and "O" buttons were able to be pushed both up and down by the user and machine, down being the users move and a button moving up being that of the machine. However, the design was changed for usability purposes so a tile being all the way down symbolized the user's move and a tile being halfway down symbolized the machine's response.

#### *3.1.1.2 Cams Iteration #2*

The second iteration had more cams, gears and parts to be machined than the first. We ran into the same problem of staying within the amount of space required to house all the necessary parts. The machine would be so large that it would not be a practical solution to the problem.

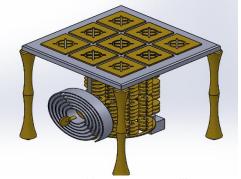


Figure 11: Cams Iteration #2

#### 3.1.1.3 Physical Library

The third design features a similar design to the one above, but uses a physical library that is rotated 90 degrees. Again, the proportions were underestimated and it was determined that this method is not feasible given the size constraints. In the image on the right it can be noted that there are several large rings. Each ring contains a series of holes that the machine reads for different outputs. The first ring contains the output for the "layer one" response, the second for "layer two" and the rest for "layer three." The explanation of these "layers" can be found in section 3.1.3.1.

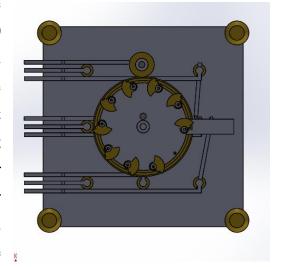


Figure 12: Physical Library

#### 3.1.1.4 Discs

A series of discs all on one drum was the next design idea we entertained. The discs served as the physical library in this design and combined with the drum allowed us to avoid using cams which makes for a smaller, more compact design. Unfortunately, this proved impossible because while we originally thought 9 discs were needed, 81 are necessary to play out every version of the game. Additionally, this design is larger than designs 2 and 3 and space constraints would not allow for its construction.

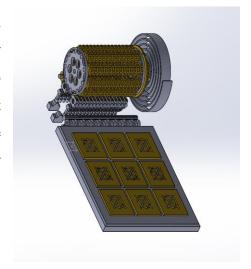


Figure 13: Discs

#### 3.1.1.5 Discs and Ring

This design features 3 smaller disks and a 24 inch diameter ring. This ring would hold the data for the 4th move in the game. The three smaller discs above it would hold the data for the preceding layers. This design is buildable, however transitioning between each ring and the clutches necessary to reset the mechanism are too complicated. Additionally, the design is larger than what we see as an ideal size and this much material would be difficult to budget. We originally planned on making the 24 inch ring thinner

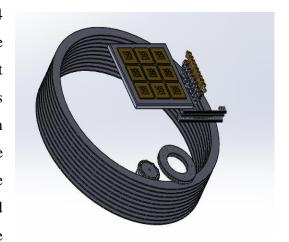


Figure 14: Discs and Ring

to cut down on cost but that would have created deflection issues and would not have reduced the large diameter. Also, getting each part to interface correctly would require extremely precise machining. After this stage of design, there was a singular disk that would operate on the same lines as a record, radiating from the center out using a three-dimensional method of detecting responses. This was scrapped due to the .03" rotational locational tolerancing that, with backlash and clutch slippage, would be exceedingly difficult to successfully build. Though a more compact system than the multi disc version, it was still well over the 1 cubic foot criteria.

#### 3.1.1.6 Music Box

We took inspiration from traditional music boxes that used star wheels and pegs to play. This idea allowed us to create a more compact version of the previous designs. The problem with a typical 30 note music box is that it requires 70 feet of punch card for the user to roll through all tic-tac-toe games with a hole size of 0.1 inches. There was also 0.28 inches horizontally between each hole and

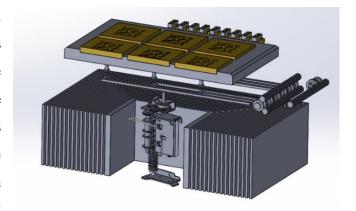


Figure 15: Music Box

0.25 inches vertically. The punch card in our design is very similar to that of a music box. In the case of a music box, the card comes across a star wheel, rotates, plucks up a comb to make a note. In our case, we eliminated the comb and put on a locking tine mechanism.

This design was promising. However, from a time efficiency standpoint, scrolling through 70 feet of data would prove to be tedious. Additionally, we would still have the rotational accuracy problems mentioned in previous designs and the issues of slippage and friction when the machine shifts between multiple gear ratios. We changed our design from a 70 foot continual roll (the first picture that you see) to a 70 foot singular roll so that the user would have to reset the machine after each use instead of having to crank all the way back through the punch card.

Since there are 9 different moves that the user can make on their first turn, we changed our design to have 9 different rolls of punch card, depending on what the player's first move is. This design includes an indexing version which has a counting star wheel instead of using just pure gear ratios as an index. The punch card would have holes on the side of it to count how many positions have passed and allow the machine to find what and where the answer is.

## 3.1.1.7 Spool Punch Cards

The nine spools that you see to the right incorporate the revelation that our group had while making the previous design. This design focuses on refining the indexing module by using an escapement mechanism. Escapements are often found in mechanical clocks but have proven to

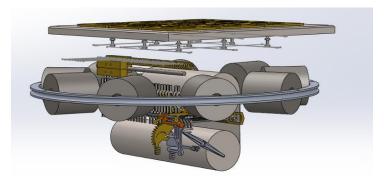


Figure 16: Spool Punch Cards

be a key part in our machine. The escapement in our machine acts as an indexer for the gear box. This escapement mechanism has a pin set in it allowing movement in the vertical axis of the escapement gear. Each hole on the cards correlates to a number of clicks. Once a tile is selected, one of the nine follower pins is released. As the escapement gear rotates forward, the pin slides along the face of the gear and into its respective hole. A clutch is then popped stopping the player from being able to move the punch card forward. The main issue with this design was the sizing of the pins. They were too small and the entire thing would have needed to be upscaled several times. On top of that, the reset mechanism would have to work in multiple axis and been difficult to implement without constant jamming issues.

#### 3.1.1.8 Final Design

The final design utilizes many of the machine elements that can be found in our previous design iterations. All of design iterations helped us reach our final design in one way or another. From the start of the design process we continued to move toward the realization of our final design using certain elements from each iteration along the way. With over 700 parts, the final design is very complex. To make understanding the design easier, we have broken up the process into 9 steps. Each step outlines one of the processes that occur to complete a game of tic-tac-toe.



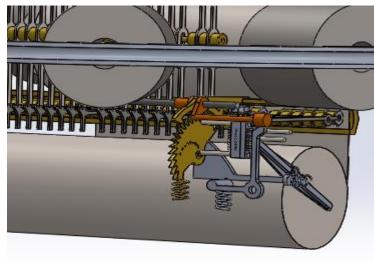


Figure 18: 3D Printed Escapement

Figure 17: Escapement in CAD Model

#### 3.1.1.8.1 Step 1: Choosing a Spool

The user manually inserts the first spool and rotates it into position to allow for interfacing of the stored data with the machine.

## 3.1.1.8.2 Step 2: Pick a Tile to Push

The user pushes down on the tile as far as it can move. This vertical distance is 0.51 inches and the tile (B) is held down by a detent (A). To signify that the machine has selected a tile, the tile is pulled down .30 inches. Since there is such a small difference between these two, the tile is made of two different types of metal. When the aluminum is visible, it signifies that the user has played that tile. If only brass is visible, the machine has played that tile.

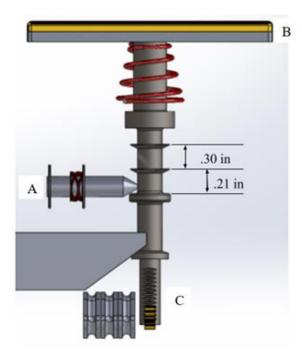


Figure 19: Tile Assembly

## 3.1.1.8.3 Step 3: Clutch Release

The motion of the button being pushed down 0.51 inches transfers the linear motion into rotational motion via the rack and pinion (C). This is visible on the bottom of the tile shaft. This rotation creates tension in the cables. These cables are run down the side of the machine and connect to the 9 clutches in the indexing mechanism. When one tile is pushed, tension is created in one cable which releases one of the 9 clutches. This is shown in the diagram below.

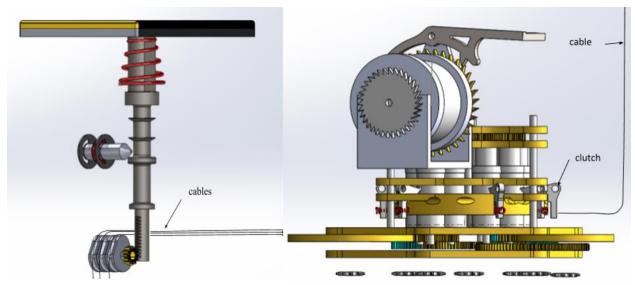


Figure 20: Tile Assembly with Cables and Indexing Mechanism

#### 3.1.1.8.4 Step 4: Engage Escapement

Once the indexing mechanism has rotated to the appropriate point, the escapement mechanism will allow the shaft connected to the gears to move. There are 9 clutches on the indexer and as mentioned above, only one is engaged at a time depending on which button the user pushes. Each of the 9 springs are in compression until the user pushes a button which causes tension in the cable attached to the clutch. The live shaft gear has 96 teeth along with 9 idling gears each having 12 teeth. Gear ratios vary from 1:1 through 9:1.

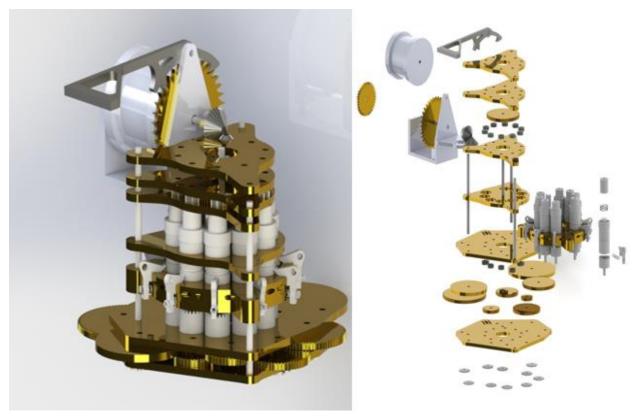


Figure 21: Rendering of the Gear Box and an Exploded View of the Gear Box

## 3.1.1.8.5 Step 5: Turn Punch Card Wheel

The user turns the crank which is attached to the physical library. As the crank turns so does the physical library (A in figure X below). While there are nine available spools, only one is engaged at a time.

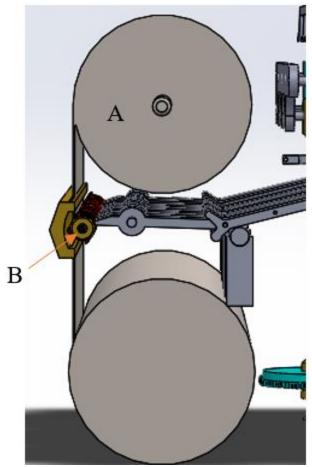


Figure 22: Diagram of the Punch Card Wheel

## 3.1.1.8.6 Step 6: Physical Library is Read

Seen above, along with the physical library, is the star wheel and tine assembly. The holes in the physical library interface with the star wheels (B). As the star wheels are spun by the physical library, they interface with the tines in a similar manner a music box uses to create music.

## 3.1.1.8.7 Step 7: Tines Move with Punch Card

When the end of each tine is moved by the star wheel, it causes the other end of the tine to move upwards since it is resting on a bar and has a hinge joint. The right side of the tine is the side that interacts with the star wheel. The left side is the side that moves upward approximately 0.5 inches. In the process of moving upward, the tine hits a hinged plate. The plate moves upwards enough that the tine resting on it falls downward. The tine that is still moving upward then comes down to rest upon the plate. The constant reading of holes on the punch card causes different tines to interact with the hinge plate, resetting the tine currently moved up with every new tine that interfaces with the computer. The y-shaped joint that is outlined in red was put in place to restrict

the vertical motion of the left side of the tine. In order to interface with the next section of the machine, it only needs to move 0.5 inches. Additional vertical motion would be problematic in the next step.

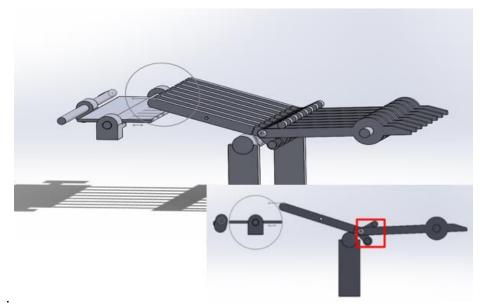


Figure 23: Diagram of the Tine Mechanism

## 3.1.1.8.8 Step 8: Motion Transfer

The pins mentioned in Step 6 have a vertical movement associated with them. When each pin moves upward, it hits a lever which slides a cam into place. The camshaft then rotates which translates the motion from the tine blocks into horizontal motion in the wedges.

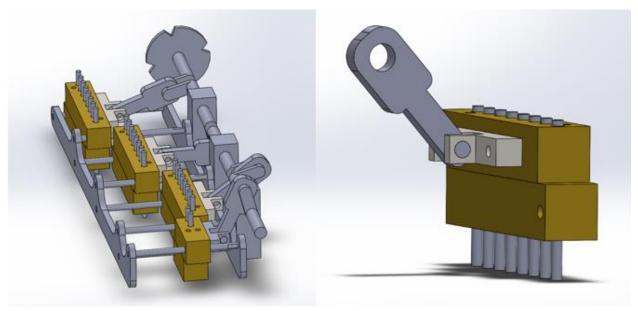


Figure 24: CAD Model of the Tine Block Sub-Assembly and CAD Model of an Individual Block

#### 3.1.1.8.9 Step 9: Machine Selects a Tile

Pictured is the wedge that was mentioned in Step 7. Each wedge moves 0.75 inches horizontally. This motion creates 0.2 inches of vertical motion downward for the tile due to the tapered shape of the wedge. When a wedge is moved horizontally, the associated tile is pulled down 0.2 inches. The image below shows all nine wedges interfacing with their respective tiles. The wedge is spring loaded, allowing for easy reset once a new tile is played.

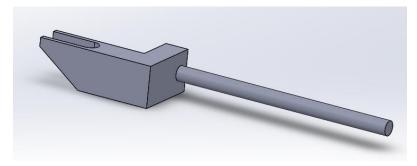


Figure 25: CAD Model of the Wedge

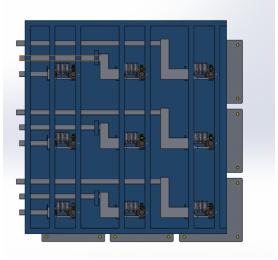


Figure 26: View of the Game Board from the Bottom

#### 3.1.2. Resets

#### 3.1.2.1 Reset Mechanisms for Tines:

The tines have a wedge block on the end of them that acts like a pendulum. As a tine swings up it moves the wedge back until the tine can clear it. When the tine clears the wedge block, the pendulum motion swings the block back to its starting position and the tine falls and rests on top of the wedge. When another tine swings up, the old tine falls as the new one moves the wedge and comes to rest on top. A simple, single position camshaft is used to swing the pendulums and reset the tines at the end of each game.

#### 3.1.2.2 Gear Box Reset:

The gear box has a clutch reset that encompasses all of the clutches. The plate is pulled upward and disengages all of the clutches in the process. These clutches need to be reset between each round of the game in order to clear old inputs and put machine on track to read the next set of plays on the physical memory.

#### 3.1.2.3 Tile Reset:

Each of the tiles is held down with a detent. All of the detents are spring loaded forward and attached to a bar in the back. After the game, the user would simply need to pull the bar back allowing the spring loaded tiles to return to their initial positions.

## 3.1.3 Calculations and Tolerancing

### 3.1.3.1 Creating a Numerical System of Data

In order to create a series of logical inputs and outputs i.e. physical memory, that the machine would be capable of reading, a game of tic-tac-toe needed to be represented in a matrix format. Changing the "X" and "O" inputs and outputs to be numbers based off of location on a grid allows for a better mapping of potential moves.

Tic-tac-toe is a solved game. Our machine plays a defensive game which means it makes the second move. It is much harder to win a game of tic-tac-toe when going second. Our team analyzed each possible game and recorded the best strategic response for the machine to make in every possible scenario. This data was collected in an excel document. This process took several days because there are over a thousand rows of data to be filled. To make coding our document easier, we assigned each of the nine spaces a number. Below is a figure outlining how we named each space.

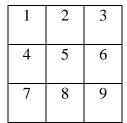


Figure 27: Naming Convention of Tiles

Our team used the defensive model found to the right to determine the best strategic output for our machine to produce in each situation. To demonstrate how our team used the data from Figure X, we have broken down how our excel document can be used into each individual move.

The example will outline a game in which the user selects tile 1 as their first move, tile 4 for their second move, tile 3 for their third move, and 8 for their final move. The user's tile choice and the computer's response to that choice are called a "layer" in this document. For example, the user's first move and the computer's response to that are called the "1<sub>\*</sub> Layer" in this document. The "X" represents the user and the "O" represents the computer.

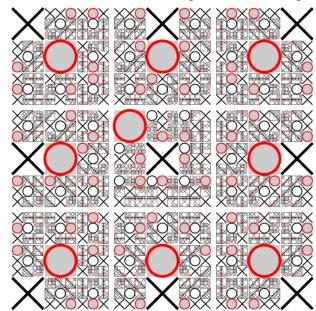


Figure 28: Optimal Strategy to play a Defensive Game of Tic-Tac-Toe

## 3.1.3.1.1 The First Move:

The user can play any of the nine options on their first turn. Strategically, the best spot to play is the middle tile (tile 5). If the user plays anywhere besides tile 5, our computer will respond by playing tile 5. If the user chooses tile 5, the computer responds by playing tile 1. The top row in the figure below outlines the possible places that the user could play. The second row contains the best strategic response for each possible input. For example, if the user played tile 1 (highlighted in yellow) the computer would respond by playing tile 5 (highlighted in green).

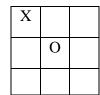


Figure 29: Game Board View after the First Move

		1	2	3	4	5	6	7	8	9
1st Layer	1	5	5	5	5	1	5	5	5	5

Figure 30: Excel Document- First Move

#### 3.1.3.1.2 The Second Move:

As the game continues, the responses become more complex. To keep track of the computer's response, each row is labeled. The column second from the left contains each rows label. Row 1.1 denotes the situation in which the user played tile 1 on their first move. Row 1.2 denotes the situation in which the user played tile 2 on their first move. 1.3 is when the user played tile 3 and so on and so forth. Continuing with the example above, the user played tile 1 on their first move so focus on row 1.1. Tile 1 and tile 5 have already been played and therefore cannot be played again in the second layer so those values are blacked out in the figure below. Continuing with the previous example, the user played tile 4 on their second move and the computer responded by playing 7. This is shown below with the user's move highlighted in yellow and the response in green.

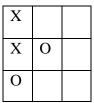


Figure 31: Game Board View after the Second Move

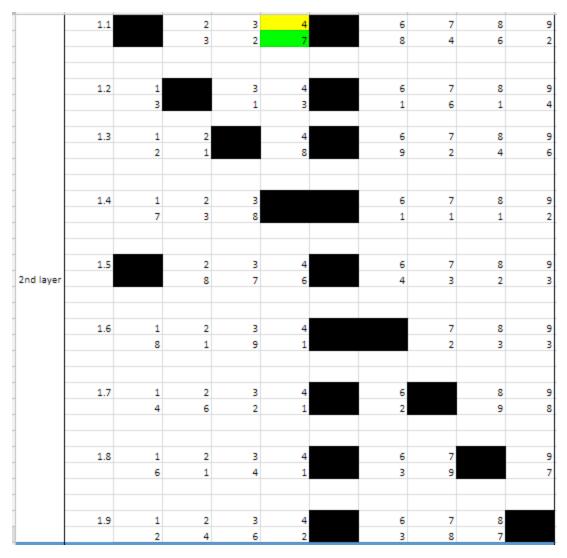


Figure 32: Excel Document- Second Move

#### 3.1.3.1.3 The Third Move:

The row's labels have grown by one number. For example, 1.1.2 user's first move was tile 1 and his second was tile 2. As you can see below, row 1.1.1 is blacked out. This is because it is not possible to play tile 1 twice. Continuing with the example, the user has played 1 and 4 and the computer has responded by playing 5 and 7 respectively. As you can see in row 1.1.4, these four tiles are blacked out because the tiles are now out of play. For the purpose of continuing the example, the user's third move is tile 3 (highlighted in yellow) and the computer's response is tile 2 (highlighted in green). The figure below only shows 1/9<sup>th</sup> of the 3<sup>th</sup> layer. Rows 1.2.1 through 1.9.9 are omitted for simplicity's sake.

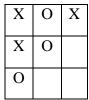


Figure 33: Game Board View after the Third Move

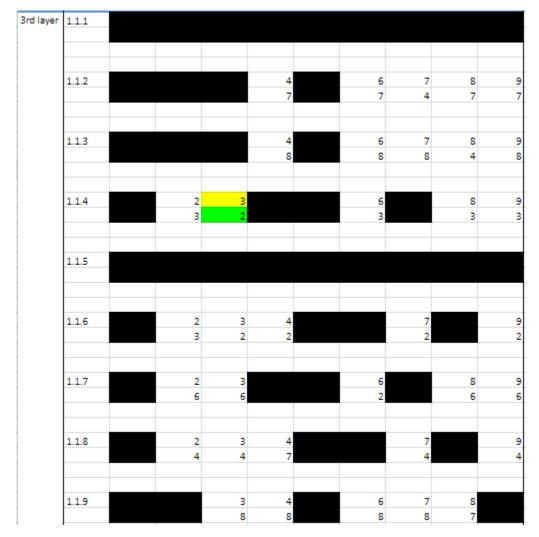


Figure 34: Excel Document- Third Move

## 3.1.3.1.4 The Fourth Move:

The figure below only shows  $1/81^{4}$  of the  $4^{4}$  layer for simplicity's sake. Continuing with the example, tiles 1-5 and tile 7 have been played. Therefore, only tile 6, 8, and 9 are visible in row 1.1.4.3. The user plays tile 8 so the computer responds by playing tile 6. The board now looks as follows:

Х	0	Х
Х	0	0
0	Χ	

Figure 35: Game Board View after the Fourth Move

The user could play a fifth tile; however, it would not change the outcome of the game. The result is a draw.

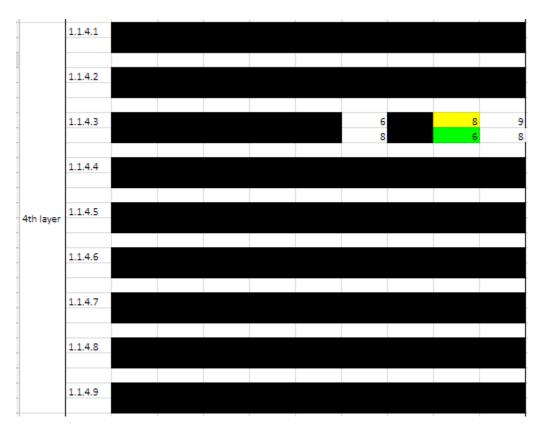


Figure 36: Excel Document- Fourth Move

## 3.1.3.2 Binary Format of Numerical Data Compilation

The original system that we created to keep track of data was a digital system. However, the punch card design runs on a binary system. The digital system allowed us to know what the proper response for the machine was but needed to be converted into a binary system so the data could then be converted into Cartesian coordinates and input into SolidWorks. Is there a hole or isn't there? The data outlined in the previous section had to be changed from a digital format into a binary one. To achieve this, we created a series of excel documents. There are 9 excel documents, one for each of the tiles that the user can select as his first move. An example of this document is shown below.

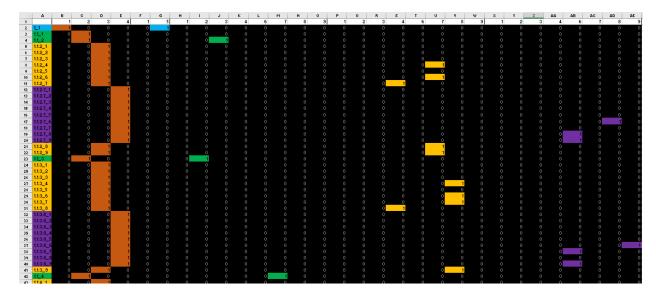


Figure 37: Binary Excel Document

This image shows a section of the binary solution to a defensive game of tic-tac-toe if the user's first move is to engage the top leftmost tile. The blue indicates the machine's response to the user's first move, the green to the second, yellow to the third, and purple to the fourth. The leftmost column indicates what section of the game is being referred to. For example, 1.1.3.8\_9 has a 1 in column 6. That means that the user's first move was to play tile 1, their second was tile 3, third was tile 8, fourth was tile 9, and the best strategic response to their fourth move is tile 6.

This binary data was more useful than the digital data, however it still needed to be altered to fit onto a punch card. To achieve this, the team used excel to change each box in the excel into a data point on a Cartesian plane. The space between each cell in the x direction is .28 inches and .25 inches in the y. The Cartesian coordinates were uploaded into SolidWorks and used to create a CAD model of each of the 9 punch cards.

#### 3.1.3.3 Hydraulic System

The hydraulic analog to digital converter takes 26 inputs in a binary state and converts them to one output with 9 states. There are 26 pins and 9 differing size diameters. Knowing only one of the pistons will be up at any one time allows for the system to determine what value is being output by any of the pins via the output piston at the back. Though the system isn't linear, in practice it would be able to accurately define which piston was actuated by scaling the output bar with a lever to increase the visible throw of the output. This wasn't produced in the final version

due to the manufacturing time involved in making a working system and other manufacturing issues. The system was reverted to a bar linkage system similar to the one shown previously.

#### 3.1.3.4 Tolerancing

In order for each part to properly interface, it is important that there is enough tolerancing to avoid problems such as shearing and travel restriction. Considerations must be made for the slight variances in size caused by machining. In general, the average rule of thumb was to leave a five to ten thousandth of an inch clearance on sliding parts during the design process. In the case of diametrical interfaces, or a pin riding inside of a bore, it is essential that the size of the pin and the hole are not the same size as friction would limit the part from moving. While it is important to allow for friction tolerancing, it is also important to limit travel. For example, the spring tab engages in vertical motion when the playing tile is pressed on and the lower portion of the tab has a rack on it that interfaces with a pinion. The hole that the spring tab travels through needs to have enough tolerance to allow for the vertical displacement of being pressed, however motion must be limited in order to keep the rack and pinion engaged without having too much room to travel radially. For reasons such as the example listed above, tolerancing between parts were restricted as much as possible while still mitigating friction. The tolerance stack up created in the design process would allow for optimal movement with minimal frictional errors.

## 3.2 Objective 2: Machining and Assembly

## 3.2.1 Machining Process

The majority of parts used in the final assembly were built in the machine shops of Higgins and Washburn shops on WPI's campus. Other parts that could not be made at WPI were outsourced to a contact at Massachusetts Institute of Technology (MIT) as a means to have parts cut with a water jet. Other standard parts (screws, etc.) and stock were ordered through McMaster Carr. In total, approximately 700 parts were used in the making of the computer, 500 of which were made in WPI facilities. The materials used to manufacture parts was primarily brass, aluminum, and 4140 steel.

#### 3.2.1.1 Manual Machining

A majority of the parts that make up our tic-tac-toe board were manufactured manually in the Higgins machine shop. Many of the parts we designed had only one or two copies needed for the construction of the board therefore, it was quicker to manually machine these parts than taking the time to write the program for the Computer Numerical Control (CNC) machining. The vertical mills in the Higgins shop were utilized for machining most of the parts that were made for the board. All of the rods that needed to be turned on a lathe were made using the manual lathe in the Higgins shop. All of the gears in our board were cut manual in Higgins using an Ellis dividing head. The dividing head allows the machinist to look up in a chart the amount of rotations needed to cut the correct number of teeth in a gear as well as the correct plate. The teeth of the gears were first cut using the horizontal mill and then parted off using the lathe.

## 3.2.1.2 Computer-Numerical Control Machining

The Computer-Numerical Control (CNC) machining was done using the Mini Mill and ST-10 (lathe). The allure of using CNC for machining is mass production and repeatability. For this reason, parts requiring high volumes were CNC machined. As there are nine tiles in a game of tictac-toe, there were at minimum usually nine parts of any given feature needed that interfaced with the tiles. For this reason, it was quicker to take a drawing for a part out of the SolidWorks file for the project and import it to Esprit, a computer aided machining (CAM) software. Once in Esprit, the part needed to be programmed once to be cut and the same program could be repeated on multiple parts with the only down time in between machining being entering new parts and reprobing surfaces. Esprit allows for a complete simulation of the part to be machined, a useful tactic to avoid potential collisions and a chance to review that all of the programming was inputted correctly. Feeds and speeds do not need to be manually entered into the machine during use, merely included in the program being created for the machining process beforehand.

## 3.2.1.2.1 Mini Mill

The Mini Mill was used to machine parts that involved engraving, horizontal cuts, vertical cuts, or drilling and tapping. All of these functions were performed with the part being placed in a stationary constraint that allowed for no movement of the part. Some of the parts machined using the Mini Mill included the tiles that the user interfaced with. As seen in Figure 38, the engraved "X" and "O" features would not be a quick or efficient process to manually perform. As an



Figure 38: Machined Tile Top

example of precision, another feature that was created on the Mini Mill was the hydraulic block. As seen in previous sections on the importance of precision in hydraulics, it was critical that the diameters of each hole were exact. The process involved milling out the base for all of the piston holes followed by the milling and reaming of each individual hole.

#### 3.2.1.2.2 ST-10

The ST-10 Lathe was crucial for cutting patterns into a part that had radial cuts. The manual lathe proved to be very efficient in making parts that required basic turning down, drilling, or tapping. The use of CAM and CNC to make some parts on a lathe were reserved for those that could not be done on a manual lathe as the tolerances on the ST-10 proved to be slightly off compared to turning parts manually. Parts turned included the spring tab.

This part was turned on the CNC lathe and the rack that interfaces with the pinion was manually added along with turning down the section that the rack went on after the part had been turned and parted. Due to the length of this part and the diameter being cut, it was necessary to have a section of the part turned and tapped with a center drill in order to insert the tailstock. Once the tailstock was inserted, the roughing, grooving, and contouring passes were done up to the final wide diameter cap before the rack. At this point, the spring tab was parted and the final roughing was done in a manual lathe with the previously turned section being held in order to avoid the chatter and tolerancing errors of a long, narrow part being machined. Another part done on the ST-10 was the sprocket gear. The general disc shape was created using a CNC lathe. Once the disc was made and parted, it was placed in a fixture in the Mini Mill and the gear teeth were milled.



Figure 39: Machined Spring Tab

## 3.2.2 Assembly

The complete design consists of several sub-assemblies. In order to begin assembly of the machine, different subassemblies were first put together. During the process of assembly, parts were tested to make sure that the interfaces were efficient. Ultimately, the computer was not fully assembled. Sub-assemblies were completed, but both time and budget caused for the project to be incomplete. Most sub-assemblies were put together using methods such as inserting screws, set screws, bolts, hand peening, and press fitting. Loctite and other adhesives were also used in ensuring that parts would remain in the right spots and not shear.

## 4.1 Results and Discussion

The chapter prior to this one described the methodology that would be used in designing and building a mechanical tic-tac-toe machine that would be capable of using a physical library to collect and store information in order to pick the most logical defensive response to the moves made by the player. That process will be examined and discussed in this section.

## 4.1.1 Objective 1: Design a Compact 3D Model

#### 4.1.1.1 Size Constraints

After many iterations, a final design was finally reached that was within the correct range of one cubic foot. There were many pitfalls before one final design was reached. The time taken and iterations made to the models is both in fault of underestimating the space needed for the shear amount of ways to play a game of tic-tac-toe and the furthering of our background understanding of different mathematical computing devices. A rough design matrix was used to conceptualize what were key factors in the final product. The most heavily weighted features were: size, ease of user interface, and mechanical compatibility of different subassemblies. The many different iterations of design ideas resulted in one outcome that met all of the necessary criteria. The final design can be seen in the figure below. Not included in the design is the outer case that would hold all of the different sub-assemblies in place as it takes away the view of the different subassemblies. While the interface of the stand was necessary, the interface of different parts to create inputs and outputs was thought of as more important to see.

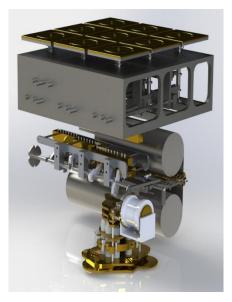


Figure 40: CAD Rendering of Final Design

During the design process, a serious concern was the loads parts would be able to handle. Due to the size constraints that the project needed to fall within, some parts such as the tines, were thousandths of an inch thick. While parts such as the tines were small, many did not transmit high loads, rather they served as a counting system where their displacement was a more important factor as the mass ratio of the tine to the pin it interfaced with was roughly 1:1.

## 4.1.1.2 Design with Intent to Manufacture

All parts that were drawn in SolidWorks had to be created with the intent of manufacturing. Drawing parts in SolidWorks that could not be machined simply wasted time. Therefore, all CAD parts were designed specific to the type of machining that would be used to create them i.e. CNC versus manual machining. While certain gears were close to the correct size and had the right number of teeth we needed, factors such as shaft diameter and overall diameter prevented the purchase of these parts. Knowing that similar products also existed, McMaster Carr was used to take the 3D models of parts that already existed for manufacturing and modifying them slightly to fit the needs of our design.

#### 4.1.1.3 Time Constraints

In order to complete as much of the project as possible, it was vital that machining of parts began by at latest mid B-term. Time spent designing parts that fit their correct tolerances for the model were made and most sub-assemblies were created and had proper interfacing. Given the amount of iterations of the model made before the final design was created, a final design was not confirmed until B- term. At this point, with the sheer volume of parts and interfaces needed to create a working 3D model some of the more complicated mates were left out. It was determined after discussion with the advising professor of the project that it was more critical to begin machining as soon as possible once a practical design was created. While all of the parts were created and put into one large assembly, not all of the parts interfaced correctly.

In order for the tines to be raised, interfacing with the tine block above them, the star gears needed to pluck along the holes of the punch card. However, the punch card in SolidWorks never had holes put in it so this feature of the final assembly did not allow for a simulation of playing the game.

## 4.1.2 Objective 2: Machining and Assembly

## 4.1.2.1 Budget

The majority of the tic-tac-toe machine was built in house requiring the purchase of bulk material and premade parts such as screws, bolts, etc. through McMaster Carr. Prices of parts resulted in the project using all of the money budgeted by WPI. Money was taken from other MQP groups that did not exhaust their funds and put towards the purchase of more materials for the project. Without completing the project and purchasing all of the necessary materials to finish, approximately \$1,300 was spent on materials.

## 4.1.2.2 Scrapped Parts

During the machining and assembly of the computer, there were many parts scrapped. As mentioned in previous sections, tolerances were expected to be very tight during machining. The scrap rate of parts made for the computer was approximately 35-50%. In order to decrease this number measures should have been taken for tighter tolerancing. Another reason for high scrap rate was that some parts were made in bulk. For this reason, one of each part used in a sub assembly was not made and tested as it was easier to repeat the same process over and over. Once all of the parts for a sub assembly were made they were tested and if one part did not fit the right constraints and had to be redesigned, it ended up being several of the same part wasted. A way to improve this in the future is make less of the bulk parts at once and first test samples of each part to make sure a portion of a system interfaces correctly.

Due to the time constraints driving the project, machining and assembly started while parts were still being refined. In some cases, there were engineering changes during the assembly process. While parts may have been designed in SolidWorks and worked in a software setting, it was realized that some parts would not interface exactly as needed in the physical world. For this reason, in some cases parts would be made and then it was discovered that changes needed to be made to the model that would result in parts requiring modification. In most cases, engineering changes happened before a part was made, but, on several occasions parts would be in the process of being made when it was decided modifications to them were required.

## 4.1.3 Objective 3: Testing and Repeatability

While the total computer was not fully assembled, specific sub-assemblies that were finished were able to be tested. These subassemblies and how they function are outlined below:

#### 4.1.3.1 Playing Tiles

The playing tiles interface with a rack and pinion surface when the top is pushed down vertically. The tile is held in place by the spring tab which rides in a slot on the top of the board that is spring loaded. The first batch of spring tabs that were made were too loose in the slots that were holding the system in place, causing for lack of interface between the rack and pinion and instead the tab would just more away from the pinion. These original section of the spring tab had two flat sides parallel one another with the other two sides being radial. The main problem of making the tab interface with the hole it had to travel through was that the clearance on the flat sides allowed for wiggle room. To fix this problem, a new set of spring tab pins were designed that had a rounded region that interface with the board having a hole concentric to the spring tab, limiting movement between parts.

#### 4.1.3.2 Tines

Once the tines were made and the connecting rivets were hand peened, they were tested with the hinge block that they interfaced with. Between each tine is two spacer blocks, both towards the front half that interfaced with the star wheel. During testing the tines were manually pushed to check if they interfaced correctly with the hinge block. The one flaw with the system is that due to the spacer blocks being at the front of the tines, the back end of them tends to walk and results in the tines next to one another pivoting and not remaining in parallel sets. In addition to the back end of the tines moving, there is too large of a difference in the tolerancing of all the tines. The tines were cut using a water jet and a different water jet needed to be used halfway through the cutting process. This affected the tolerancing of each tine. With each tine having a slightly different length, it is nearly impossible to get them to all interface with the star wheels properly.

#### 4.1.3.3 Crankshaft

The crankshaft was one of our sub-assemblies that was built successfully and is fully functioning. The crankshaft has four individual positions, all located at 90 degrees from one another, that allow the system to index between all four layers of the game. The crankshaft allows the computer to know what level the game is in to allow for the correct response. With a four position system, only one level of the game is interfacing with the output at a time and this allows the correct move to be read from the punch card as it rolls over the tines. Riding inside of the blocks were a series of pins. These pins are able to move vertically within the riding blocks to allow them to interface with the tines underneath and the arms above which indicate the output tile

the board responds with. These pins are contained within the riding blocks with 1/16th inch brass pins that were hand peened into each one and then turned down on the manual lathe. The reason for this is that each pin had a vertical stop placed and peened inside of it to restrict the motion within the riding block.

## 4.1.3.4 Indexing Gear Box

Once assembled, the gear box did not rotate with ease. All of the gears meshed with one another, but, causing the gears to rotate as an assembly did not work. To mediate this problem, the gears were turned within their assembly for several hours by hand to allow for the gears to wear into one another. All gears in this sub assembly were made of brass.

## 4.1.3.5 Gear Box Clutches

The assembly of the gear box was the last sub assembly put together before the project was stopped. While the lower portion of the gear box, listed in the section above, was able to move as intended, once the addition of the clutch mechanisms and more gears were added, the system ceased to work. The amount of torque and shearing that occurred did not allow for the gears to spin properly, resulting in some shearing between gears and their arbors and the system not working. This sub assembly had a total of 170 parts within it. The main cause of the sub assembly not being operational was tolerancing errors. Given the small scale parts were manufactured at, machining and being off by a couple thousandths on a surplus amount of parts adds up. While tolerancing errors on a couple parts would not be an issue, the stack up of slightly off parts was too much for the system to be able to overcome.

## 4.2 Conclusions

## 4.2.1 Challenges

## 4.2.1.1 Output

In the end, we were not able to finish what we set out to accomplish. We ran out of time and money to finish all of the parts required to make this a fully functioning, playable tic-tac-toe board. Another major issue we ran into was machine tolerancing. Due to the extremely small nature of the gears we made and the number of gears made, the gears did not all mesh perfectly and we ran into issues getting the gear box to spin freely. At that size, gears being off by just one or two thousandths of an inch create meshing problems that quickly add up when hand making that many gears.

#### 4.2.1.2 Punch Cards

In order for the data seen in the excel sheets in previous sections to be mechanically readable it was required that it was transformed into a binary code. While this took approximately two weeks to accomplish, the task of manufacturing the actual punch cards proved to be just as difficult as designing them.

In order for the design to work, the holes imprinted in the punch cards needed to be extremely accurate. It was determined that the most time efficient and precise way to go about this was having the card water jet cut. The holes were all cut in the proper locations once cut with the water jet, but, having to outsource the part to be cut outside of WPI campus did cause for a time delay in getting the part back.

The punch card was one of the last parts done during the machining process, meaning that the budget for the project was running dry and there was not enough money to buy enough material for nine spools. For this reason, one spool was bought and the outputs for a game assuming that the player pressed tile one first was made. While having all nine spools would be necessary for a complete machine, having one and starting with a specific tile would still be able to show that the computer was able to play through a game of tic-tac-toe. Due to time constraints, the cut spool was not rolled and placed in the sub assembly to interface with the tine system. One factor that was noted with the unrolled sheet of data was that there was some bends in the corners of the material. It is assumed that if the spool was rolled and used, there would be some deformation and bending that would not allow for the smooth rolling of data needed for the star gears to interface with the holes.

#### 4.2.1.3 Machining Availability

For the majority of the project, access to machines in Higgins shops, where the majority of manual machining was done had a vast amount of availability. However, in Washburn shops, where the majority of CNC machining was done, availability of different machines was limited. Machining was limited due to the shear demand of projects that needed computer aided machining done along with the presence of various lab groups, such as ME 1800, an introduction to machining course that had the CNC machines booked during regular business hours on Tuesdays and Thursdays, and an adult class that utilized machines in the mornings until 10:30 am multiple days per week. As CNC machining was CAM intensive, the staff of Washburn shops were often utilized

to review and aid in the CAM aspect of machining, meaning that time must have been reserved with the staff to have appointments to review programs before machining.

#### 4.2.1.4 Time

Like most projects, a limiting factor was time. While approximately 500 parts were able to be machined in house, the sheer magnitude of parts necessary to create a working model ultimately was too great for a completed machine. Factors to consider in loss of time include the time making parts that ultimately ended up being scrapped and available machine time. It was decided that it was imperative to begin parts during the design phase of the project that were likely to not change even if there were engineering changes, such as the playing tiles that the user interfaced with; regardless of if the mechanisms within the computer changed, the user would still press a board tile that was engraved with an "X" and "O."

## References

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## Appendices

## Appendix I: Analytical Engine

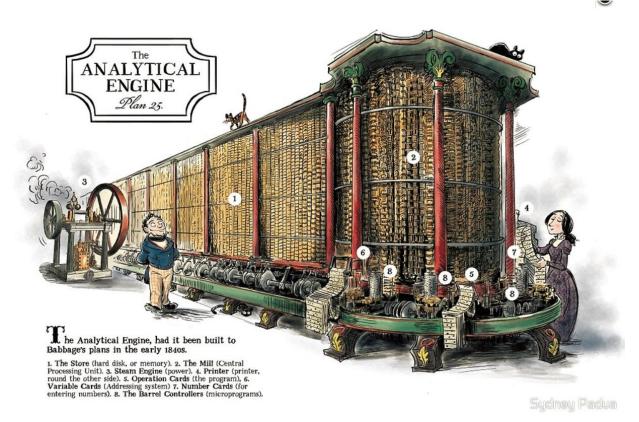


Figure 41: Analytical Engine [1]

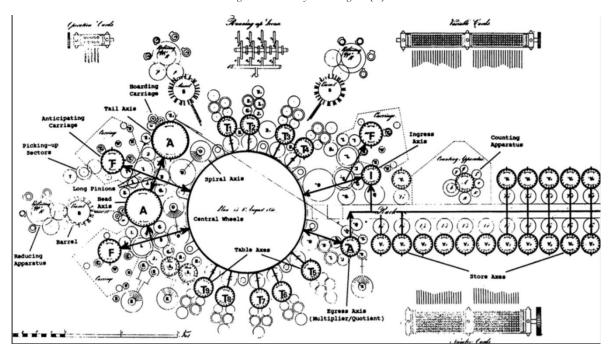


Figure 42: Analytical Engine [2]

Figure X: Engine [3]

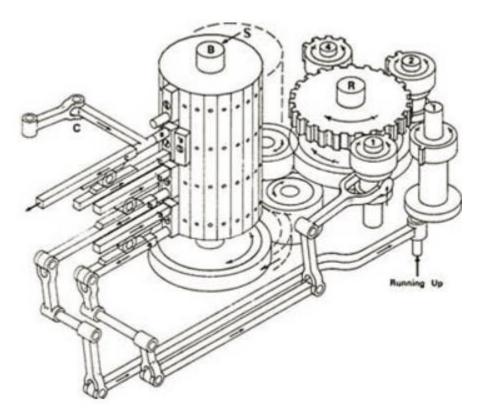


Figure 43: Analytical Engine [3]