



Predicting the Price of a Stock

An Interactive Qualifying Project

submitted to the Faculty of

WORCESTER POLYTECHNIC INSTITUTE

in partial fulfilment of the requirements for the degree of

Bachelor of Science

by

Steven Chelak

Date:

August 29, 2021

Project Advisor:

Professor Mayer Humi

This report represents the work of one or more WPI undergraduate students submitted to the faculty as evidence of completion of a degree requirement. WPI routinely publishes these reports on its web site without editorial or peer review. For more information about the projects program at WPI, see <http://www.wpi.edu/Academics/Projects>.

Table of Contents

Abstract	3
Executive Summary	4
Introduction	5
Research	6
Stock Prices	6
Drivers of Supply and Demand	6
Survey	6
Creation of Prototype Model	9
Stocks Selected	9
Autocorrelation	12
Linear Trendline	14
Fourier Series	16
Complete Prototype Model	17
Accuracy of the Prototype Model	19
Creation of the Moving Average Model	21
Accuracy of the Moving Average Model	24
Creation of the Volatility-Driven Model	25
Accuracy of the Volatility-Driven Model	27
Conclusion	28
Bibliography	29
Appendices	30

Abstract

This project seeks to create a model that can be used to make short-term predictions for the price of stocks. Stock prices depend on many different factors, which cannot all be implemented into a single model. Instead, the model created in this project will primarily rely on the patterns observed in historical stock data. These patterns, when combined with other model improvements, will allow investors to make an educated prediction for the price of a stock in the near future.

Executive Summary

There exists a need for investors to make educated decisions when trading in the stock market. Articles, podcasts, expert forecasts, and advice from friends are often the primary sources of information that new investors use to make their decisions. Mathematical models can also be used to help investors make informed choices with their assets. One benefit to using models is that their historical efficacy can easily be evaluated whereas other sources of information may require more baseless trust.

This project involves the construction and analysis of a prototype model as well as a few refinements that seek to improve upon the prototype model. The prototype model, utilizing linear trends and fourier series, was provided by Professor Humi as the groundwork of the project. This model is the result of previous research conducted by Professor Humi and the students he has advised on this project.

In addition to modeling, this project includes the execution of a research survey designed to analyze college students' investing habits. Fifty WPI students were surveyed in the Ruben Campus Center to get a better understanding of their stock market experience and tendencies. The research concludes that WPI students, by and large, do not attempt to invest in the stock market and would benefit from a mathematical model that they can trust.

In order to gauge the efficacy of the models in this project, several stocks were selected from the healthcare industry to test prediction quality. The historical period of Nov 2018 - Nov 2020 for each stock was used as the data input for the models. The prototype model, which utilizes solely historical stock prices as an input, was able to accurately predict prices up to roughly nine days into the future on average.

To improve upon the prototype model, a moving averages model and a volatility-driven model were created. By smoothing the historical stock data, the moving averages model aims to eliminate noise and better reveal underlying trends. The moving averages model did not demonstrate improvement over the prototype model, however the volatility-driven model was able to accurately predict stock prices up to roughly fourteen days on average, a noticeable improvement over the prototype model.

All modeling in the project was done using MATLAB and was completed from Fall 2020 to Summer 2021. One must consider the impact of the Covid-19 pandemic on the historical stock prices, especially since the stocks analyzed are in the healthcare industry. This project does not constitute professional investing advice. All investments contain risk, and one should not risk money they cannot afford to lose.

Introduction

Investing in the stock market is a very overlooked activity that thousands of young adults never attempt. Many fear the potential of losing large sums of money or believe that investing is too difficult for them to understand. While some people do lose everything in the stock market, there are ways to avoid such risk and have the odds in your favor. For example, the S&P 500, an index of the 500 largest companies in the US stock exchanges, has long-term annualized average returns of 10-20%.

I was inspired to take on this project because I want to develop a tool that myself and others could use to make more calculated investments in the stock market. Oftentimes, new investors will purchase and sell securities based on gut feelings or news articles they read online. The news they have “discovered” is likely already *priced into* the market. This leaves casual investors with few techniques for making educated short-term investments. Developing a new and effective technique has long been an interest of mine.

As a Mechanical Engineering major, it is important to develop methods and then evaluate the effectiveness of those methods. This project is particularly relevant to those skills, as it involves developing, improving, and evaluating a model. In any engineering project, the same steps are taken. Documentation of results and use of statistical analysis are valuable techniques that can be applied to a broad group of studies.

This project will provide me with valuable skills that I can use during the course of my career. Primarily, the ability to use a program like MATLAB is a skill that can be used at any job. It is important to clearly demonstrate, using figures and calculations, the significance of one’s findings. The skills used, for both conducting the analysis of this project and creating this report, will be immensely useful in future career roles.

This submission shall qualify as an *Interactive Qualifying Project (IQP)* at Worcester Polytechnic Institute (WPI). WPI defines an IQP as a project that solves a problem “at the intersection of science and society”. The stock market is a lively embodiment of our society, as its prices are governed by the Law of Supply and Demand. Any change in the world, good or bad, that impacts people has the ability to impact stock prices. Additionally, many people rely on investing as a means of generating both income and wealth for the future of their family. This project uses mathematical science to hopefully improve the wealth of small investors.

Research

Stock Prices

In order to begin predicting the price of stocks, one must first understand the factors that dictate the price of a stock at any given moment. At the base level, the price of a stock is determined by the supply and demand of that stock in the market. When there are many buyers that want to purchase a stock (high demand), the price of the stock generally increases. On the other hand, when many people are attempting to sell the stock, the price generally decreases. Companies may also adjust the scarcity of a stock by issuing more shares or purchasing back shares. These changes in supply can move the stock price, especially when large quantities of shares are involved.

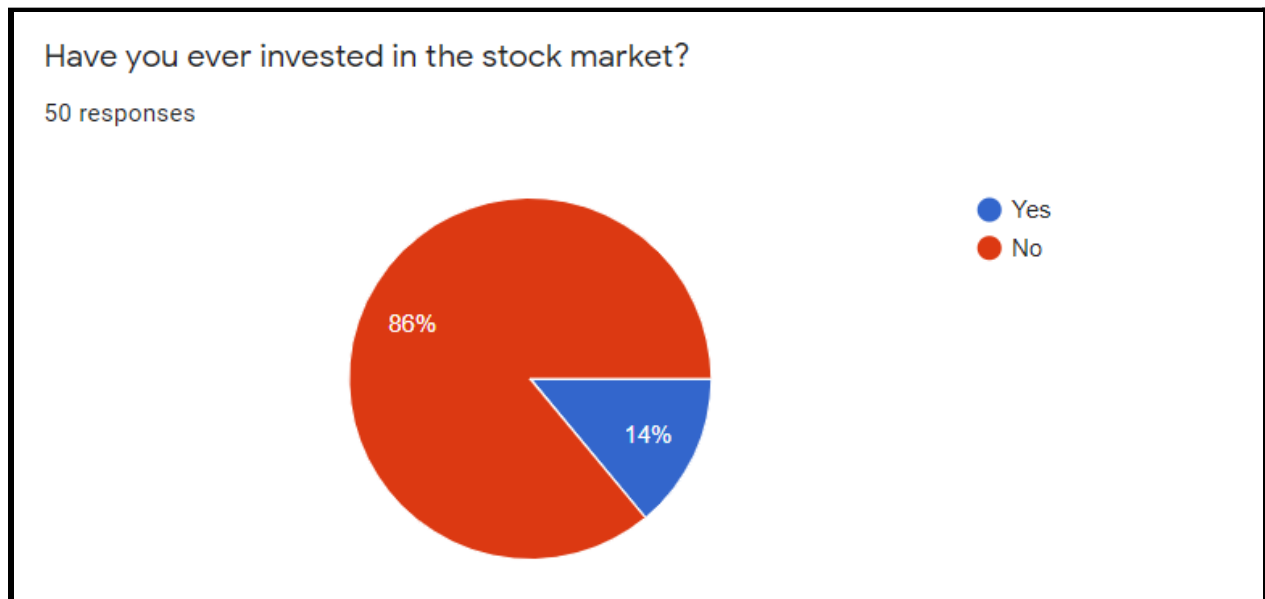
Drivers of Supply and Demand

There are many drivers of supply and demand when it comes to stocks. They might include earnings reports, company news, and orders made by politicians or other wealthy investors. When a company reports its earnings, stock prices are bound to react as investors either gain or lose confidence in the stock due to the company's changes in revenue and costs. Similarly, news articles and press releases can inform investors of reasons to buy or sell their shares. Some investors will try to mimic the moves made by people of status, such as politicians, as these people often have insider information regarding the future price of stocks. The more drivers that can be incorporated into a model, the more accurate predictions it will yield. However, it can be difficult to turn factors such as news articles into numerical values that can be used with a model. Additionally, some events can impact nearly the entire stock market such as the Covid-19 pandemic which caused a crash in March 2020.

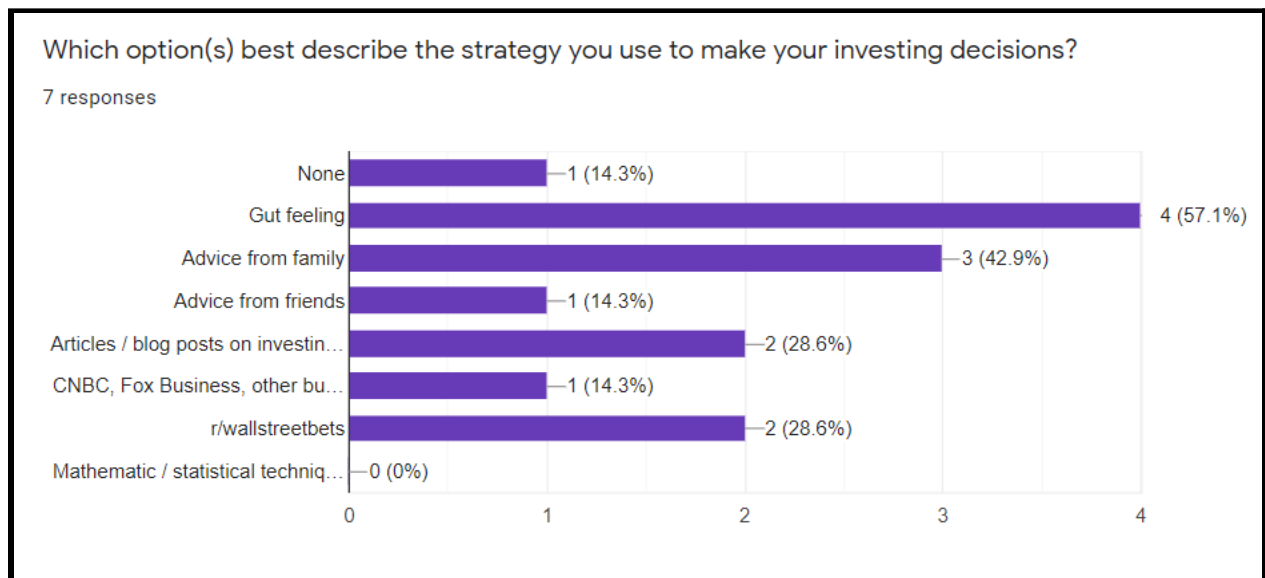
Survey

A survey was constructed in order to better understand the investing habits of college-aged individuals. The aim of the survey was to gauge trading activity, methods, and frequency among the population. Fifty WPI students were selected systematically from the Ruben Campus Center. Each table in the building was approached and asked to participate in a short survey. The process was repeated until fifty responses were collected. The sample is meant to be representative of the entire WPI student body. However, one might make the argument that the subset of students located in the Campus Center may be more social and more inclined to take risks than the average WPI student. This possibility is largely a result of the current Covid-19 pandemic, which has made leaving your dwelling a "risky" endeavor. This possible bias has been noted, although it is not believed to have a large impact on the survey results.

The first result worth noting is that 86% of students surveyed had never done any investing.



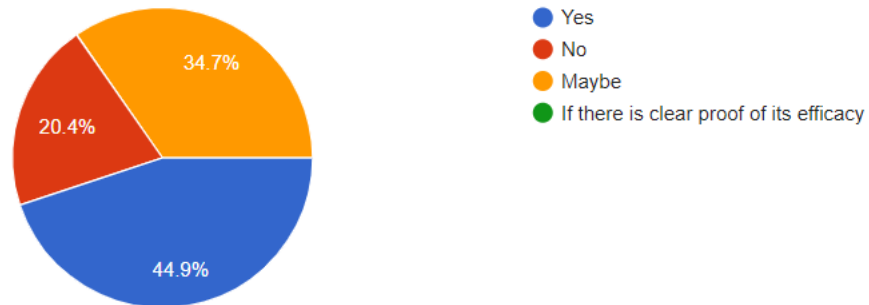
Among the 7 students that had invested, none of them had ever used a model to make predictions about the future prices of stocks.



And perhaps most important, a majority of students would be open to considering using a mathematical model to help inform their investing decisions.

Would you use a mathematical model to help make investing decisions?

49 responses



There is a clear willingness among students to learn more about the potential advantages of using a model to predict the future price of stocks. However, one would imagine that new investors would want to see proof that a model is reliable before trusting it to advise their transactions.

Creation of Prototype Model

The prototype model for near-future predictions serves as the groundwork for this project. Once the prototype model is created, several doors open regarding minor improvements and additional input factors. For this project, the prototype model was discovered in previous years' work, and the steps for creating it were provided by Professor Humi. However, MATLAB is not a program of intuitive use, so the development of the prototype model proved to be a challenging task, providing important lessons in MATLAB and overall familiarity with the program.

Stocks Selected

The first step in creating the model was selecting stocks to study. The following 16 securities were selected:

- **Johnson & Johnson (JNJ)**

Johnson & Johnson is a multinational corporation founded in 1866 that engineers consumer health products, medical devices, and pharmaceuticals. It owns several household brands such as Tylenol, Motrin, and Zyrtec as well as many surgical devices and standard hospital equipment. It is one of the most prominent companies in the sector, which is why the value of its stock is expected to grow.

- **Gilead (GILD)**

Gilead Sciences is an American pharmaceuticals company that focuses on antiviral drugs. Additionally, Gilead has become involved in Coronavirus treatments, including the drug Veklury and antiviral “cocktails”. The company is a giant that employs 11,800 people, so it should be relatively stable in years to come.

- **Becton Dickinson (BDX)**

BD is multinational medical device company that produces equipment and disposable devices for hospitals and clinics. BD recently acquired Bard Medical. BD's lineup includes a plethora of devices found in hospitals, and BD continues to have very large contracts with hospitals and clinics around the world. Overall, there are positive prospects.

- **Medtronic (MDT)**

Medtronic, headquartered in Ireland for tax purposes, is an American medical device company that produces instruments for a large variety of health needs, including surgery. Medtronic devices are commonly found in hospitals and clinics. Medtronic is a growing

company with positive prospects that may one day have the name recognition of companies like JNJ.

- **Hologic (HOLX)**

Hologic is a medical device company focused on Women's Health. Headquartered in Massachusetts, it is at the forefront of engineering Breast Cancer and GYN health devices. Hologic acquired Cynosure and then sold it shortly afterwards, netting a substantial loss.

- **Boston Scientific (BSX)**

Boston Scientific is a medical device company that focuses on instruments for interventional procedures. The company is best known for its stent, a device used to open blood flow in failing arteries. Boston Scientific is seeing steady increases in its financial metrics and is outperforming smaller interventional device companies.

- **ICU Medical (ICUI)**

ICU Medical is a California-based medical device company that specializes in vascular therapy, oncology, and critical care applications. ICU's technology is designed to prevent bloodstream infections. This is accomplished through their advanced IV therapy products.

- **Fresenius Medical Care (FMS)**

Fresenius Medical Care is the leader in the world of Kidney Dialysis. Their Dialysis devices are found in hospitals across the country. Prospects for Fesenius are quite good, as kidney dialysis remains to be a much needed treatment.

- **Abbott Laboratories (ABT)**

Abbott Laboratories is an American medical supplement company. Its products include baby formula and mineral-rich supplements to aid in preventing dehydration. It is perhaps best known for its nutritional aid Pedialyte, among other products. Abbott also has an extensive device lineup, with many cardiovascular products. ABT is a S&P 100 component.

- **Cardinal Health (CAH)**

Cardinal Health, a medical solutions company, is the 14th largest revenue generating company in the USA. Its products are found in 90% of hospitals in the country. Cardinal Health is a S&P 500 component that has made several acquisitions over the years. Its

main function is production and distribution of medical devices and equipment. CAH has a positive outlook.

- **Stryker (SYK)**

Stryker is a medical technology company based in Michigan. Its products include hospital beds, surgical instruments, and other specialty devices. Stryker's joint replacement technology is at the forefront of the market. The company is a S&P 500 component.

- **Edwards Lifescience (EW)**

Edwards, based in California, specializes in artificial heart valves. It also designs devices related to other cardiac functions. Edwards acquired CAS Medical Systems in 2019 and continues to specialize in heart valves. The company is a S&P 500 component.

- **Varian Medical Systems (VAR)**

Varian specializes in cancer treatments through radiation. Its products include software and hardware-related devices. Cancer detection, through high end x-ray and scanning devices is one of Varian's main specialties. A leader in radiotherapy, Varian has strong potential to continue growth.

- **Danaher (DHR)**

Danaher is an American conglomerate that holds many medical science and industrial companies. It mainly focuses on environmental quality and general life sciences. Danaher also has some diagnostics divisions. It is a S&P 100 component.

The stocks were selected for a number of reasons. Firstly, they are securities in the healthcare industry. Studying the market in one particular industry narrows down the amount of variables that could potentially disrupt the accuracy of models created. The stocks are also priced between roughly \$20 - \$250 per share. Selecting stocks with similar prices may also improve the chances of creating an accurate model of their behavior. Lastly, these stocks were selected as their historical prices seem to reflect market factors rather than displaying massive volatility from unpredictable events.

For creating the prototype model, 502 days of historical closing prices were downloaded from Yahoo Finance and saved as a CSV file for each stock. Two years of data was deemed a sufficient quantity to create a model.

Autocorrelation

The first step towards creation of the prototype model is *autocorrelation*. The autocorrelation function (ACF) is used to measure the similarity of data points over time. Starting with the most recent point, the function examines the correlation of the point with the point before it, continuing to add one point at a time. As the lag (the number of points from the most recent one) increases, the autocorrelation usually decreases in value.

$$r_k = \frac{\sum_{i=1}^{N-k} (Y_i - \bar{Y})(Y_{i+k} - \bar{Y})}{\sum_{i=1}^N (Y_i - \bar{Y})^2}$$

Figure 1: The autocorrelation function

The ACF is used in the prototype model to determine a relevant period, the number of days into the past that each stock's closing prices demonstrates a non-zero correlation.

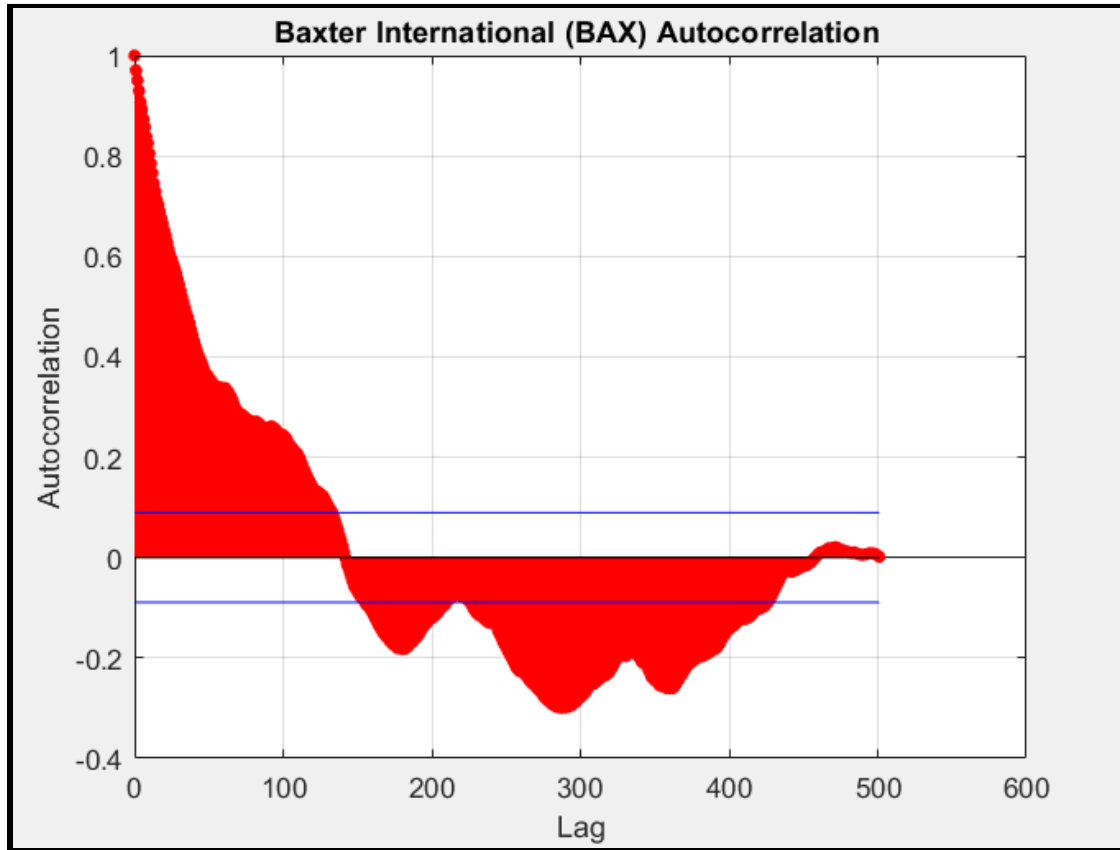


Figure 2: Autocorrelation on BAX

The ACF performed above reveals a relevant period of 143 days into the past (x-intercept). This relevant period will become the subset of data used for the rest of the prototype model steps. The reason for this being that the prototype model seeks to utilize the direction in which the price is currently trending.

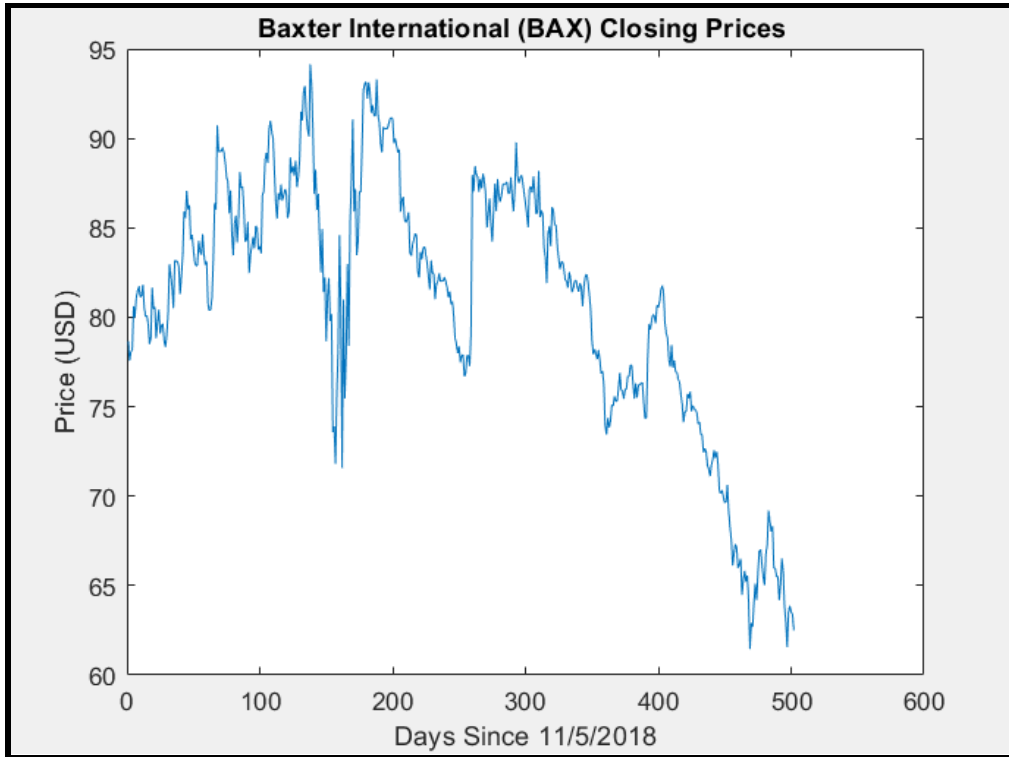


Figure 3: BAX closing prices

The findings of the ACF can be visually confirmed using the graph of closing prices. A substantial correlation can be seen 143 days into the past on the graph above (starting at $x=500$ and looking left).

Linear Trendline

With the relevant period of each stock determined, the next element of the prototype model is a simple linear trendline. The regression equation, $y = a + bx$, for the trendline is found using the following formulas.

$$a = \frac{(\sum y)(\sum x^2) - (\sum x)(\sum xy)}{n(\sum x^2) - (\sum x)^2}$$

$$b = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2}$$

Figure 4: Coefficients of linear regression



Figure 5: Relevant period of ABT with linear regression

The linear regression composes half of the prototype model. The next element of the prototype model is creating a model of the residuals from the linear regression. As seen above, the residuals appear to oscillate above and below the trendline.

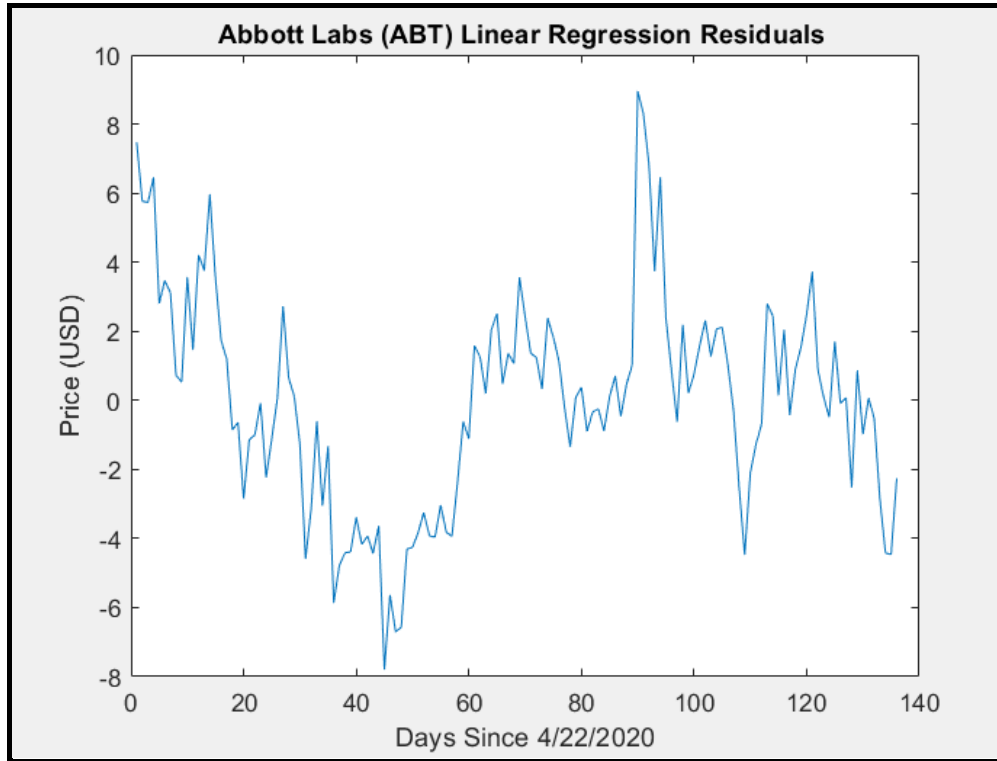


Figure 6: The residuals from Figure 4

Fourier Series

Fourier Series are used in the prototype model to model the residuals from linear regression, such as the residuals shown above. A Fourier series is a periodic function that combines sine and cosine waves in a process known as weighted summation. Fourier series are mainly used for signal processing (such as with sound or electromagnetic waves) and approximation, the latter of which will be utilized extensively in the model. The basic composition of a Fourier series is shown below, where a_0 , a_n , and b_n are coefficients derived from the integrals displayed in Figure 7.

$$f(x) = \frac{1}{2} a_0 + \sum_{n=1}^{\infty} a_n \cos(nx) + \sum_{n=1}^{\infty} b_n \sin(nx),$$

Figure 7: Fourier Series

$$\begin{aligned}
 a_0 &= \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) dx \\
 a_n &= \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cos(nx) dx \\
 b_n &= \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \sin(nx) dx
 \end{aligned}$$

Figure 8: Fourier Coefficients

Applying a three-term Fourier series to the residuals and adding the series to the linear regress of the relevant period yields the prototype model.

Complete Prototype Model

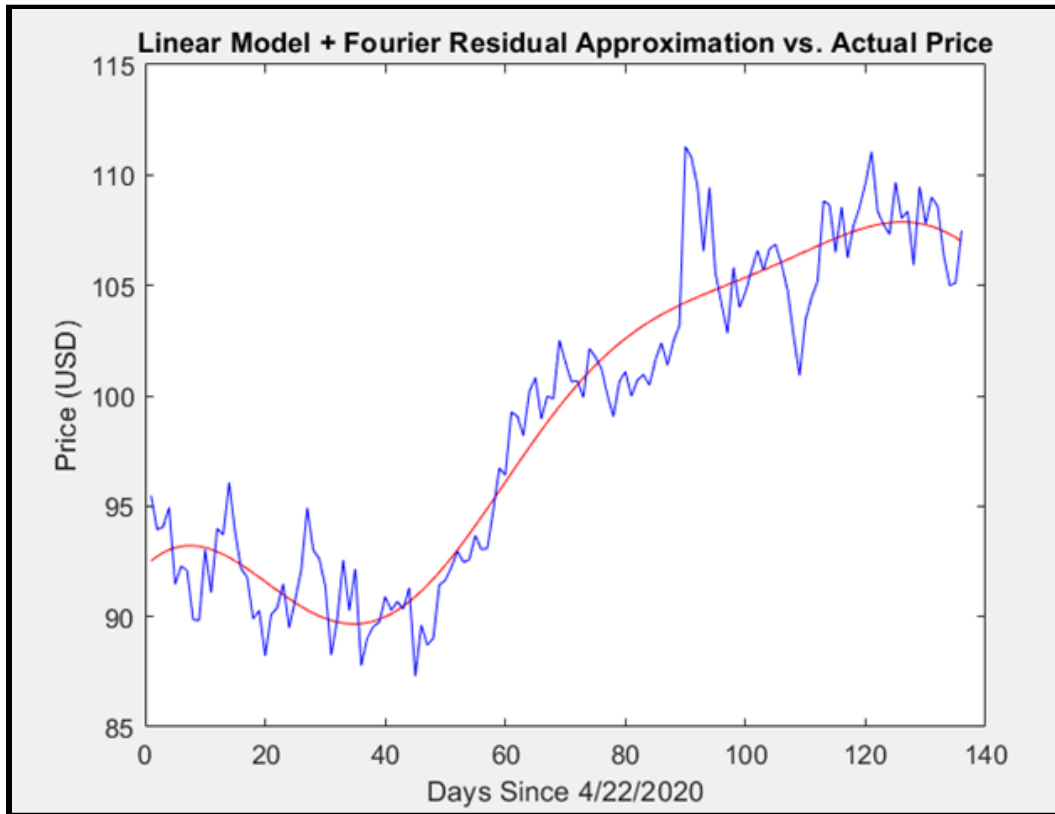


Figure 9: The prototype model for the relevant period of ABT

In order to use the prototype model to make predictions, a noise band around the model was created to reflect the maximum and minimum residuals obtained from the data used to create the model.

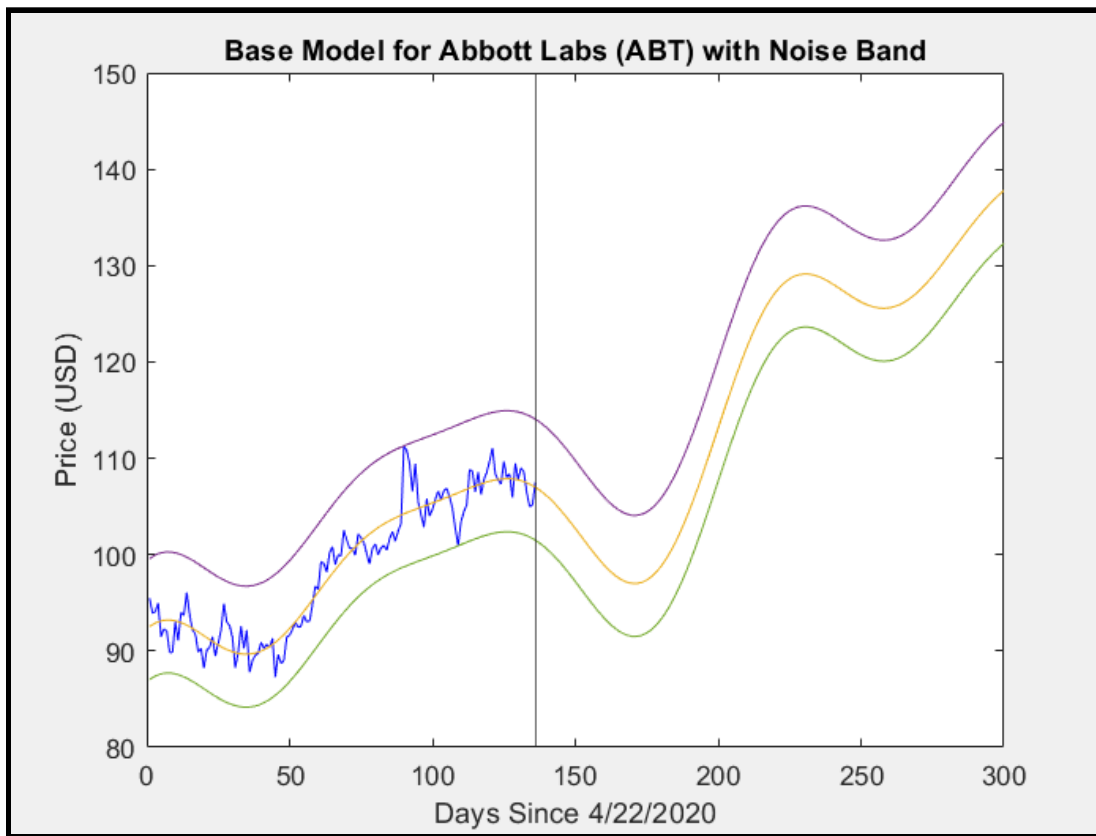


Figure 10: Base model for ABT with Noise Band

Accuracy of the Prototype Model

In order to determine the accuracy of the prototype model, future stock data was compared to the model and the number of days that the future data remained in the noise band was noted. The model, on average, was able to provide a reasonable prediction for up to 9 days into the future.

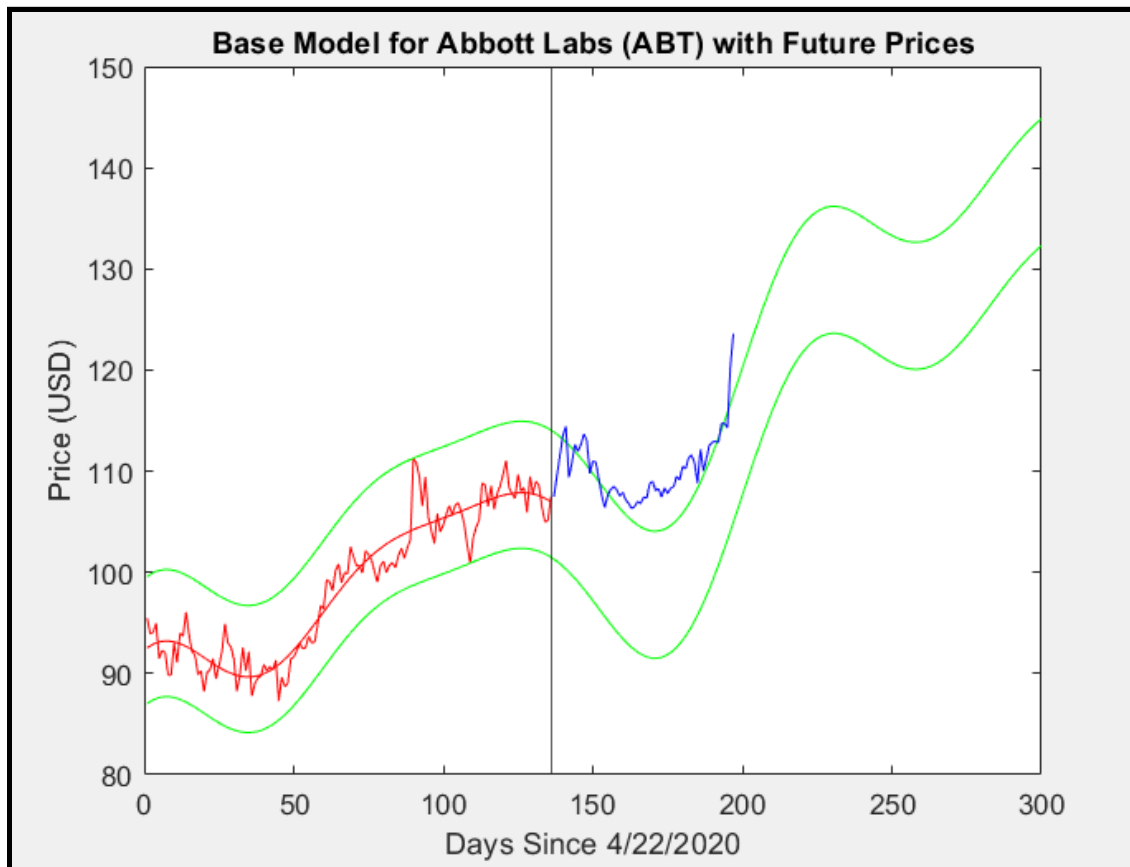


Figure 11: The future prices for ABT remain within the noise band for 4 days.

The vertical line in Figure 8 indicates the point at which the stock prices switch from historical to future. The historical prices were used to create the prototype model. The future prices are independent from the model and are the prices which the model seeks to accurately predict.

Model	Days In Band
ABT1	4
BAX1	16
BDX1	3
BSX1	6
CAH1	1
DHR1	6
EW1	6
FMS1	4
GILD1	3
HOLX1	6
ICUI1	10
JNJ1	56
MDT1	6
SYK1	6
VAR1	4
ZBH1	6
mean	8.94
median	6
standard deviation	12.58

Table 1: Prediction quality of prototype model

The prototype model, as expected, was unable to predict very far into the future. In order to improve the accuracy of predictions, several measures were considered. The hypothesis was that market indices, such as the NASDAQ Composite, could be utilized. One way of doing so would be to project the index into the future, using the same method as the prototype model, and then use that projection to influence the projection of an individual stock. The influence could be weighted by considering the correlation coefficient of the stock's closing prices and the index's closing prices.

Creation of the Moving Average Model

In order to improve upon the prototype model, the implementation of moving averages was considered. The moving average technique smooths the stock data in an attempt to better represent price trends by minimizing the impact of the inexplicable “noise” in the data. The moving average function works by replacing the raw data points with the corresponding average value of 10 days before and after said data points.

```
[n,m]=size(ABT(:,5))
tend=n
for i=10:tend-10
    az=0;
    for j=1:20
        az=az+prclose(i+j-10);
    end
    prsmooth(i)=az/20;
end
```

Table 2: Moving average technique in MATLAB

Table 2 displays the moving average portion of the MATLAB script for the moving average model. The closing price data points are smoothed using the average value of a 20-day window centered on each point. The smoothing is not applied to the first and last 10 data points because it is not possible to fit a 20-day window around them.

With the data smoothed, the moving average model is then created in the same manner as the prototype model. The aim of the smoothing being to negate the effects of minor fluctuations in the stock price in order to better represent the underlying trends.

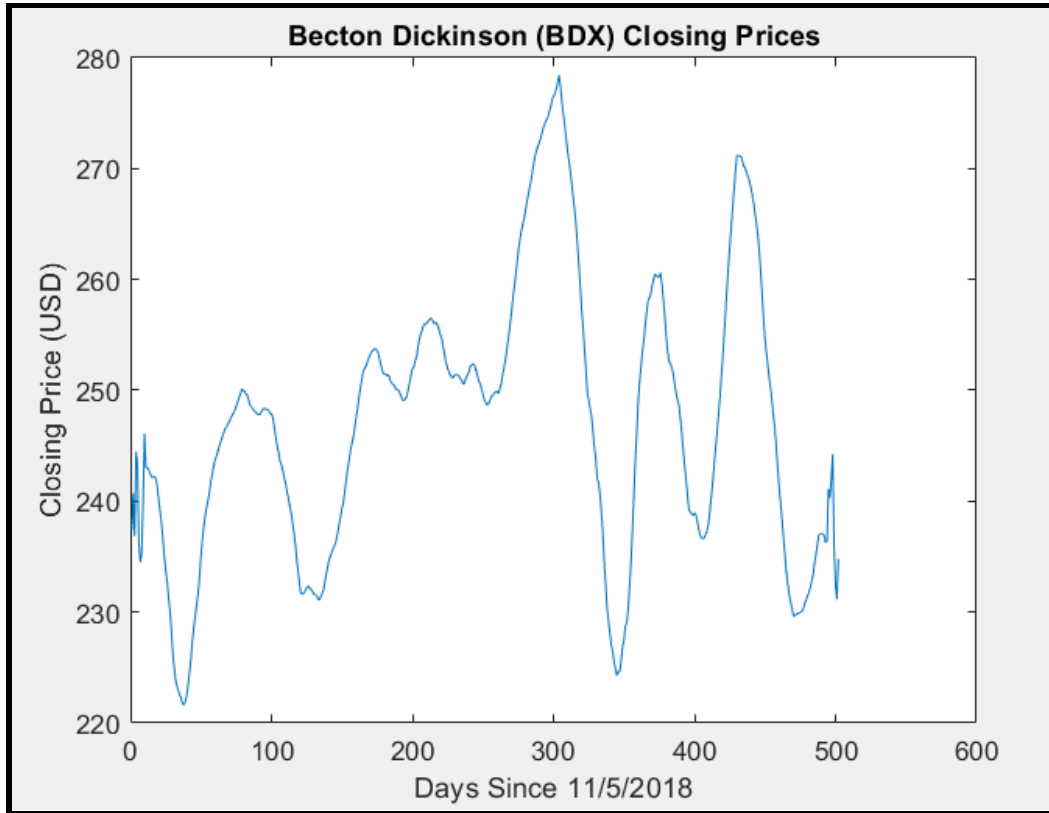


Figure 12: The BD Closing Prices after smoothing

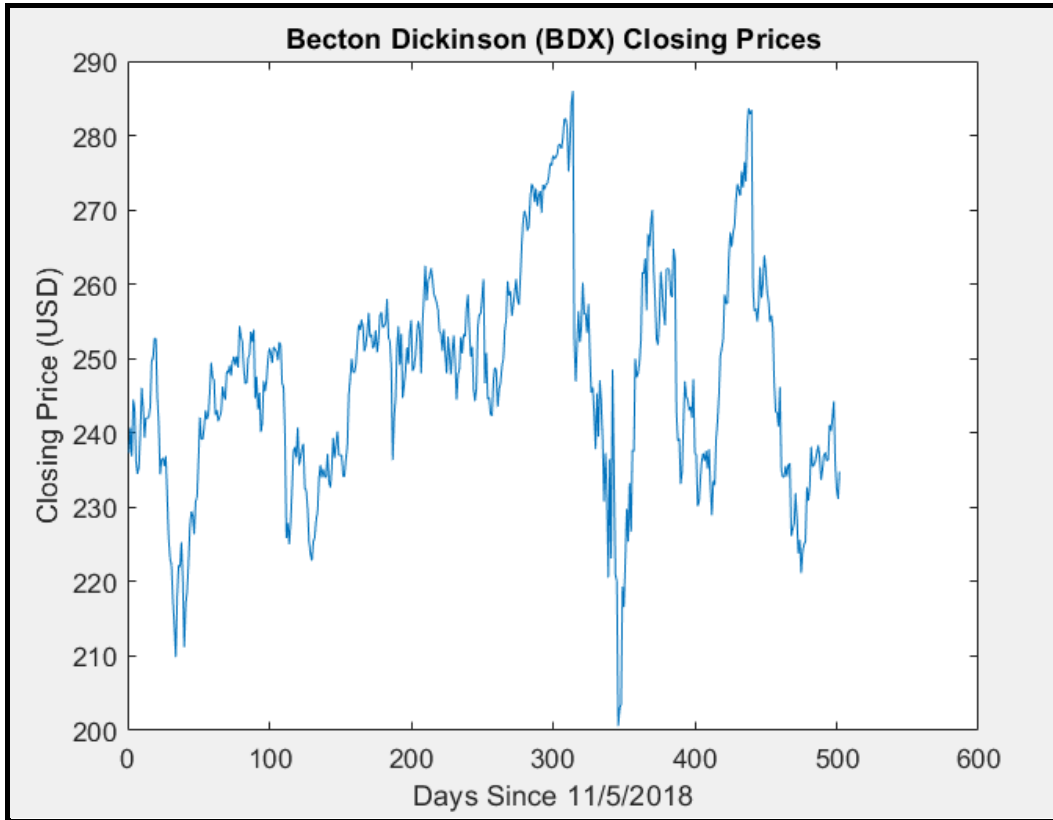


Figure 13: The BD Closing Prices before smoothing

Accuracy of the Moving Average Model

In order to determine the accuracy of the moving averages model, future stock data was compared to the model and the number of days that the future data remained in the noise band was noted. The model, on average, was able to provide a reasonable prediction for up to 4 days into the future.

Model	Days In Band
ABT2	3
BAX2	3
BDX2	4
BSX2	1
CAH2	1
DHR2	6
EW2	5
FMS2	2
GILD2	2
HOLX2	4
ICUI2	4
JNJ2	16
MDT2	6
SYK2	5
VAR2	3
ZBH2	1
mean	4.13
median	3.5
std deviation	3.46

Table 3: Prediction quality of moving average models

Unfortunately the moving average model did not improve upon the prototype model. This would appear to indicate that the prediction error associated with the prototype model is not a direct result of the noises in the price trends.

Creation of the Volatility-Driven Model

The volatility of a stock is a good indicator of how drastically one can expect the stock's price to change over a period of time. Volatile stocks are known for their prices undergoing significant changes in short amounts of time, while stocks that are not volatile tend to behave more predictably and have less noise in the data.

One measure of volatility is standard deviation. The standard deviation of a stock's historical closing prices is calculated as follows.

$$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{N}}$$

σ = population standard deviation
 N = the size of the population
 x_i = each value from the population
 μ = the population mean

Figure 14: Standard deviation formula

Stocks whose closing prices have a higher standard deviation over a historical period are considered more volatile. In order to incorporate standard deviation into the model, it was decided that the historical volatility of the stock should be used to adjust the impact of the fourier series from the prototype model. Stocks with higher volatility, and therefore more noise, may be better modeled by a fourier series as the fourier series is the modeling element that attempts to model the unexplained variation in the stock prices. The linear trendline will still be the backbone of the model; it is simply the fourier series that is adjusted.

On the other hand, stocks with low volatility are likely best modeled by the linear trendline as one does not expect them to behave as erratically. Therefore, each stock's standard deviation was converted to a relative volatility coefficient that was multiplied by the fourier series from the prototype model. Relatively volatile stocks would have a coefficient greater than one, increasing the effect of the fourier series, while relatively stable stocks would have a coefficient greater than zero and less than one, diminishing the effect of the fourier series.

The relative volatility coefficient for each stock was calculated by first finding the standard deviation of each stock's historical closing prices and then calculating a mean standard deviation for all sixteen stocks. Each standard deviation was then divided by the mean standard deviation, yielding the relative volatility coefficient (RVC).

$$RVC_{\text{stock}} = \sigma_{\text{stock}} / \mu_{\text{SD of all Stocks}}$$

Stock	Standard Deviation	Relative Volatility Coefficient (SD / mean SD)
abt	10.5415	0.847608475
bax	7.2516	0.583078084
bdx	14.6929	1.181409341
bsx	3.4447	0.276977367
cah	4.0798	0.328043737
dhr	32.3971	2.604947733
ew	9.8207	0.78965124
fms	3.4974	0.281214806
gild	4.872	0.391742019
holx	8.0968	0.651037926
icui	29.5052	2.372419255
jnj	7.818	0.628620505
mdt	9.4647	0.761026413
syk	18.9422	1.523082034
var	19.4112	1.560792831
zbh	15.1523	1.218348233
mean	12.43675625	

Table 4: Calculating relative volatility coefficients

```

for x=1:300
    prd(x)=p(1)*x+p(2)+0.847608475*f(x);%relative volatility coefficient%
end

```

Table 5: A relative volatility coefficient multiplied by the fourier series in MATLAB

Accuracy of the Volatility-Driven Model

In order to determine the accuracy of the volatility-driven model, future stock data was compared to the model and the number of days that the future data remained in the noise band was noted. The model, on average, was able to provide a reasonable prediction for up to 14 days into the future. This was a noticeable improvement upon the prototype model.

Model	Days In Band
ABT3	5
BAX3	48
BDX3	4
BSX3	44
CAH3	3
DHR3	6
EW3	6
FMS3	7
GILD3	7
HOLX3	6
ICUI3	7
JNJ3	56
MDT3	6
SYK3	6
VAR3	5
ZBH3	6
mean	13.88
median	6
stdev	17.20

Table 6: Prediction quality of the volatility-driven model

It appears that by adjusting the influence of the fourier series, the model was able to make better predictions for most stocks.

Conclusion

Predicting the price of stocks is not easy. If there was a sure way to do it, investing would change drastically and everybody would partake. While many good modeling methods have been invented in the decades since the required technology became available, nobody has come close to fully “cracking the code”. Models for stock prices are limited by the number of inputs they have. In the case of this project, the models were limited to only making predictions based on historical stock data. Other sources of information have the potential to improve the model predictions, however some are easier to incorporate than others. For example, one can factor in trends in market indices, but it would be much harder to factor in something like comments from a popular investing talk show.

This project aimed to create and improve upon a model that can make short-term predictions for the future price of stocks. The models were able to do so, but one must consider the substantial margin of error that is the noise band. The model is not believed to be a standalone source of investing information, but it may be paired with other sources to aid short-term decision making.

The real success in this project would be the wealth of knowledge it has generated in the area of MATLAB programming and general modeling techniques. These skills are very useful and will surely be of benefit in the future.

Bibliography

“Autocorrelation Function.” *Autocorrelation Function - an Overview | ScienceDirect Topics*, www.sciencedirect.com/topics/chemistry/autocorrelation-function.

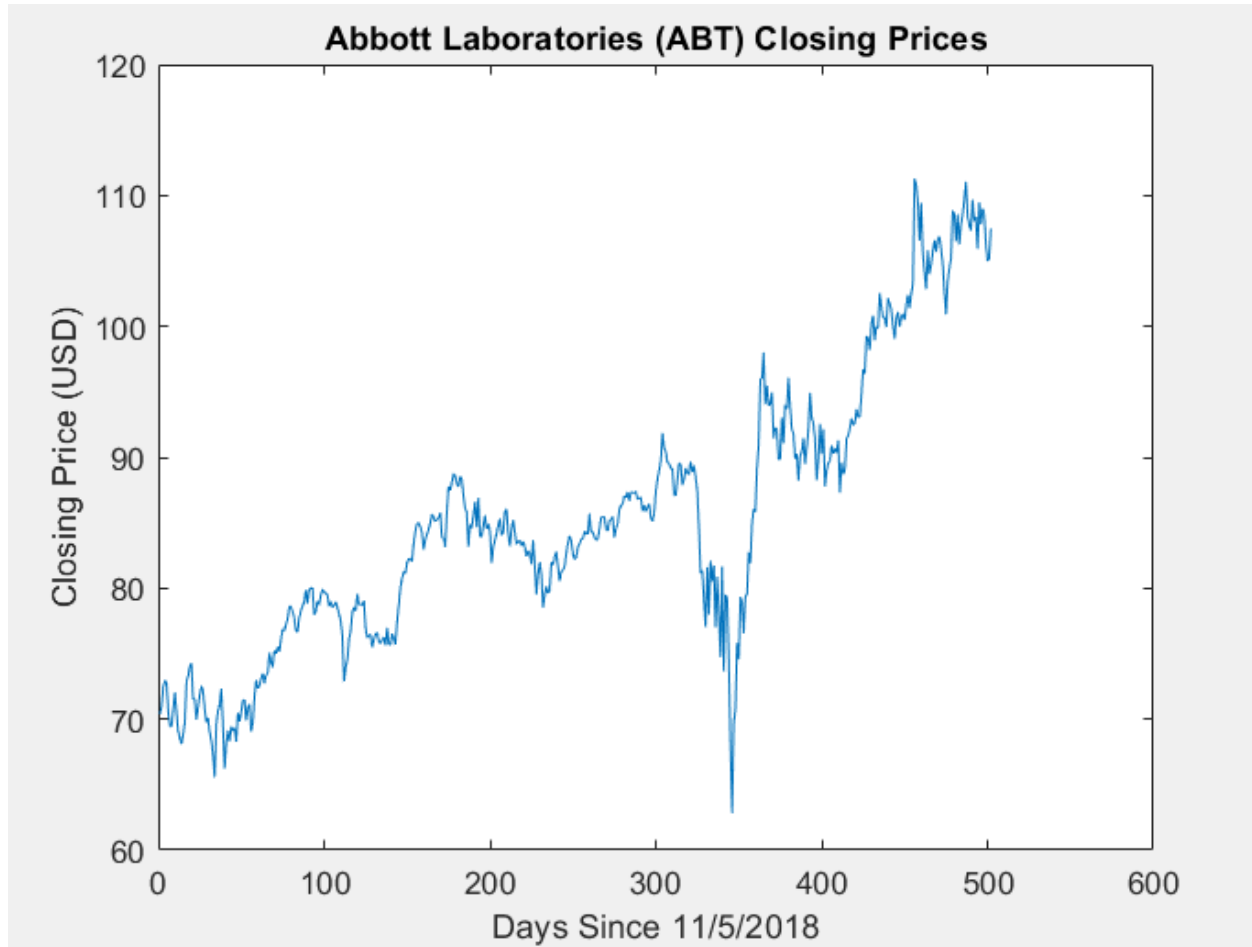
Fernando, Jason. “Moving Average (Ma) Definition.” *Investopedia*, Investopedia, 10 Aug. 2021, www.investopedia.com/terms/m/movingaverage.asp.

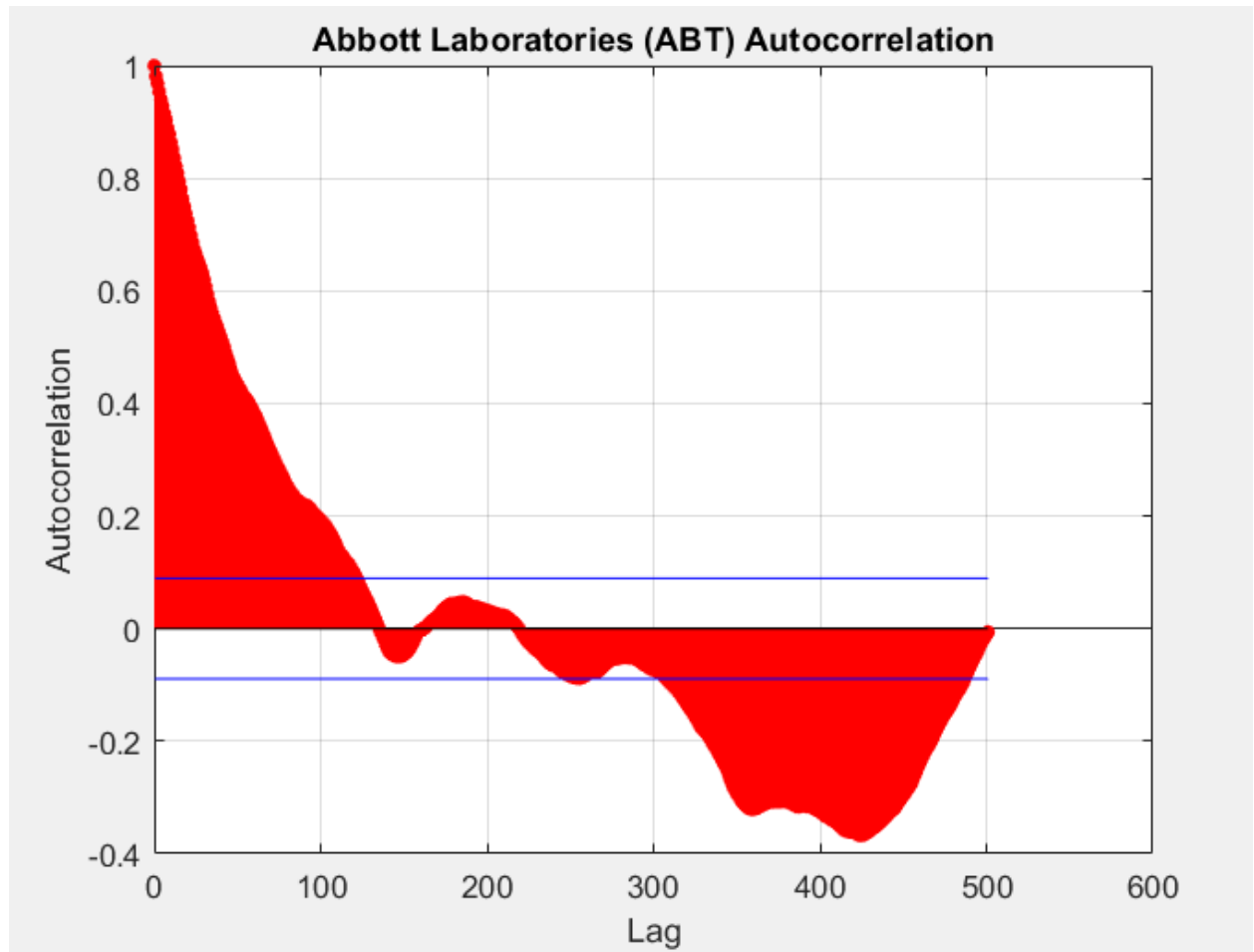
“Fourier Series.” *From Wolfram MathWorld*, mathworld.wolfram.com/FourierSeries.html.

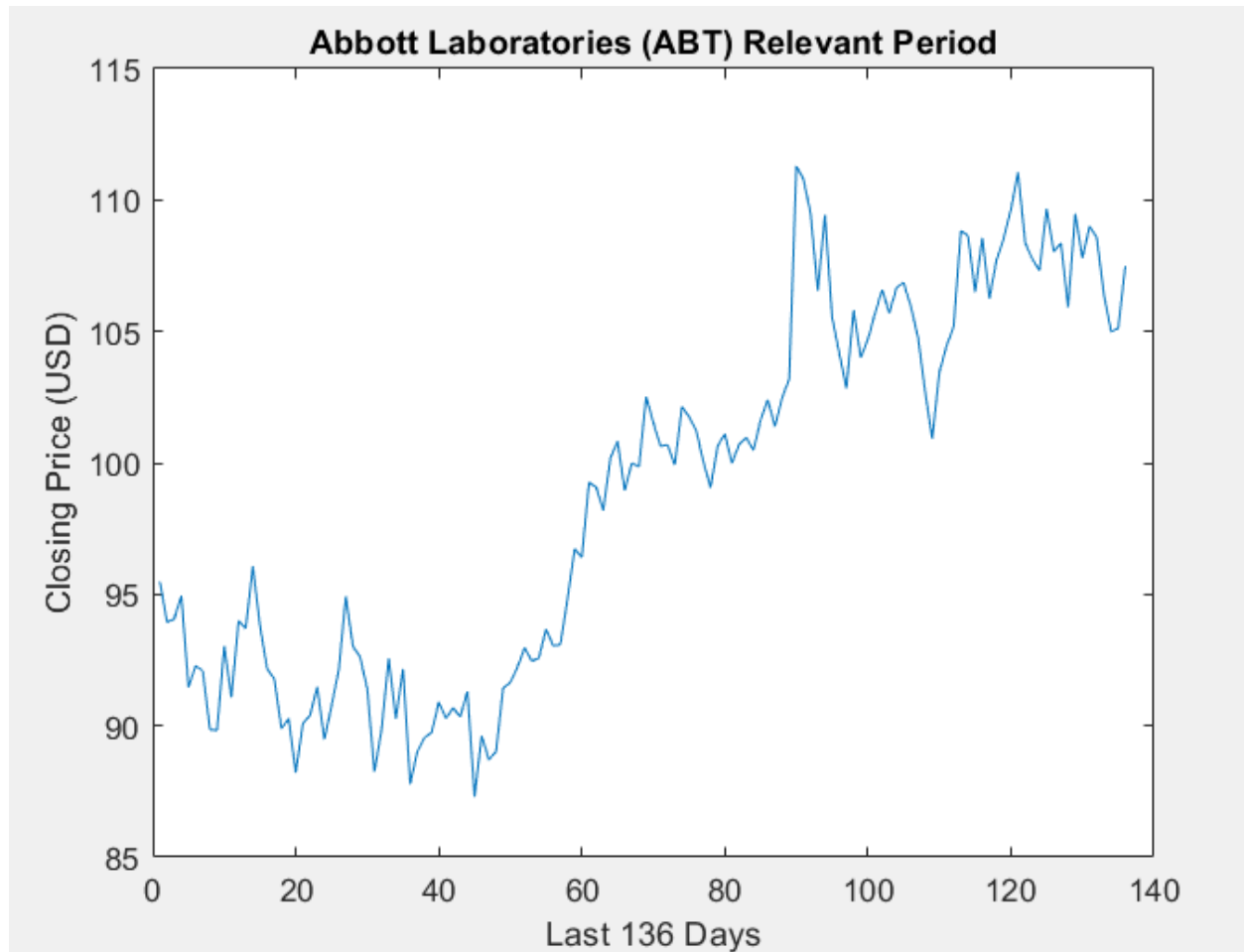
“Matlab.” *MATLAB Documentation*, www.mathworks.com/help/matlab/.

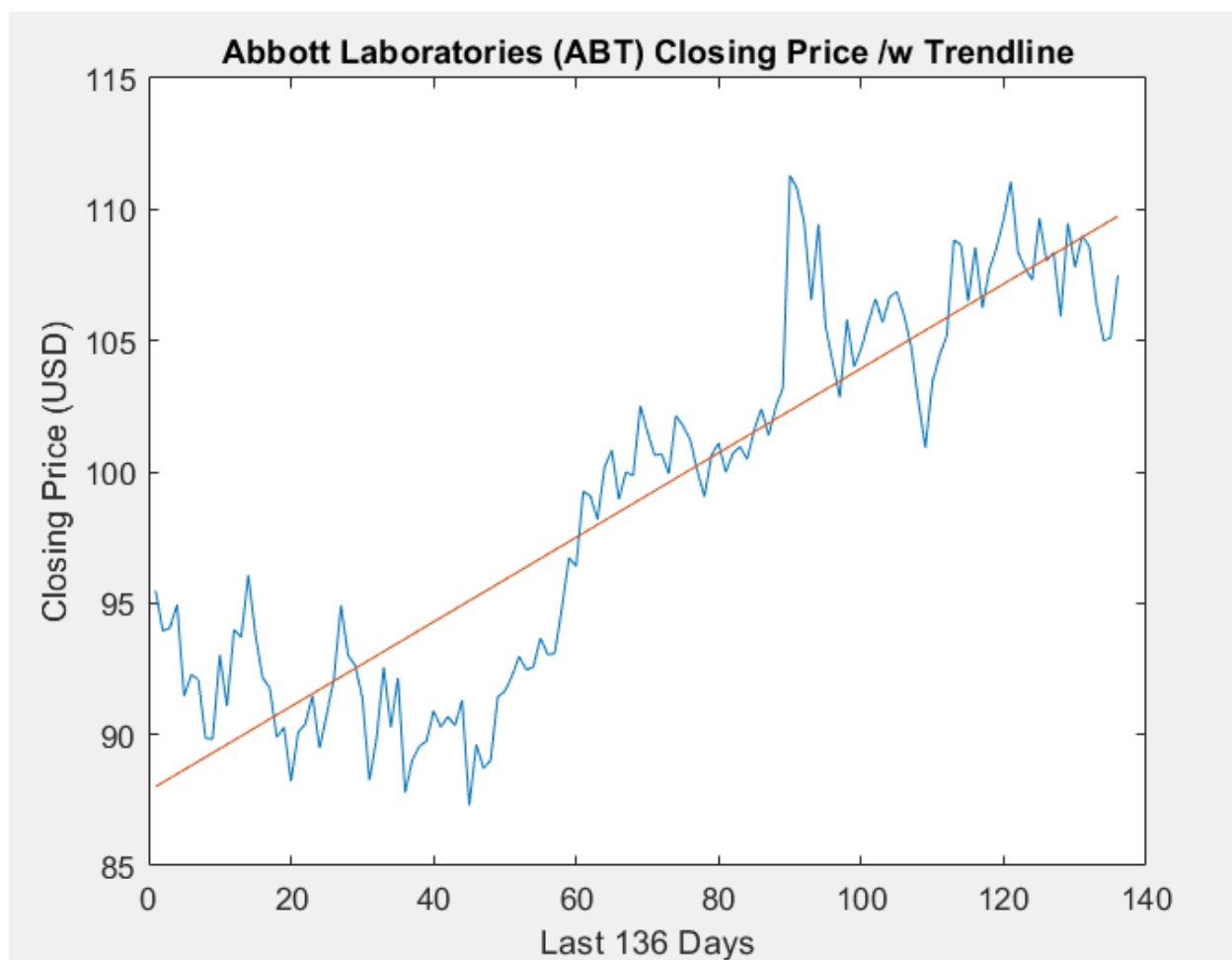
Wohlner, Roger. “How Are Stock Prices Determined?” *TheStreet*, TheStreet, 30 Jan. 2020, www.thestreet.com/markets/how-are-stock-prices-determined.

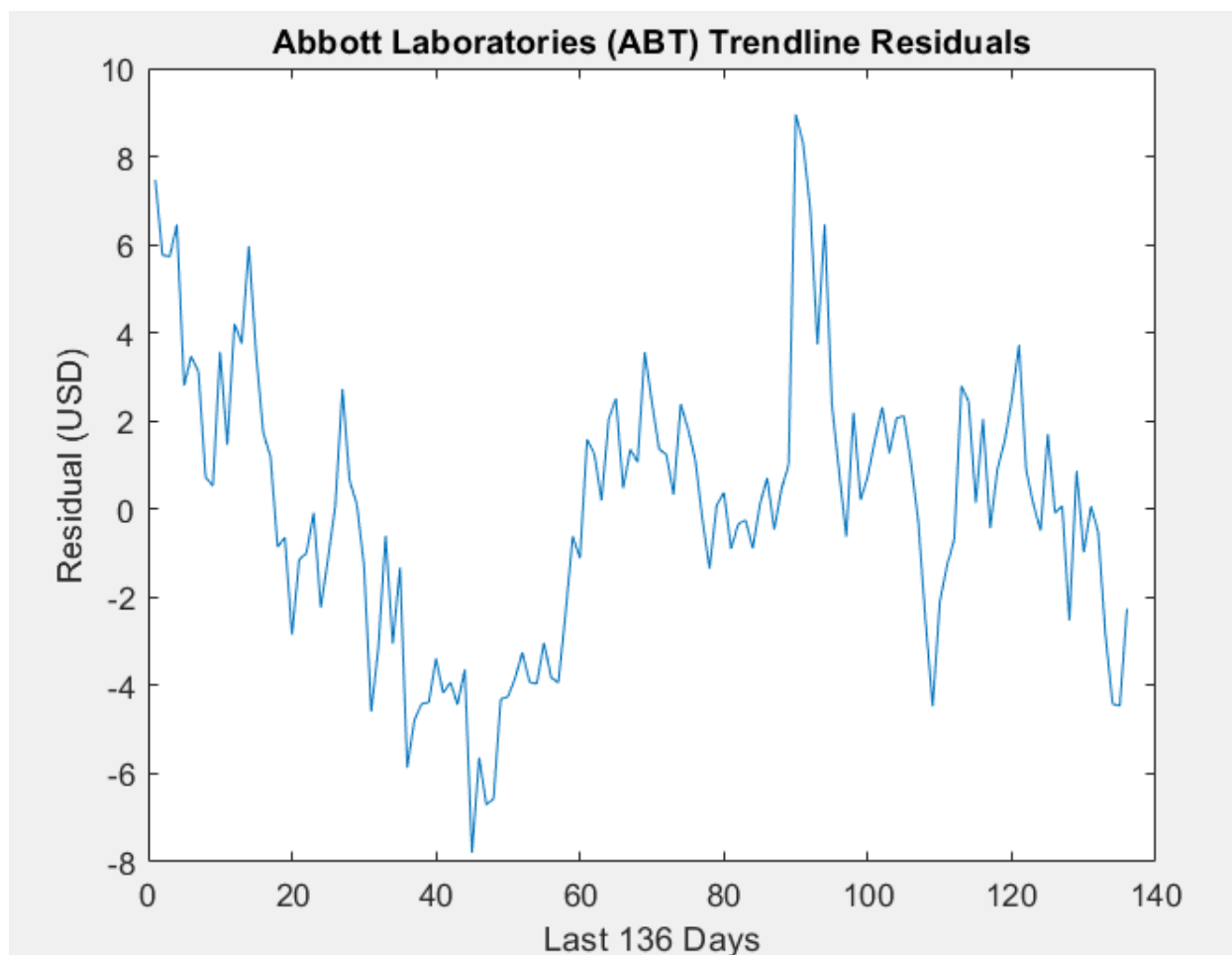
Appendices

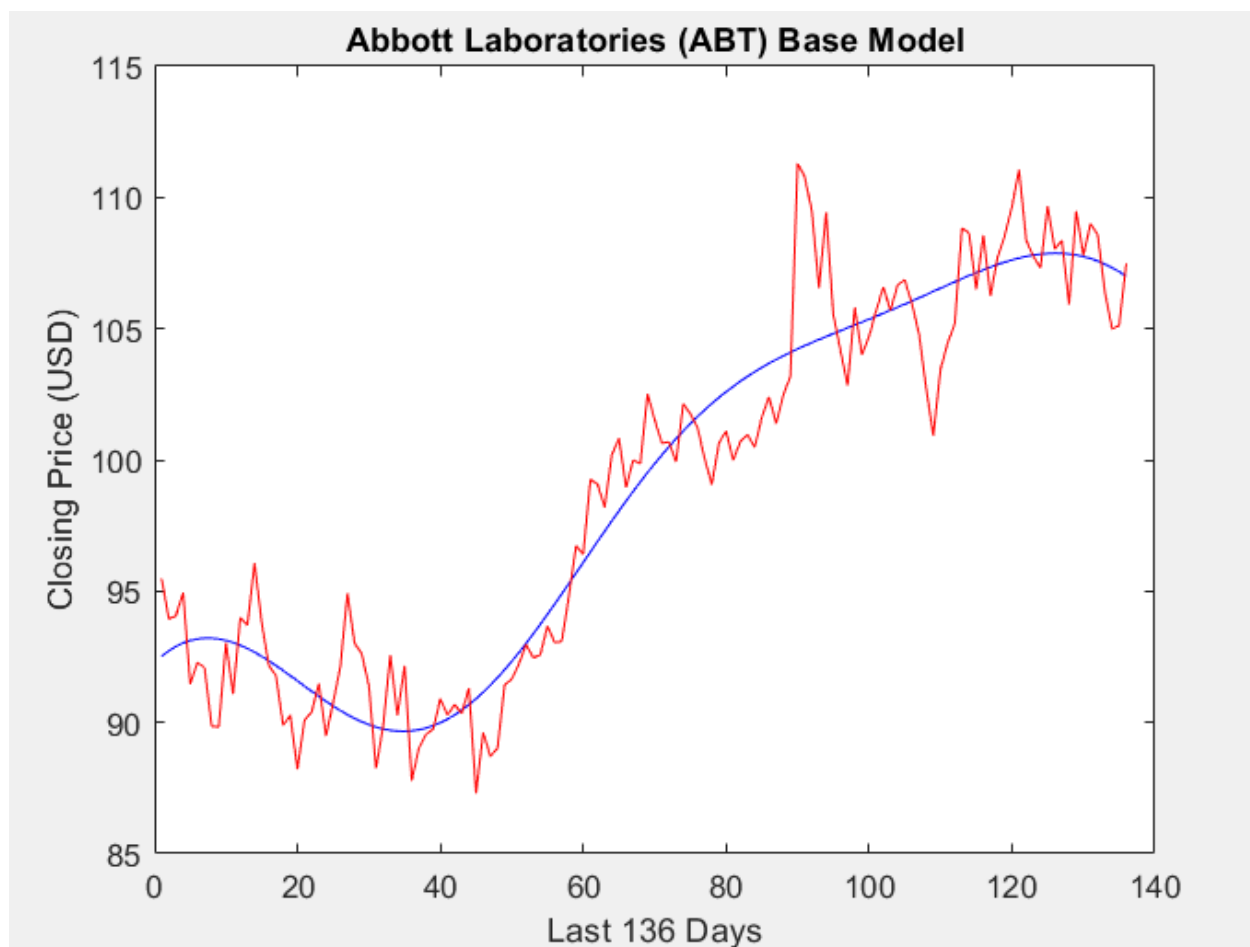


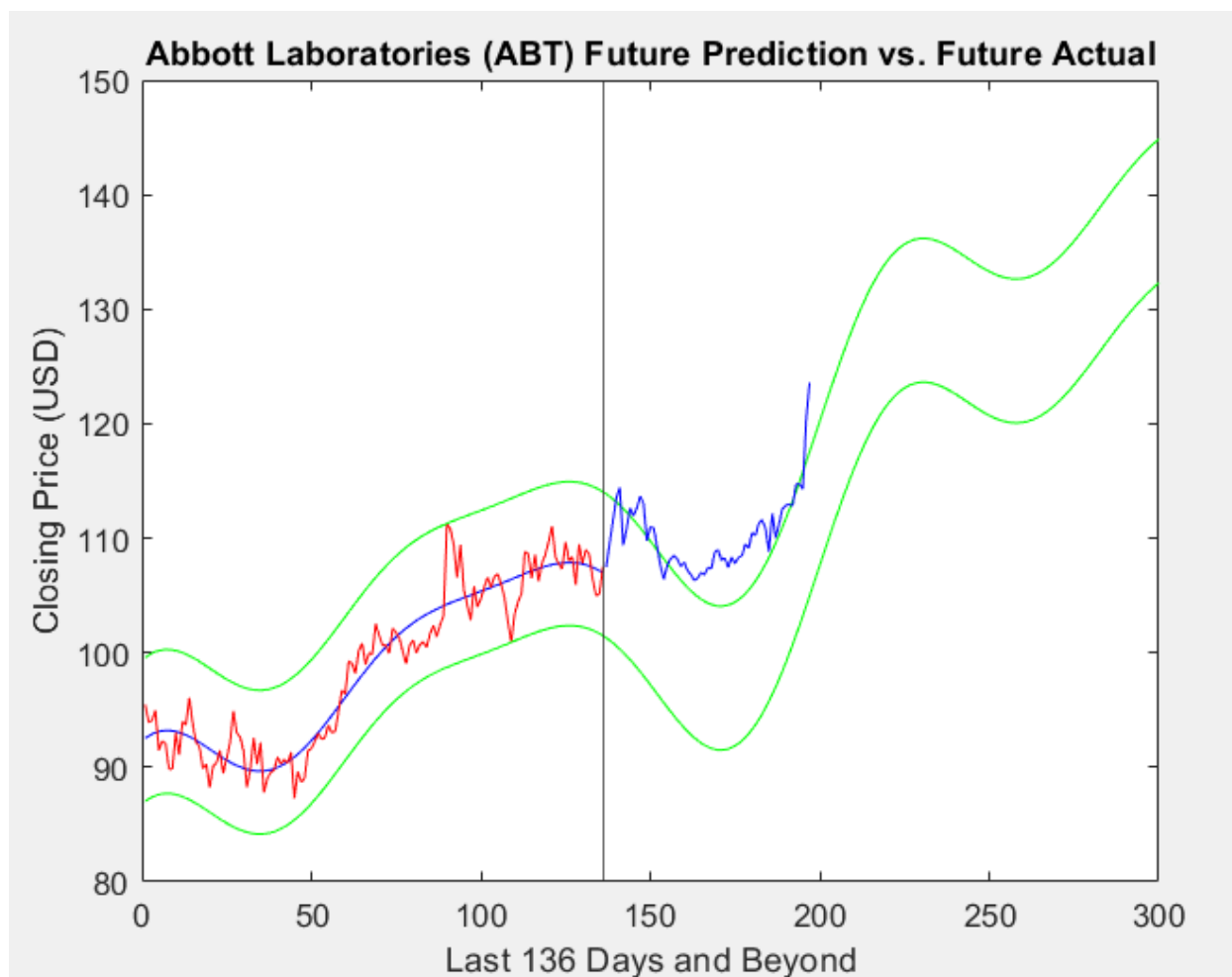




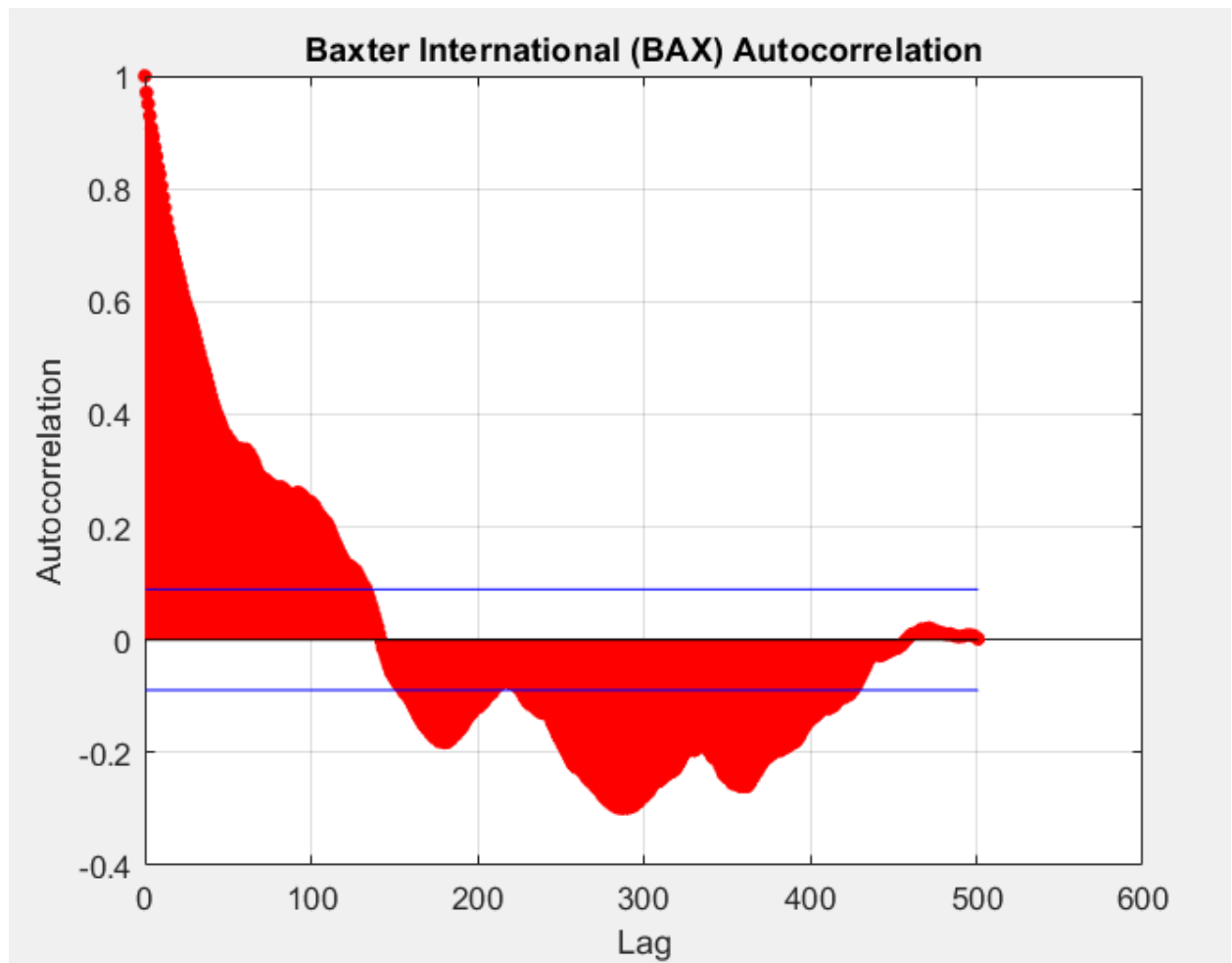


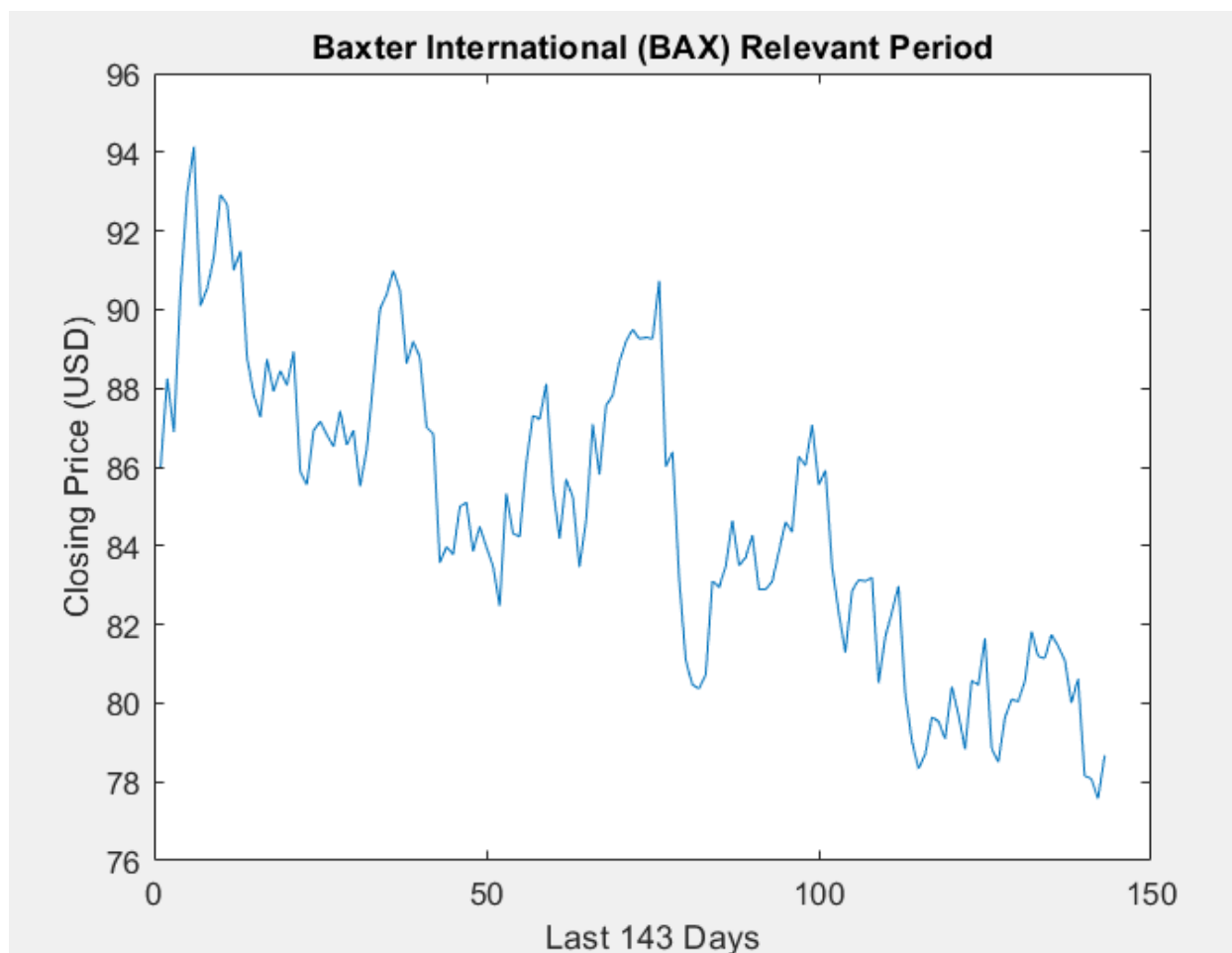


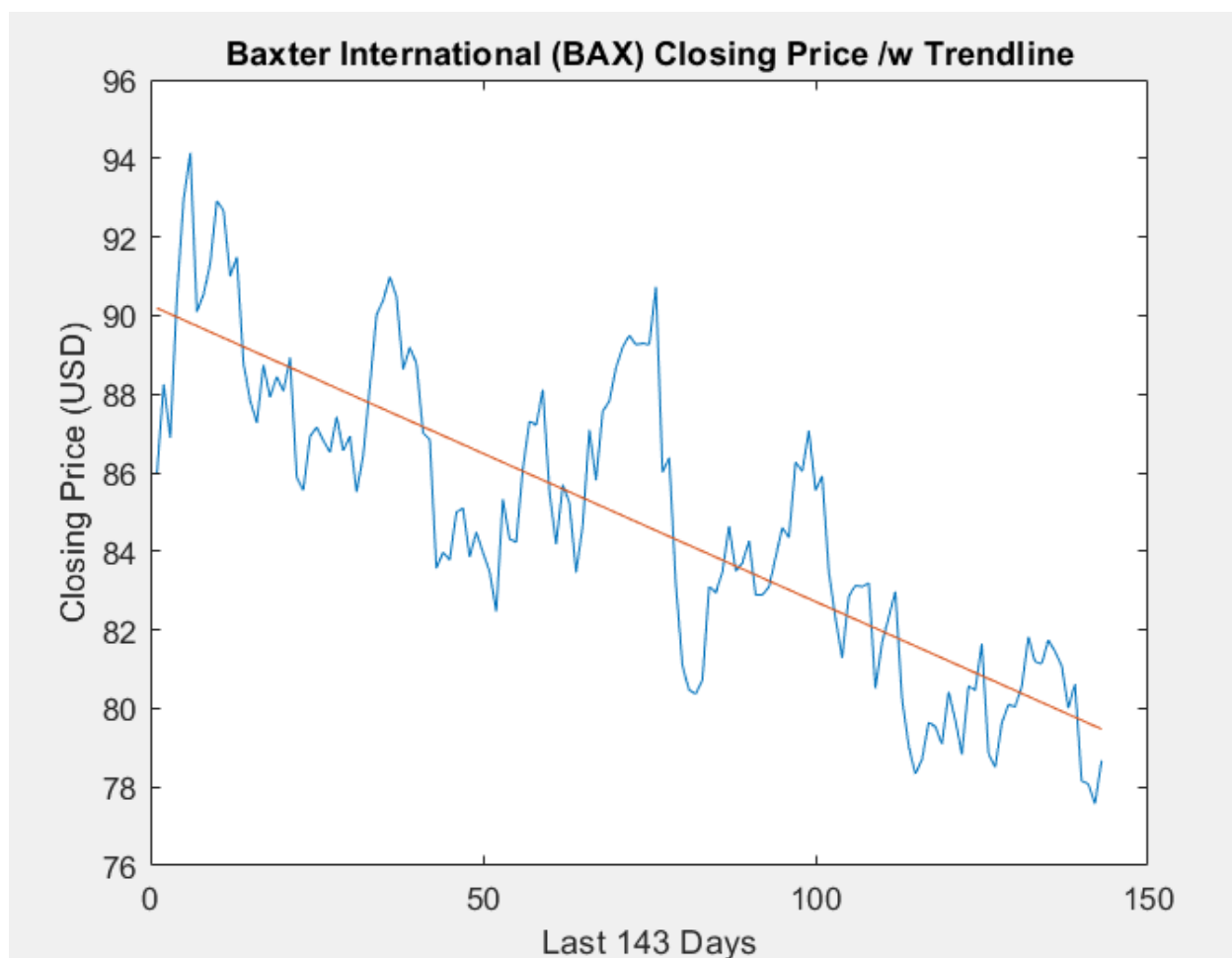


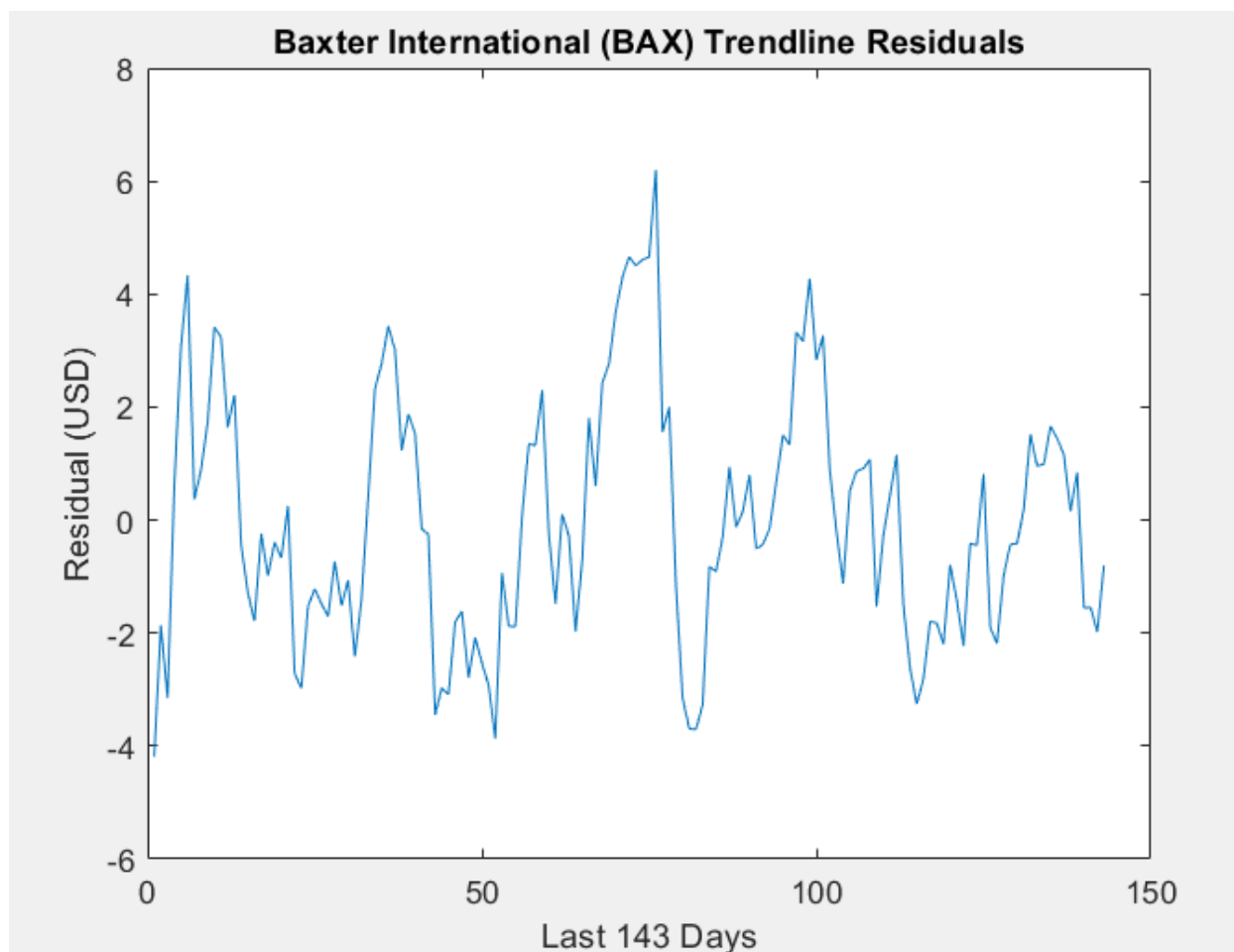


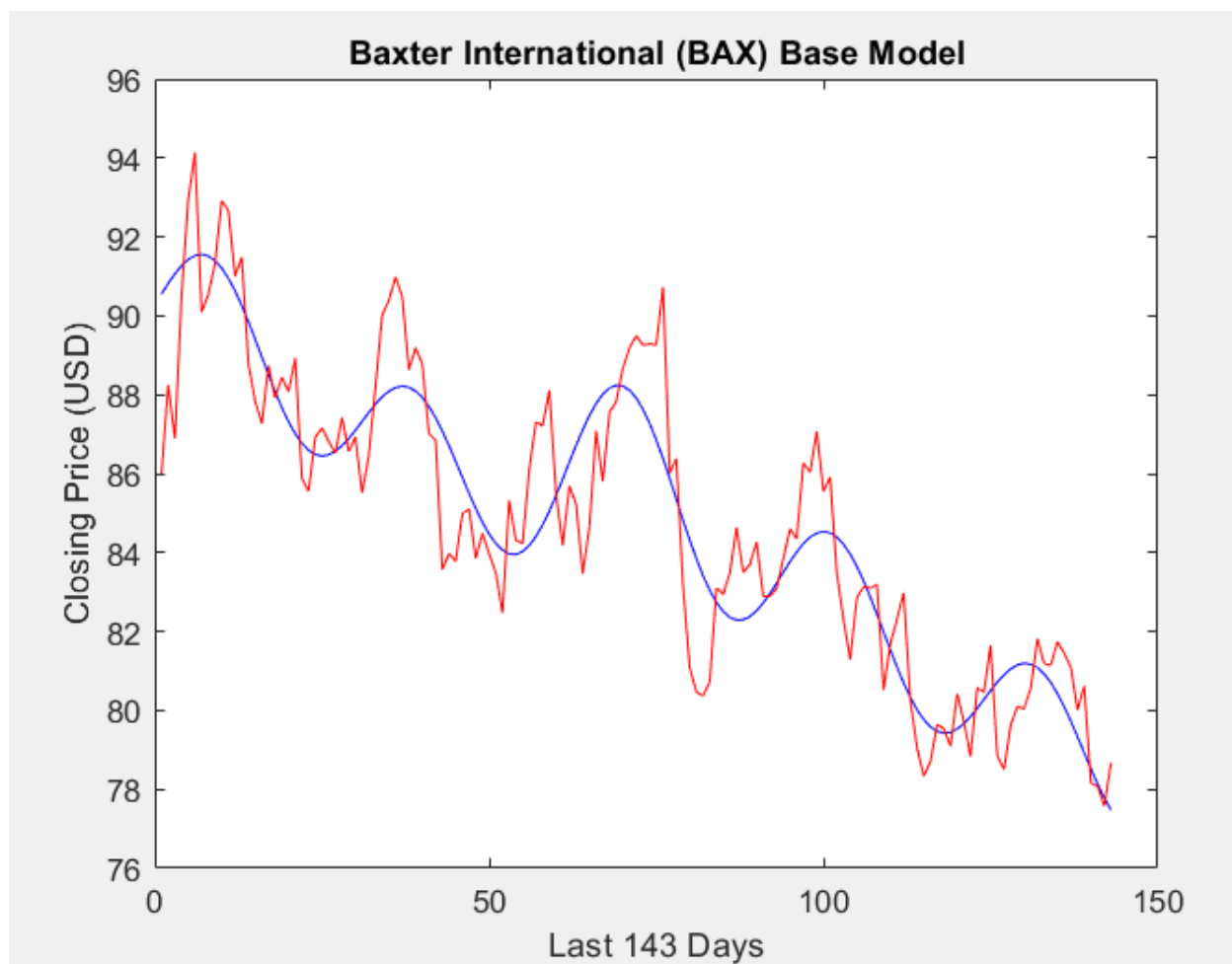


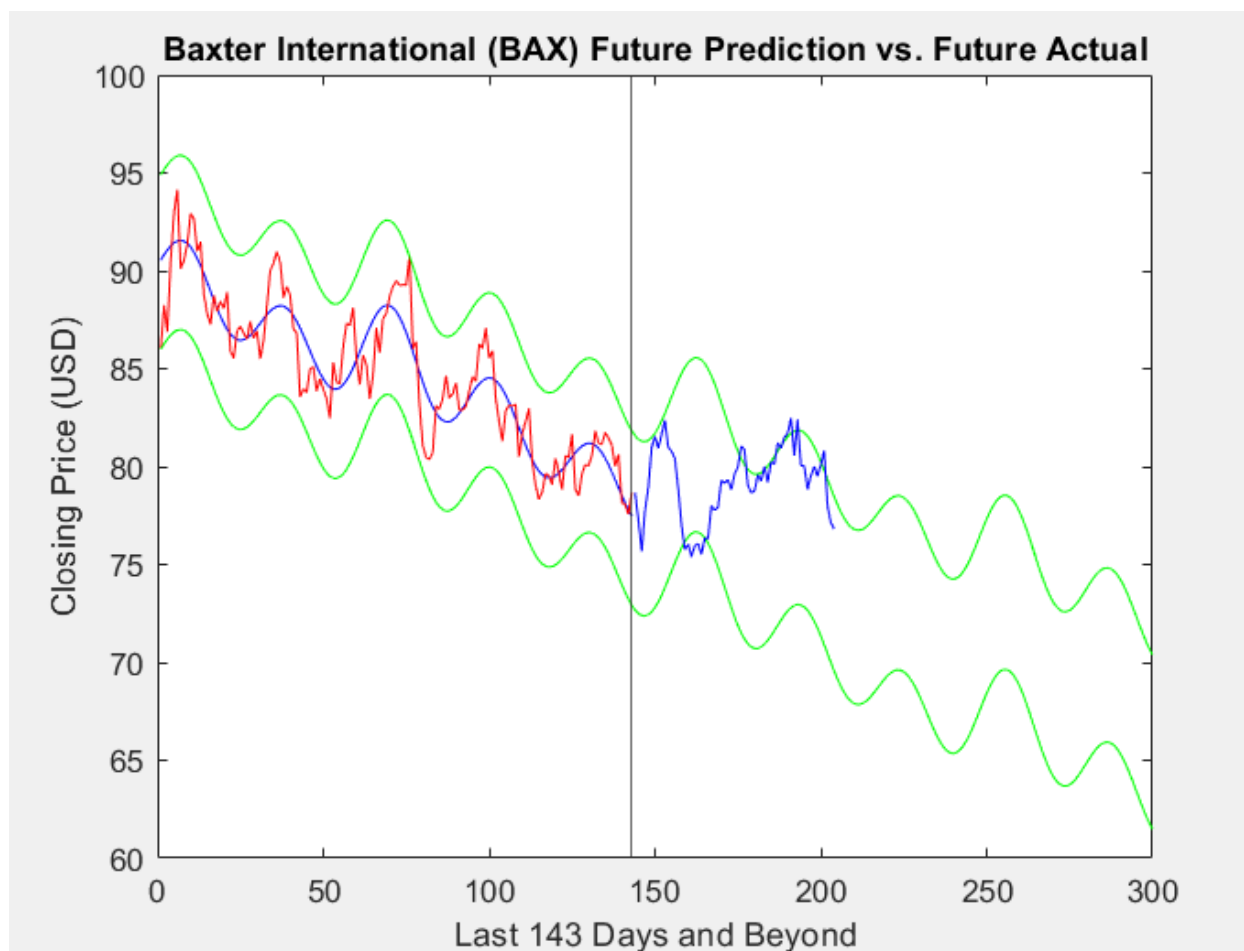


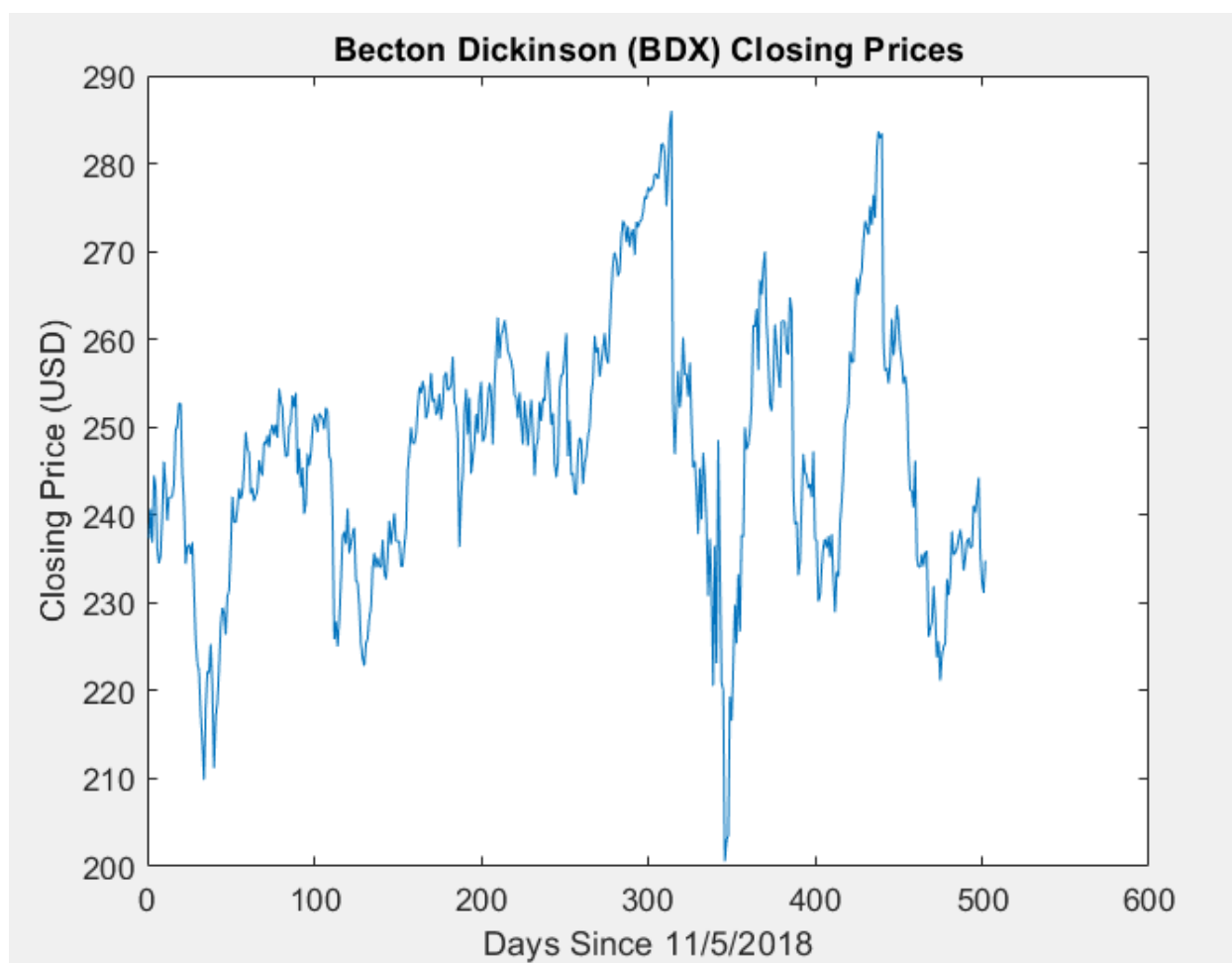


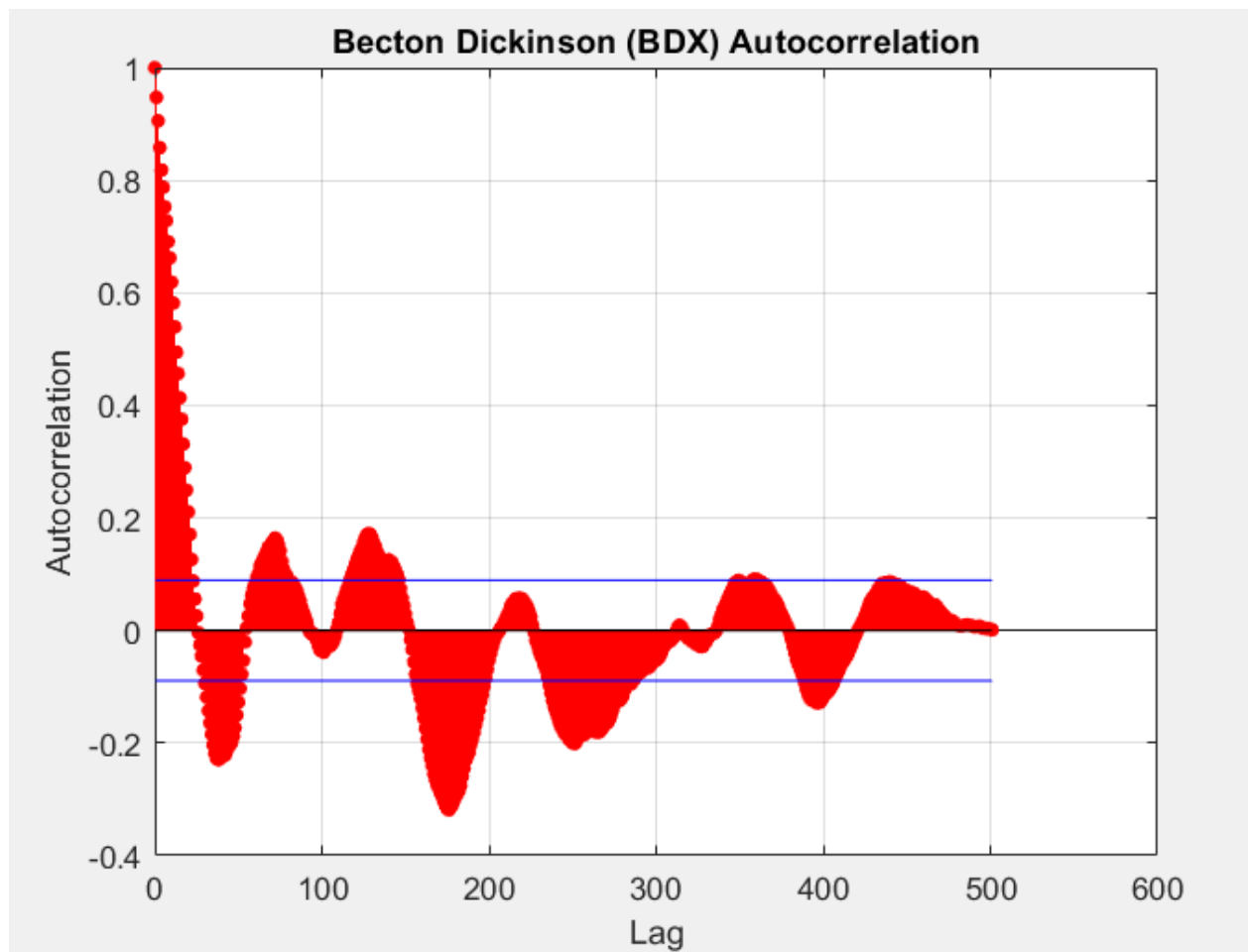


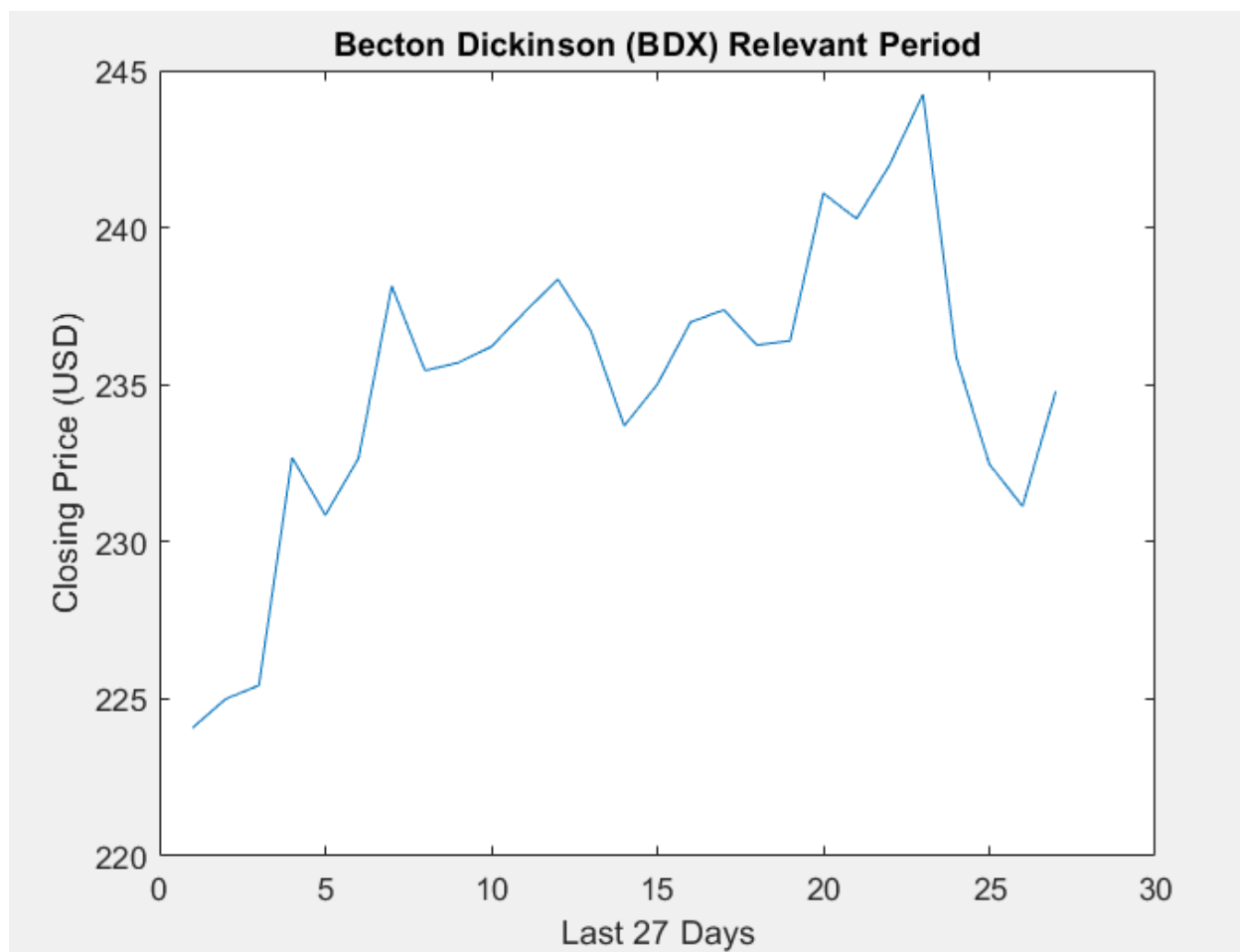


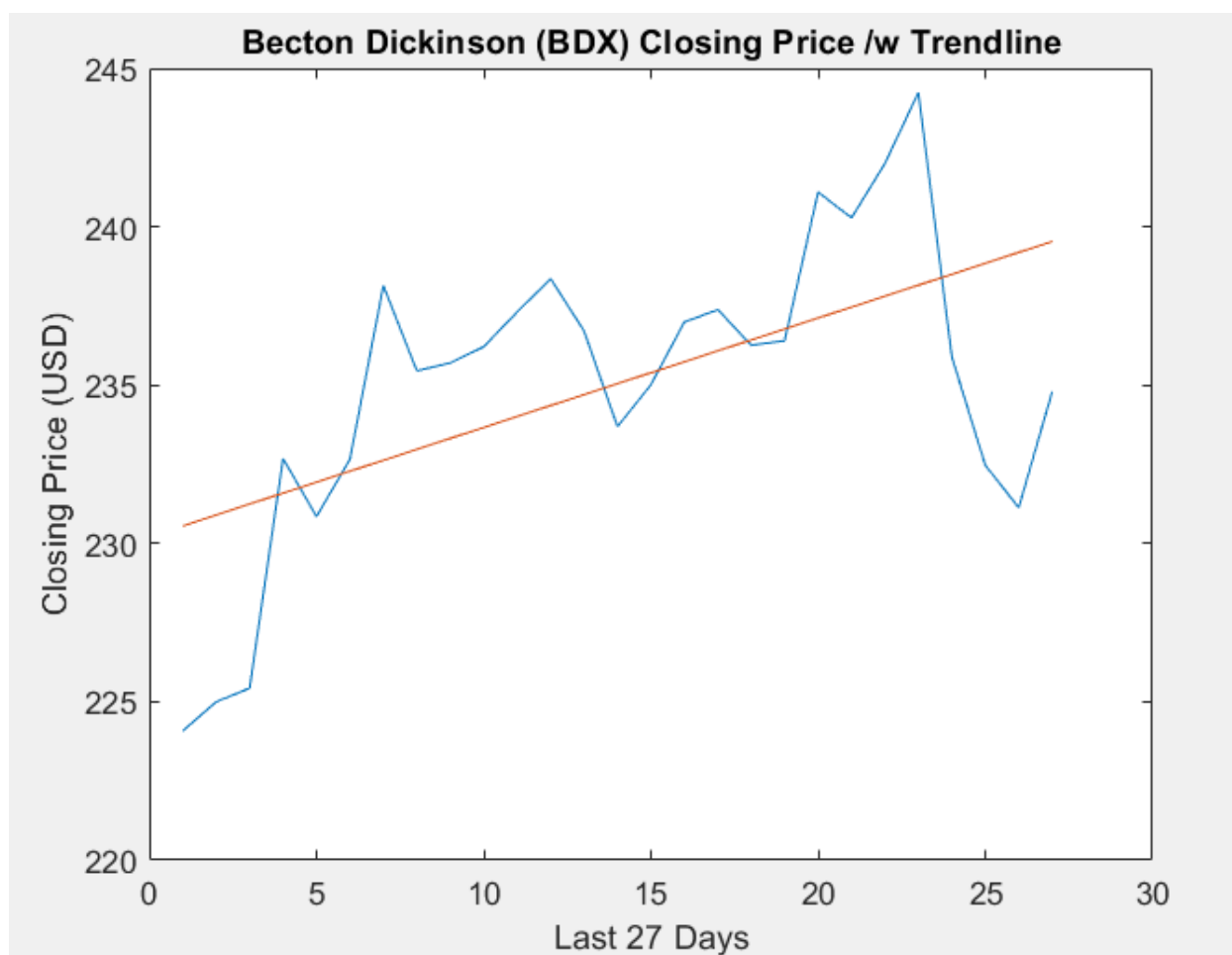


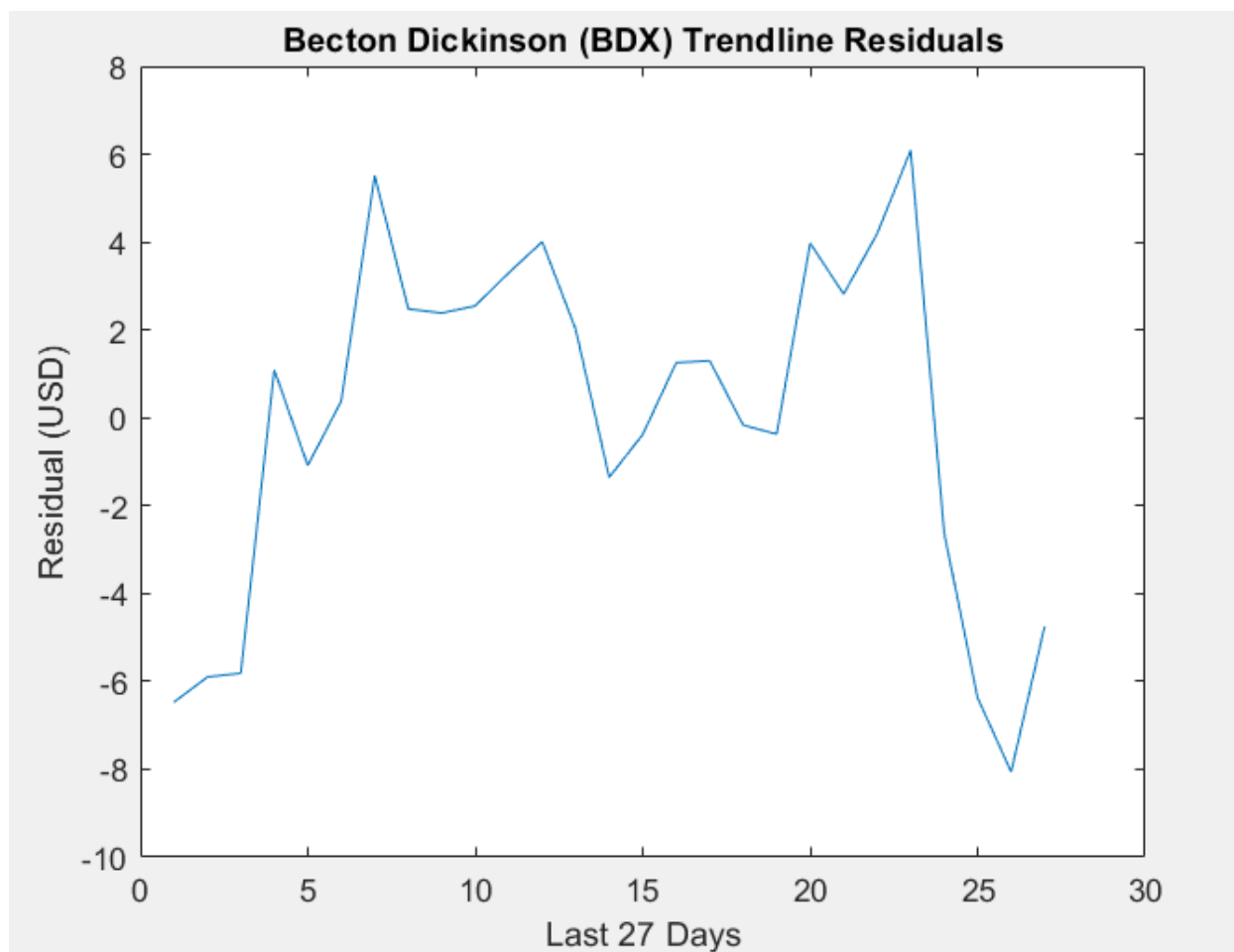


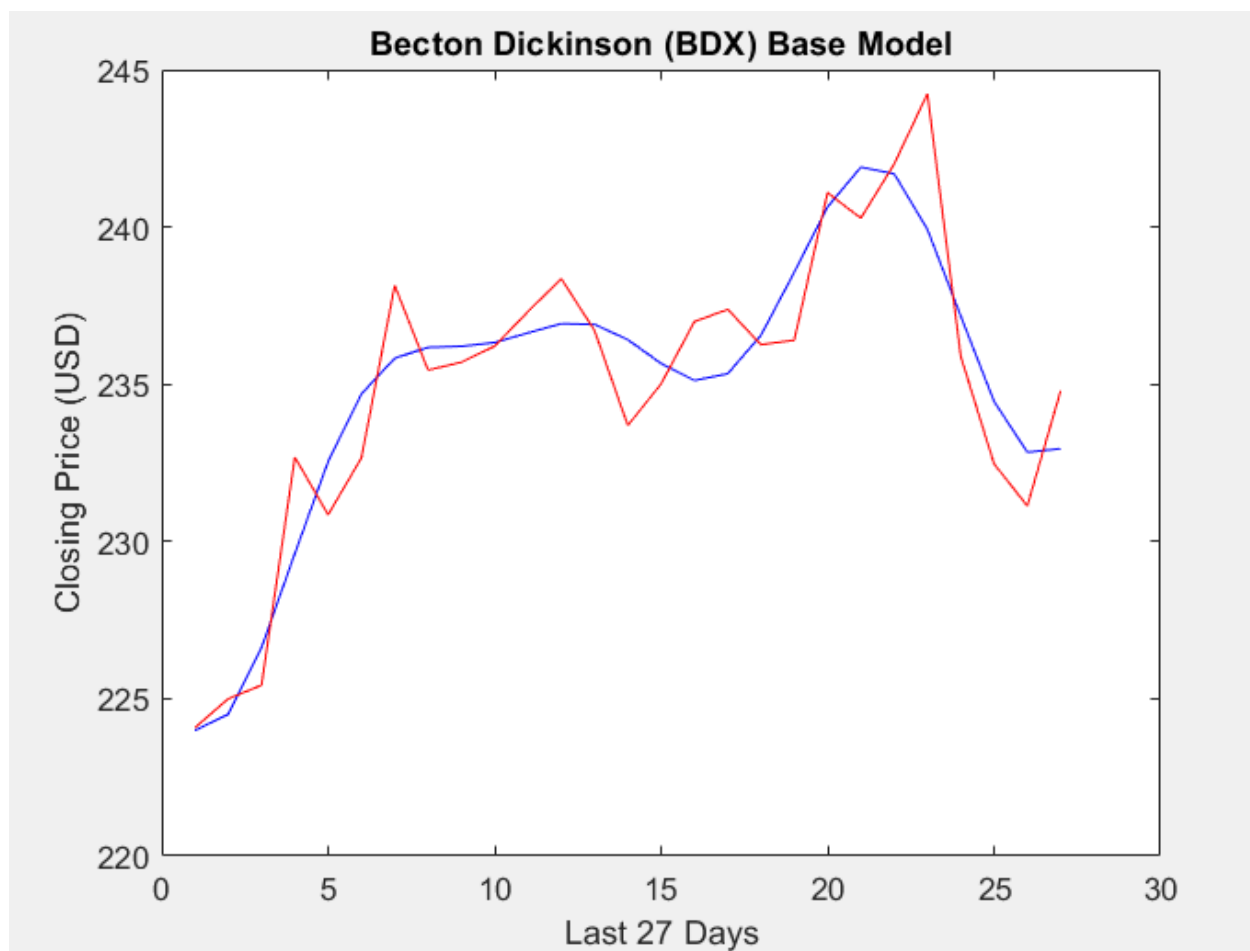


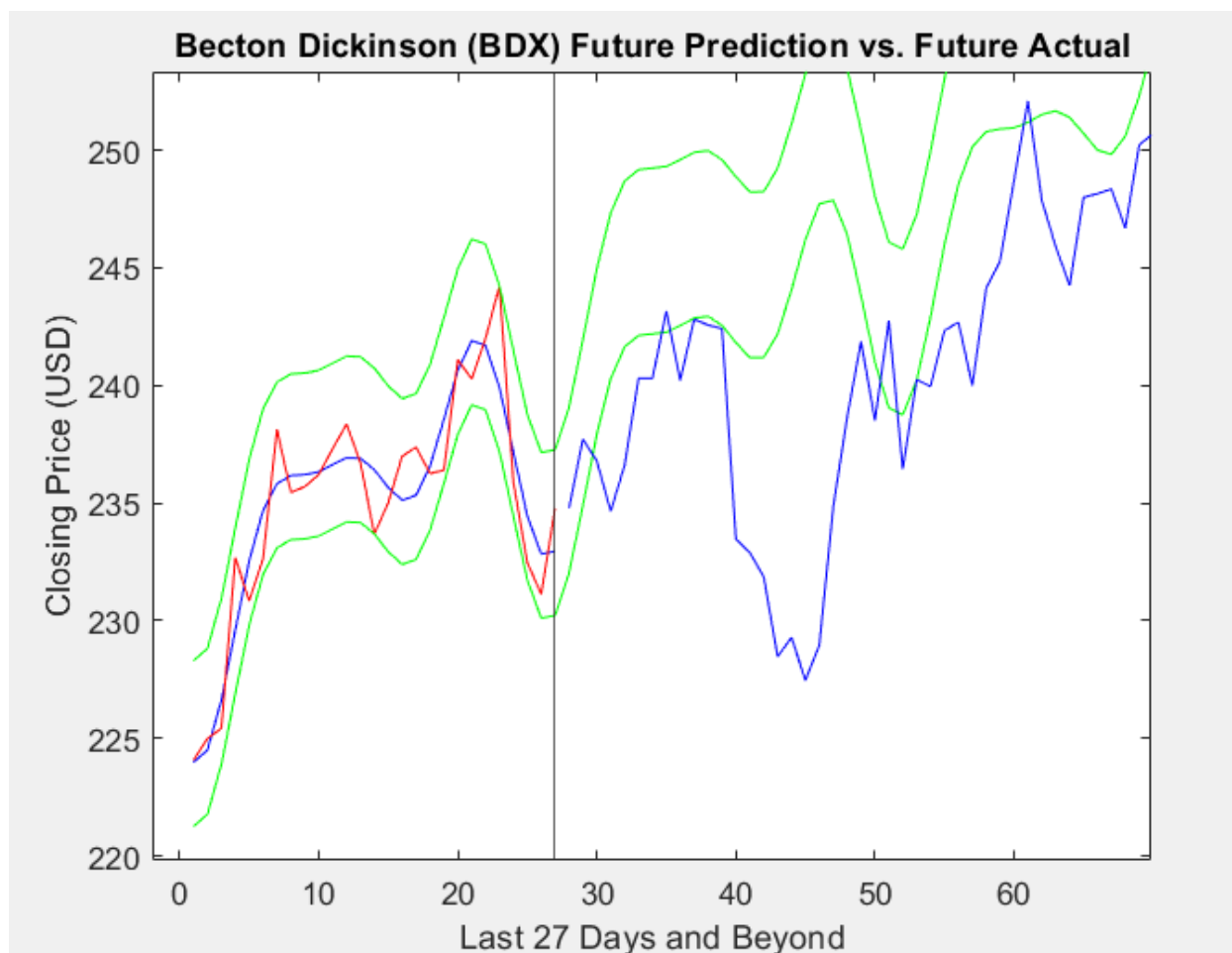


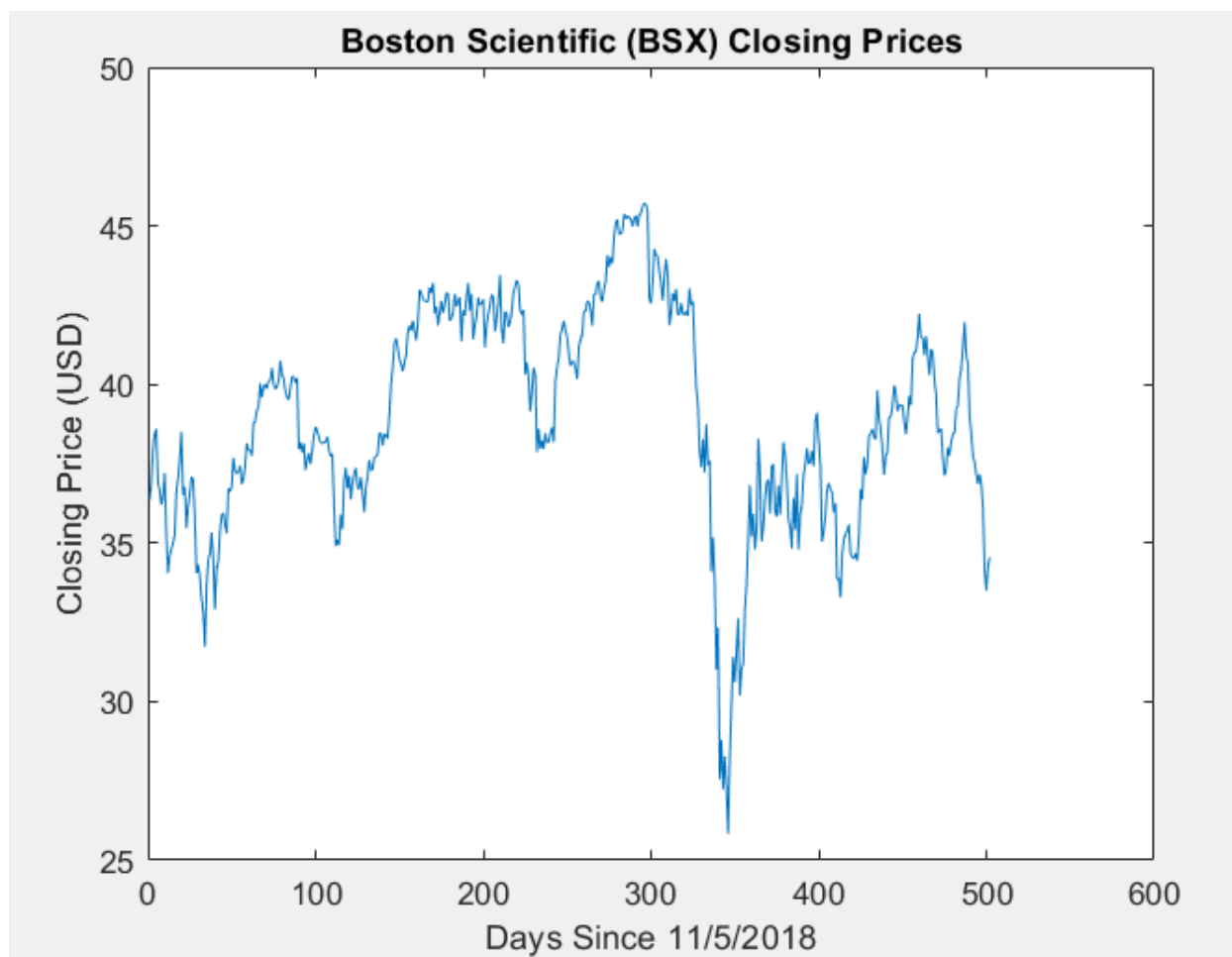


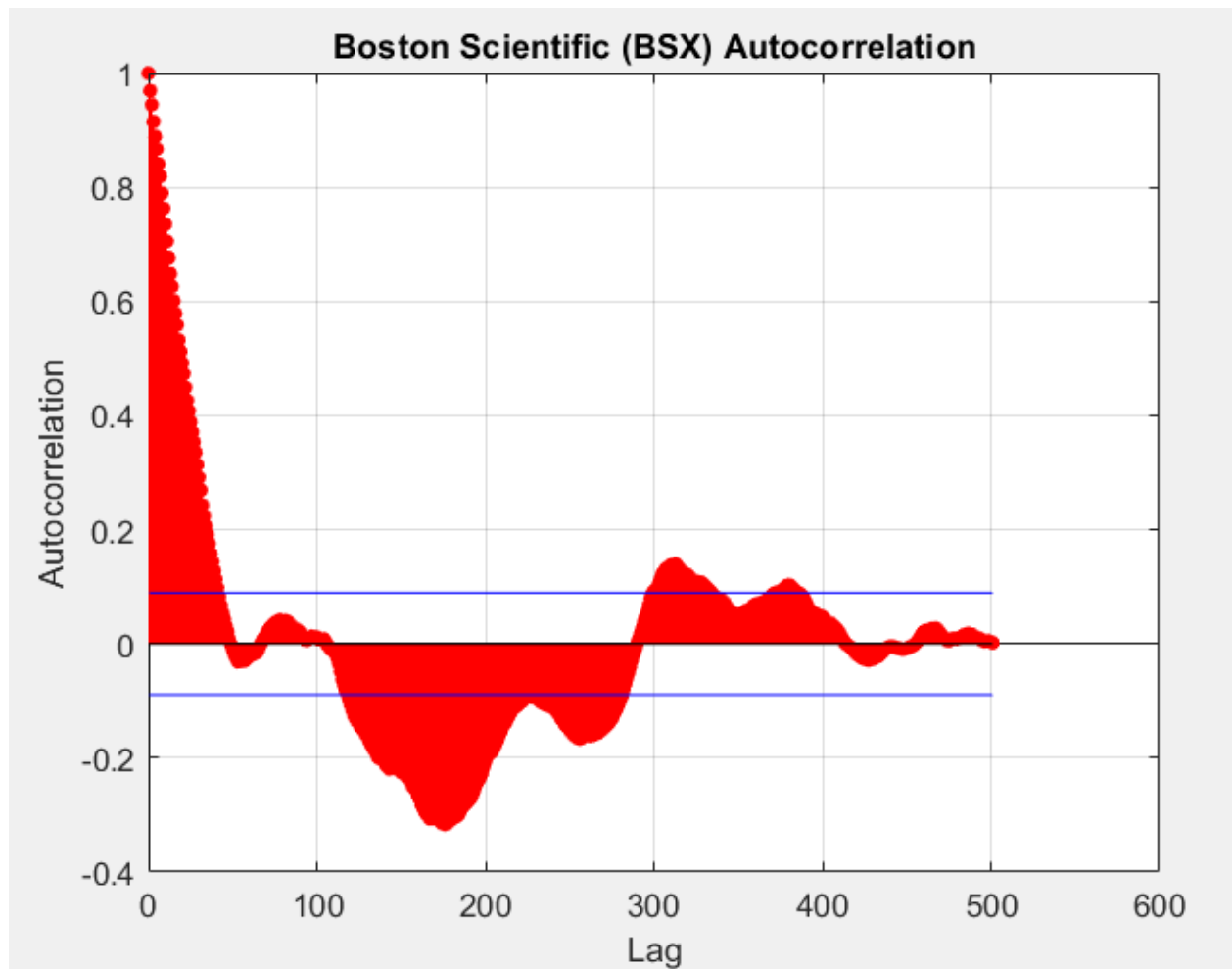


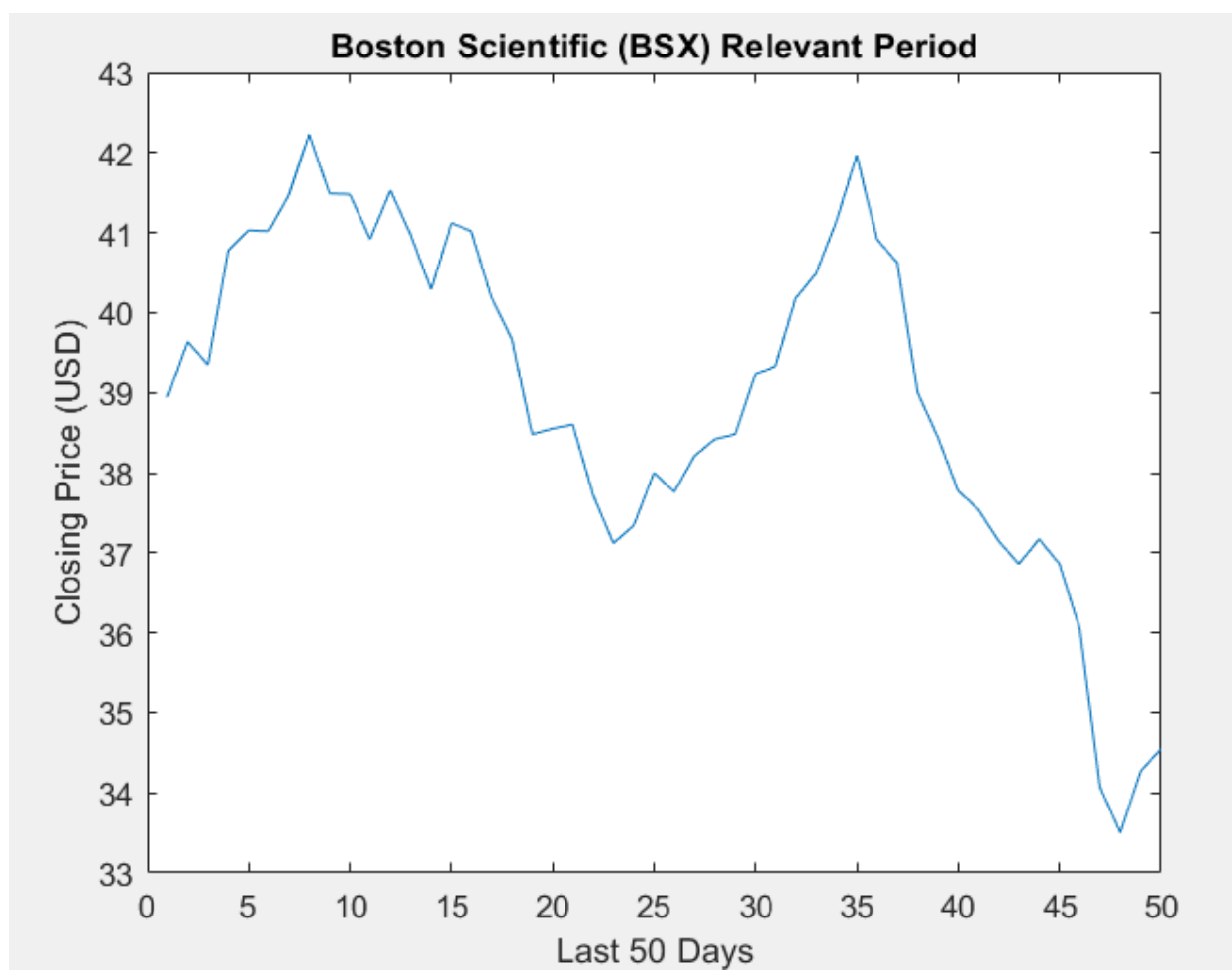


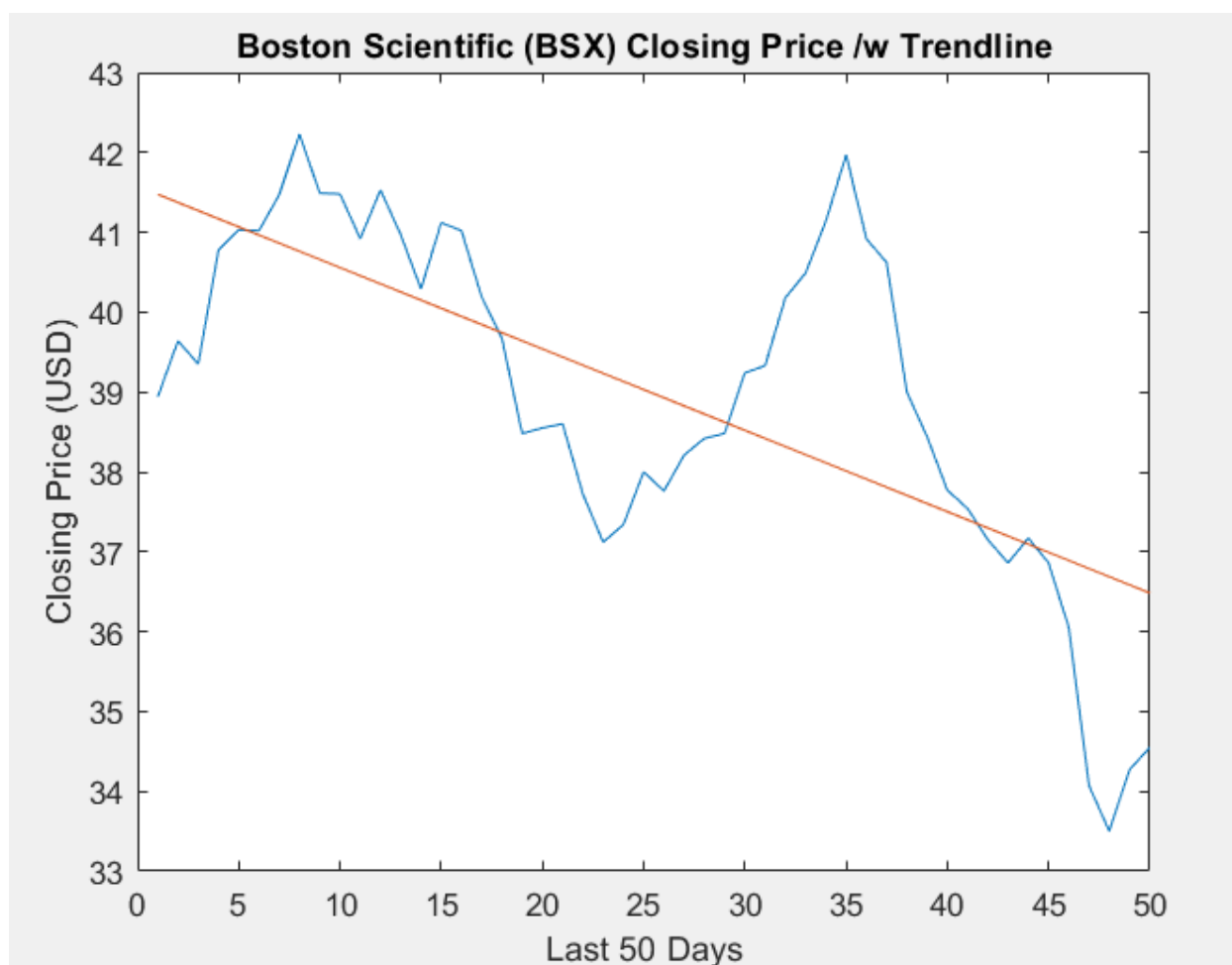


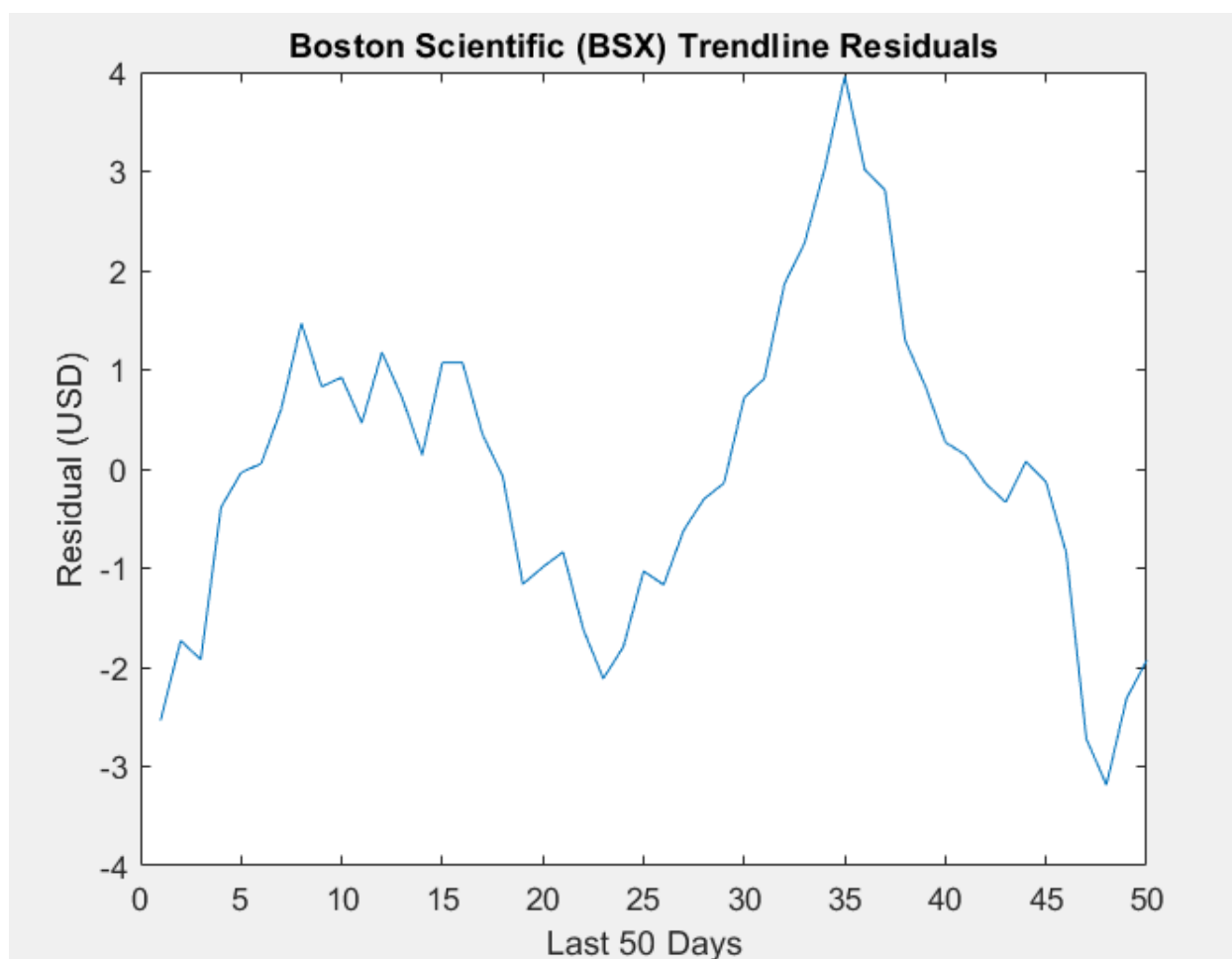


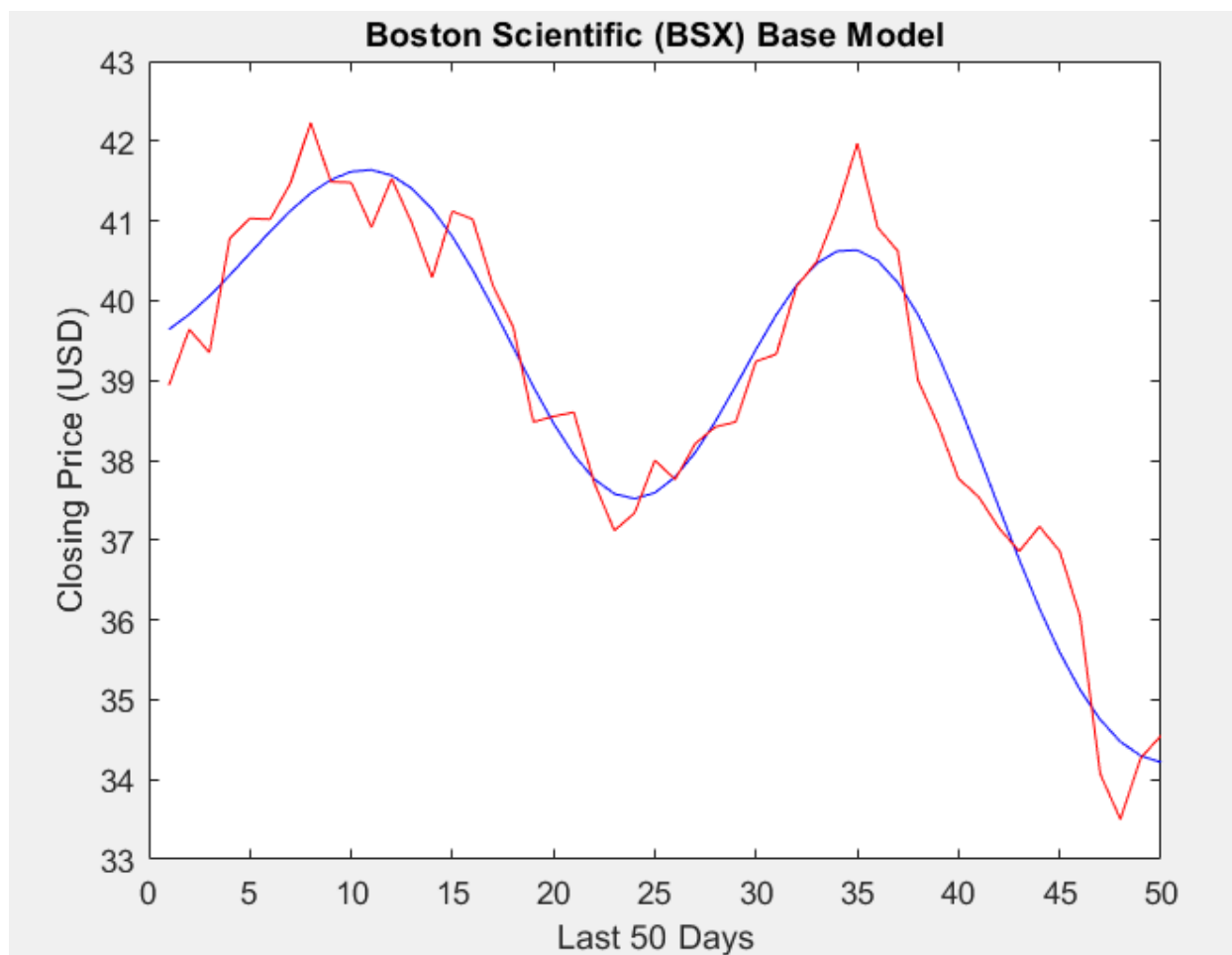


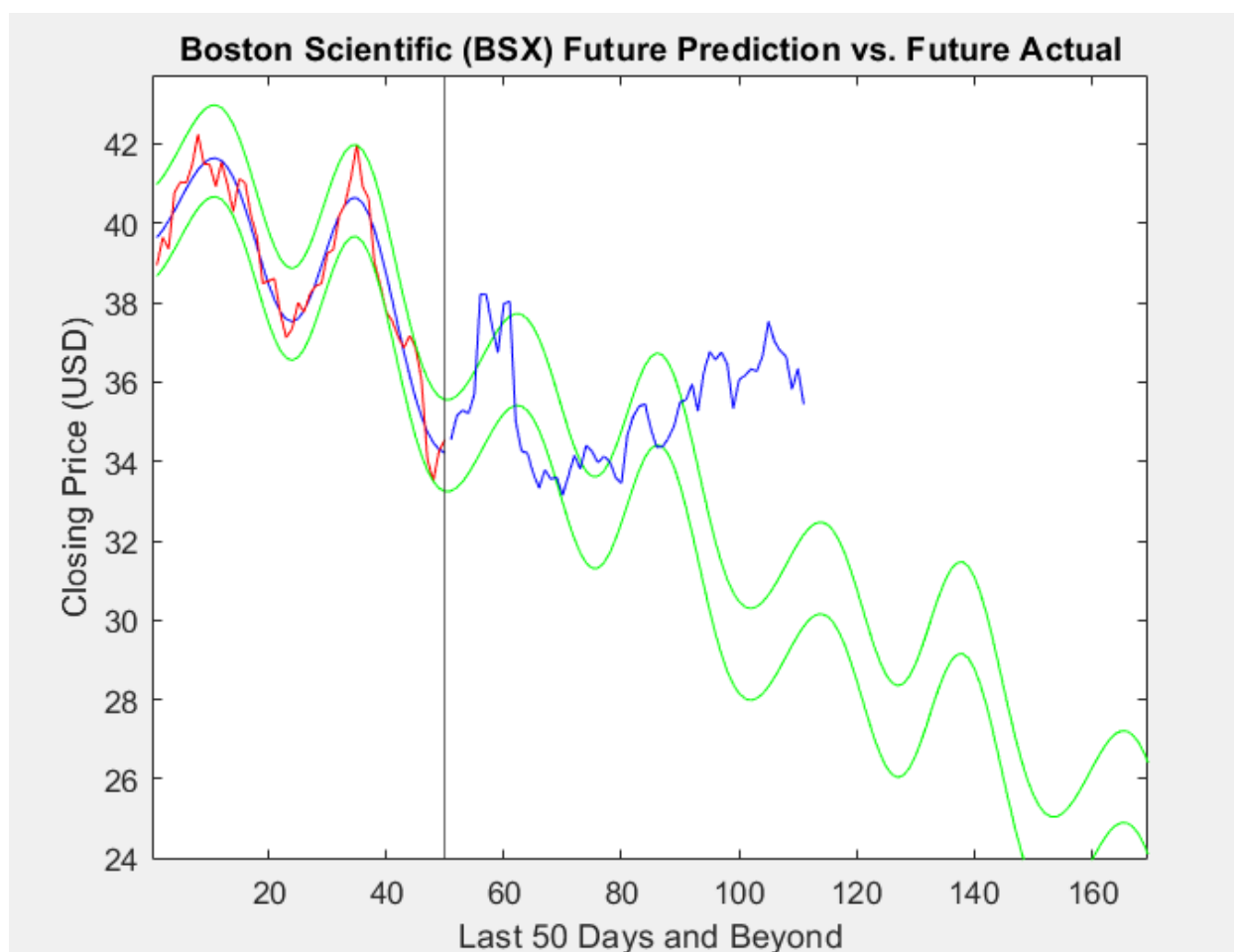


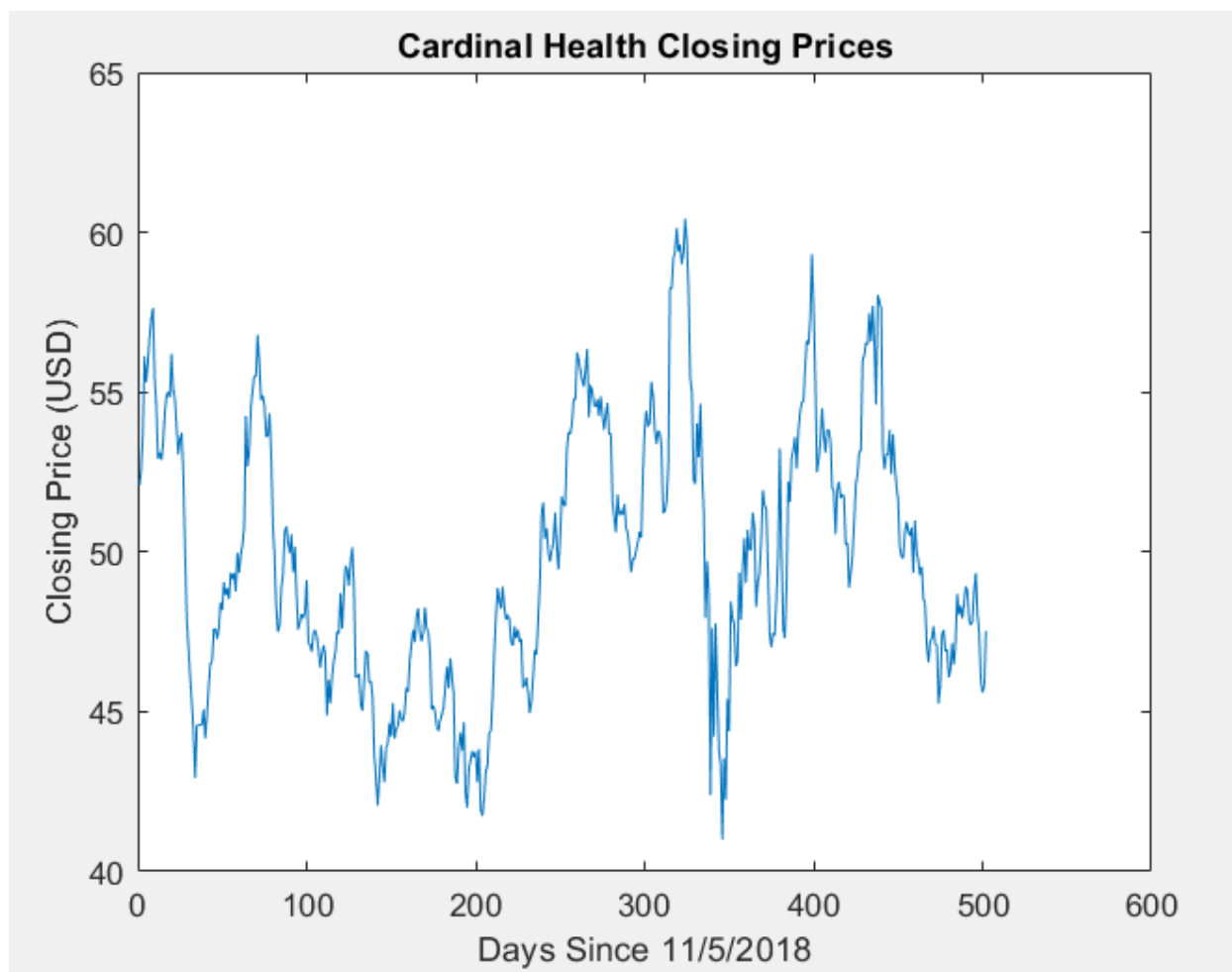


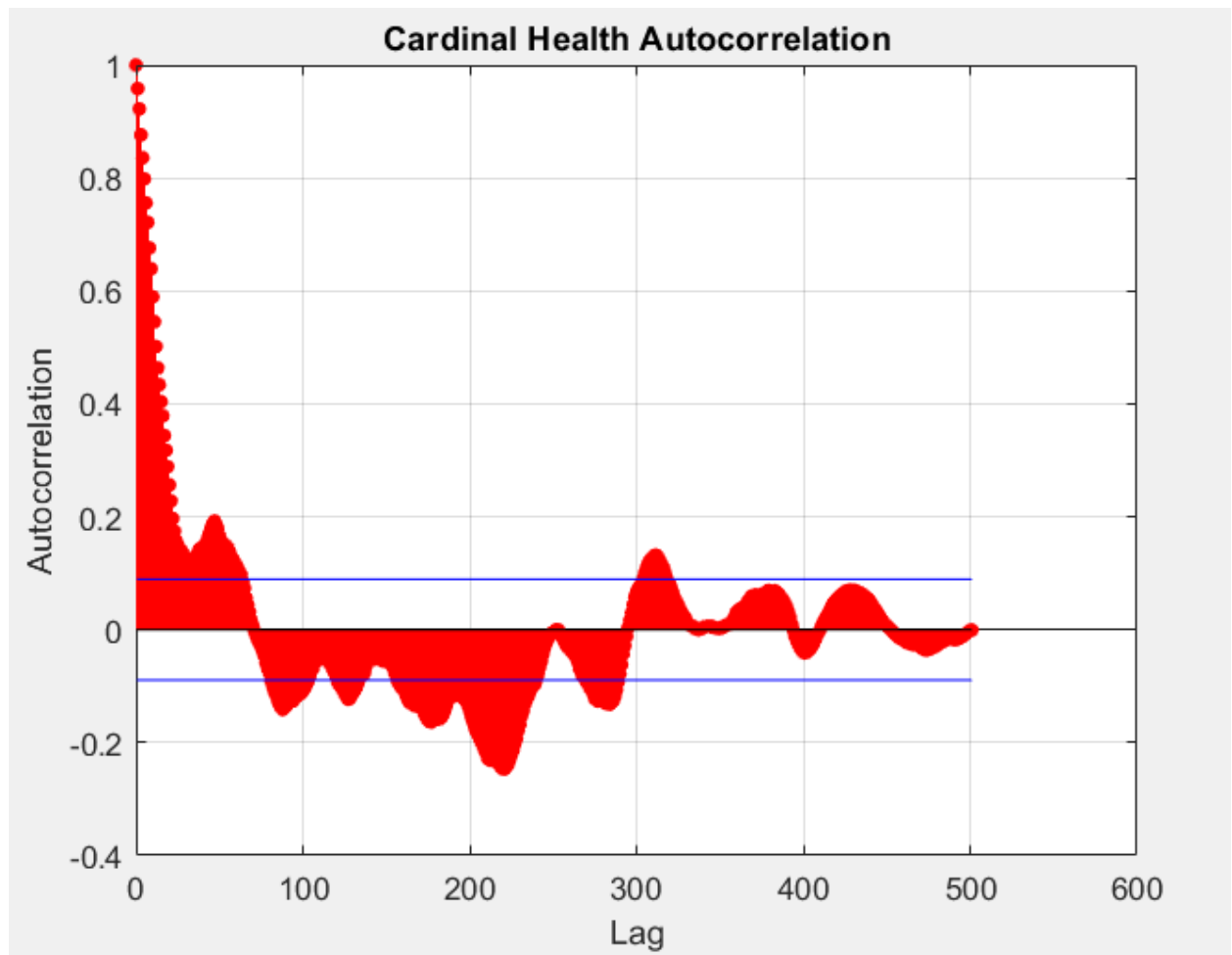


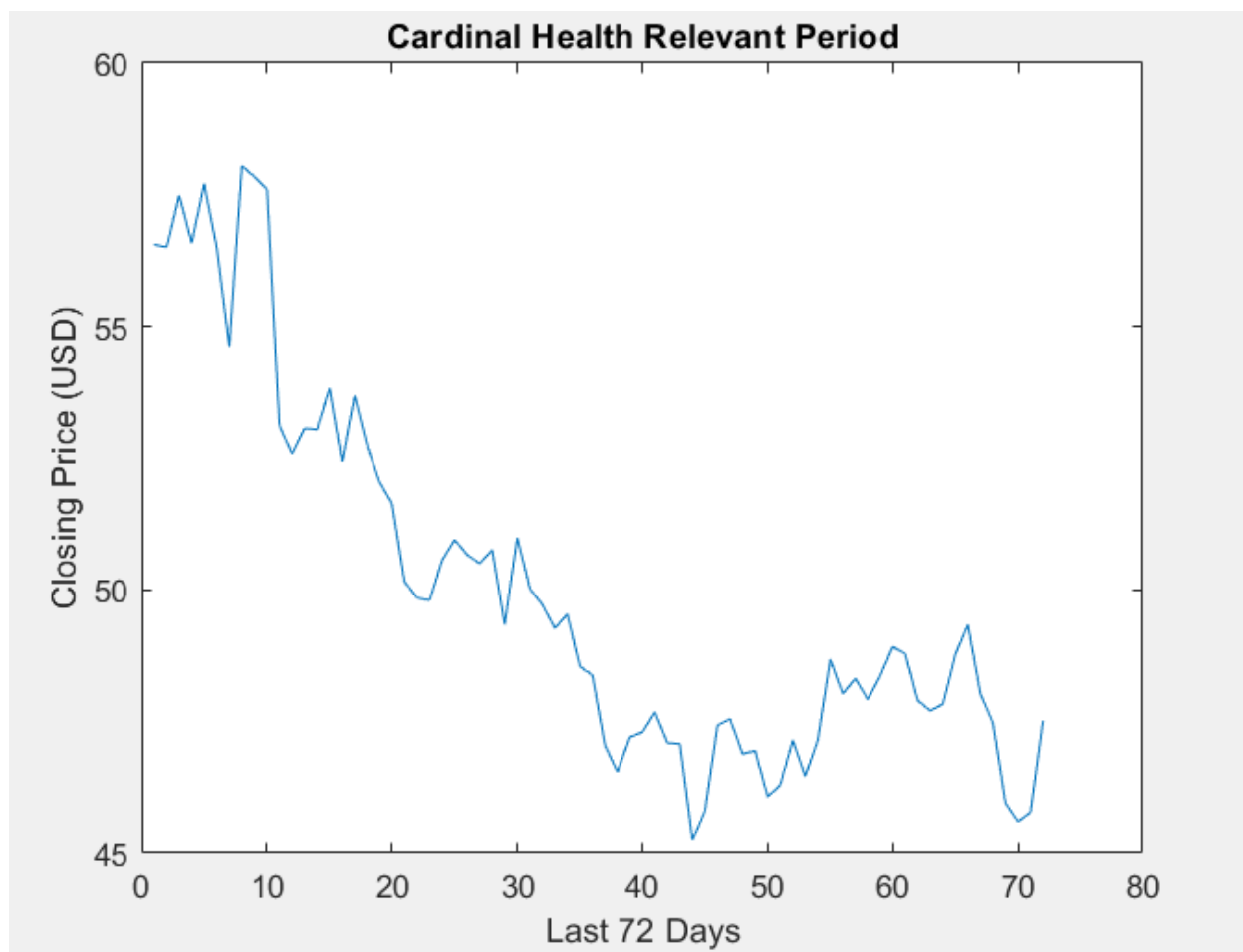


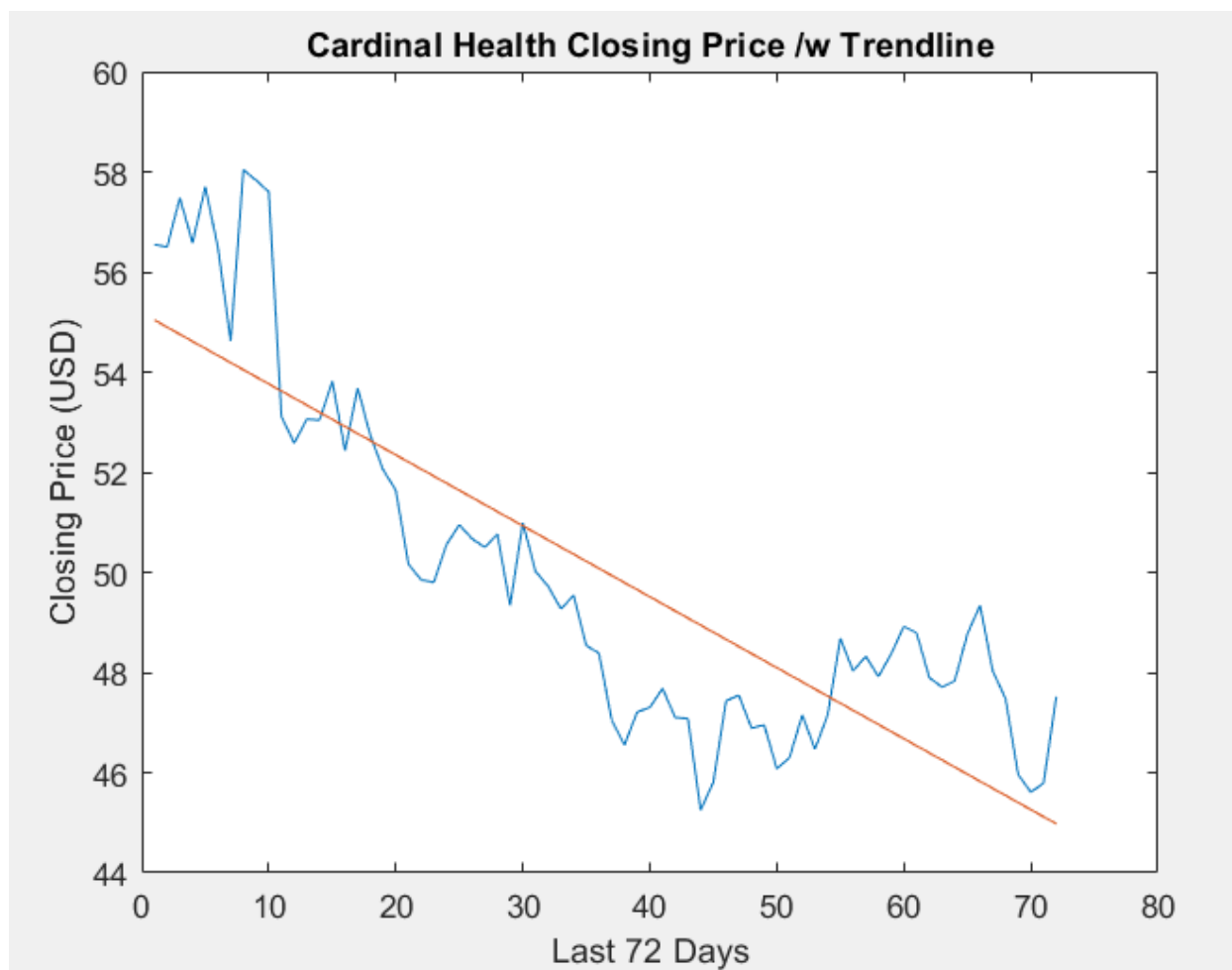


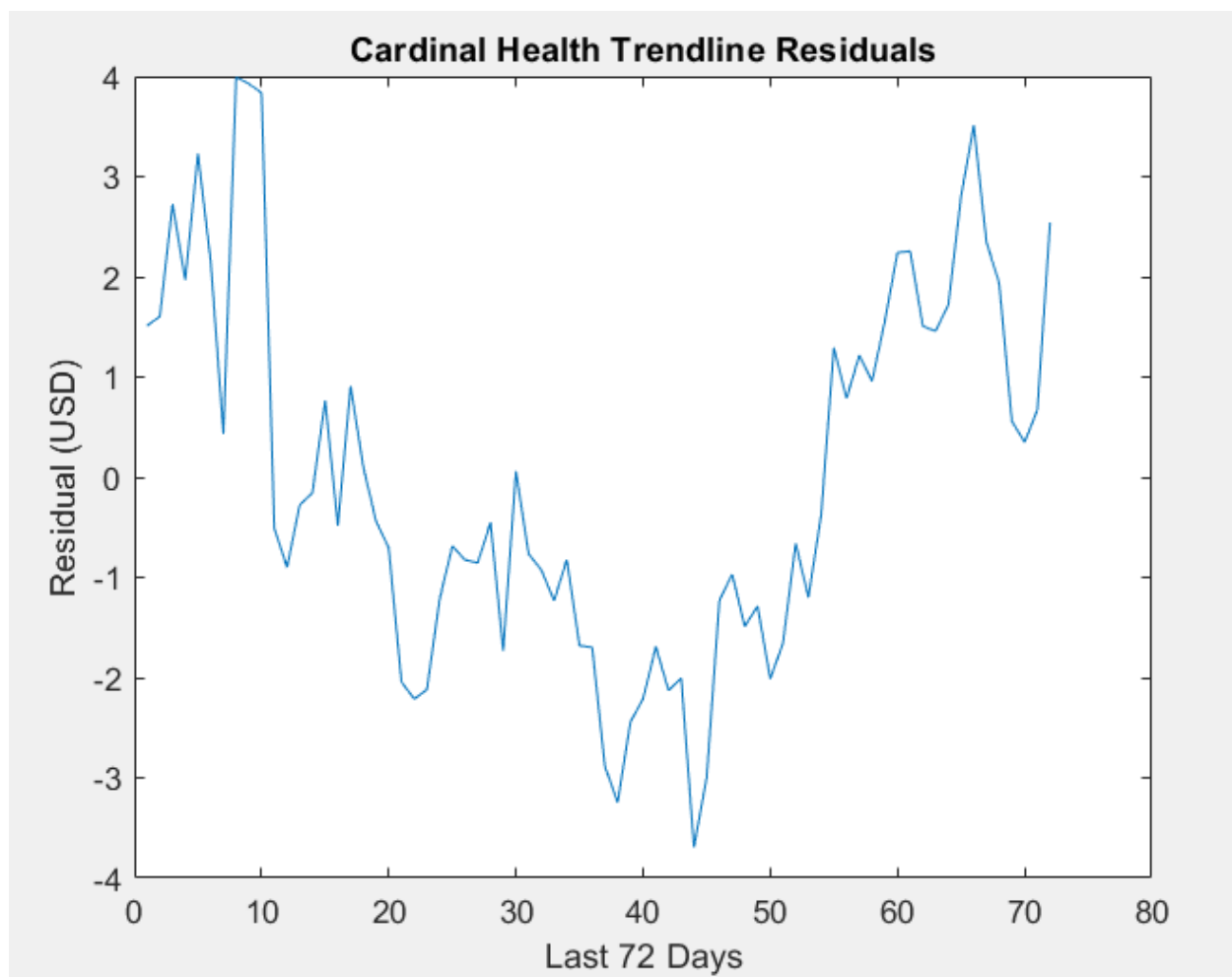


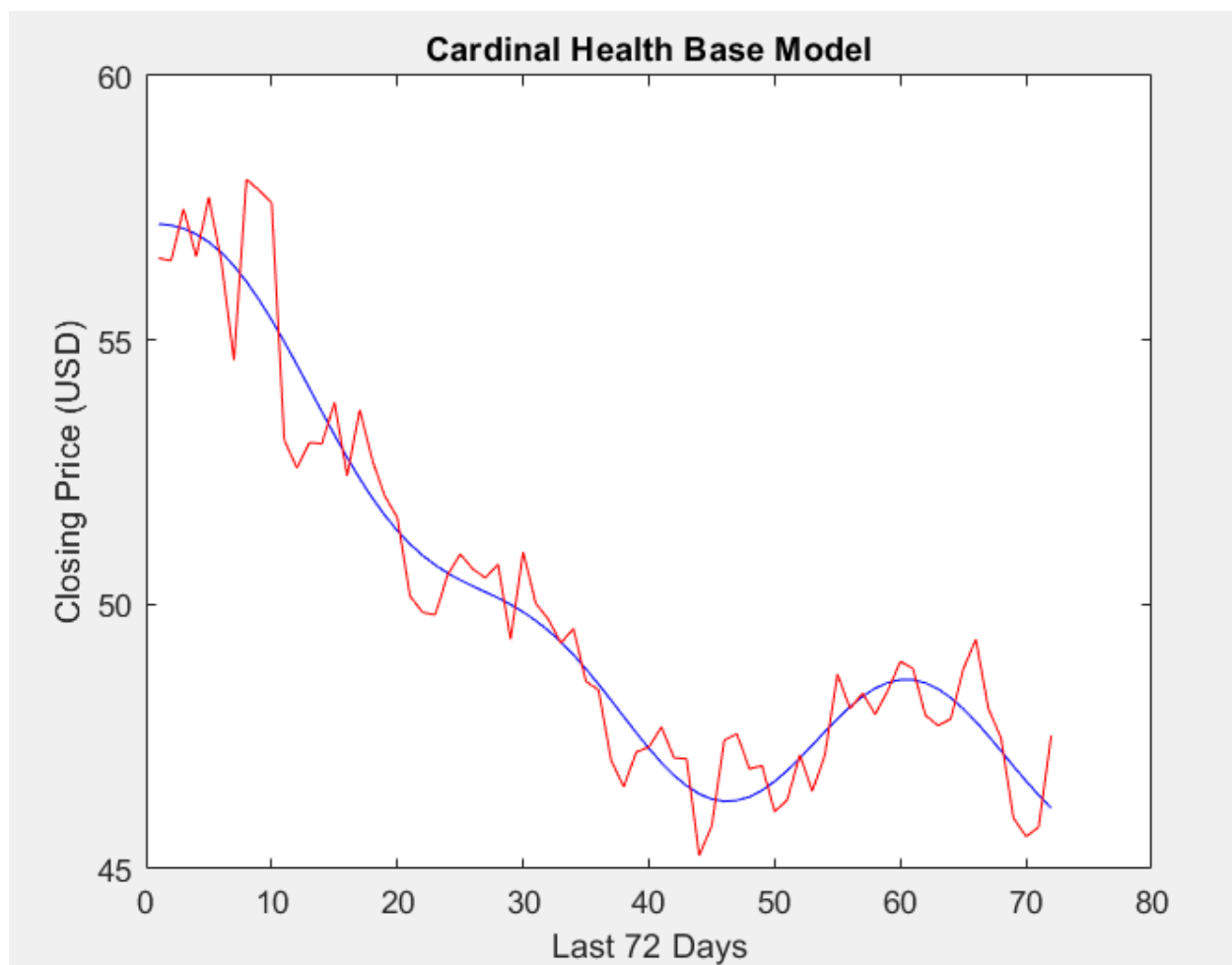


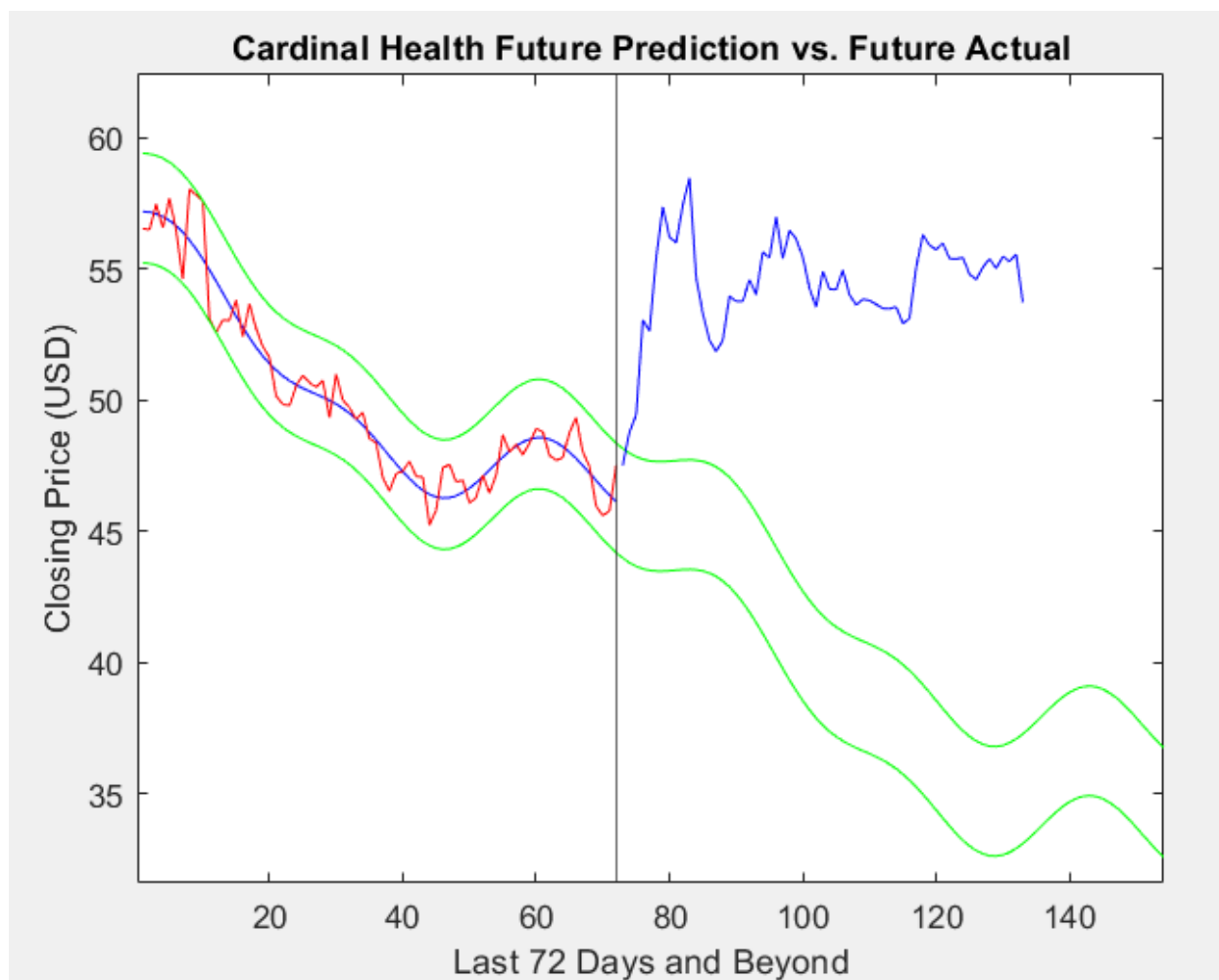


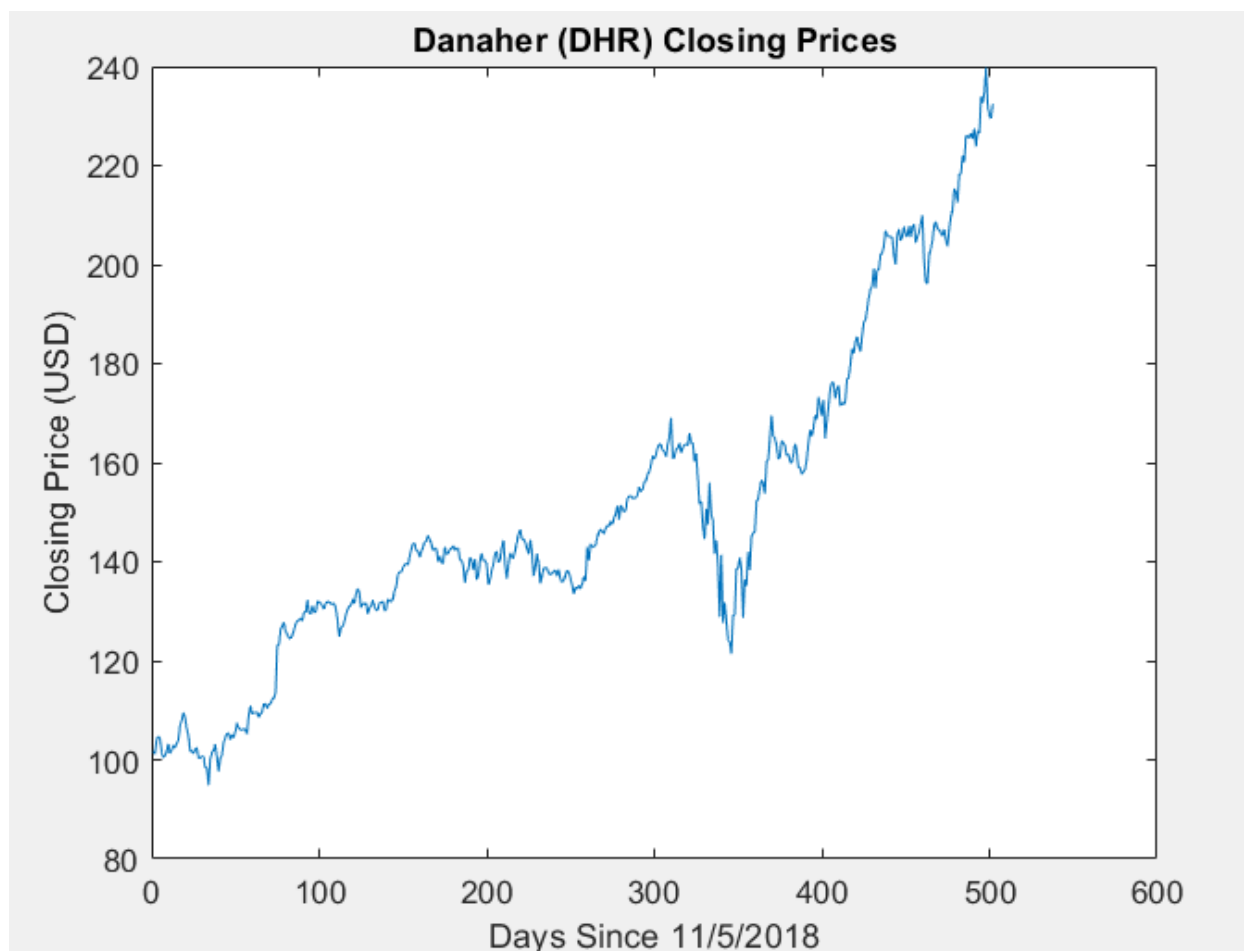


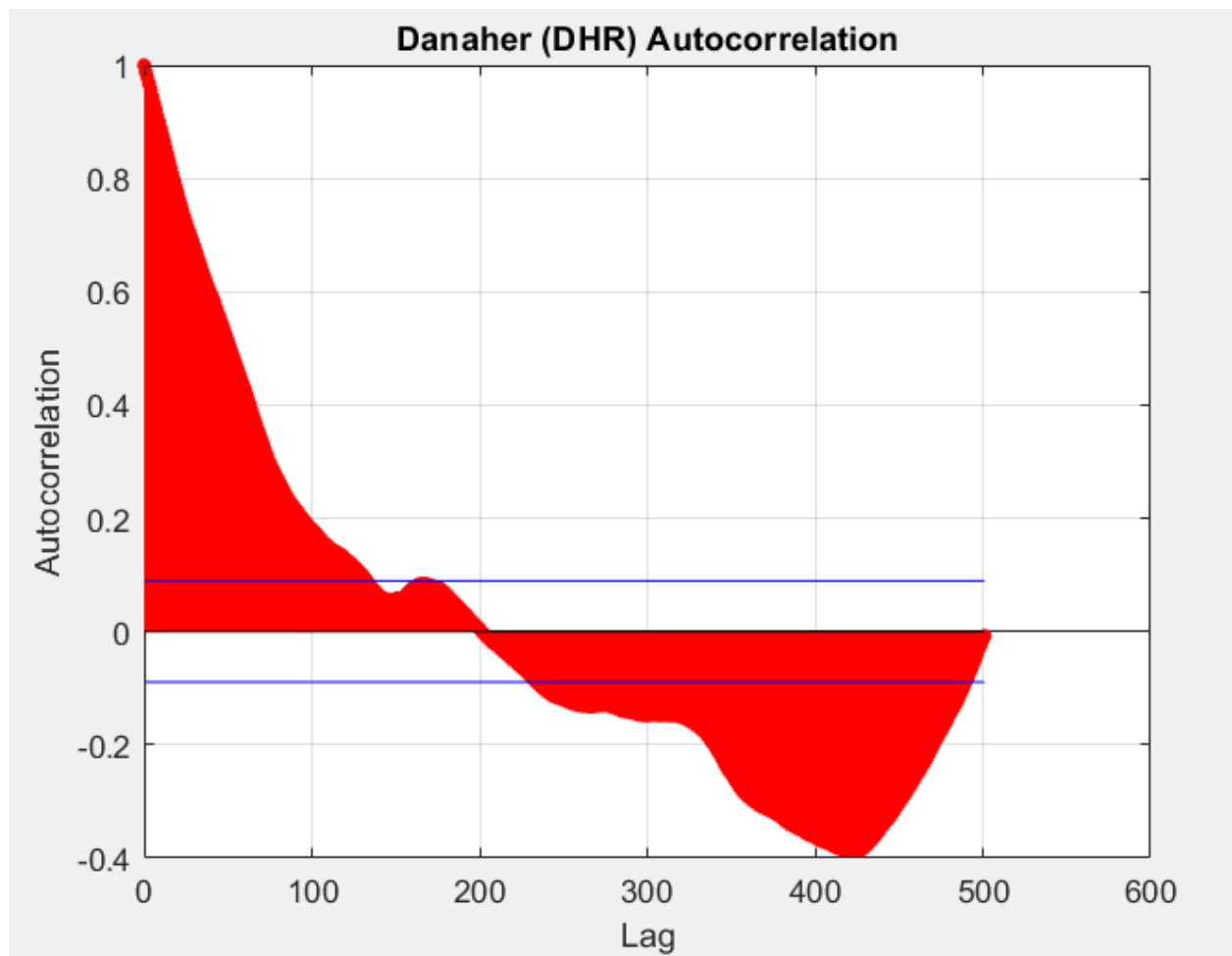


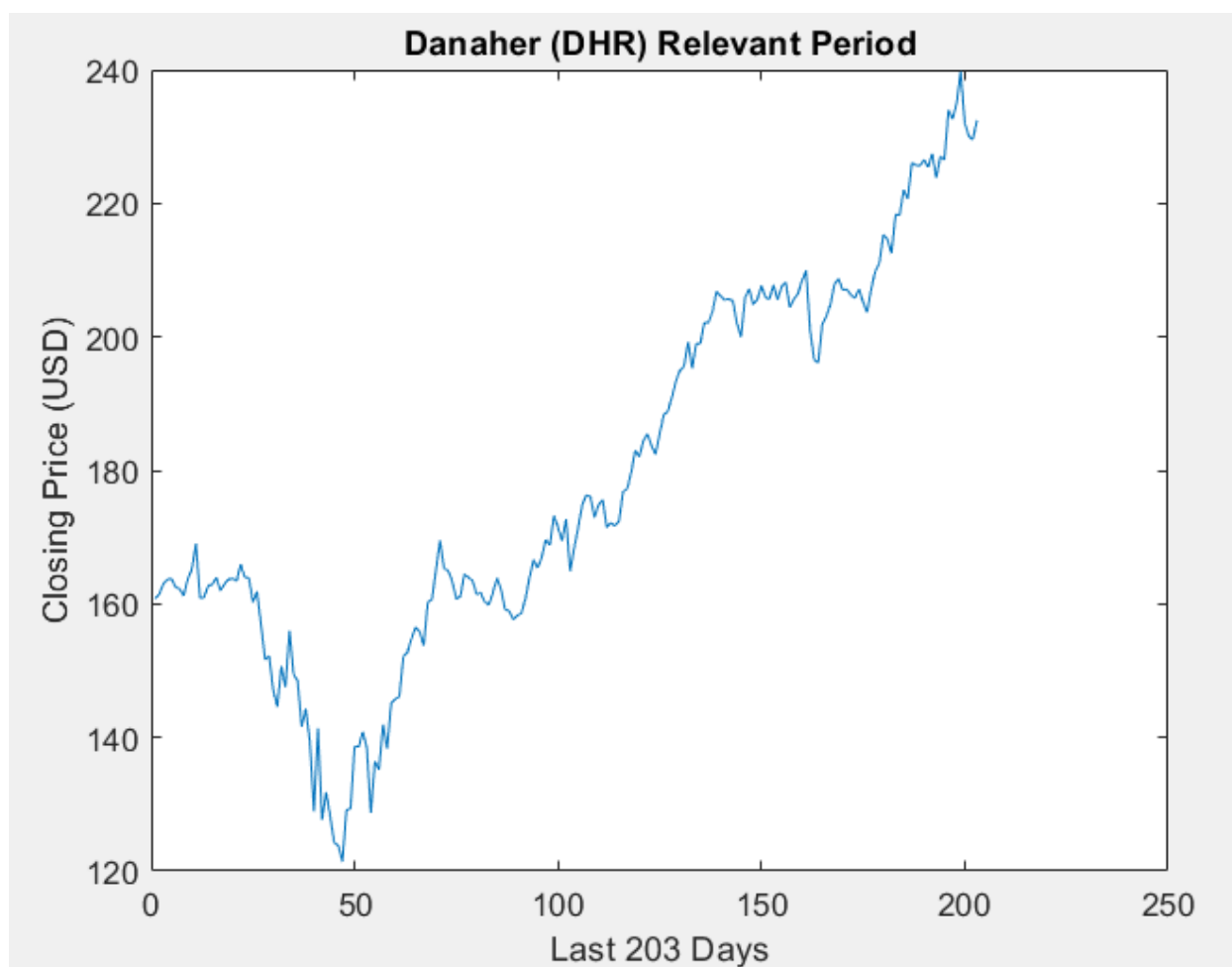


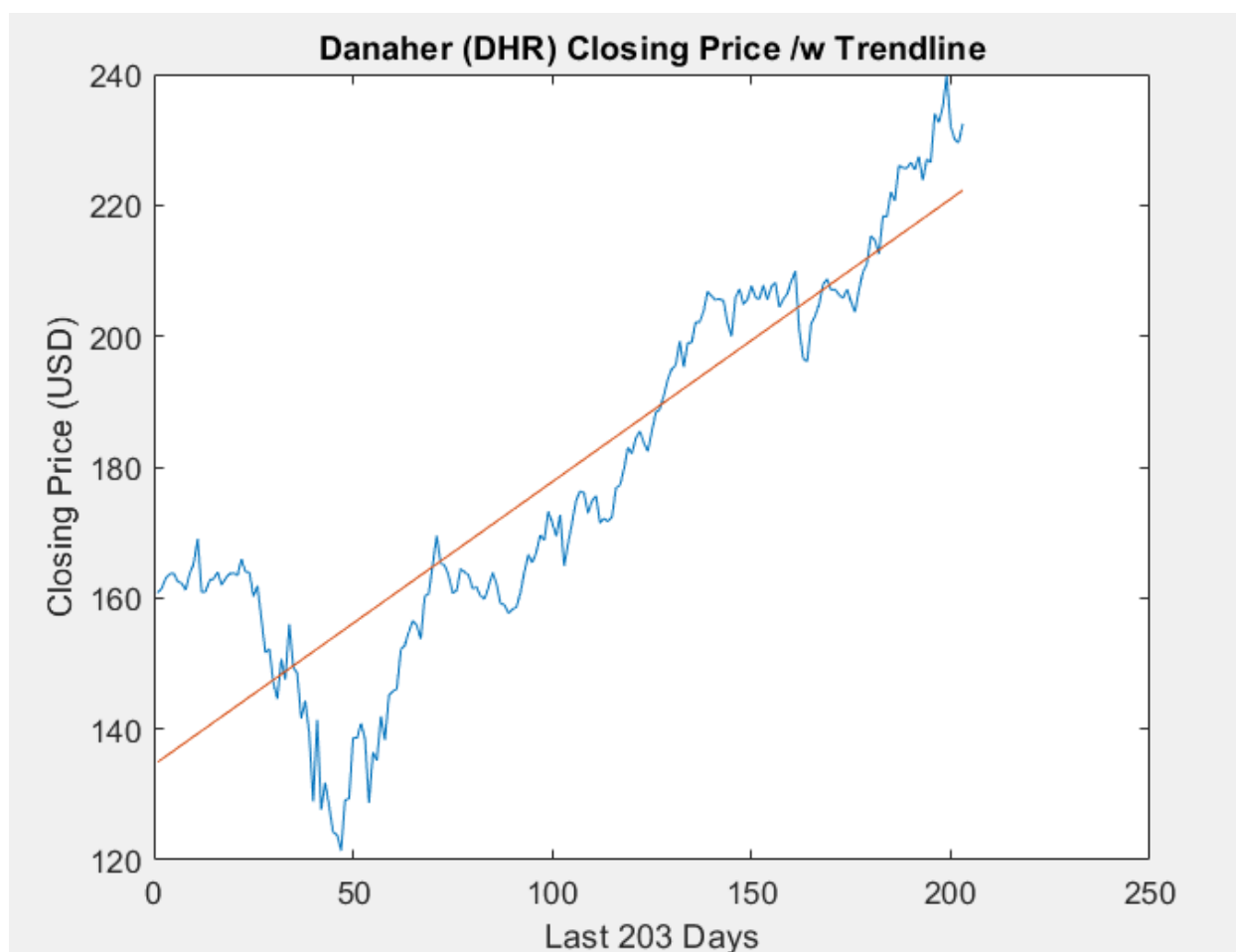


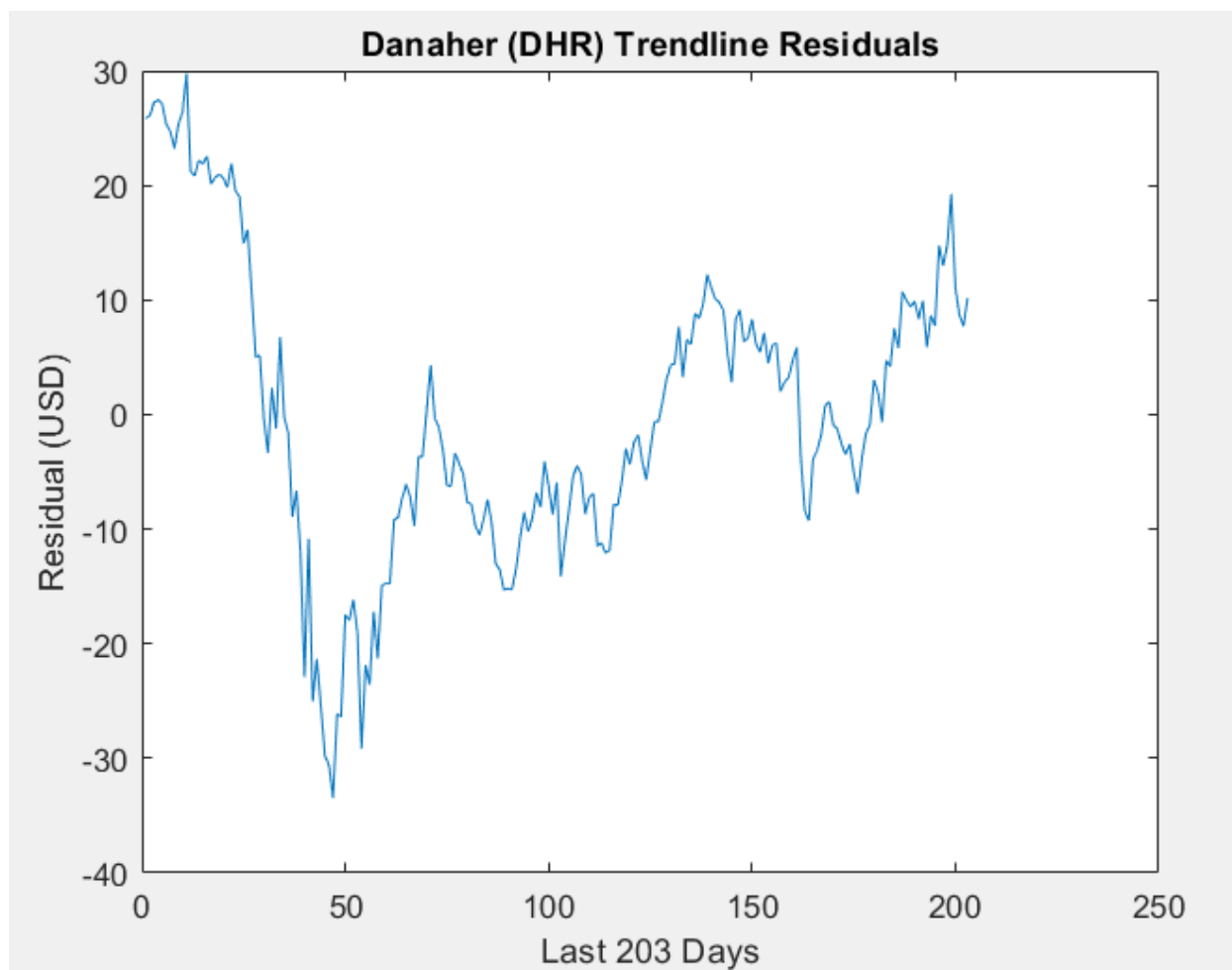


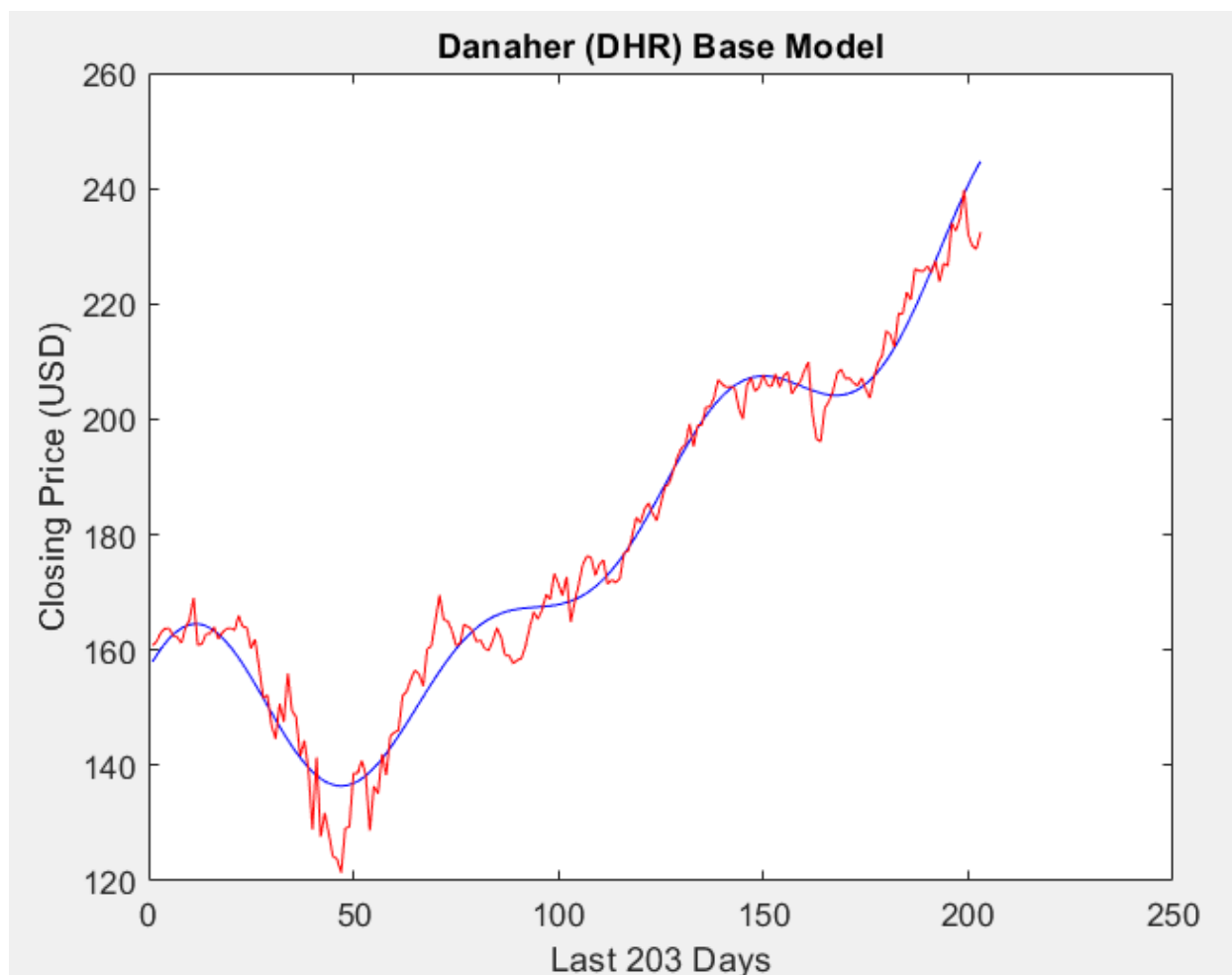


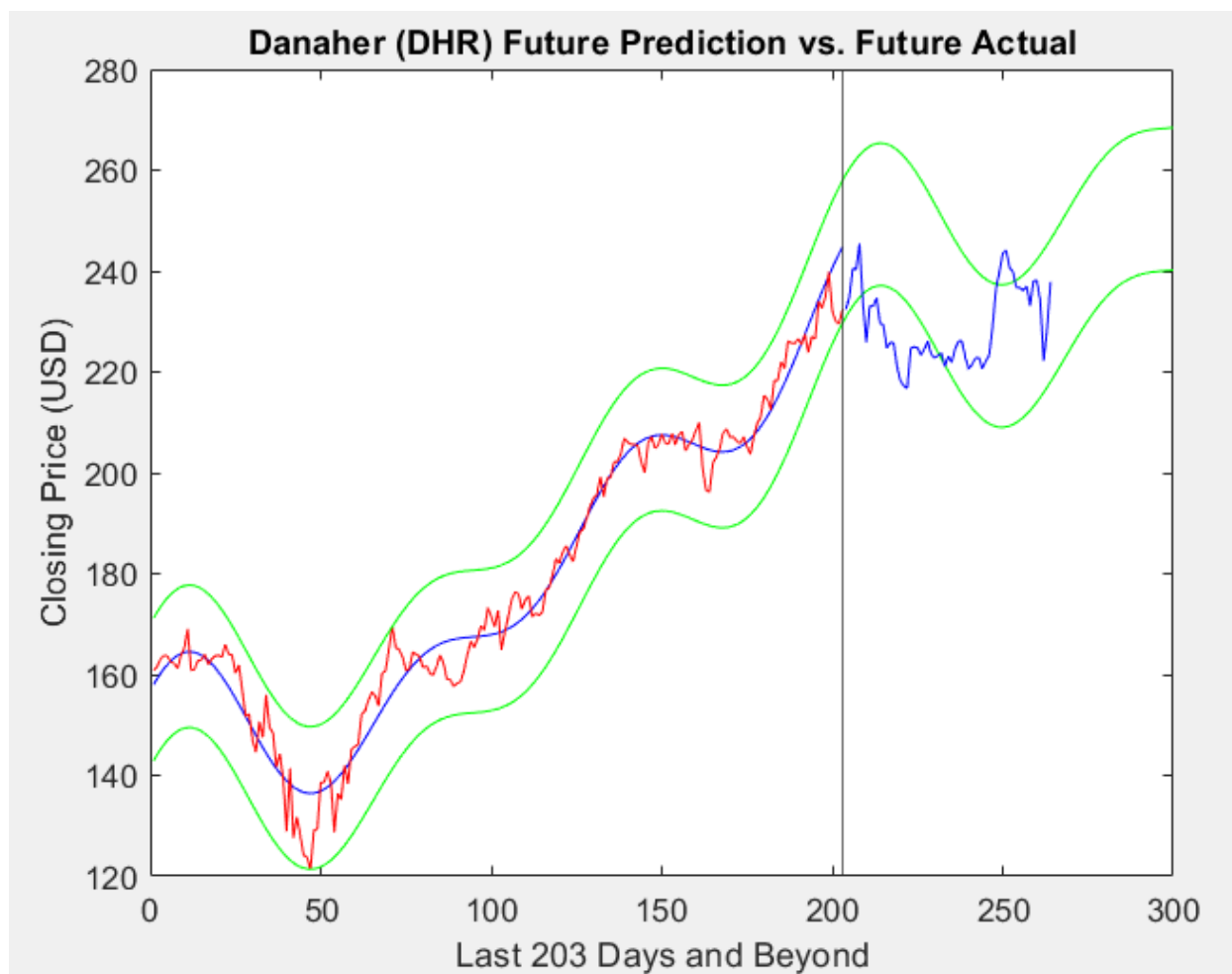


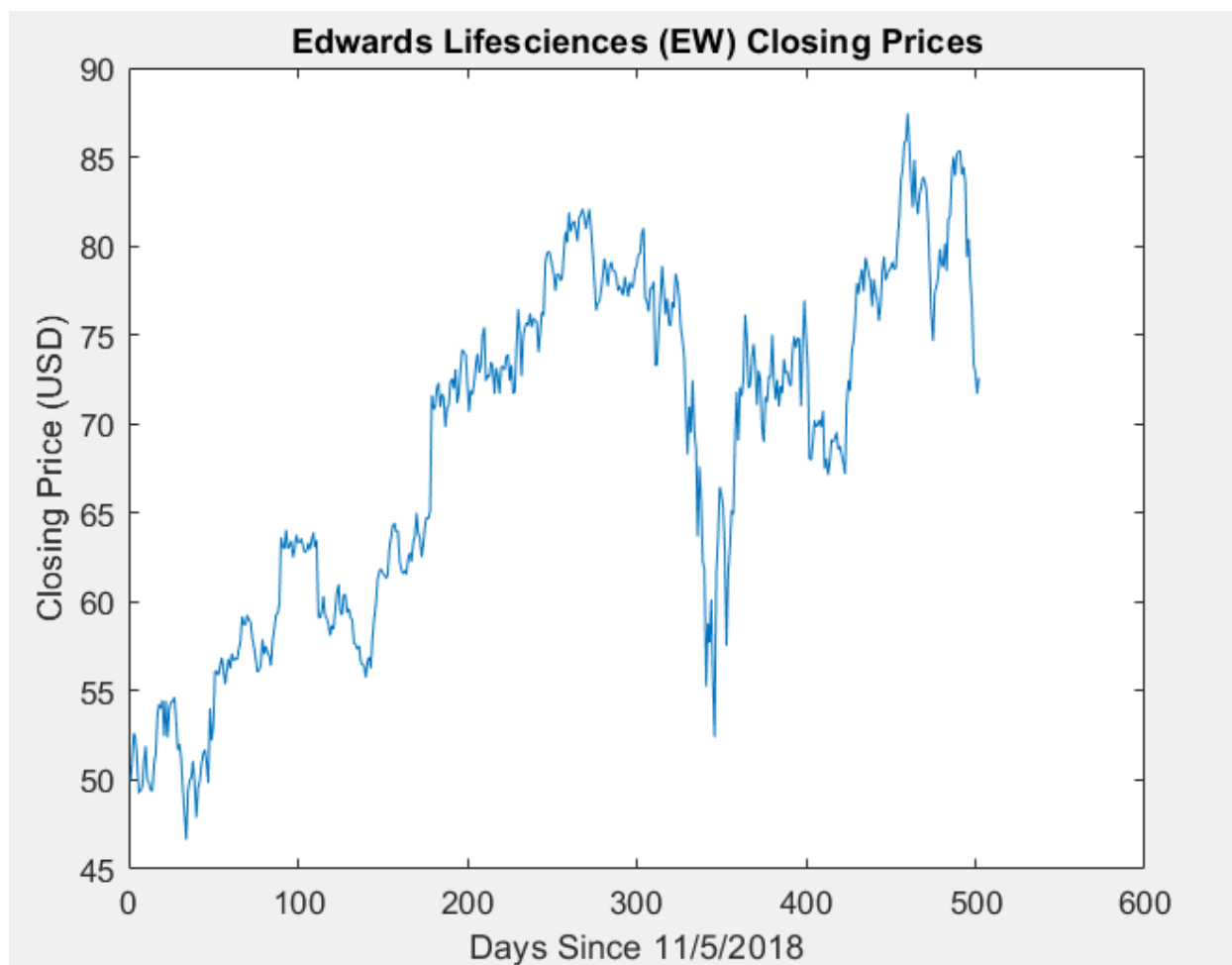


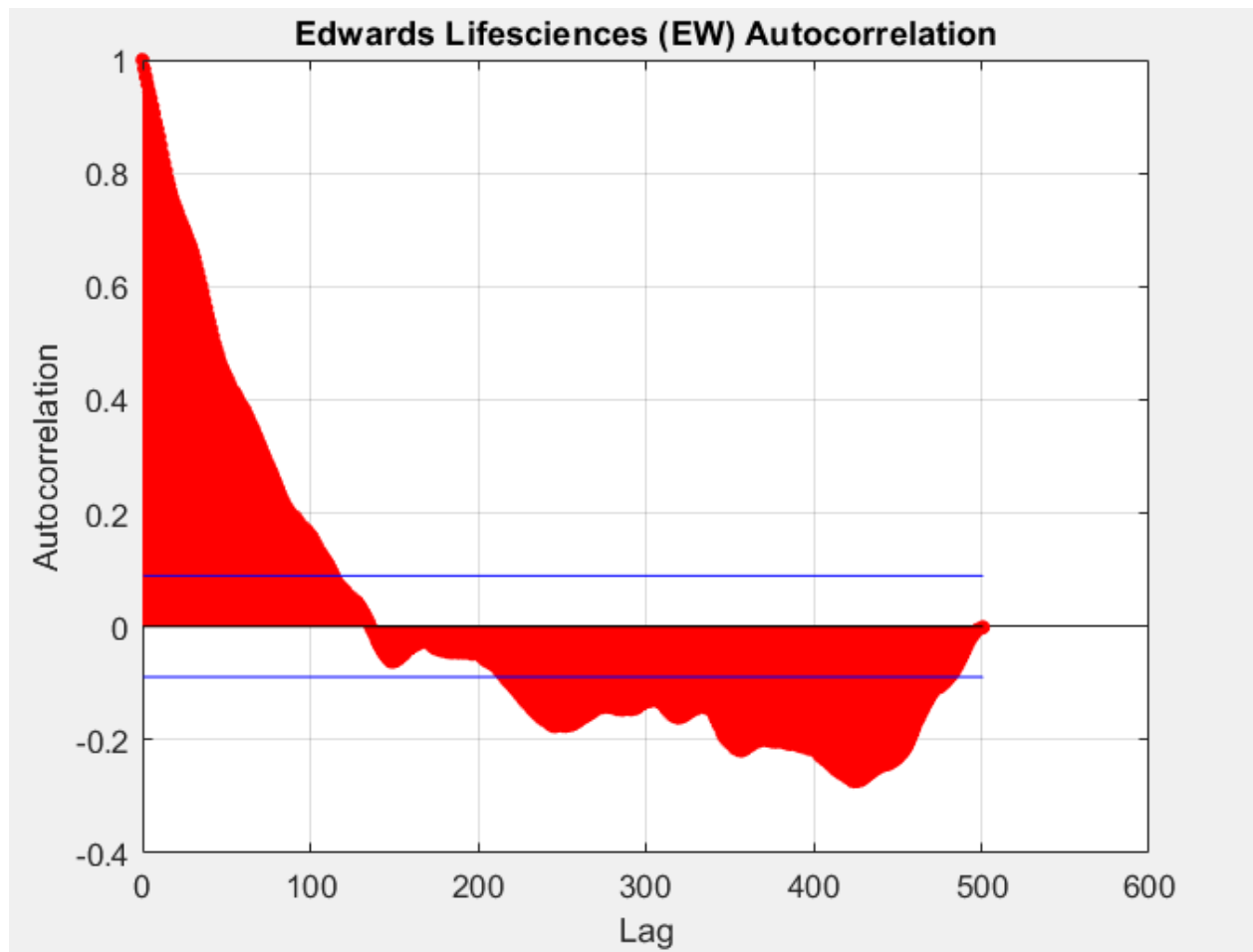


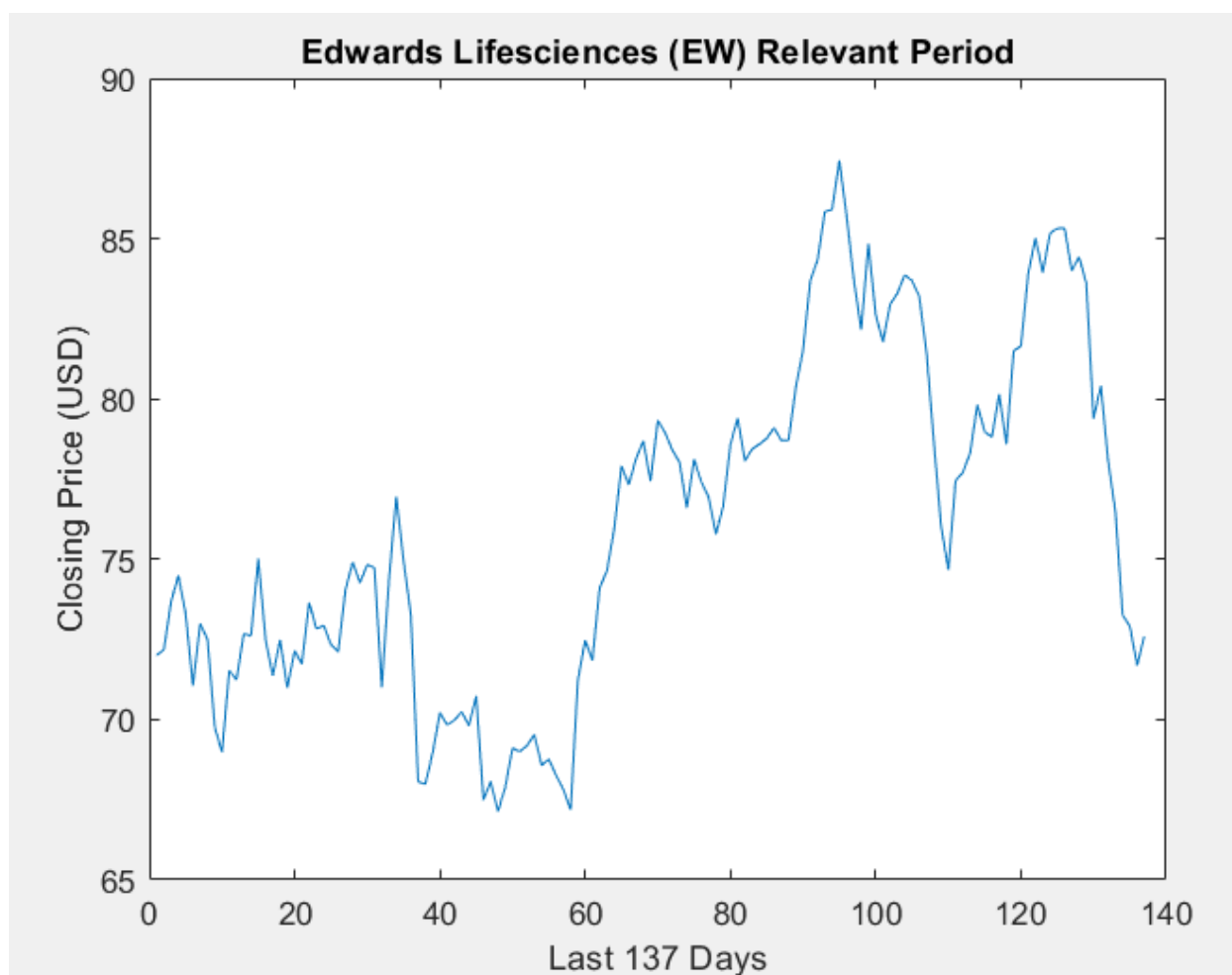


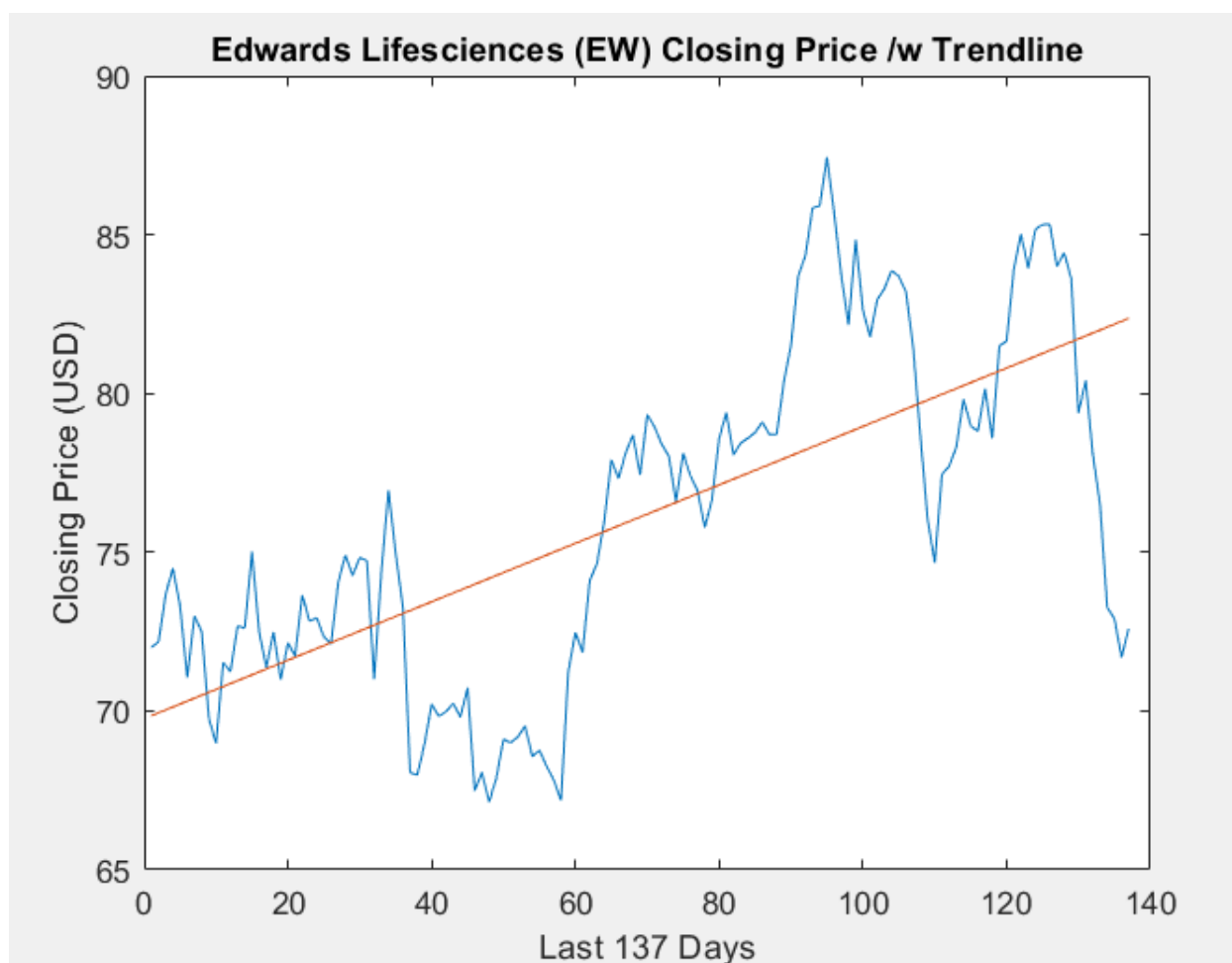


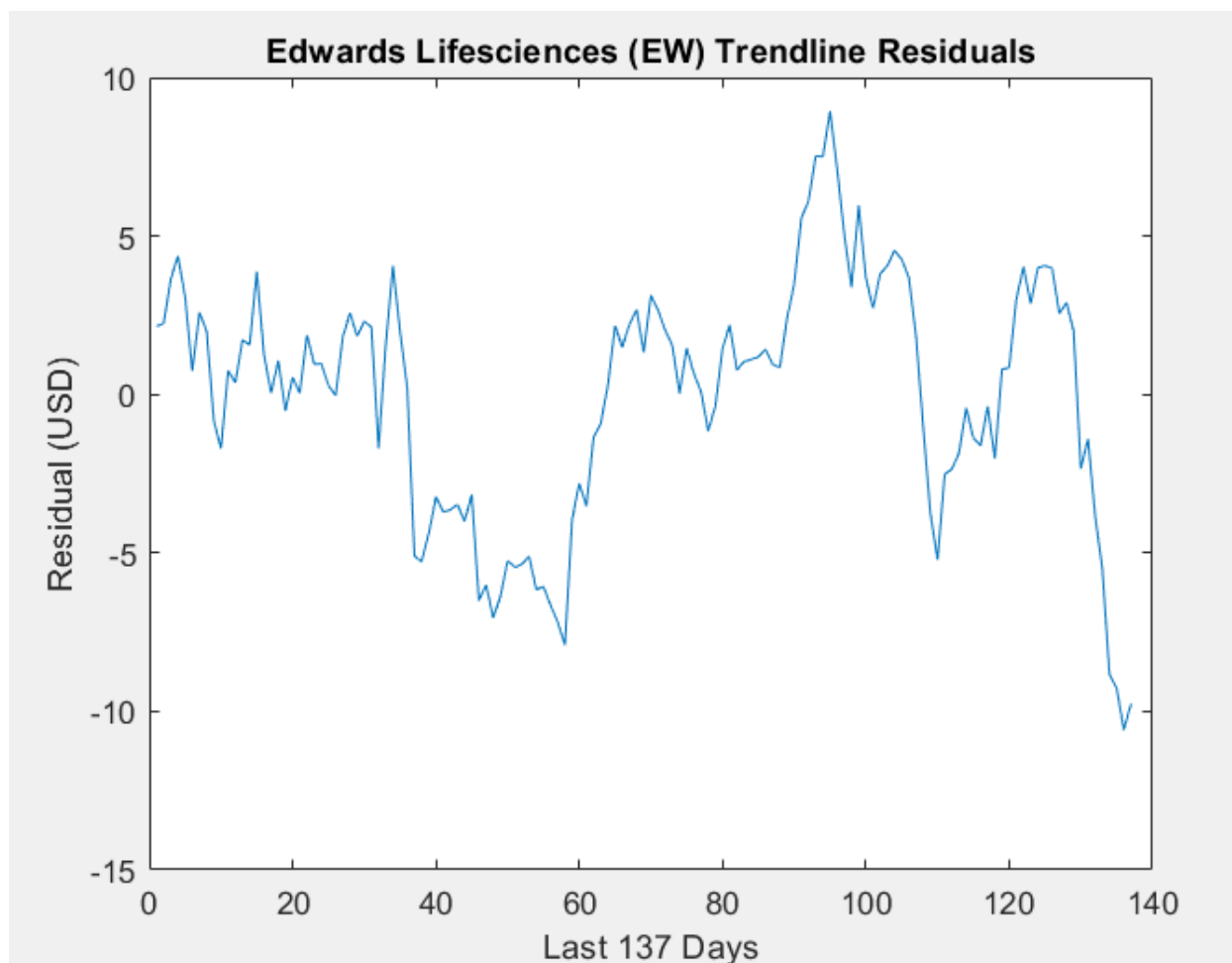


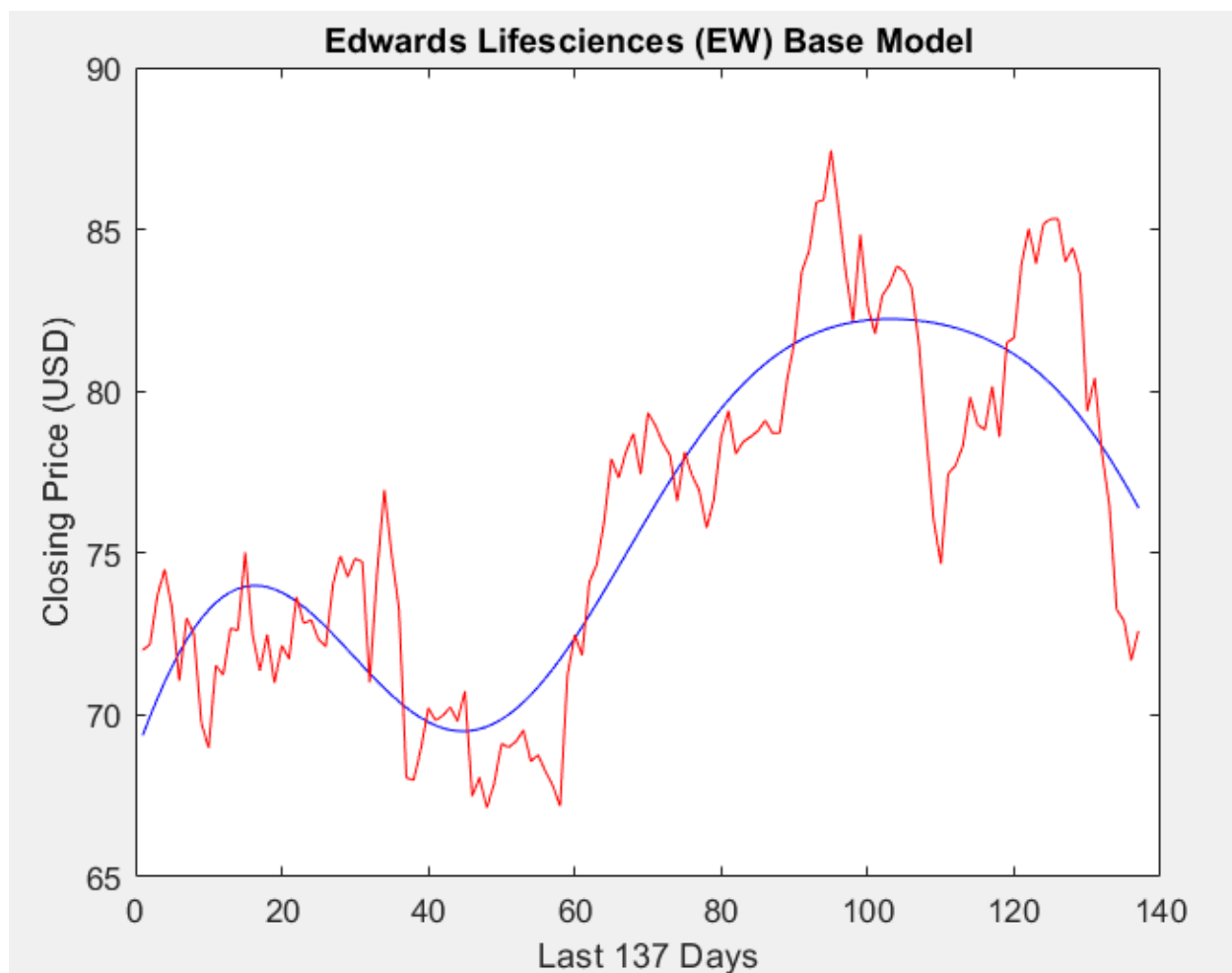


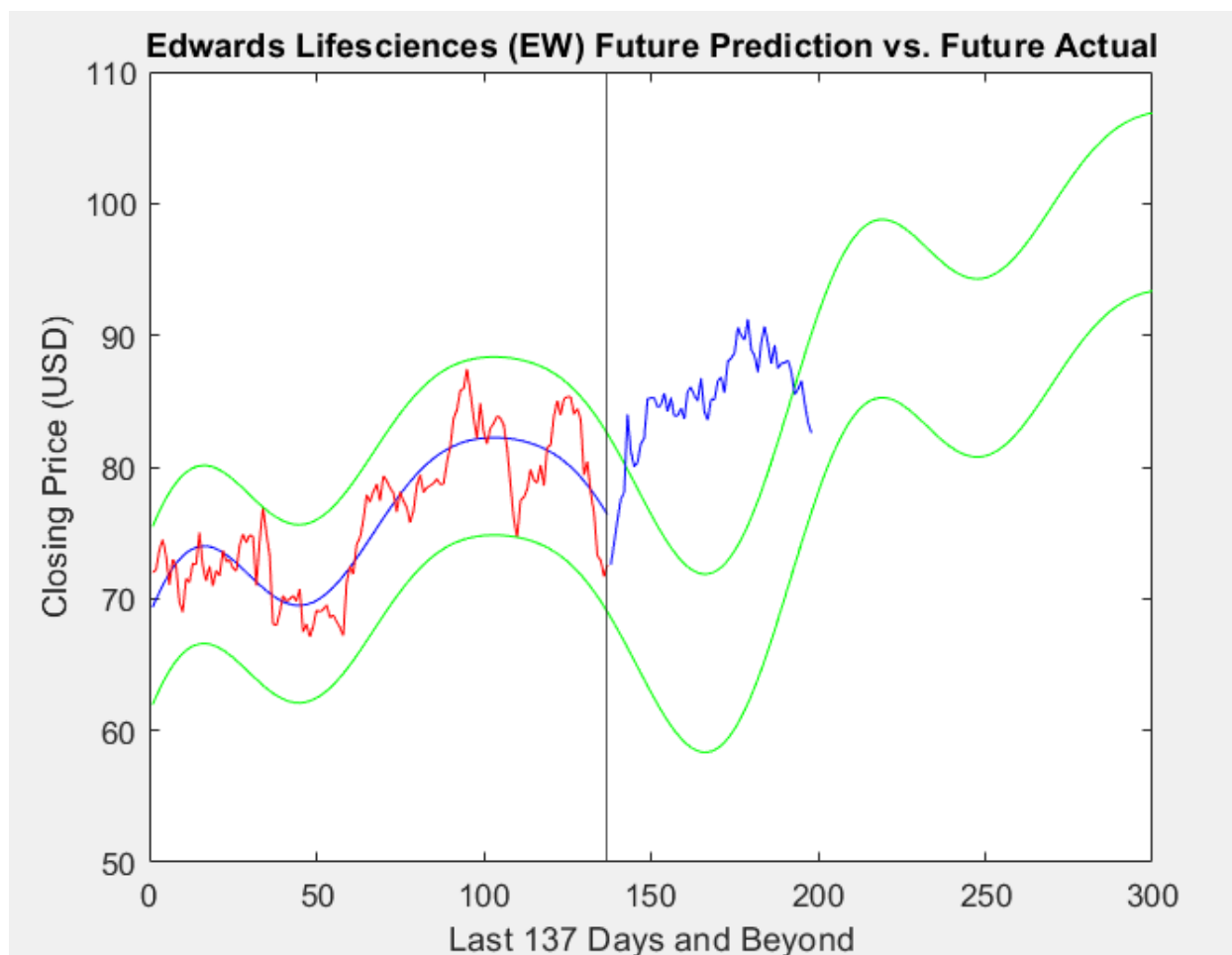


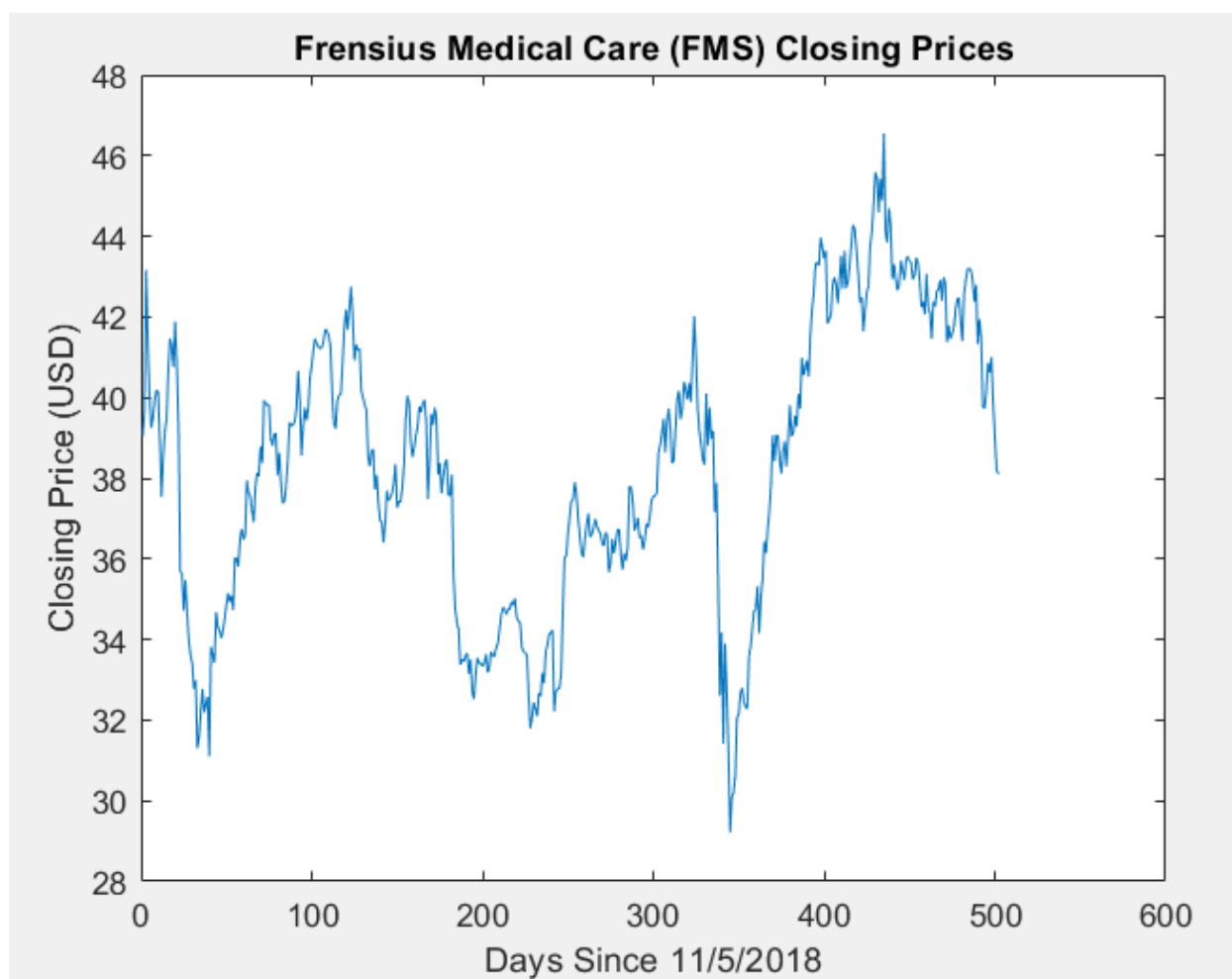


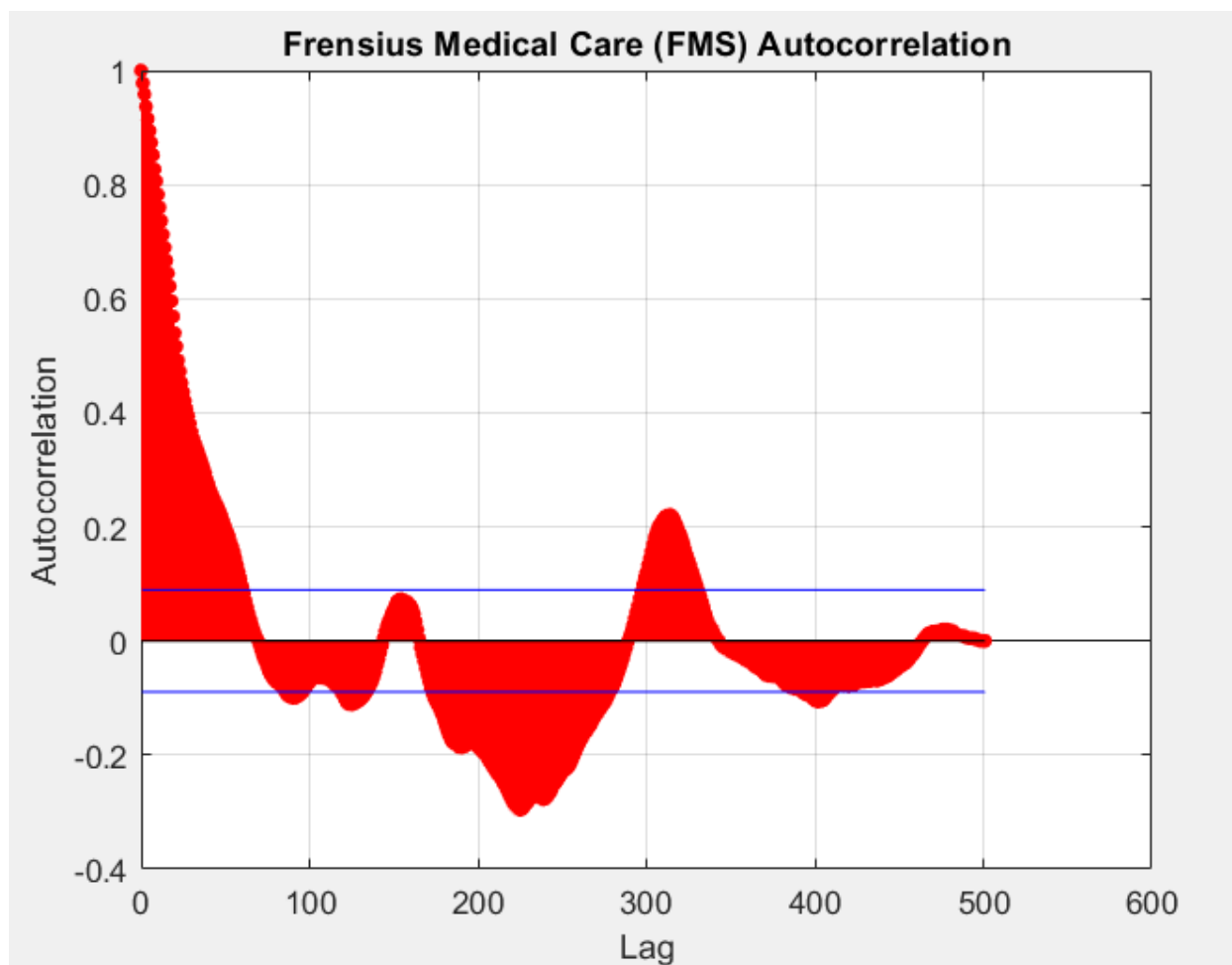


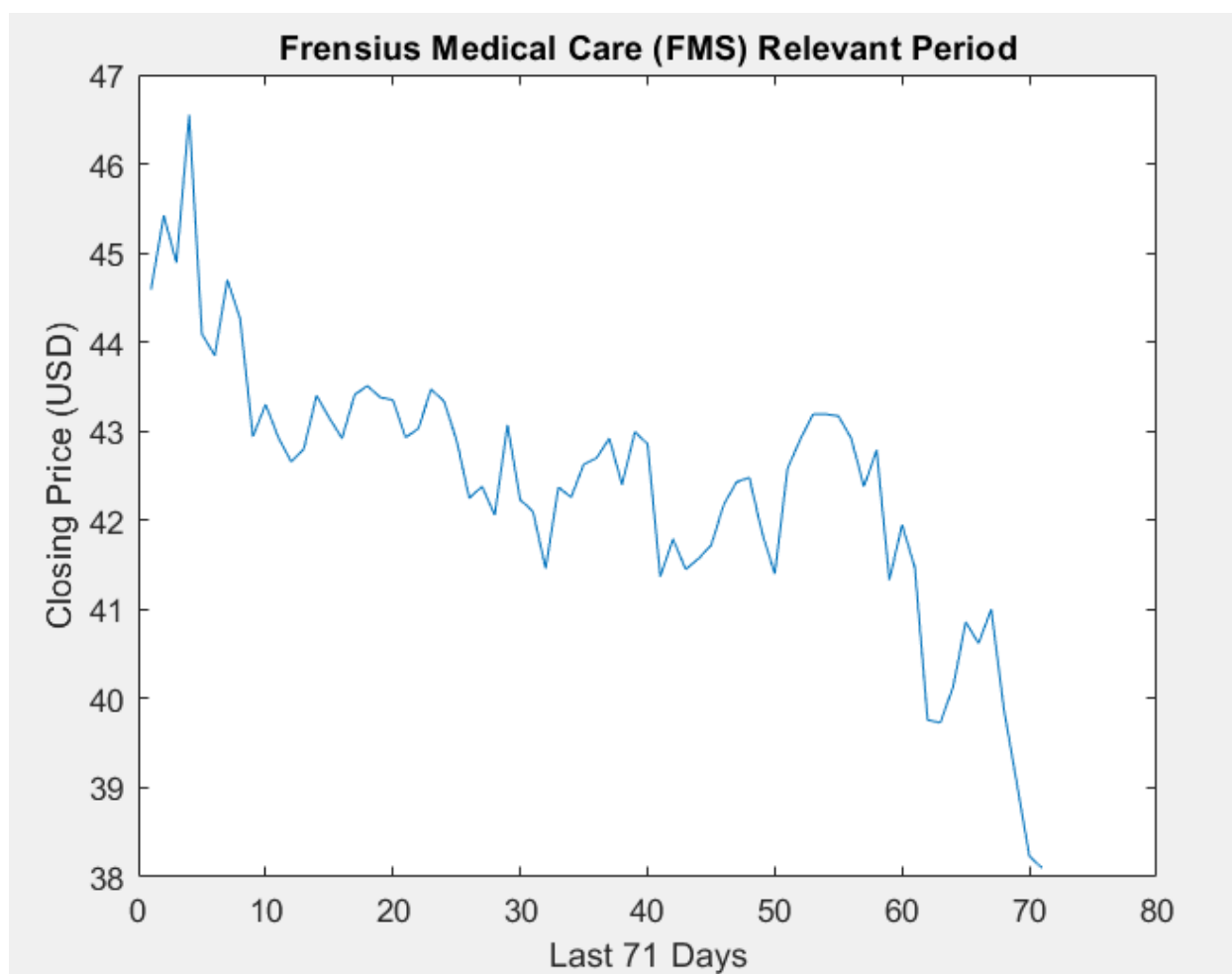


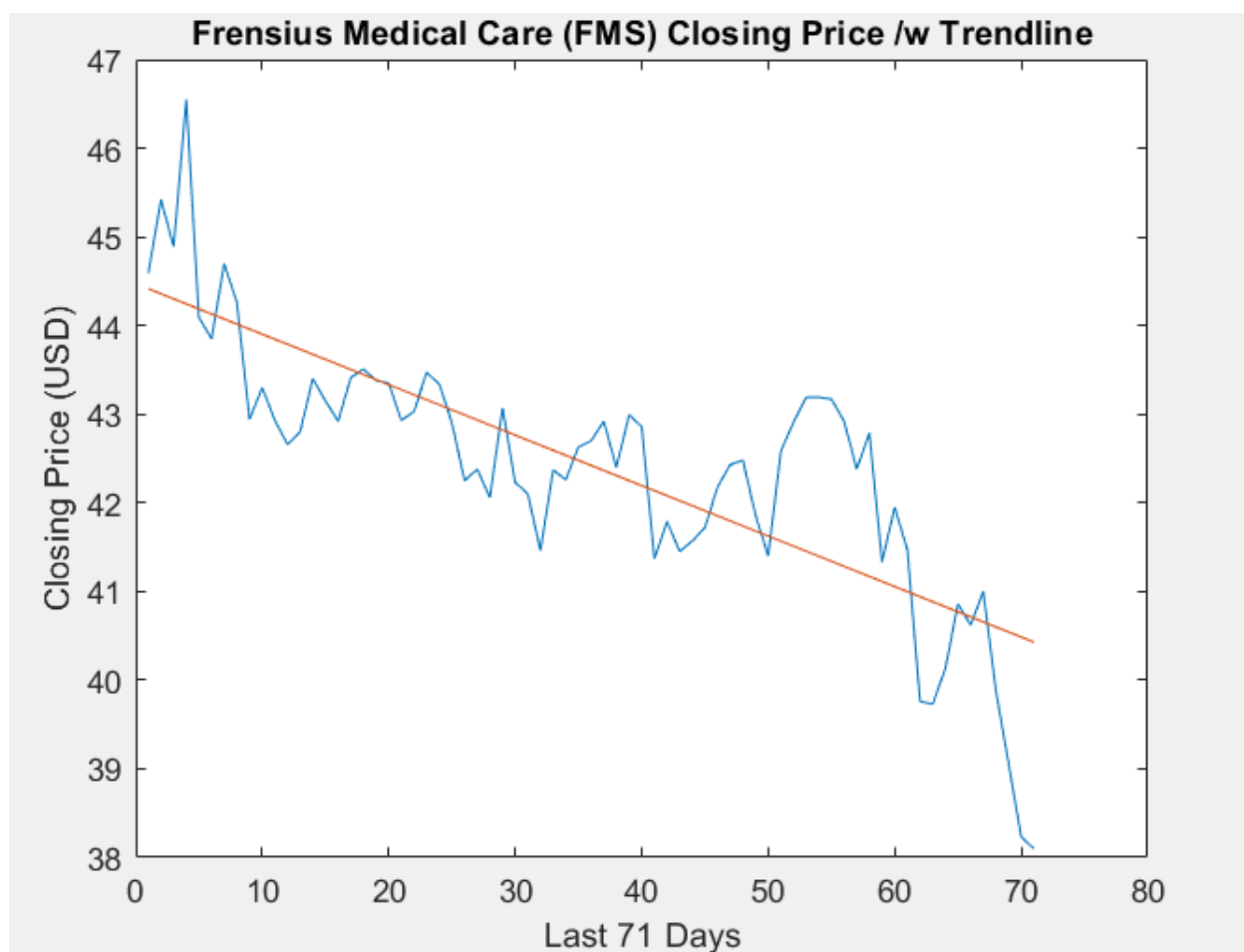


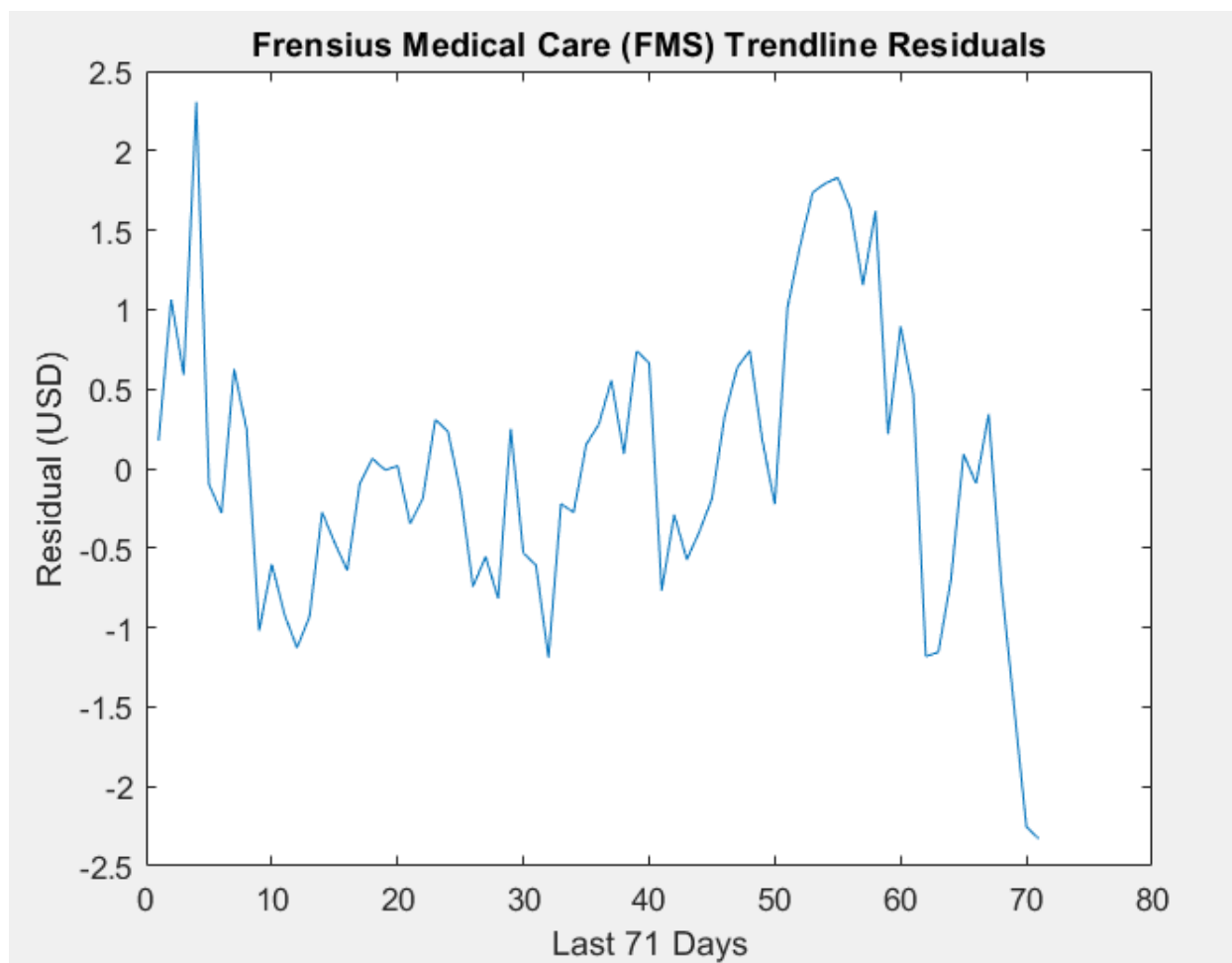


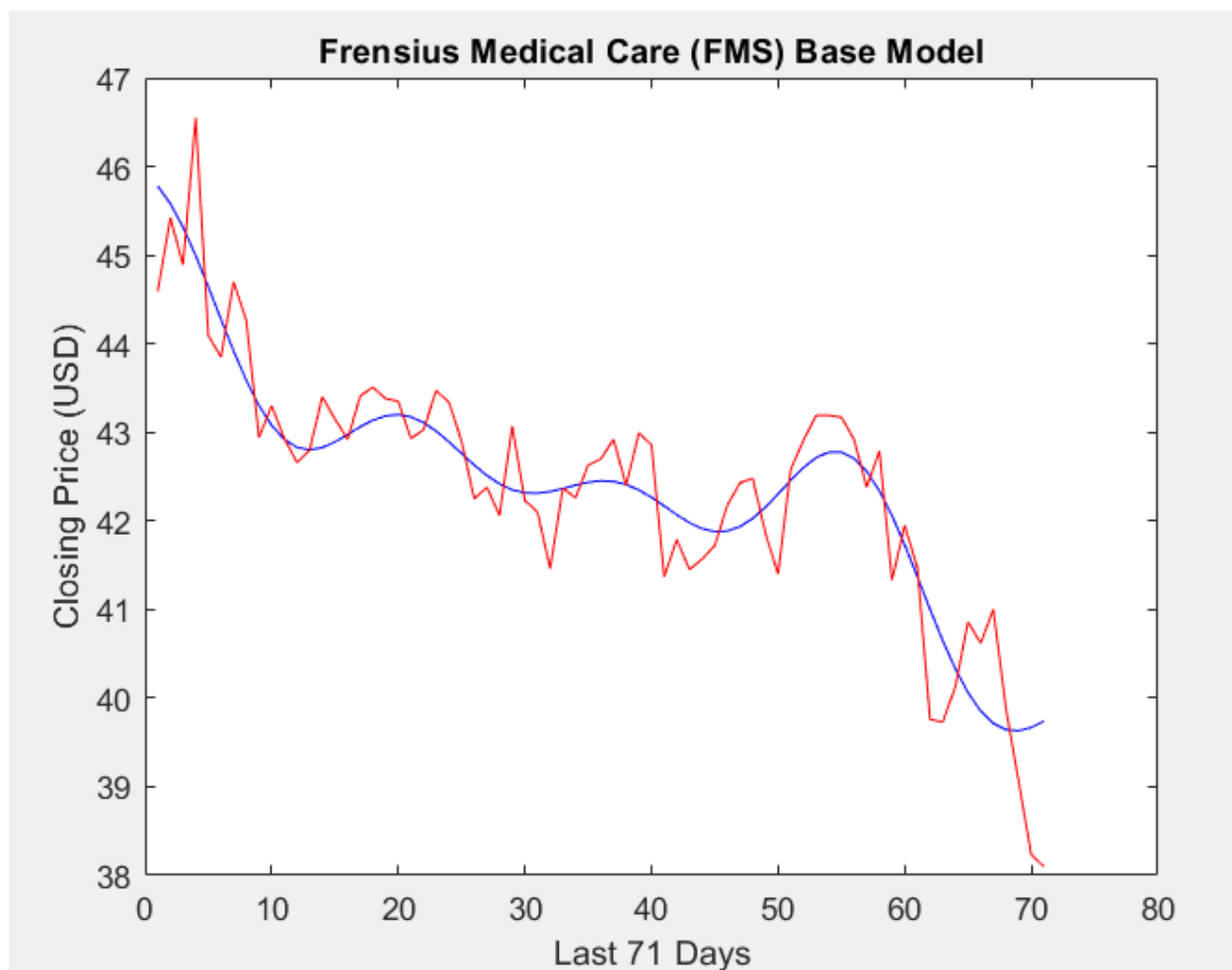


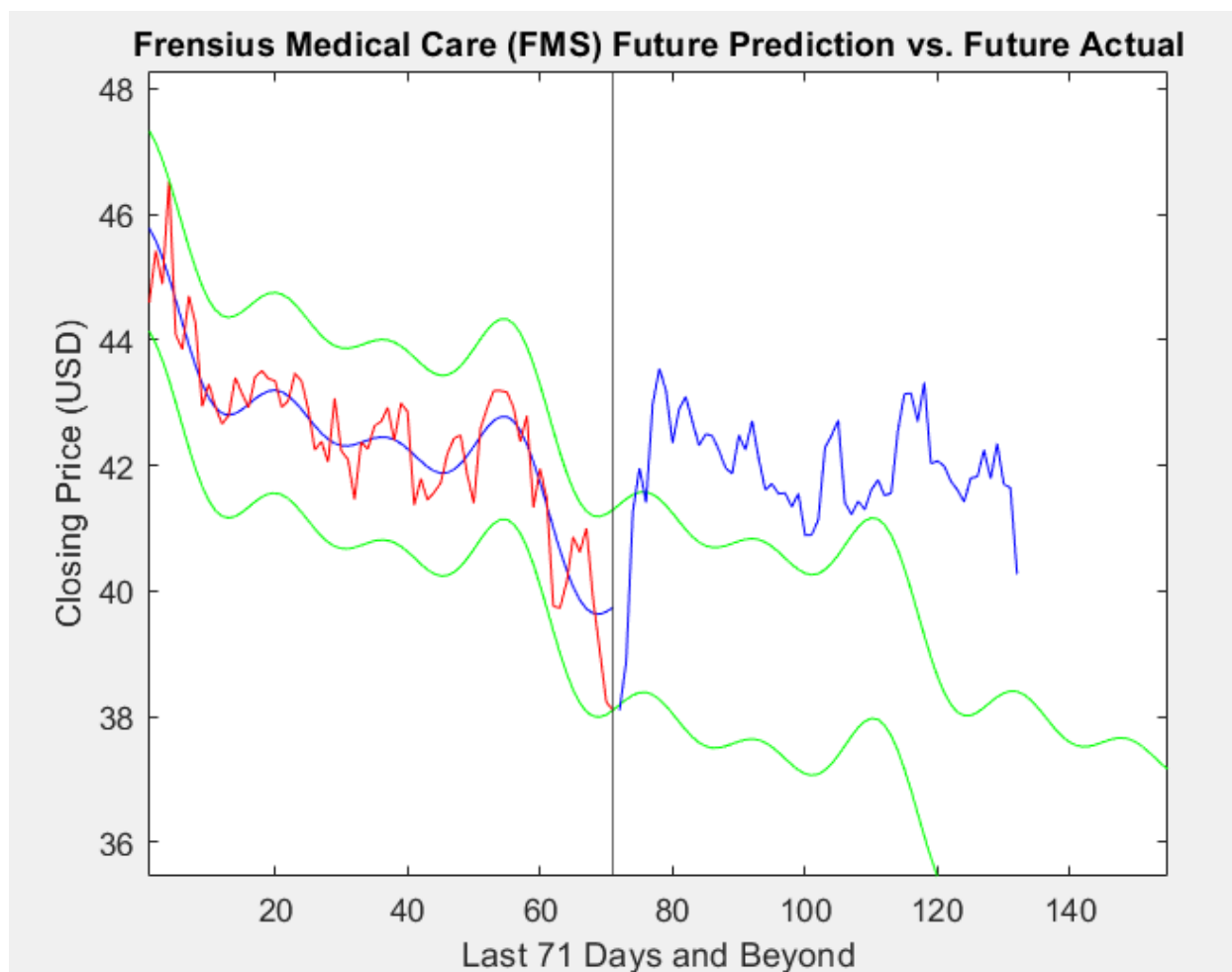


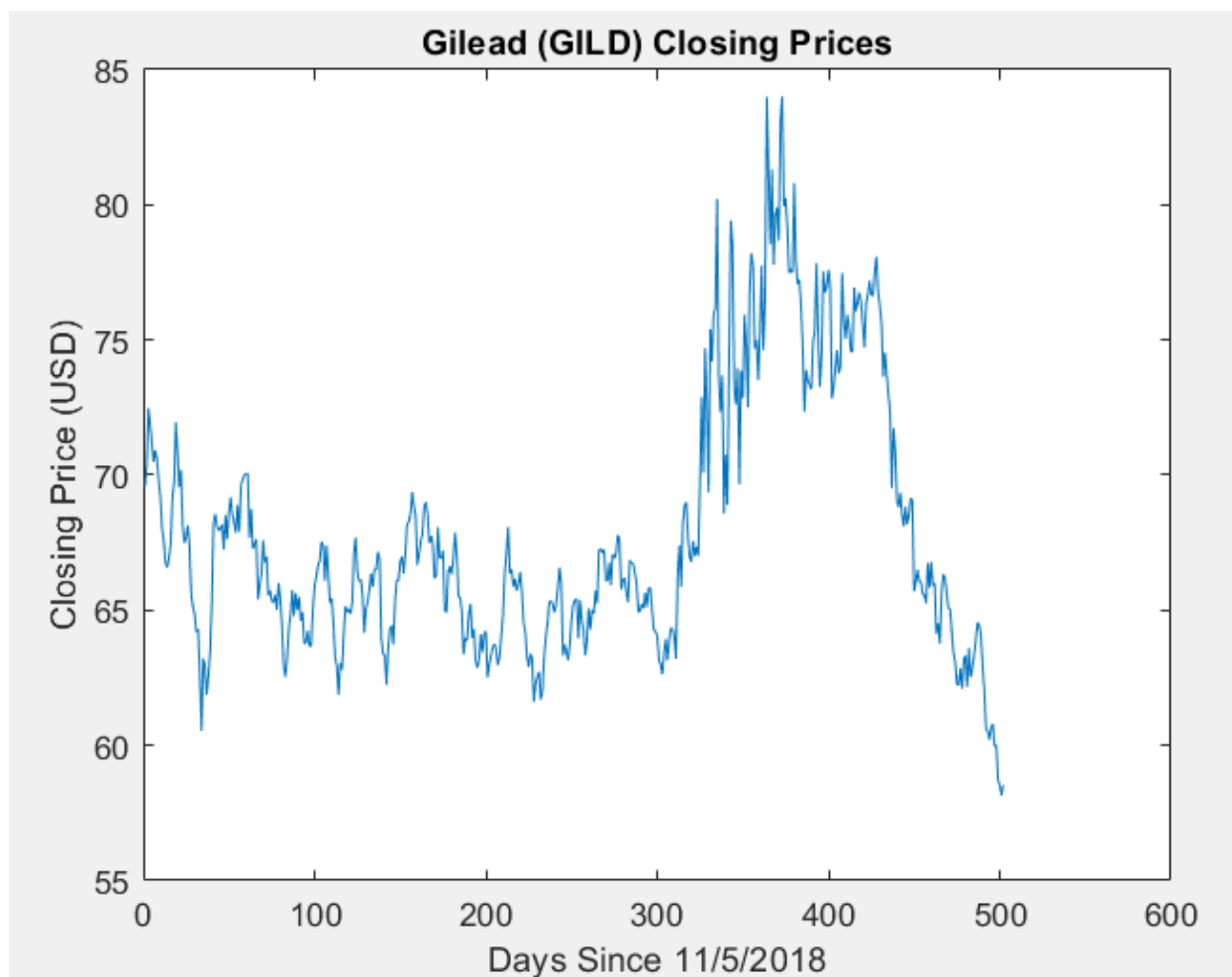


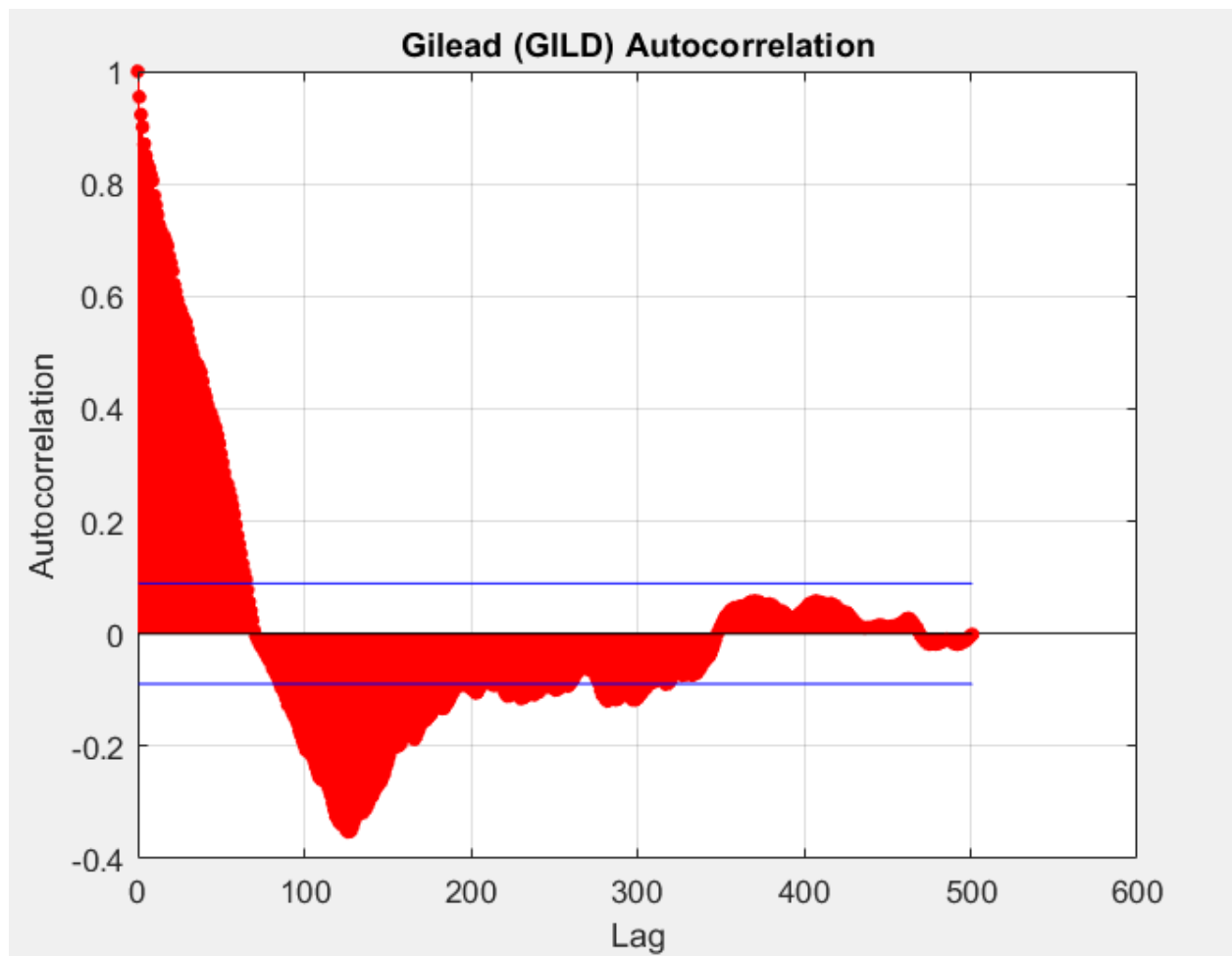


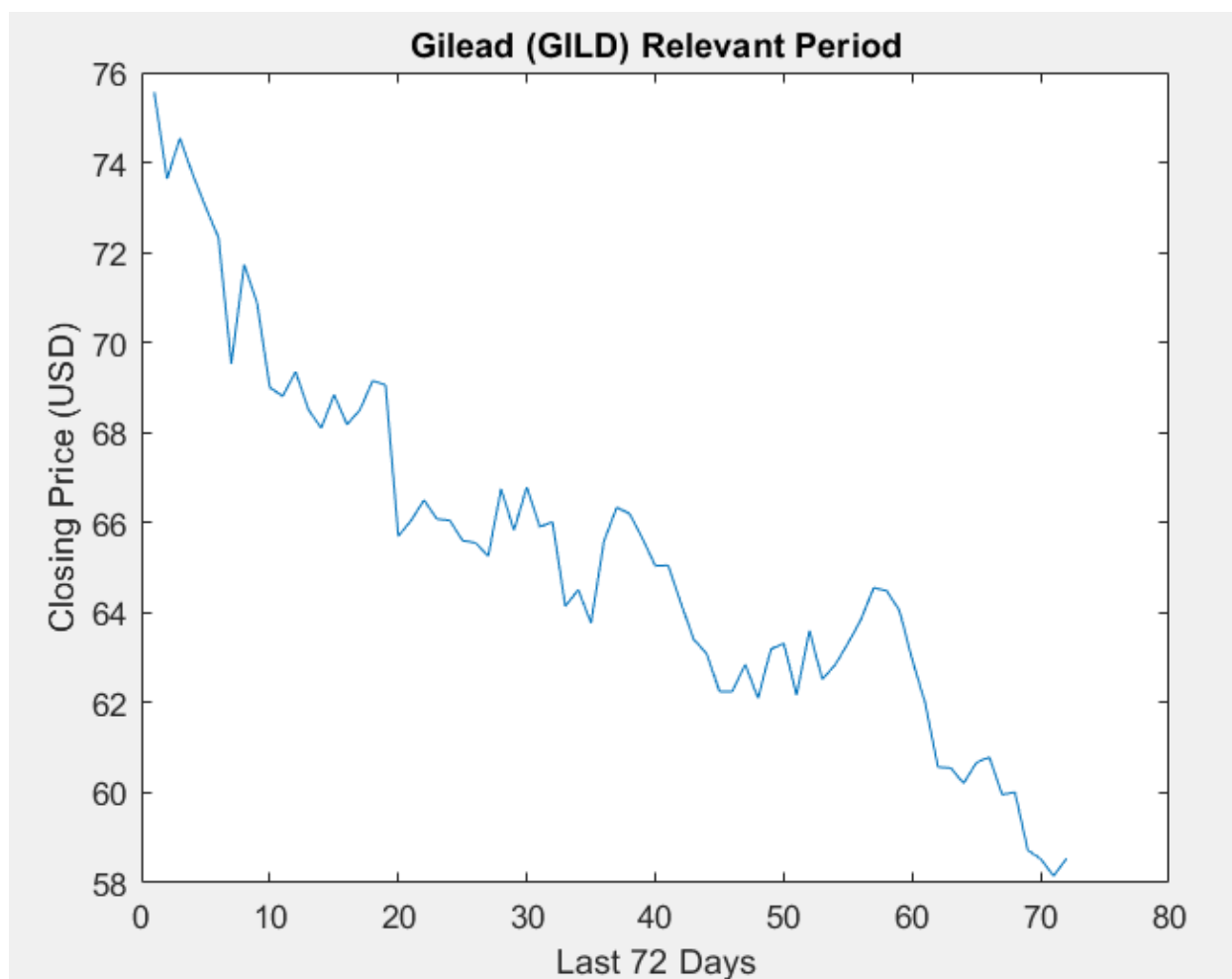


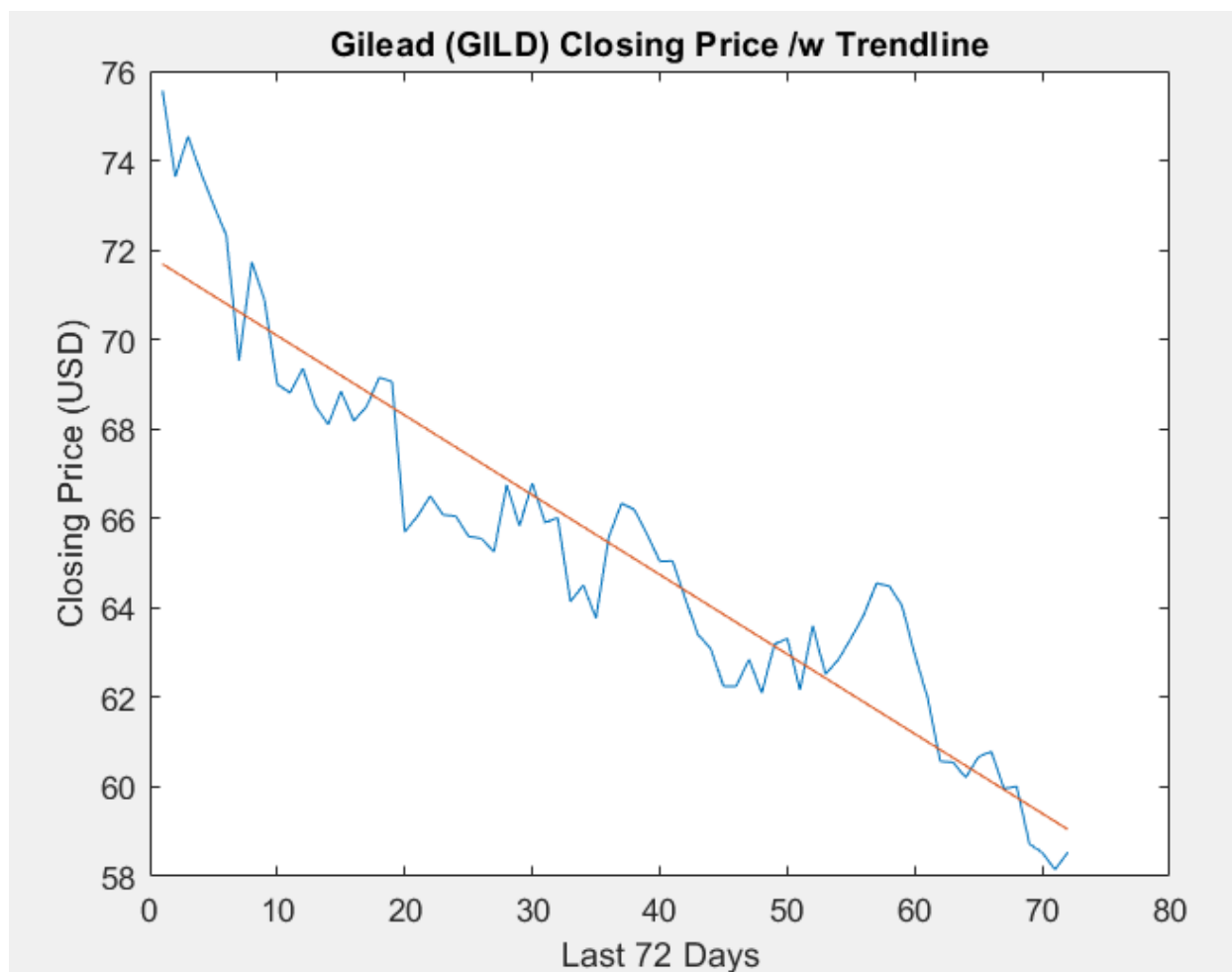


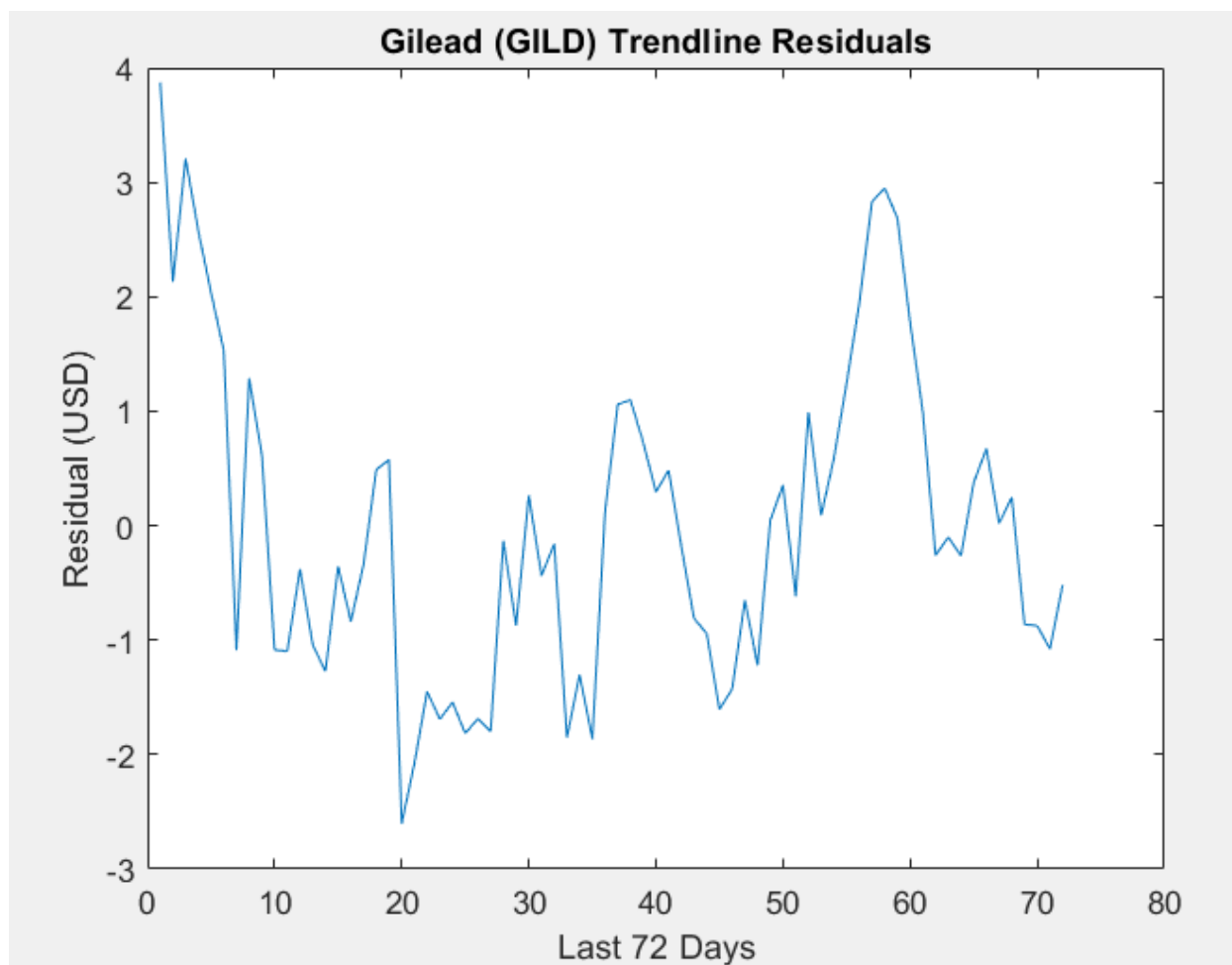




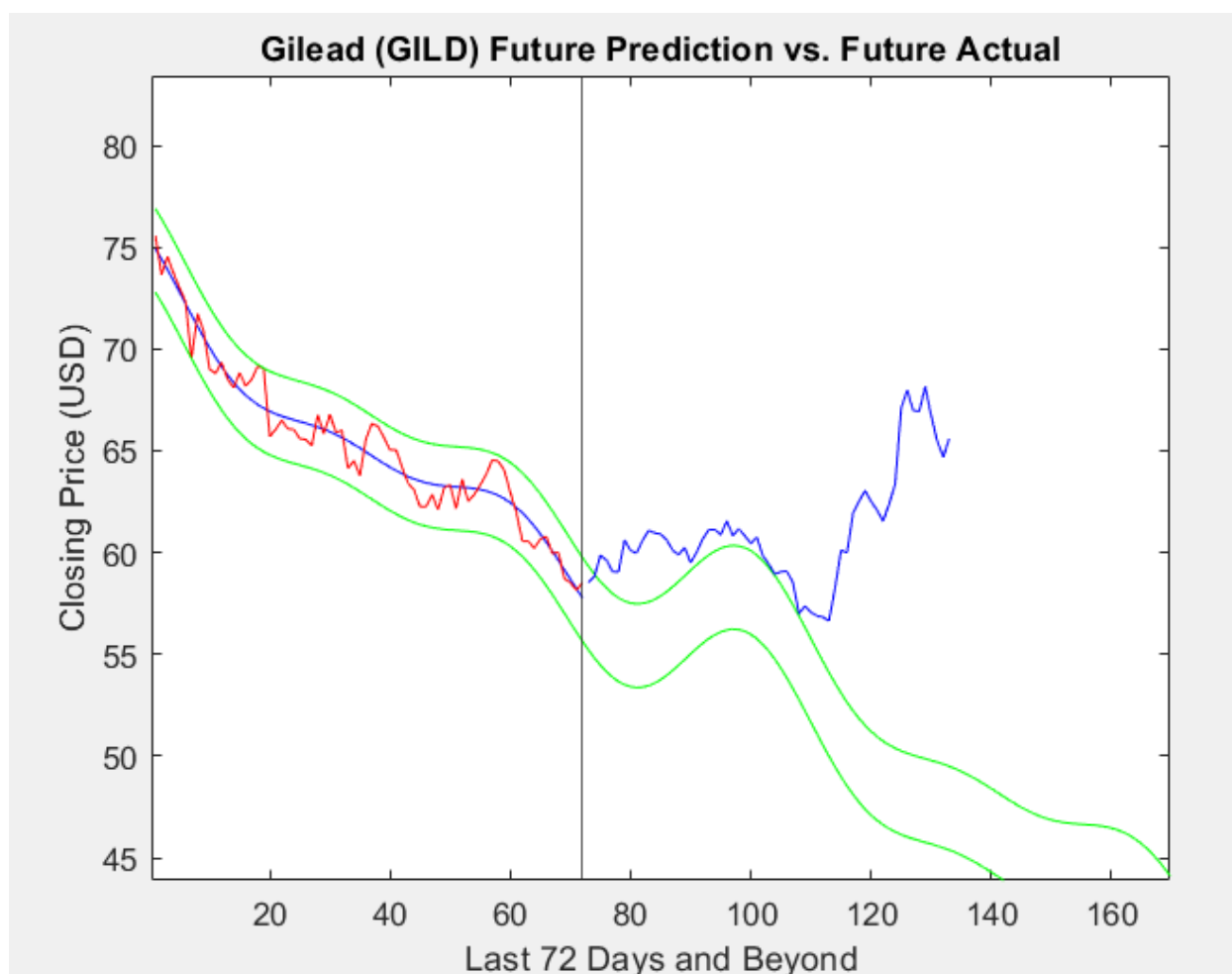


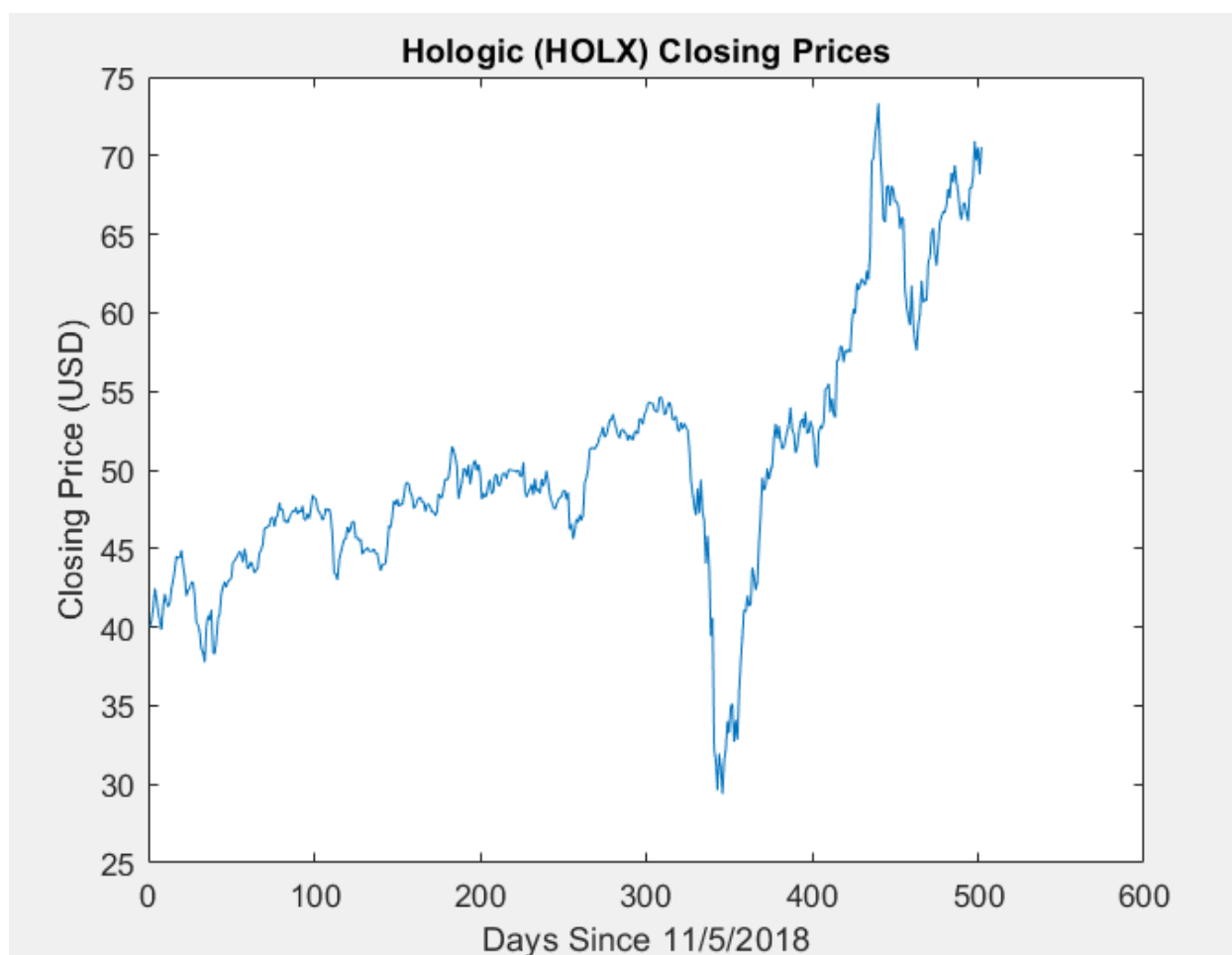


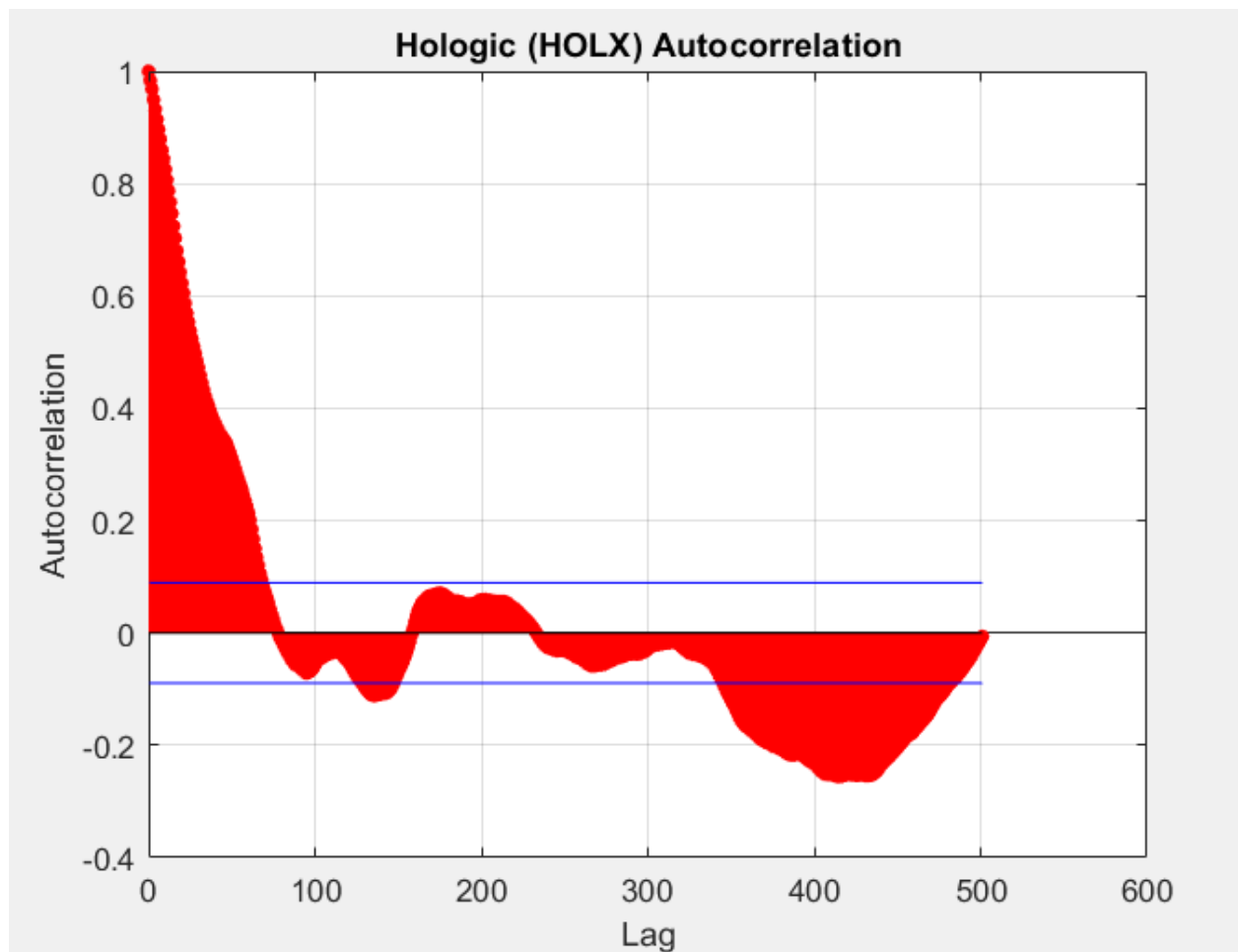


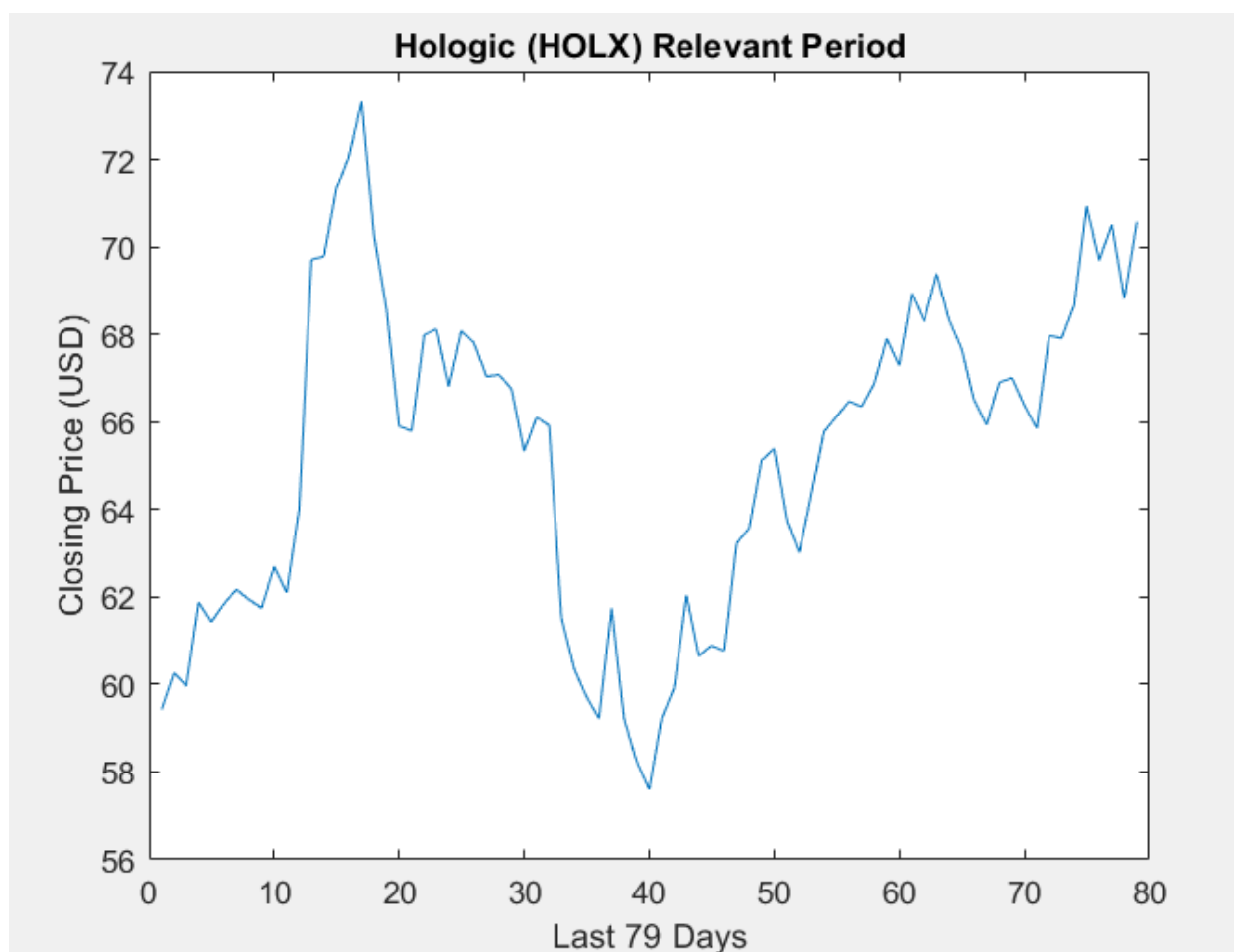


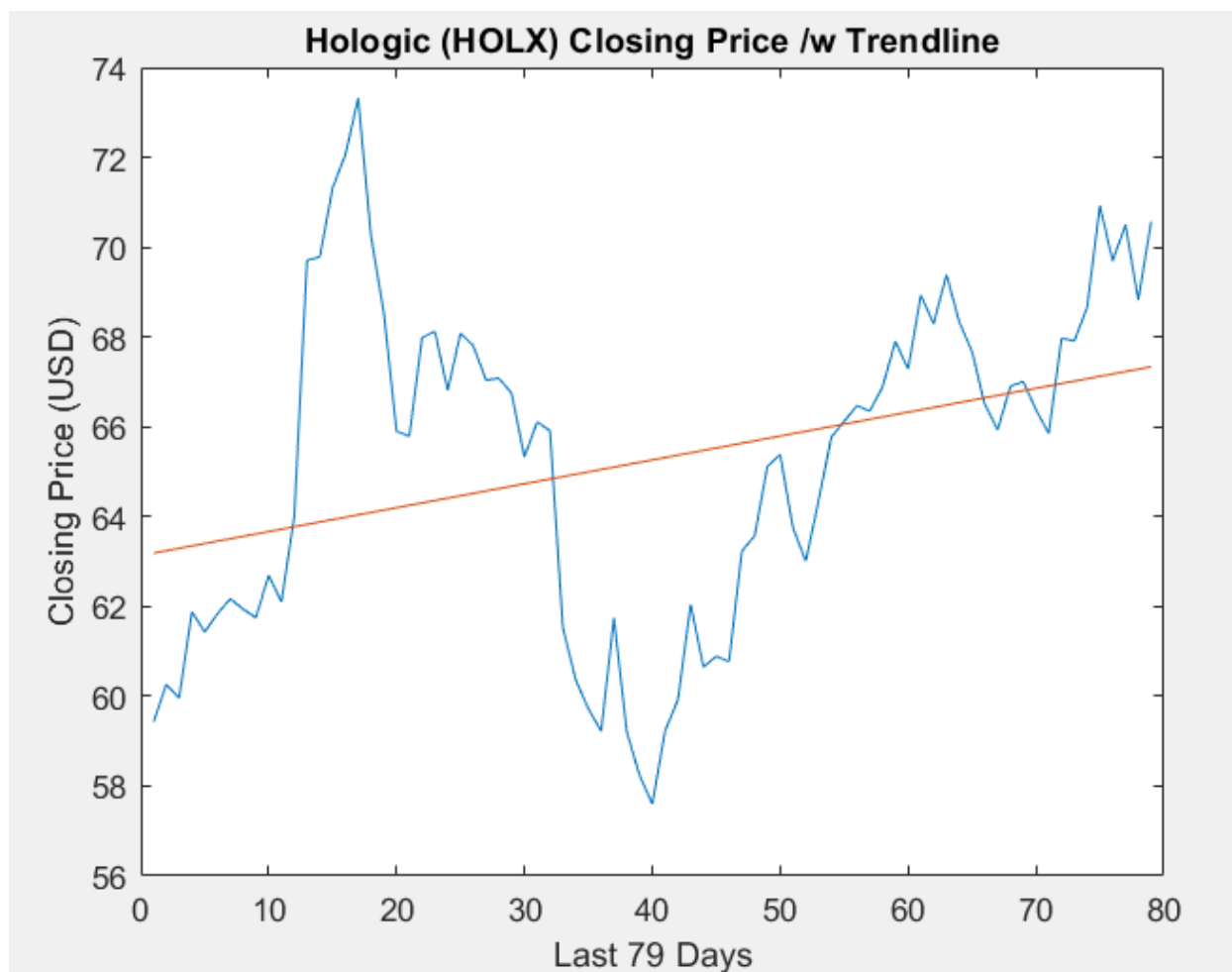


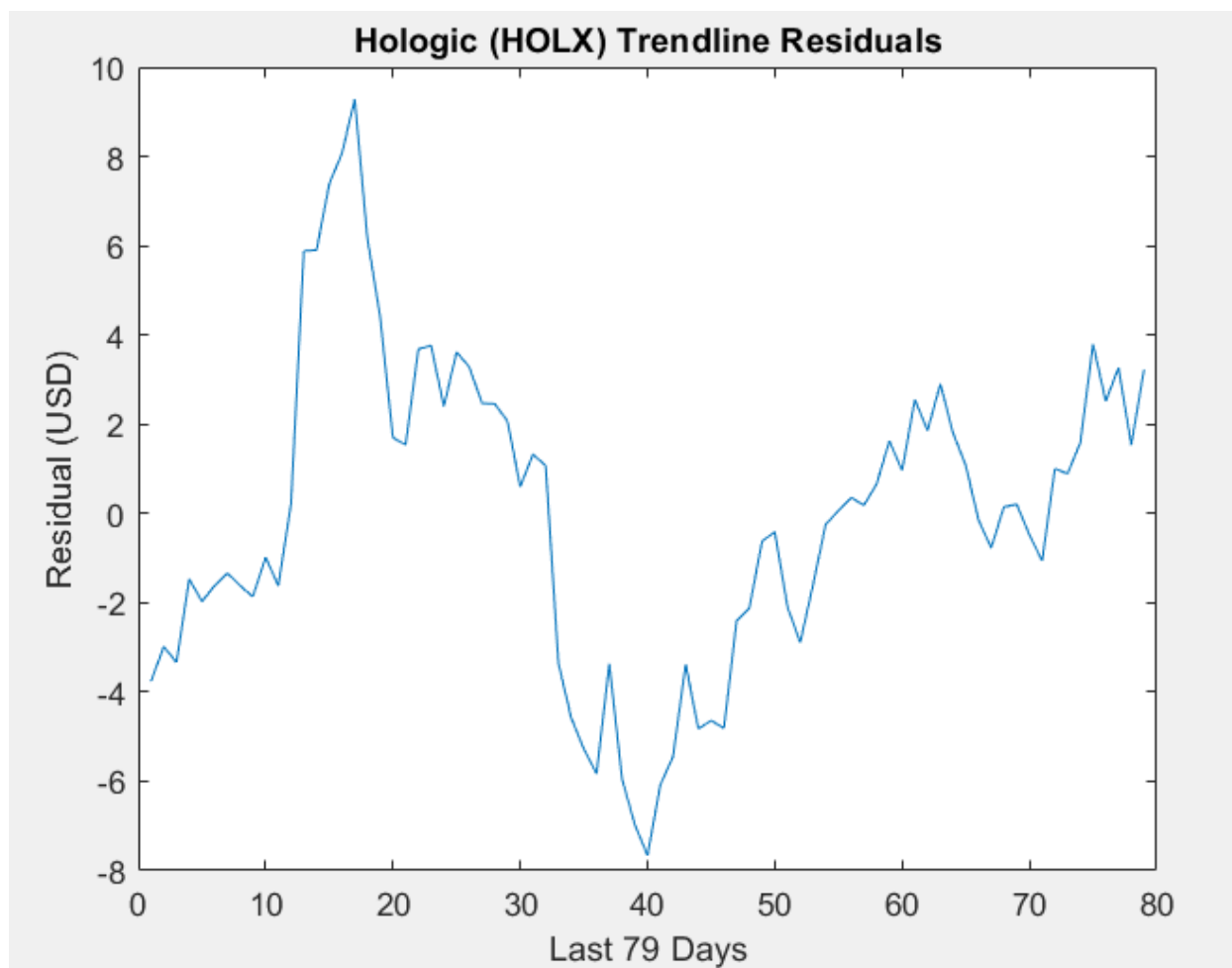


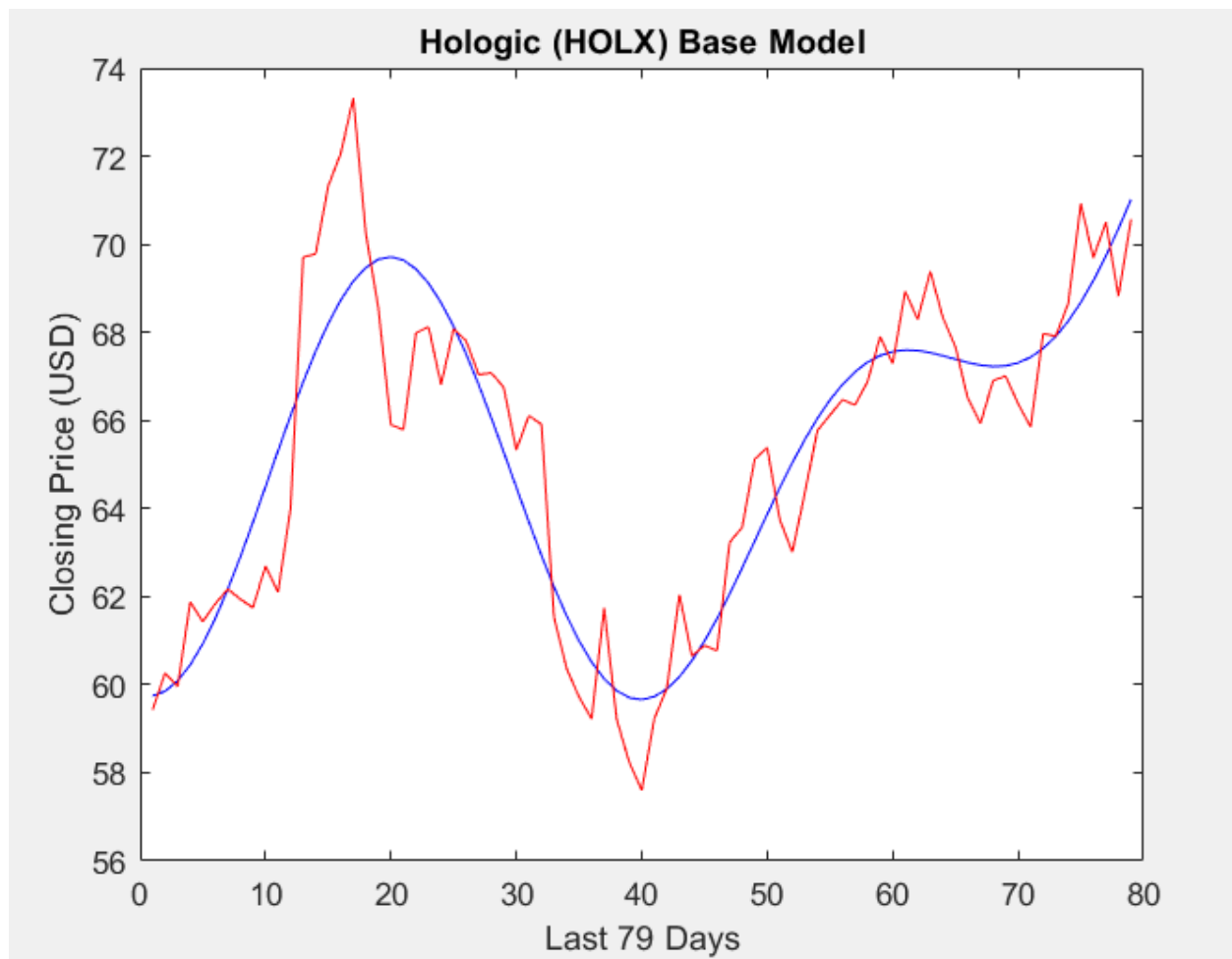


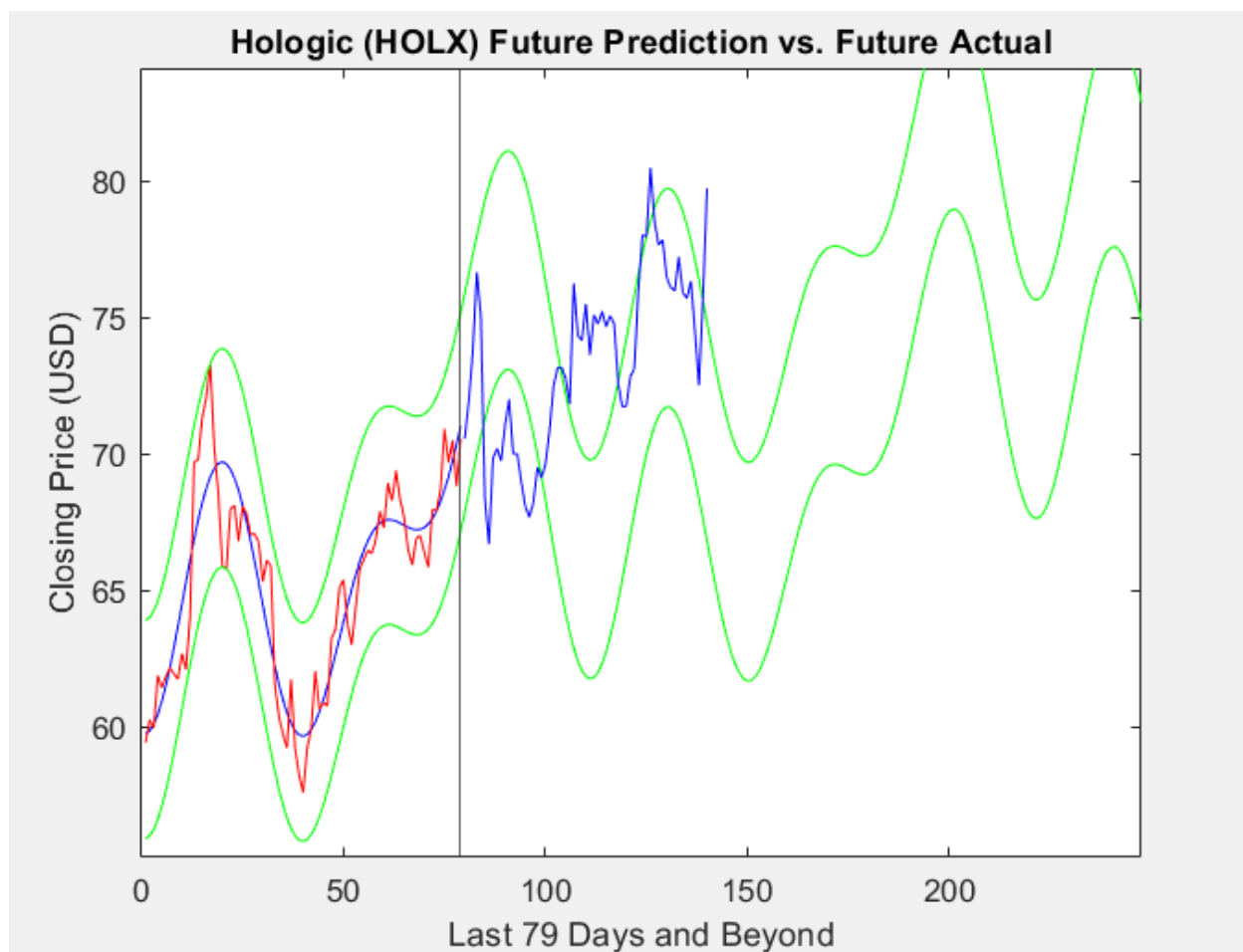


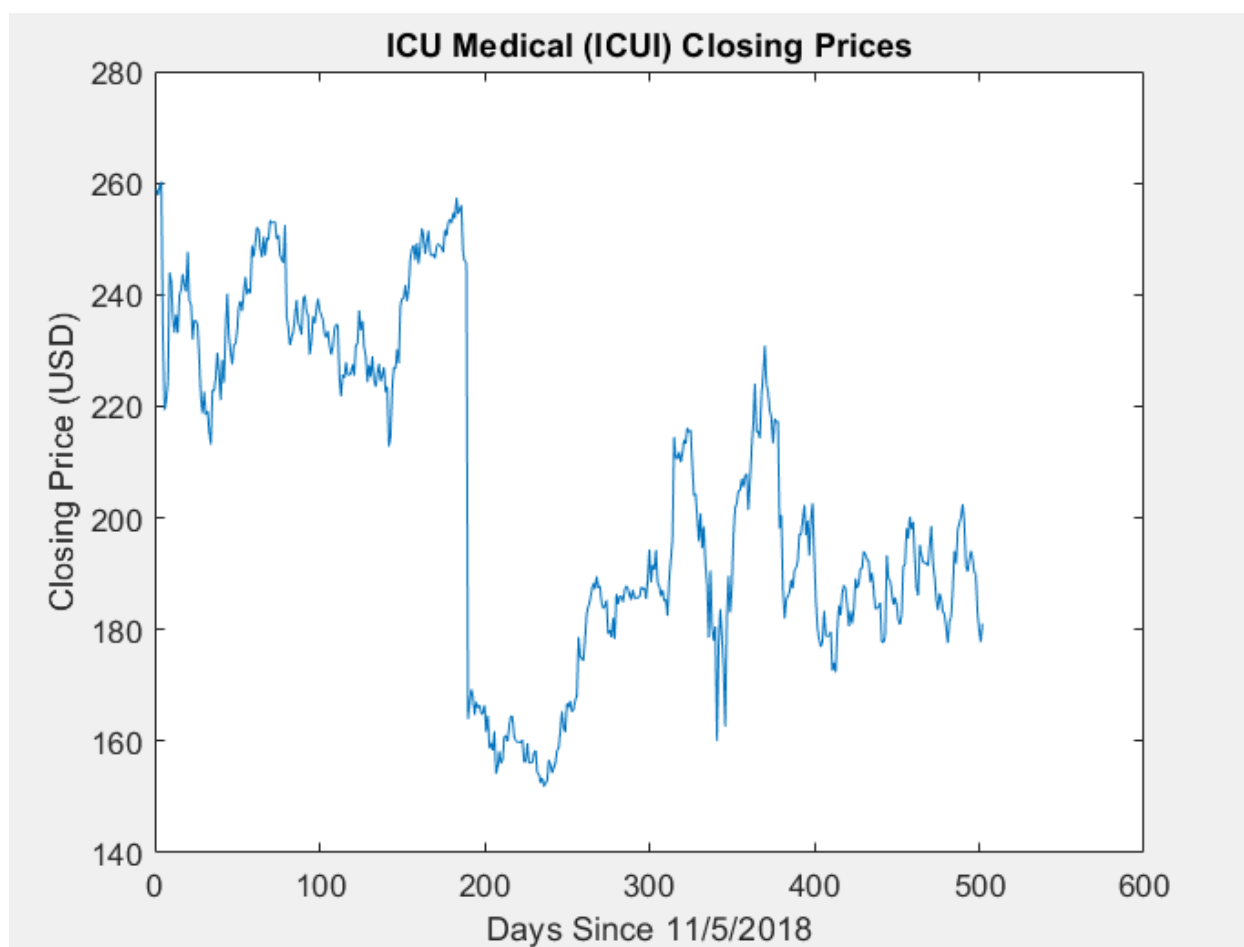


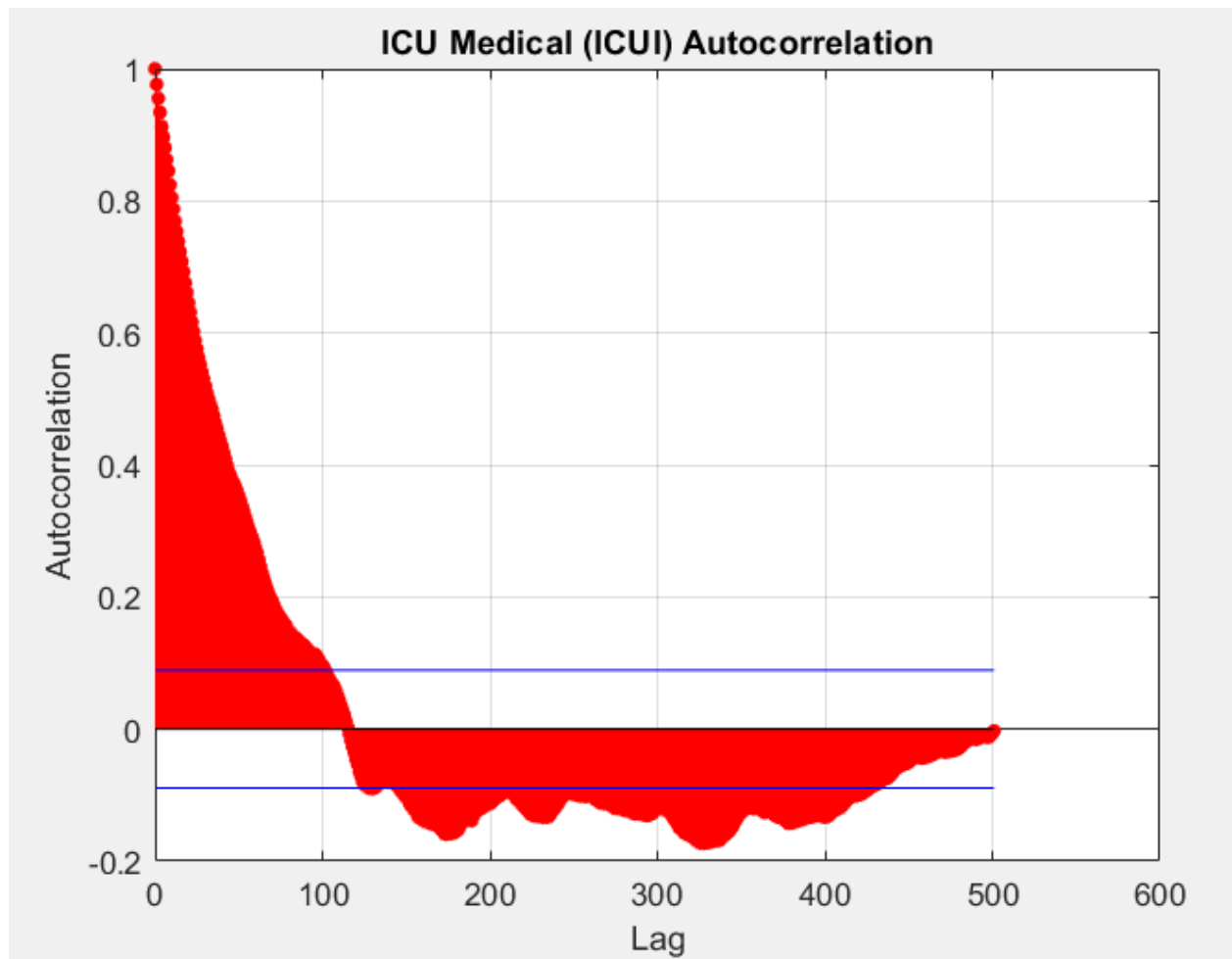


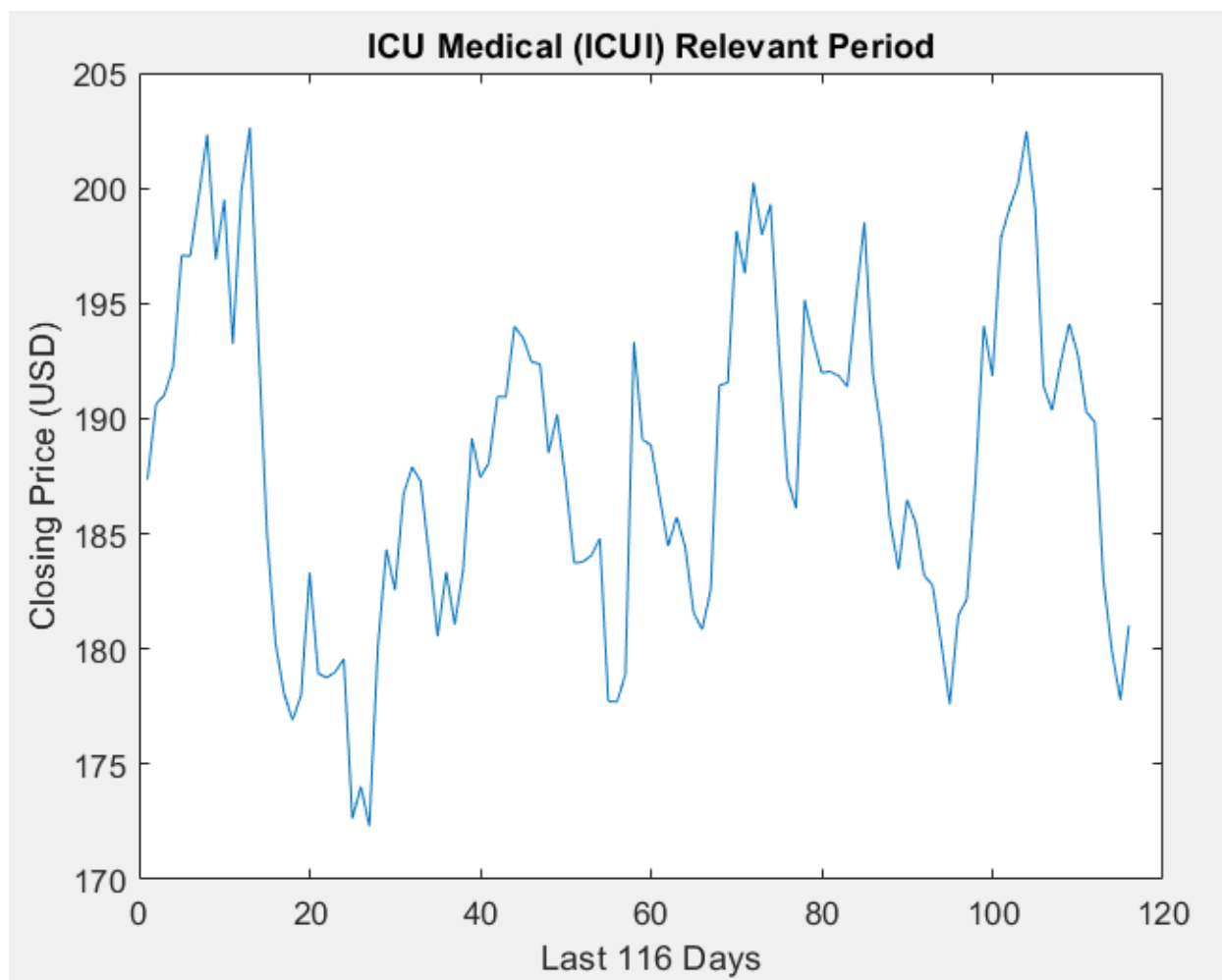


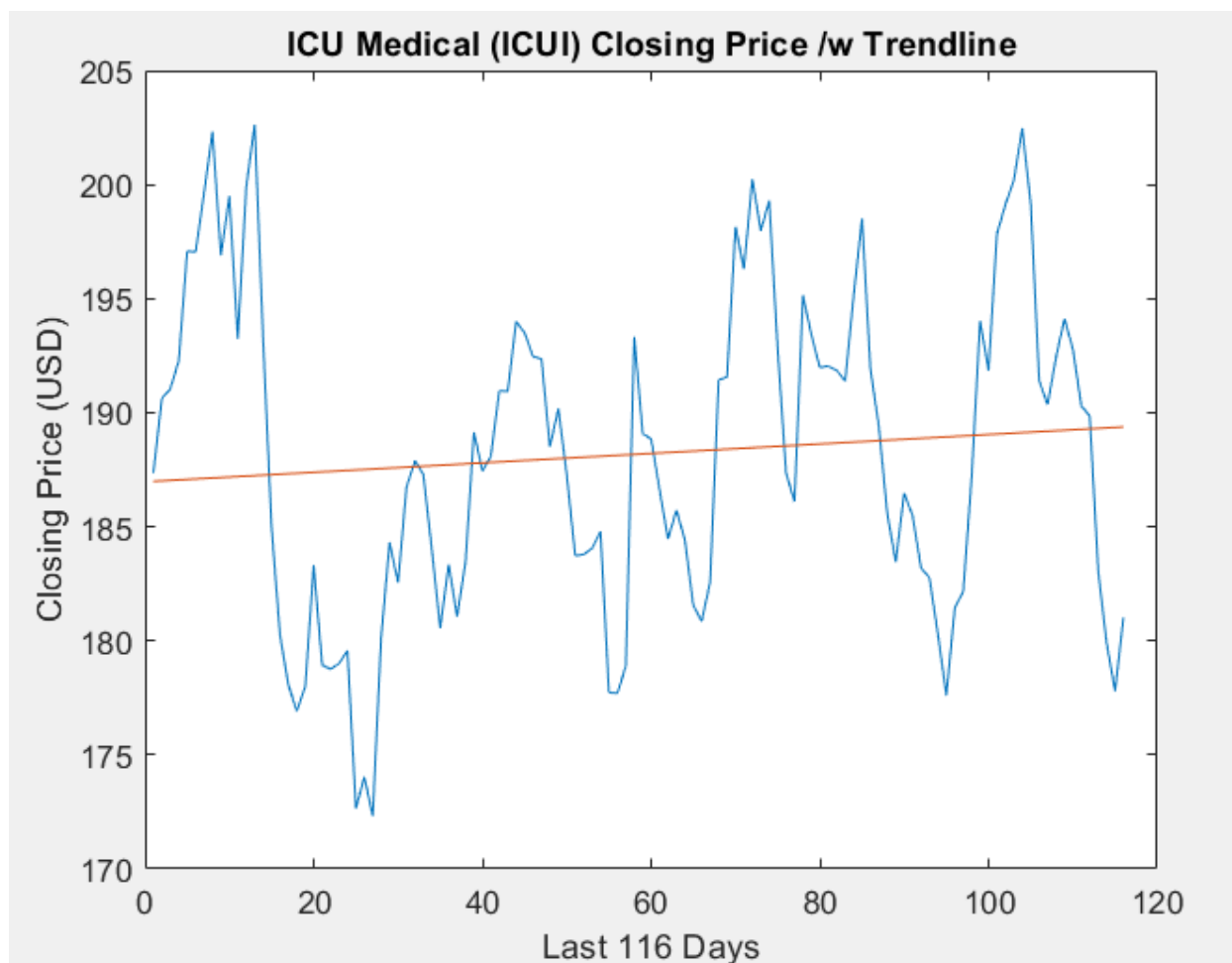


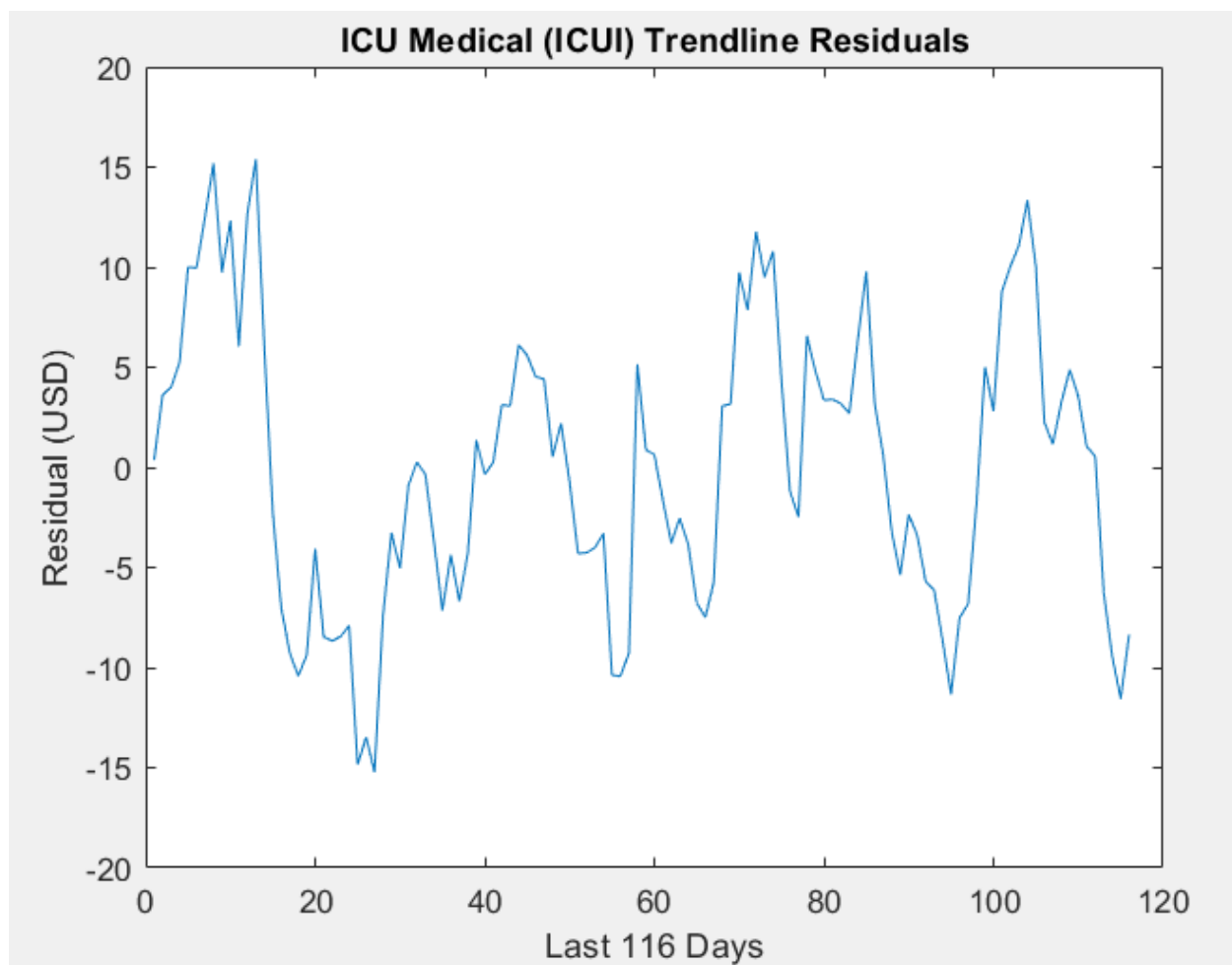


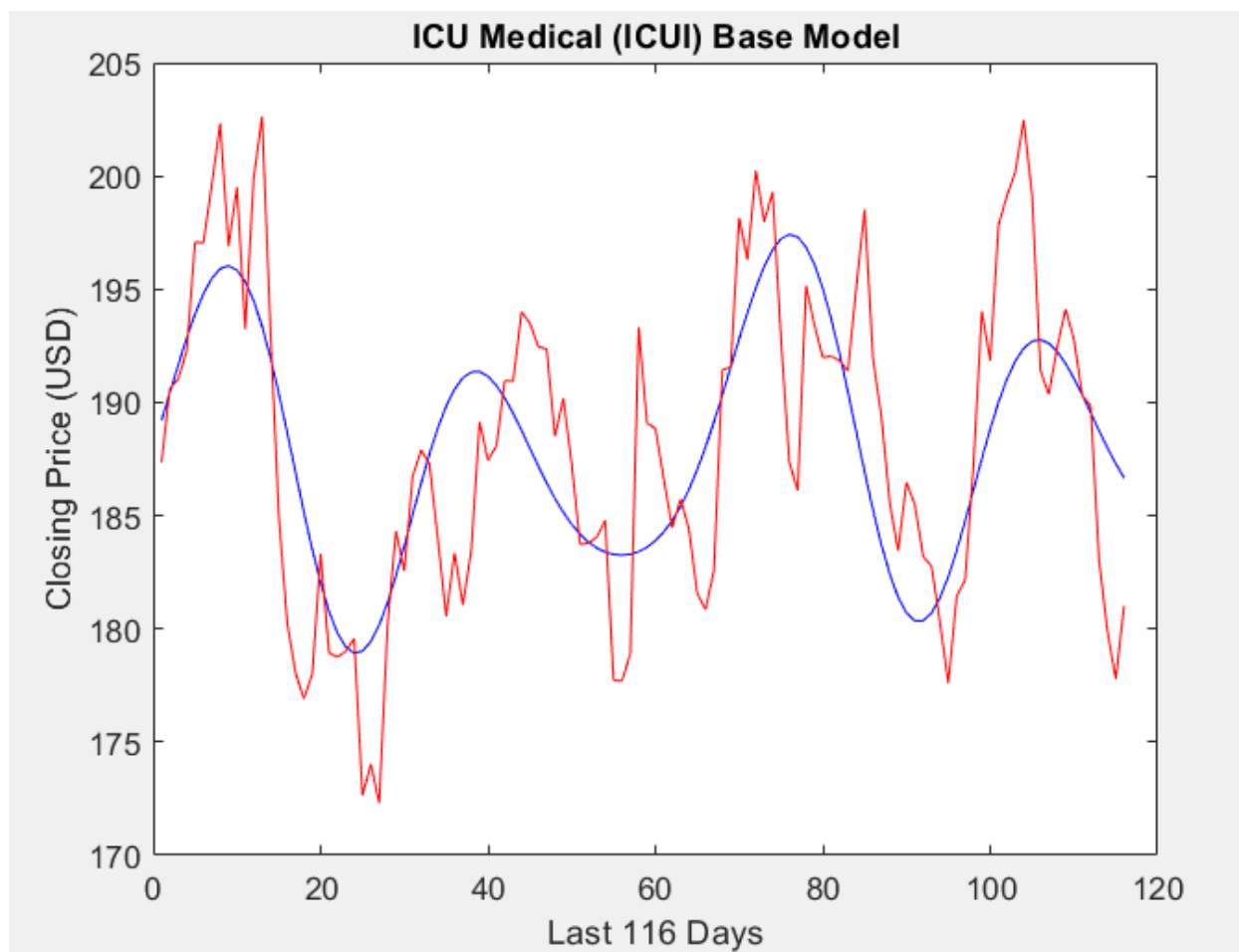


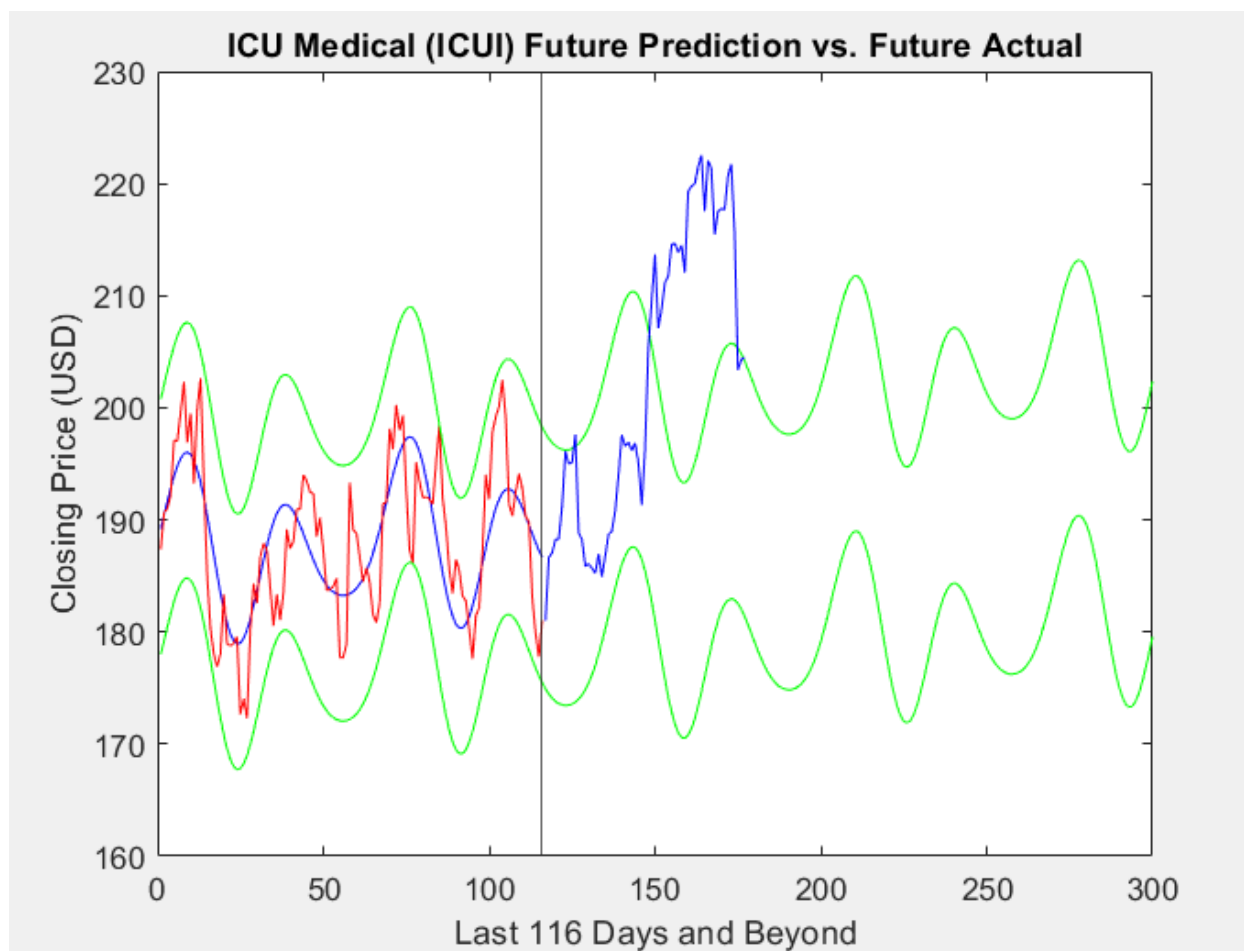


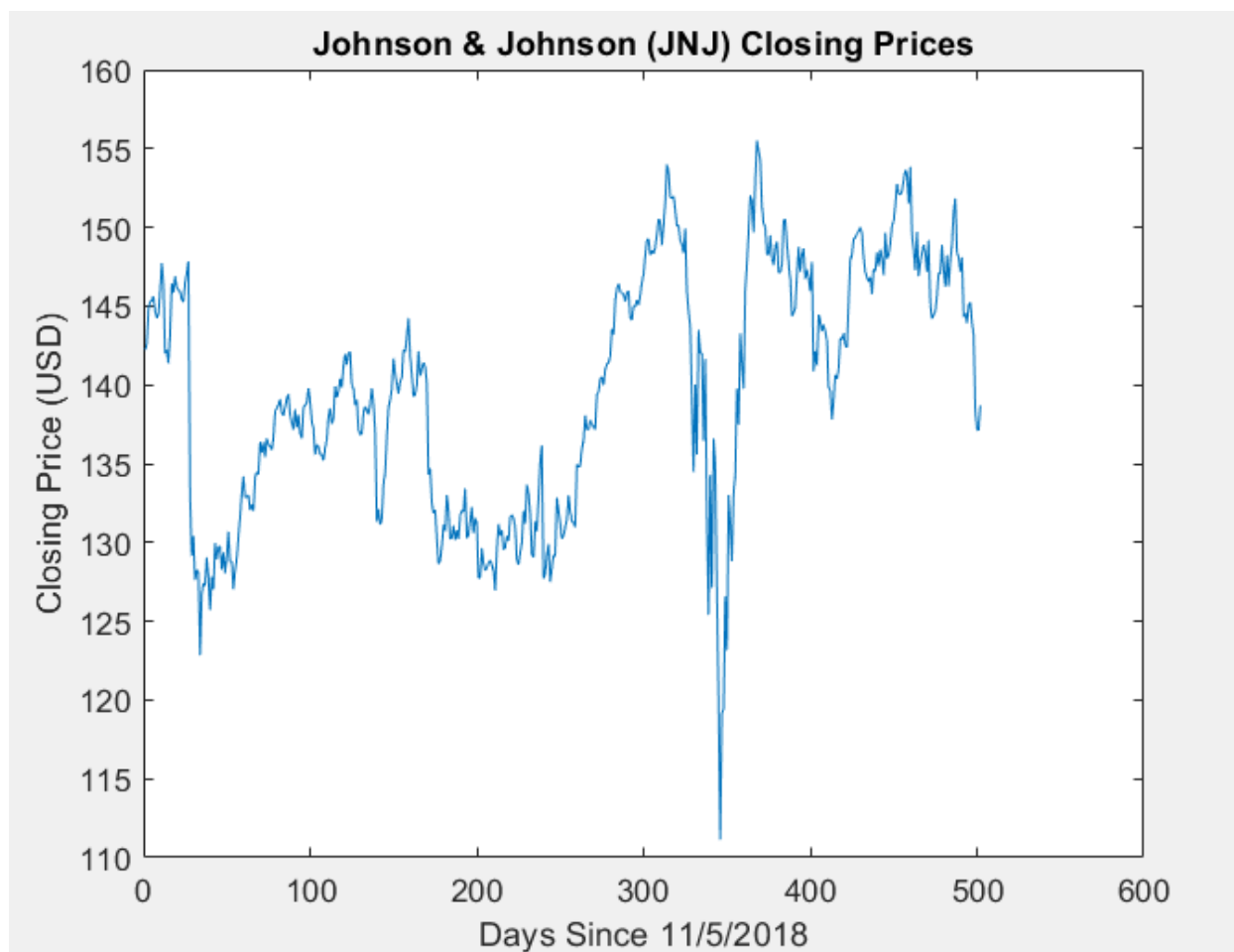


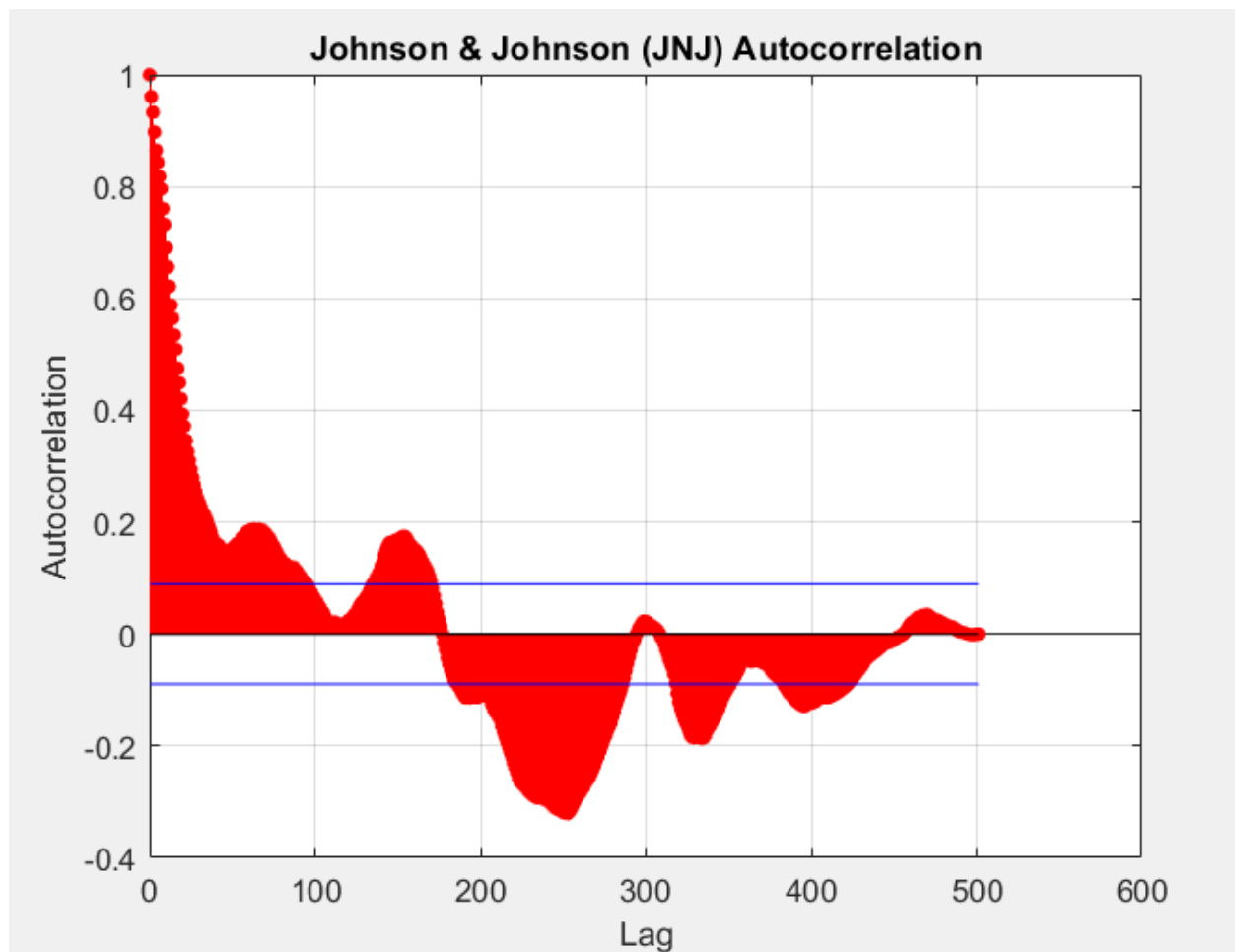


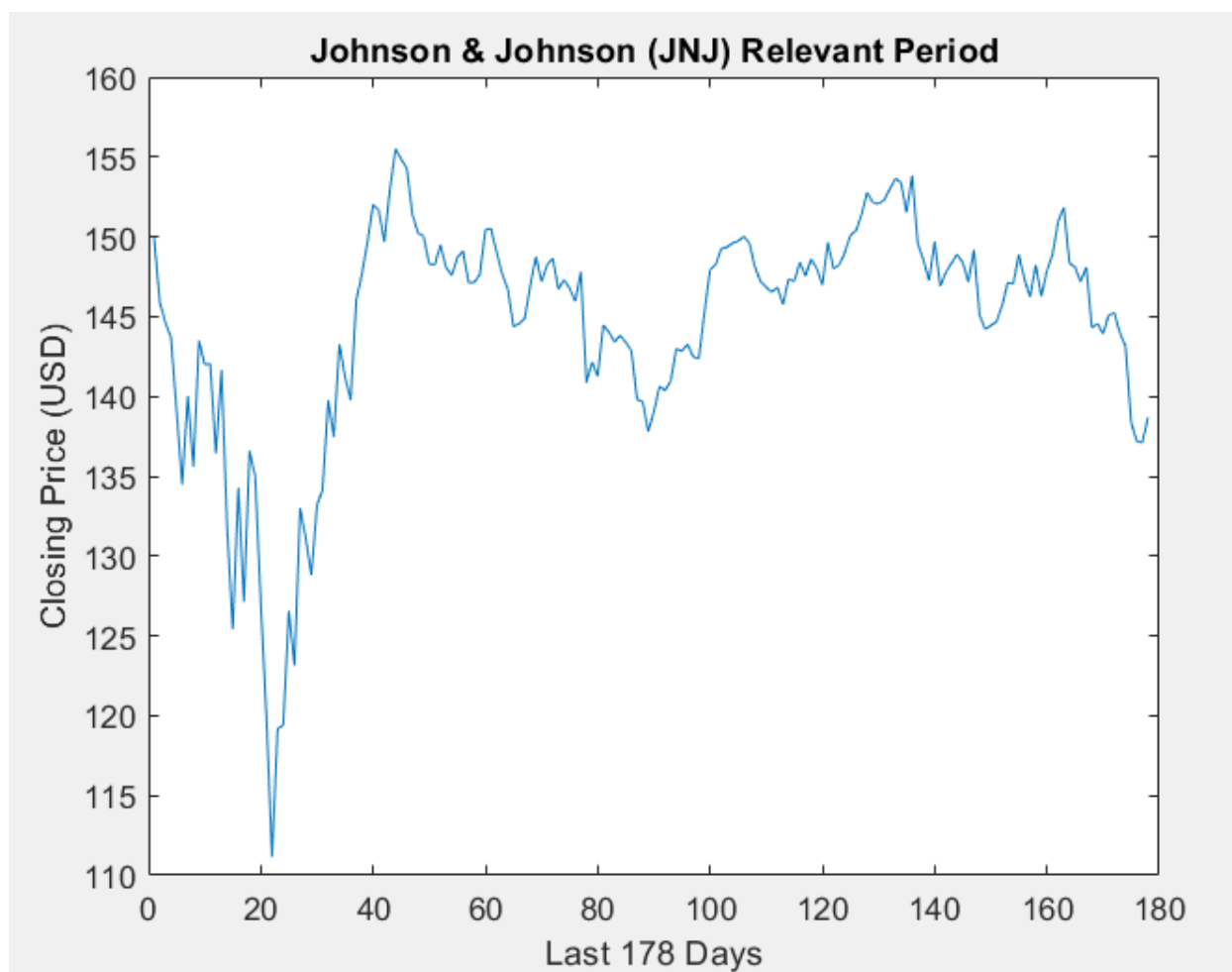


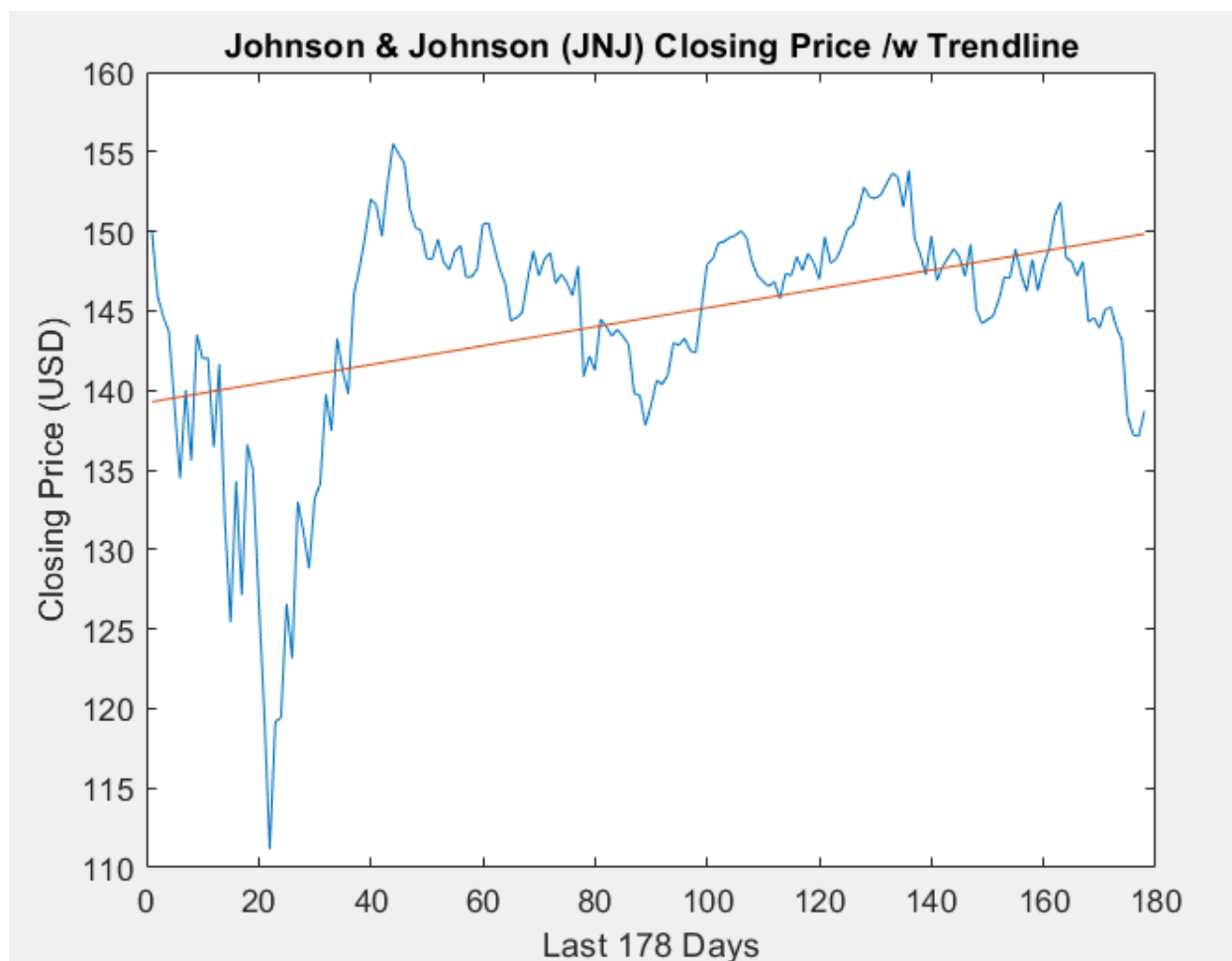


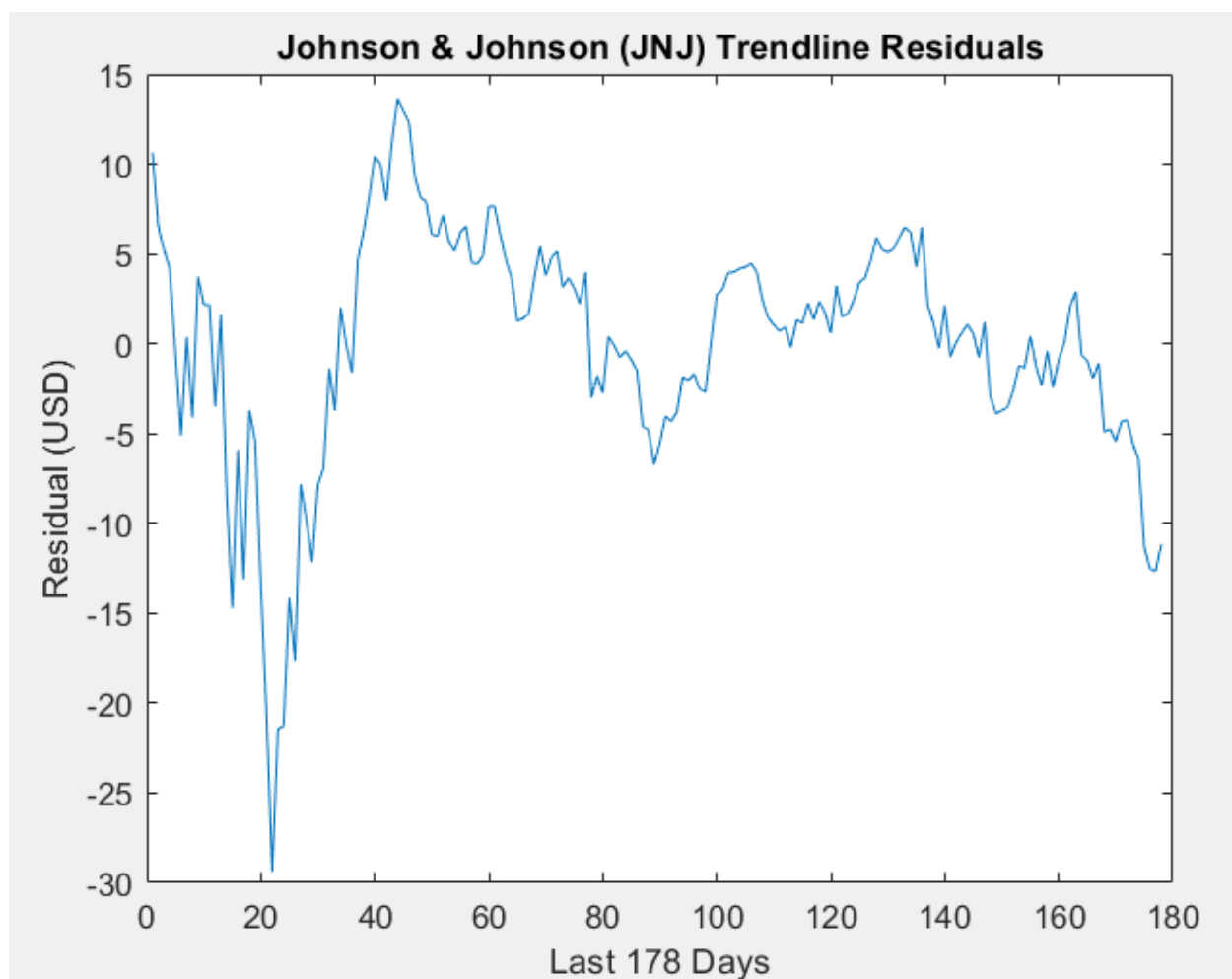


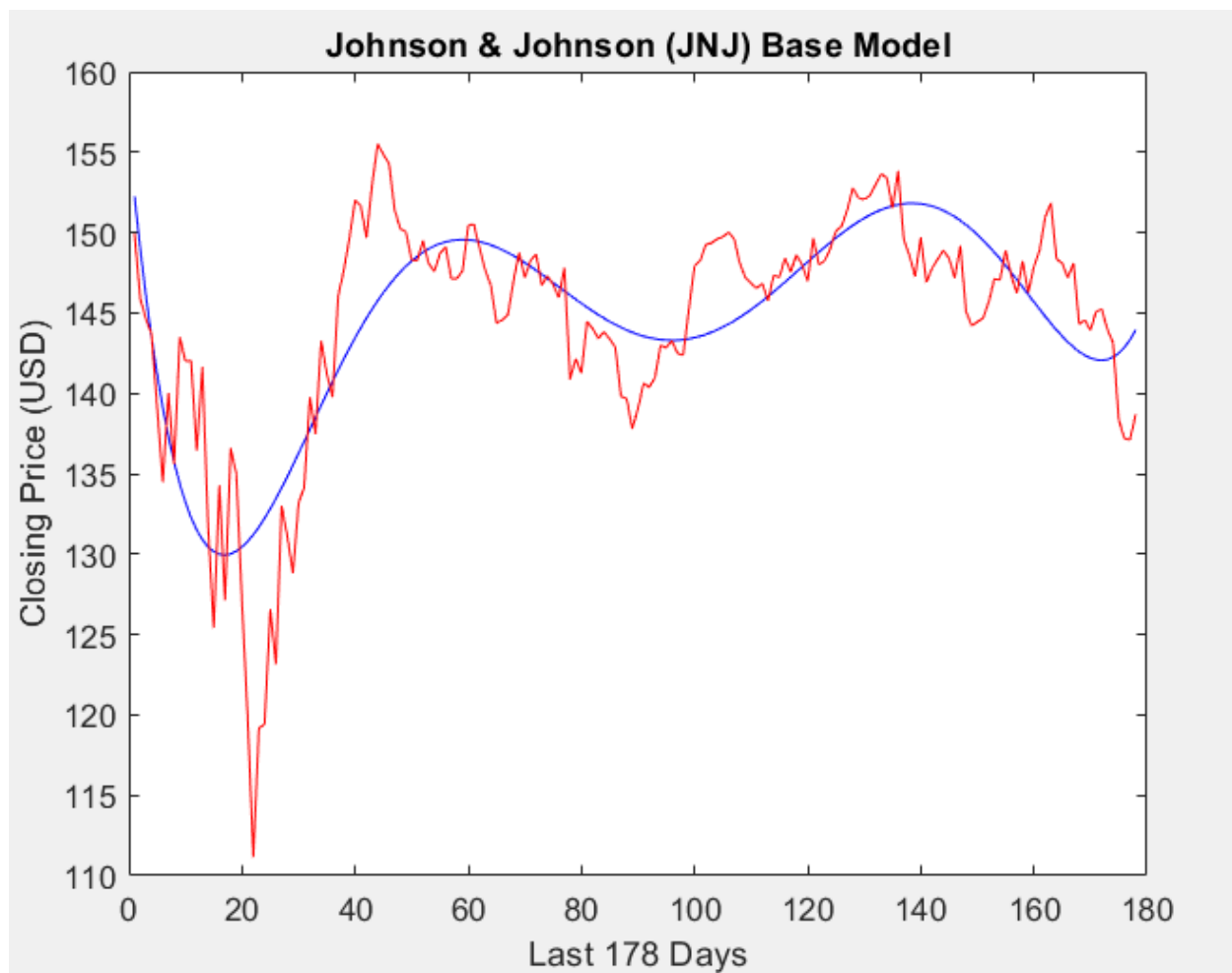




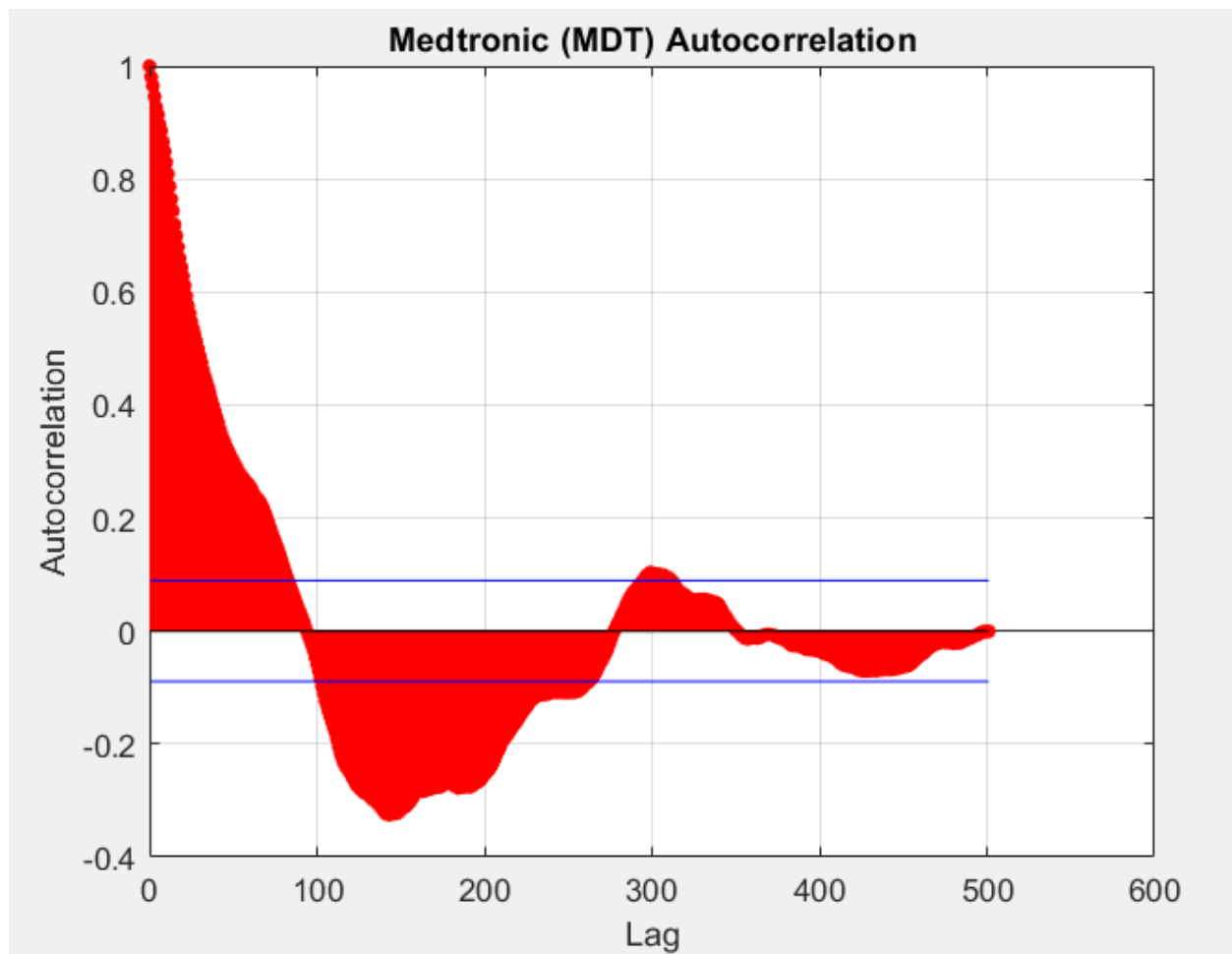


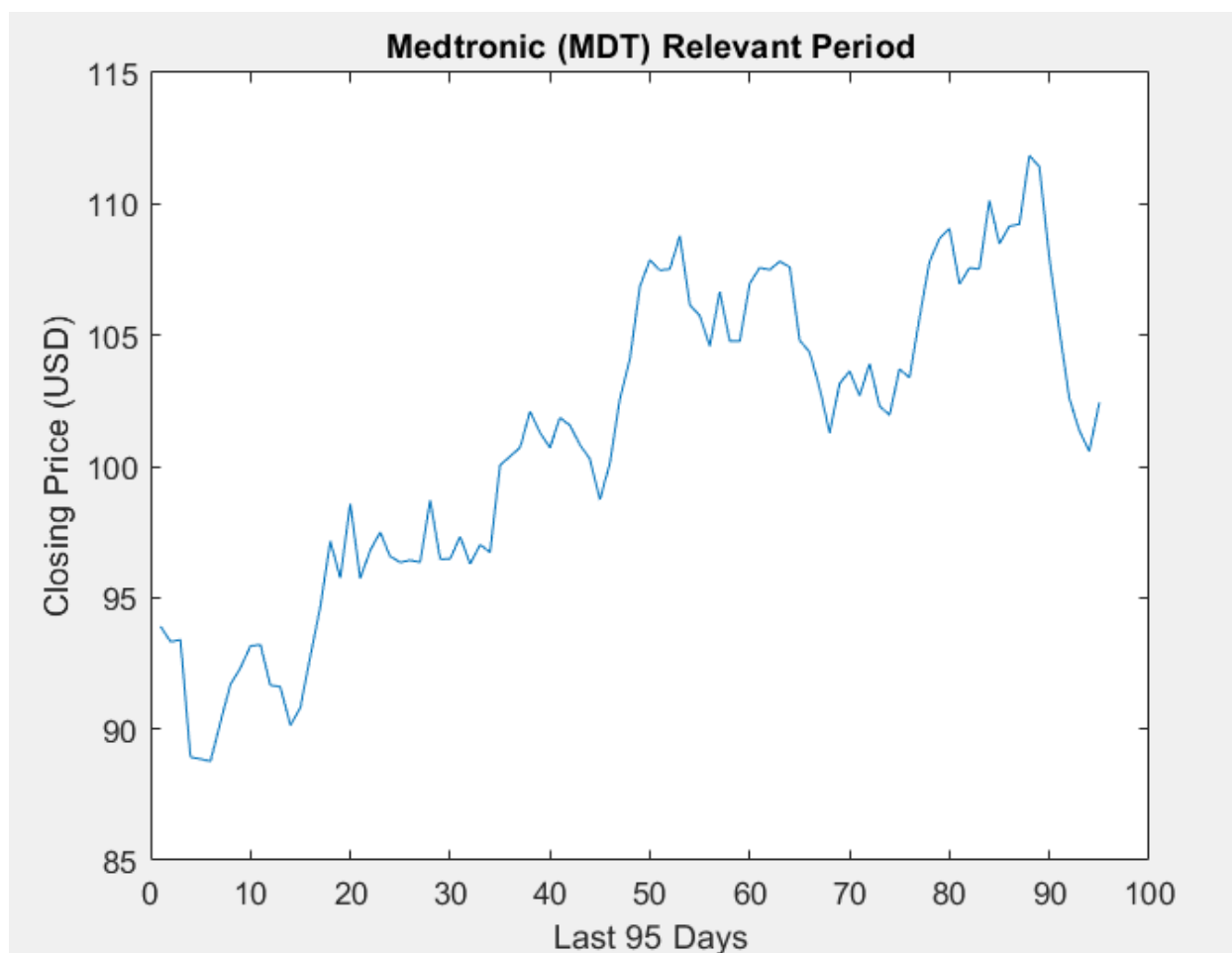




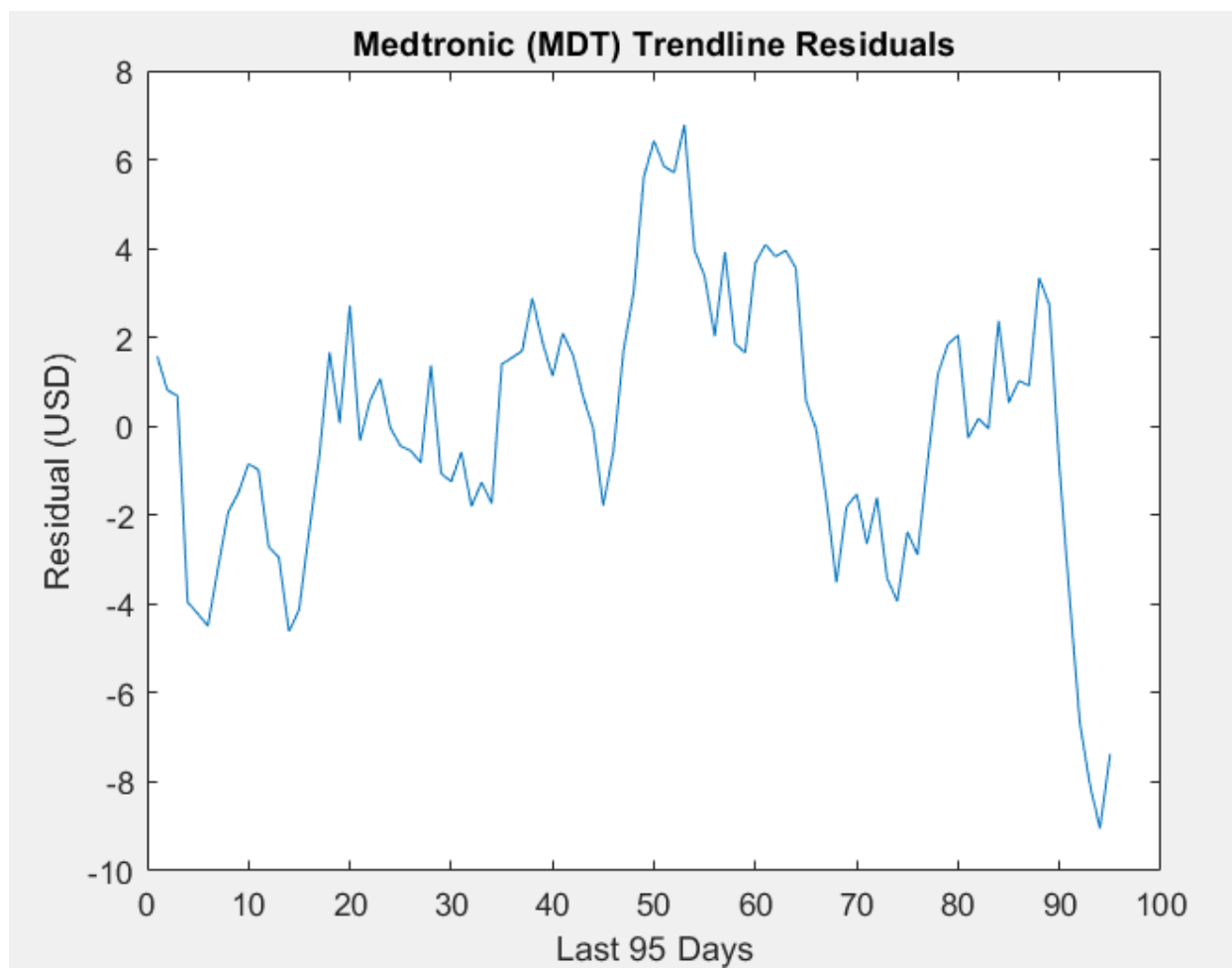


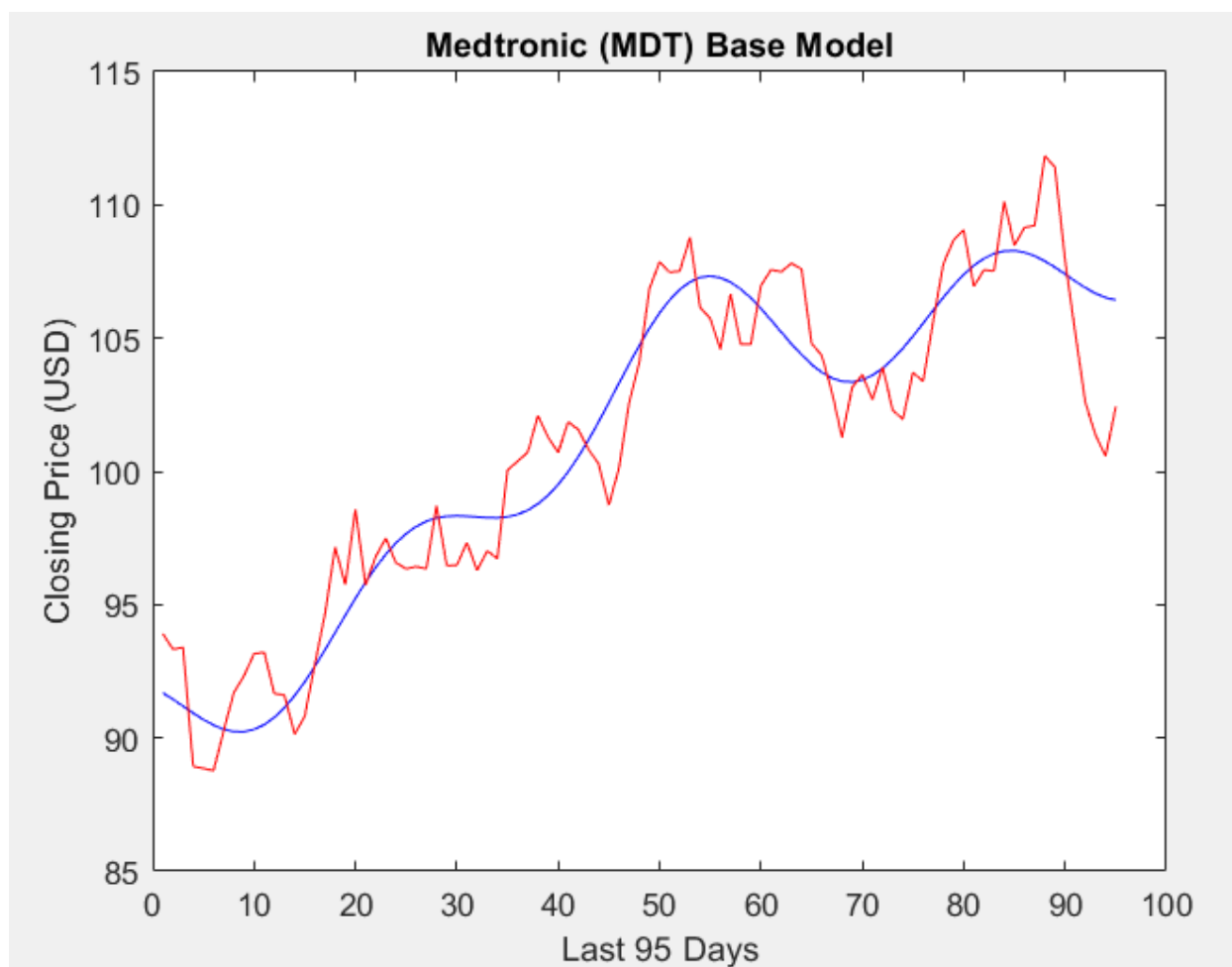


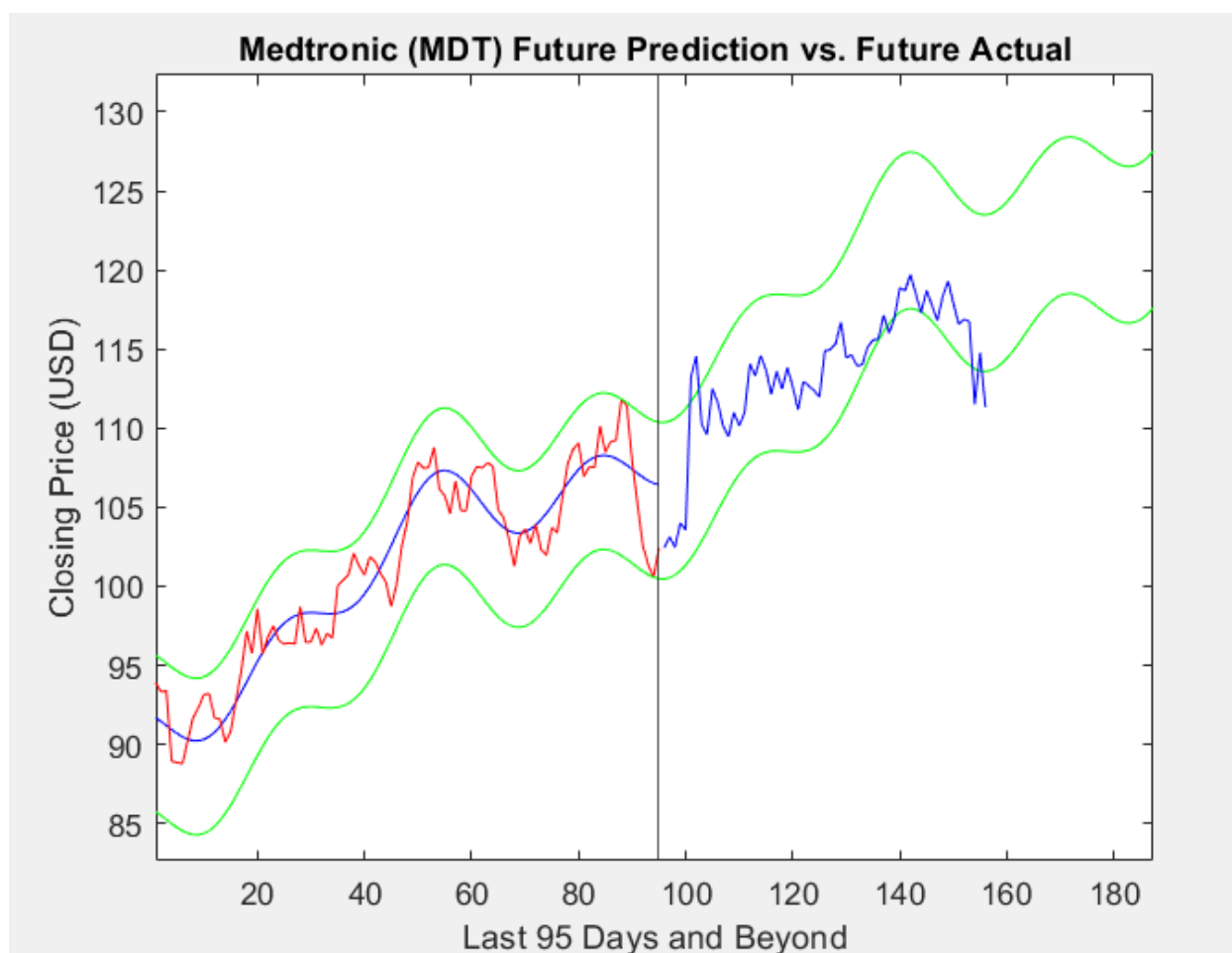




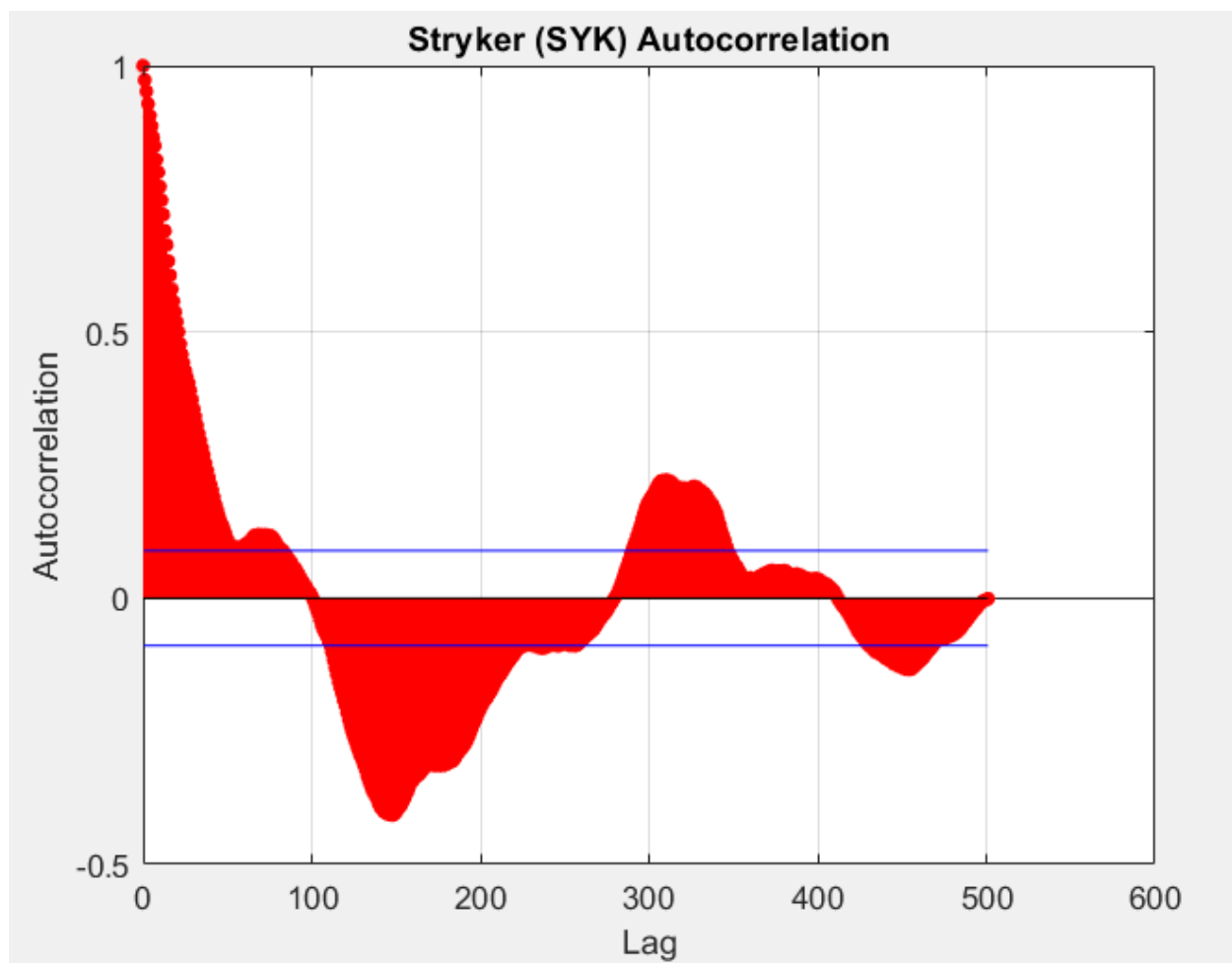


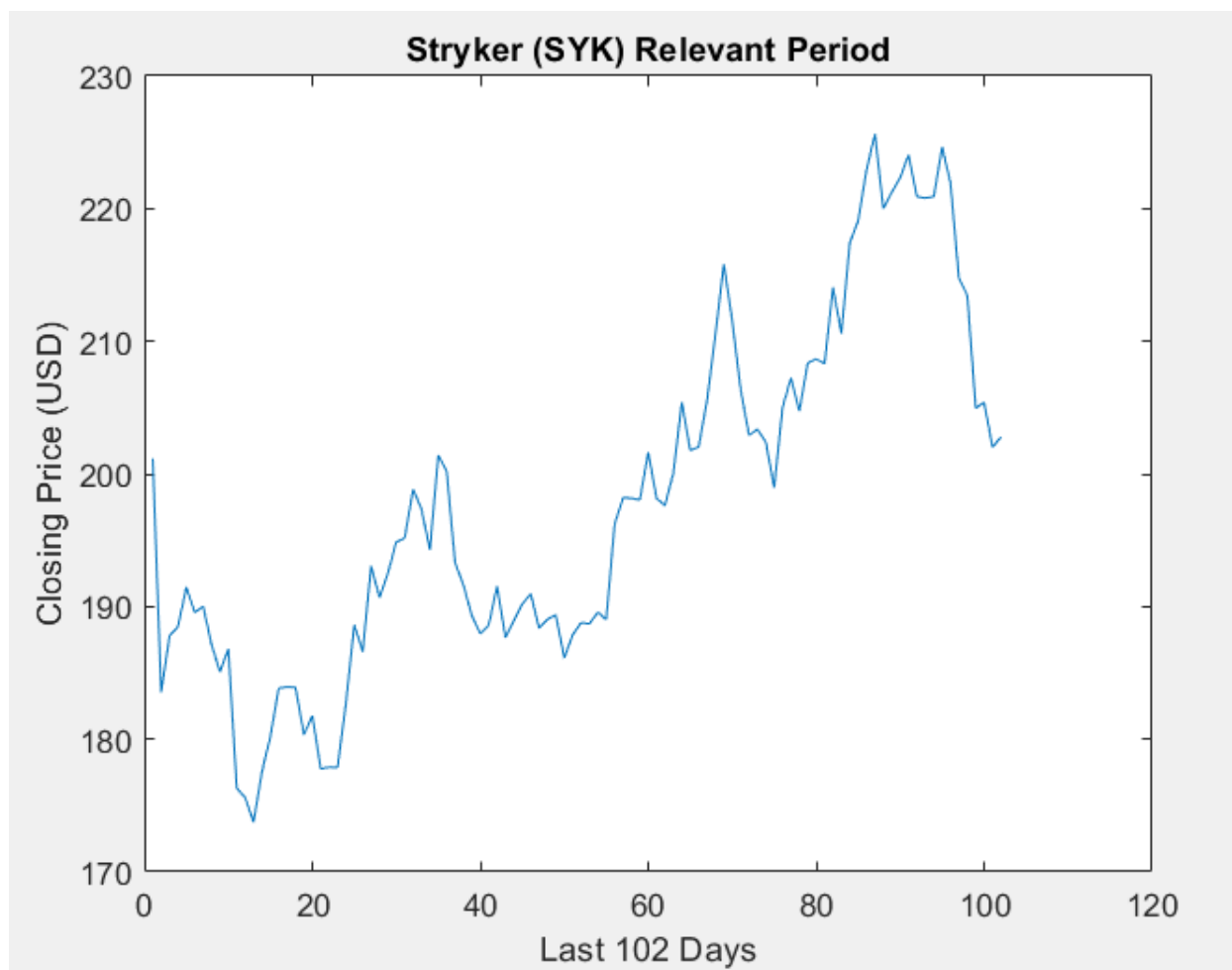




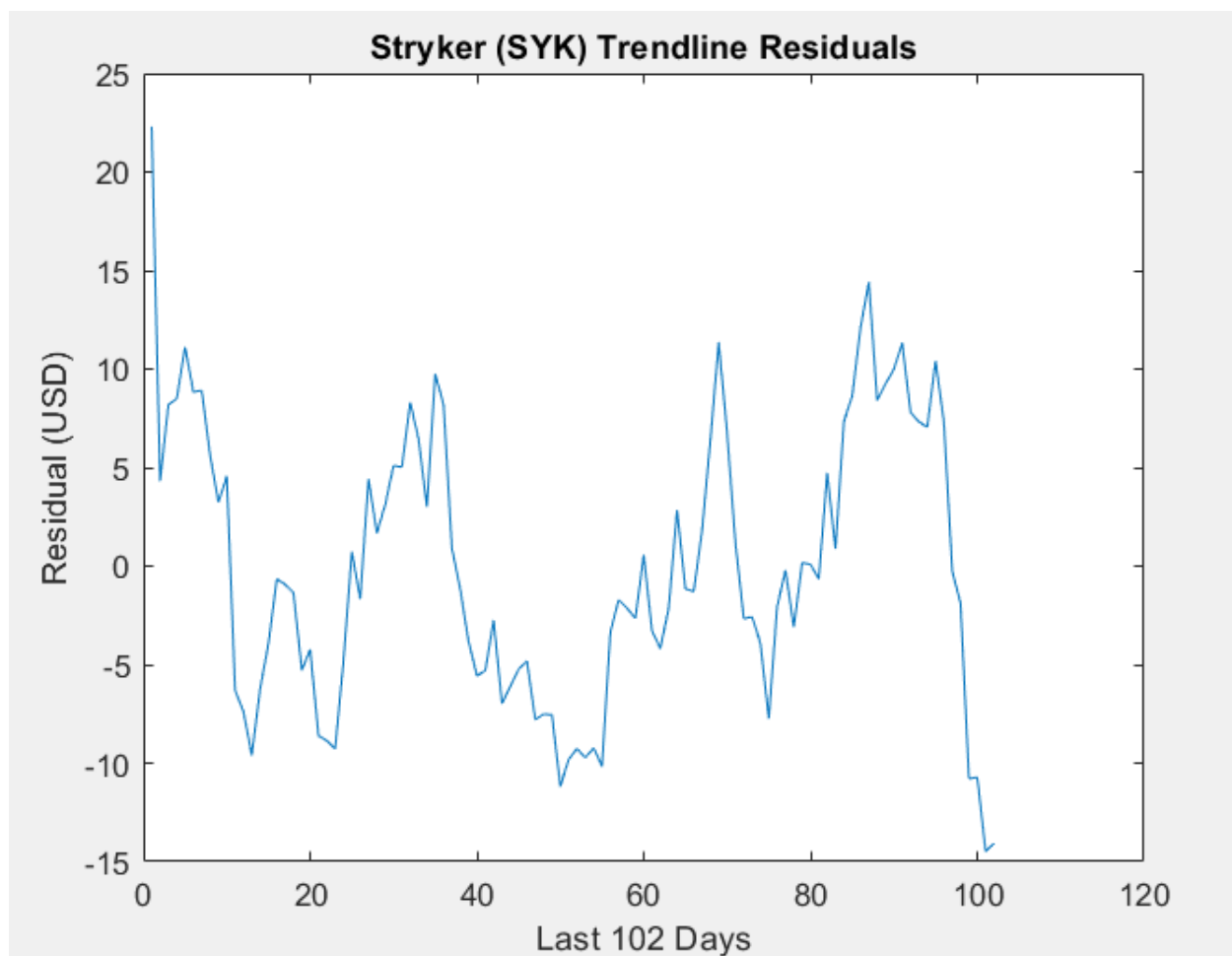


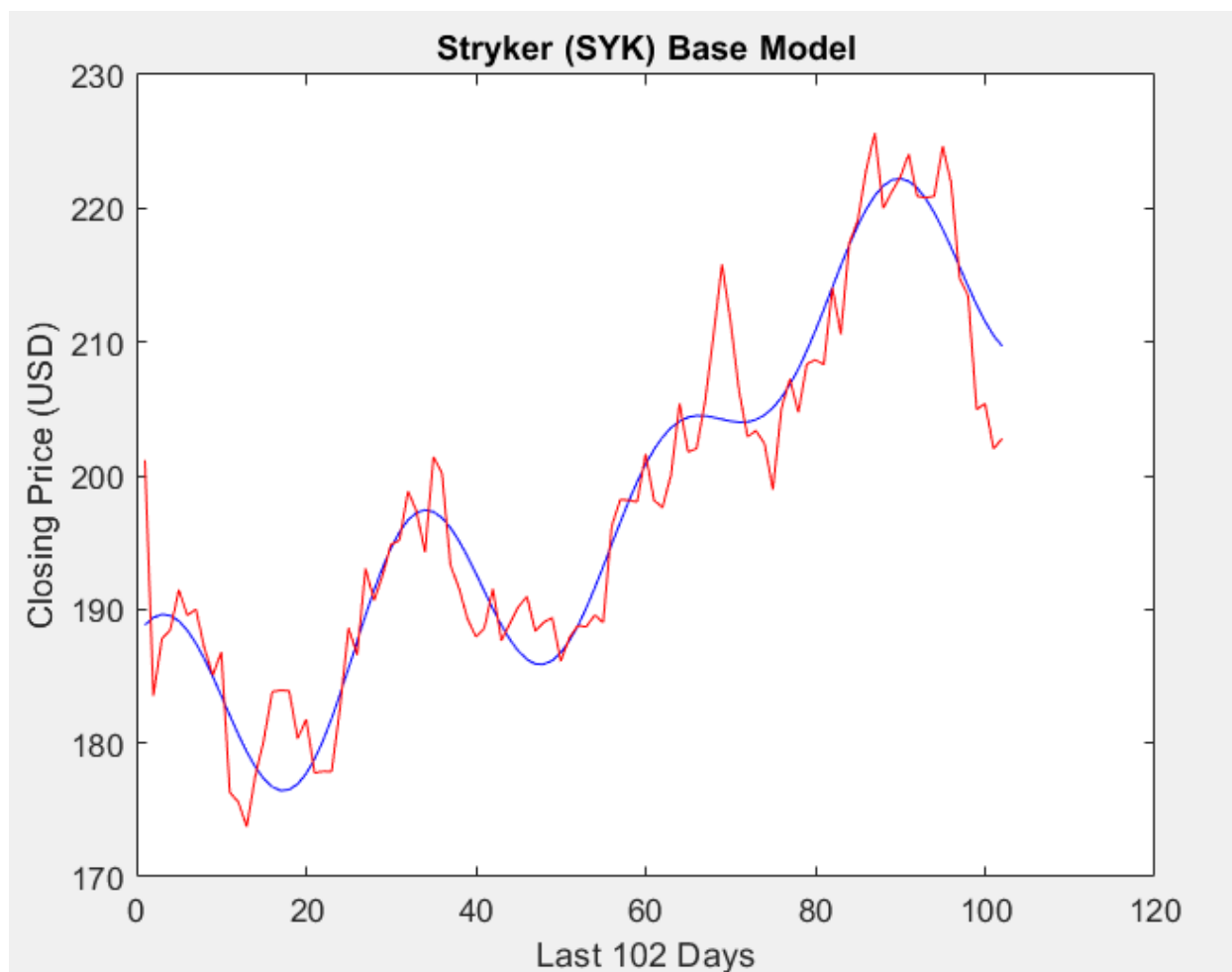


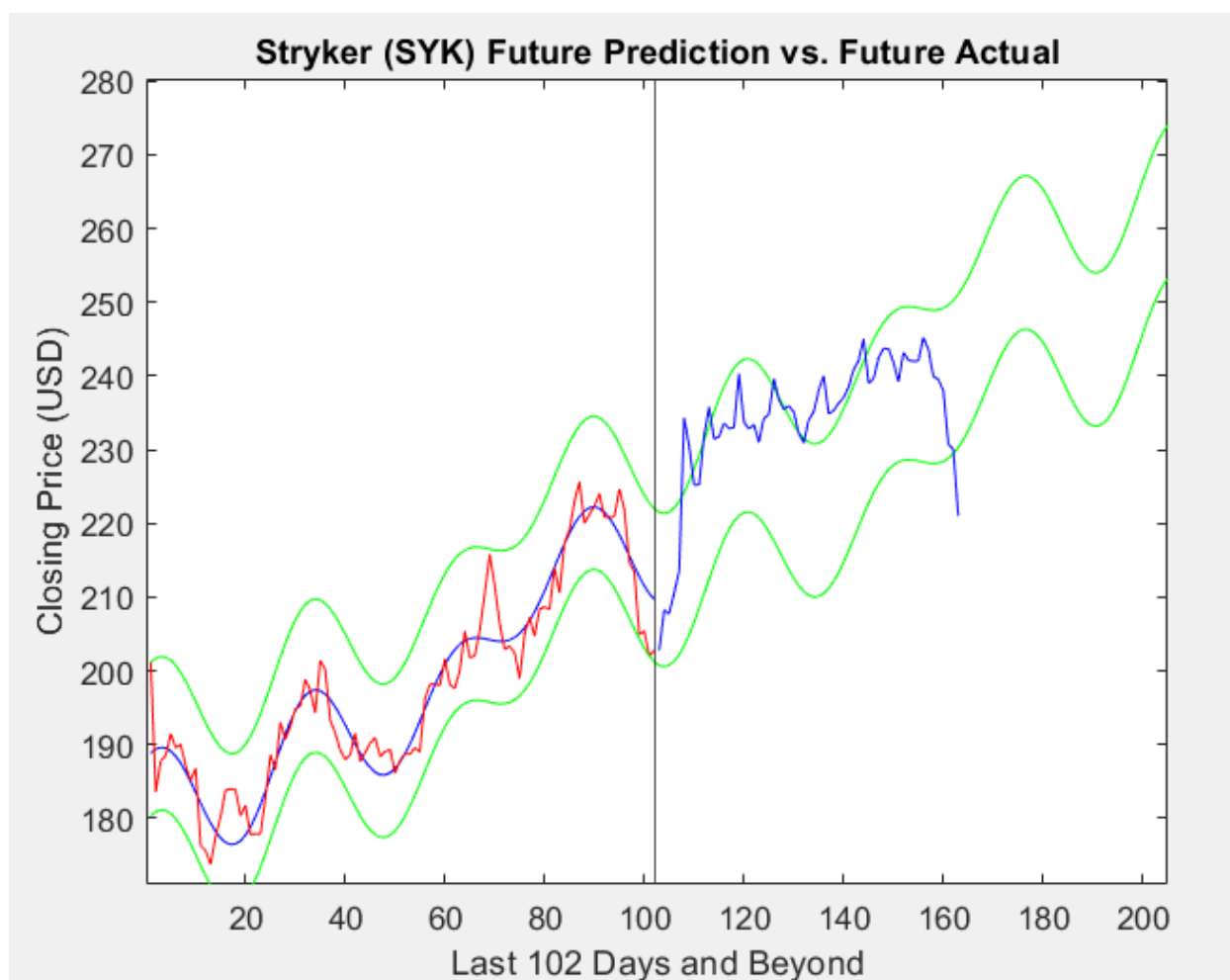


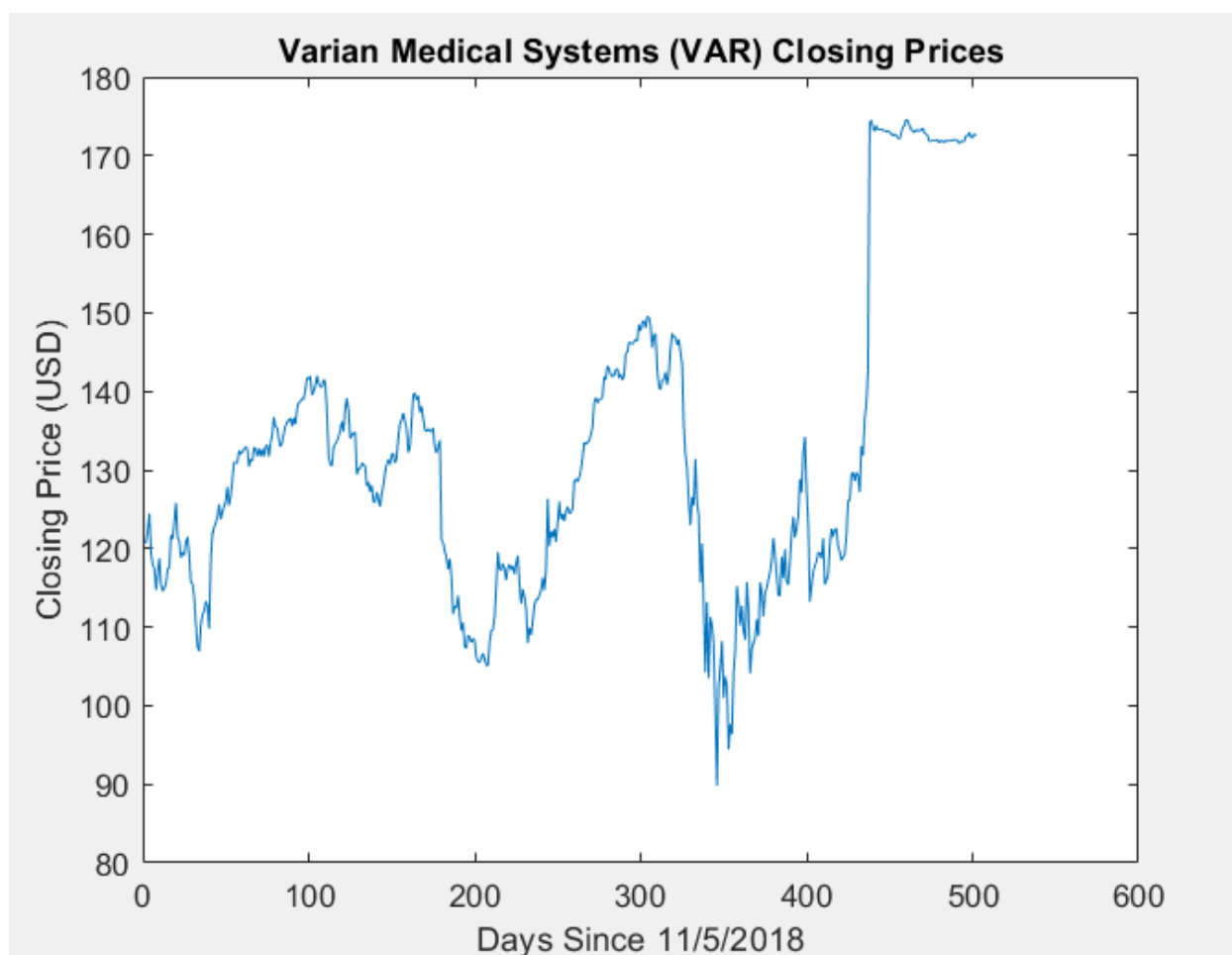


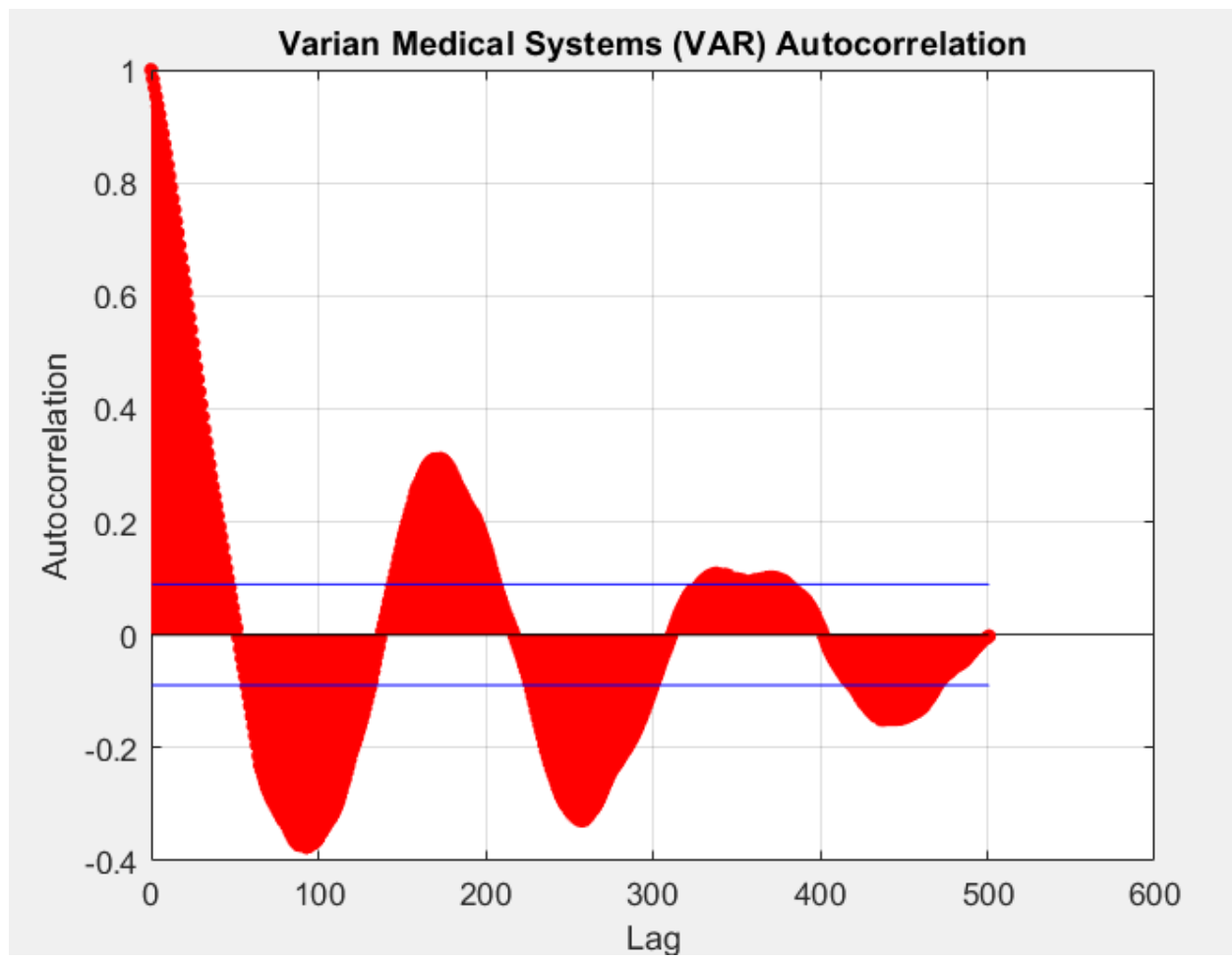


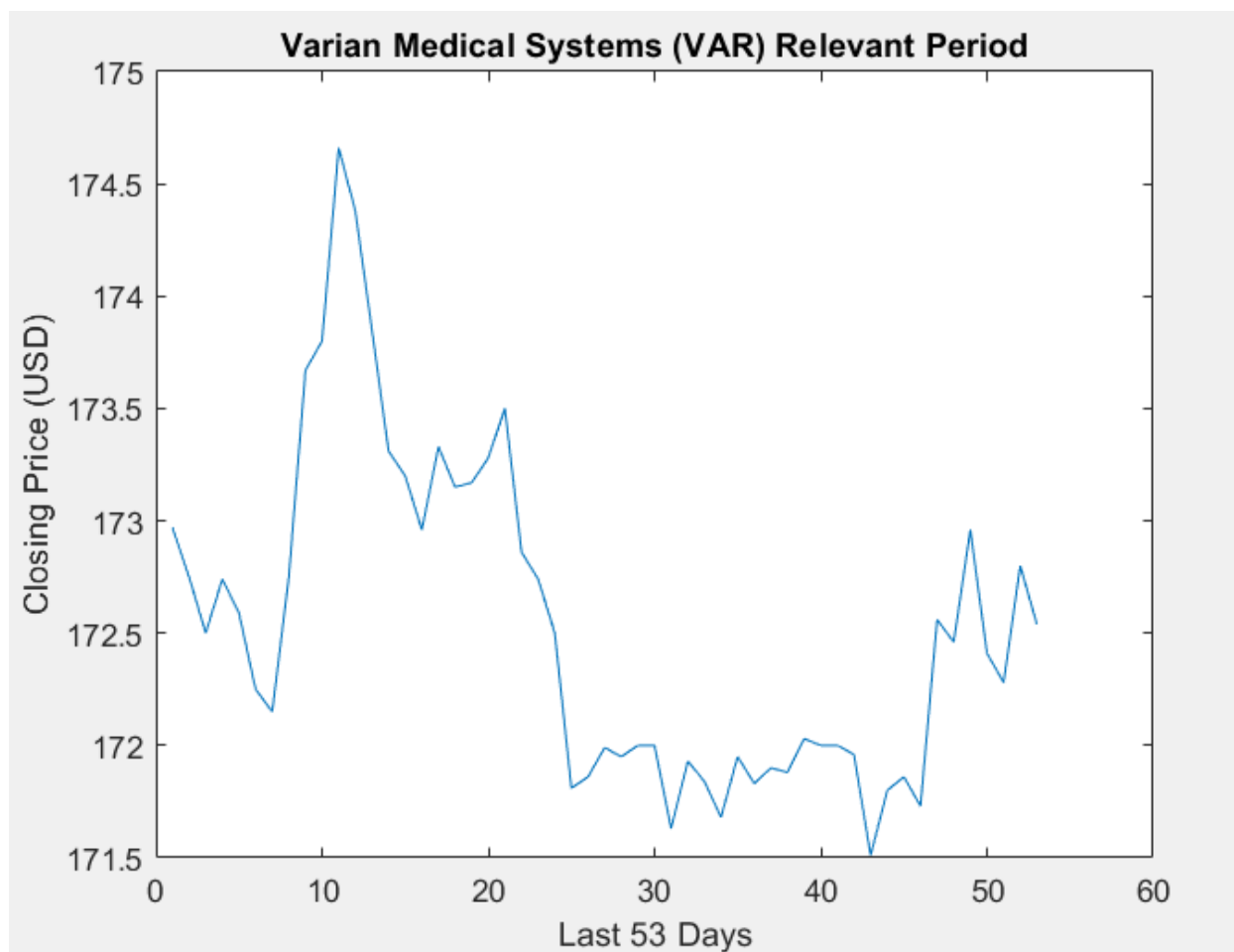


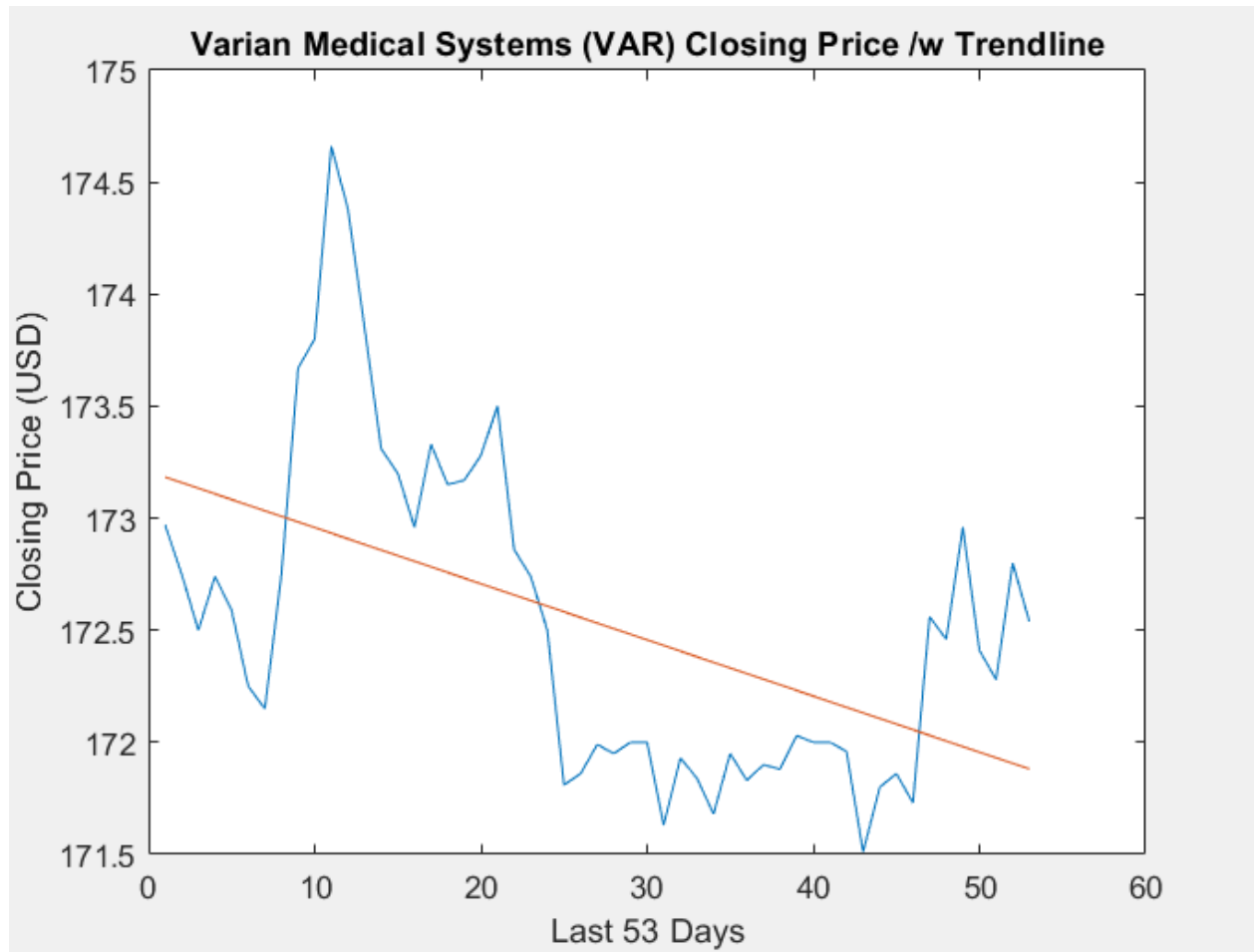


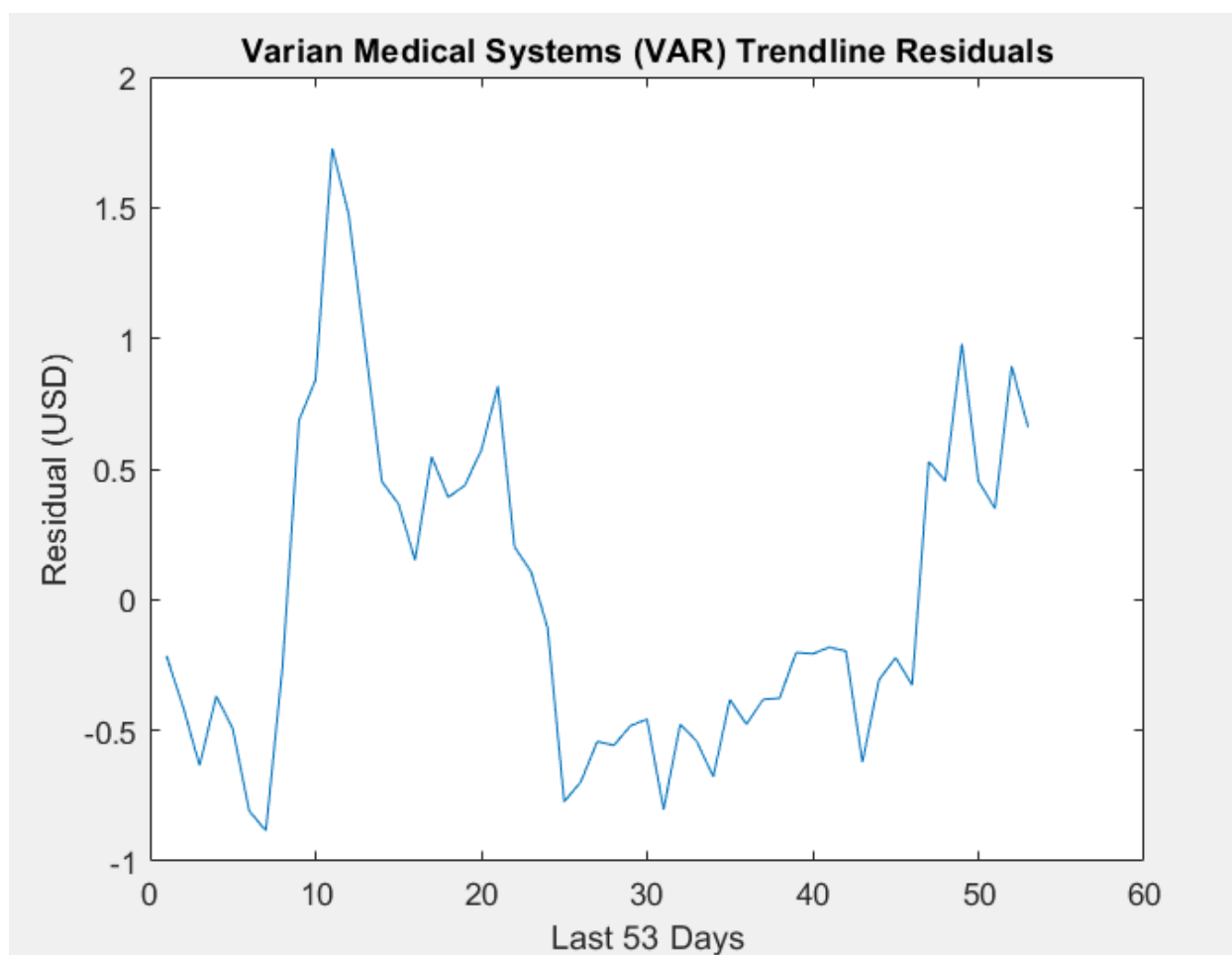


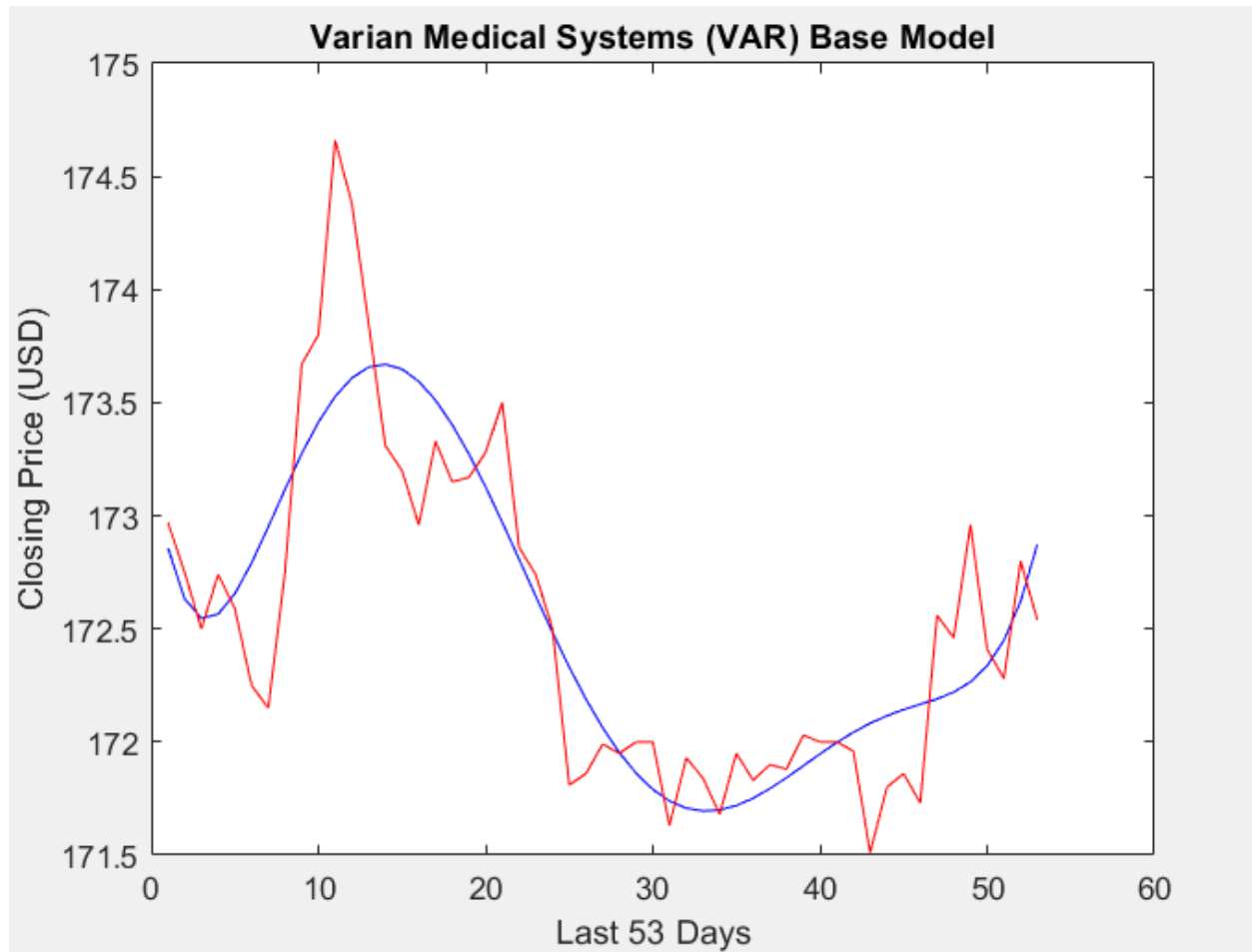


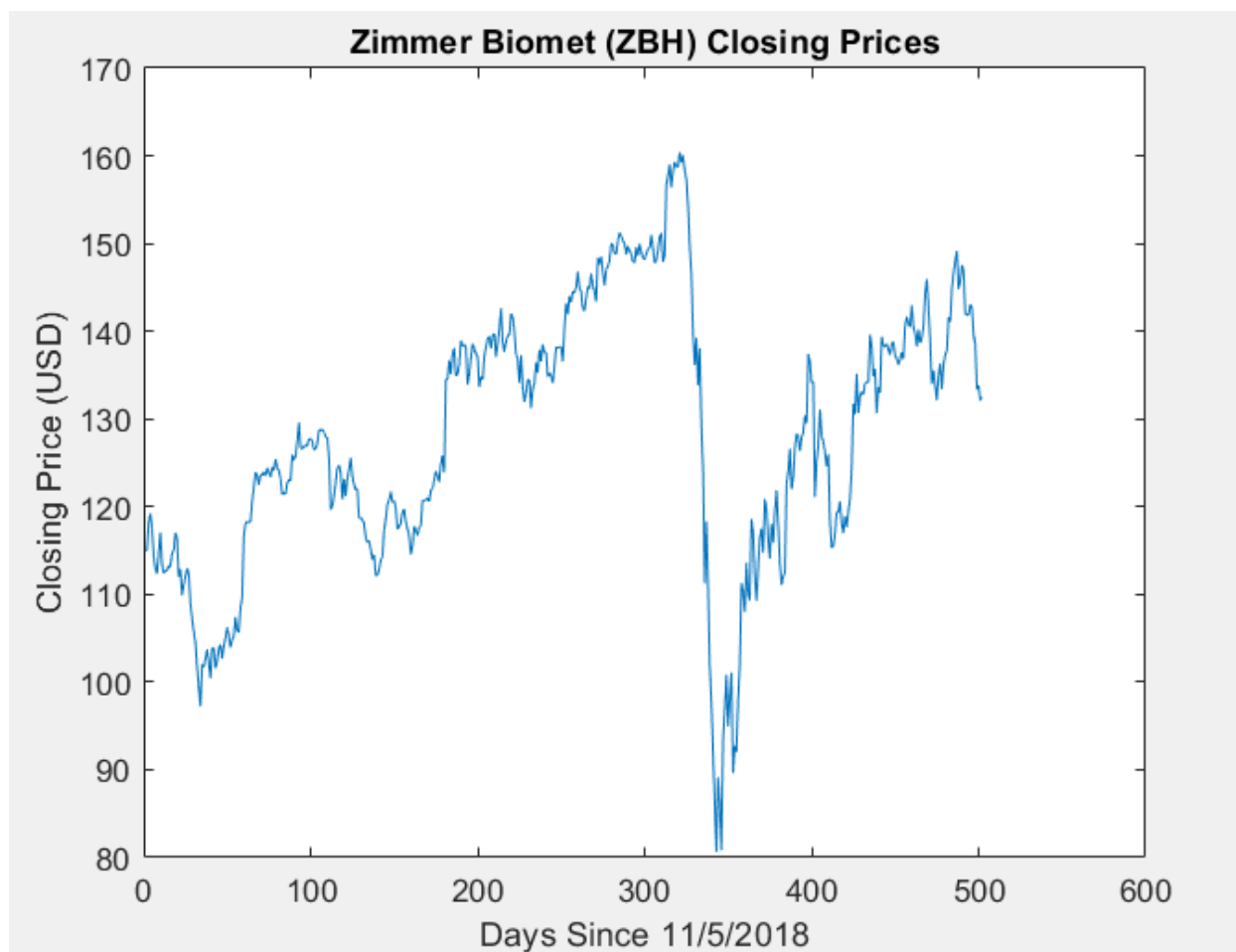


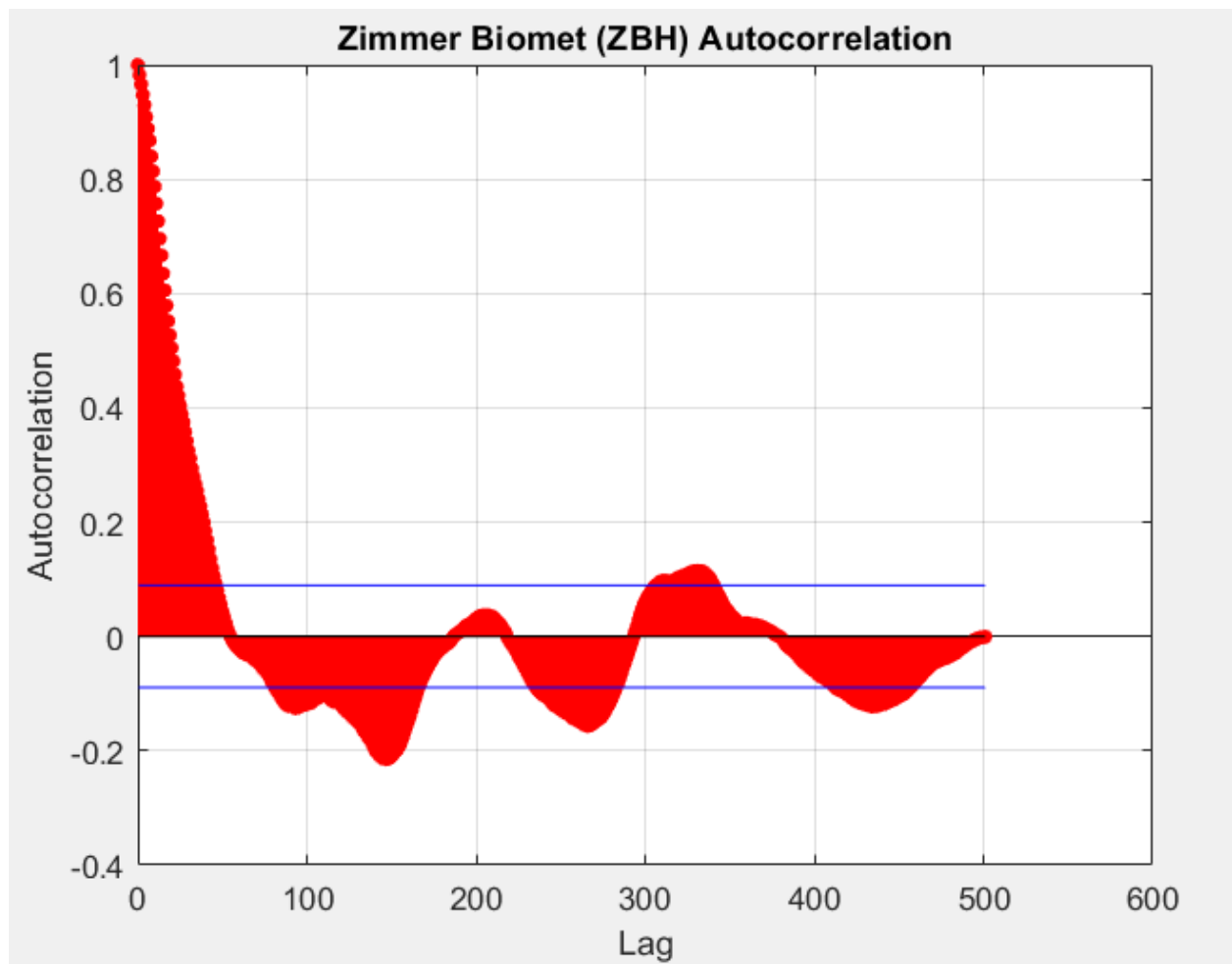


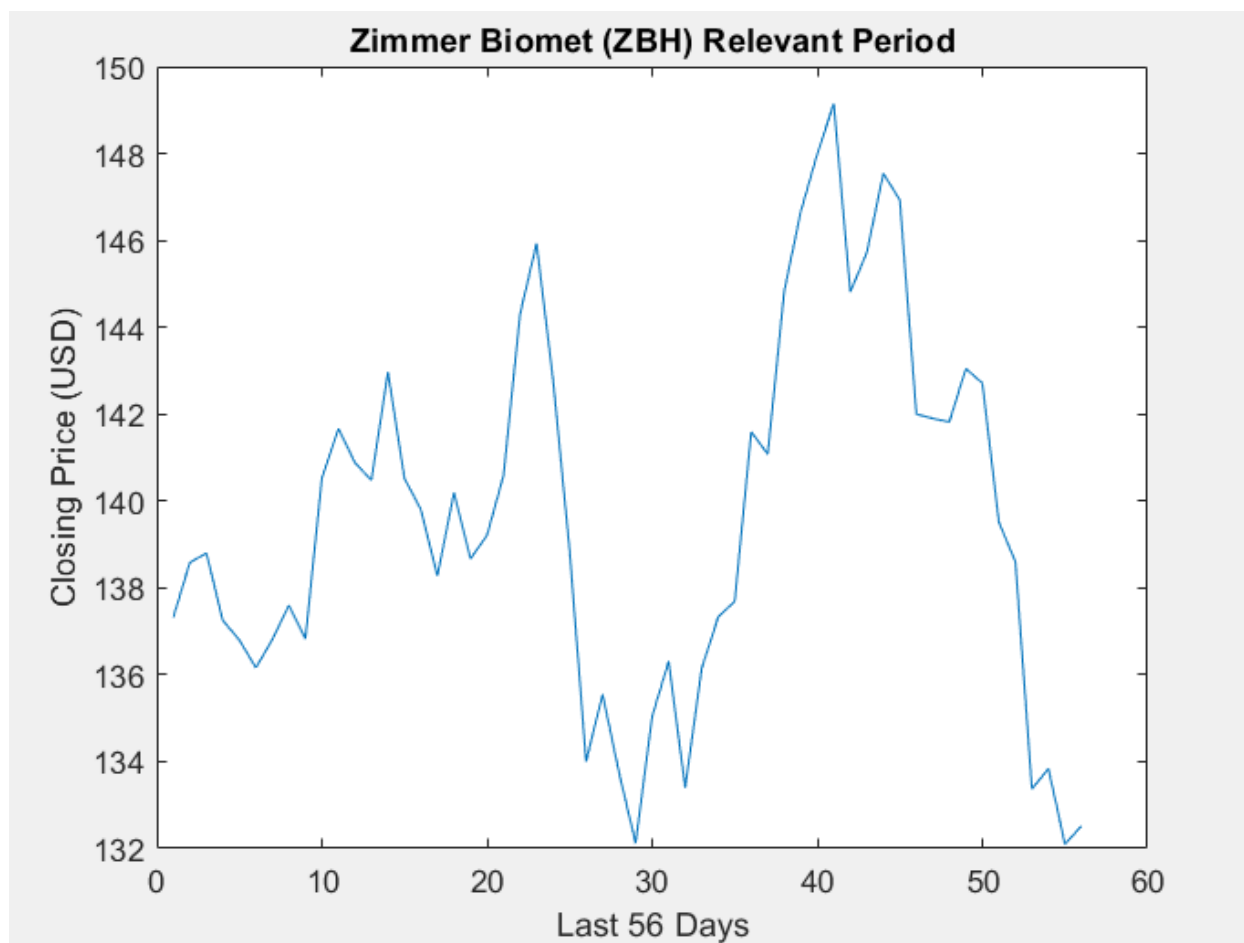


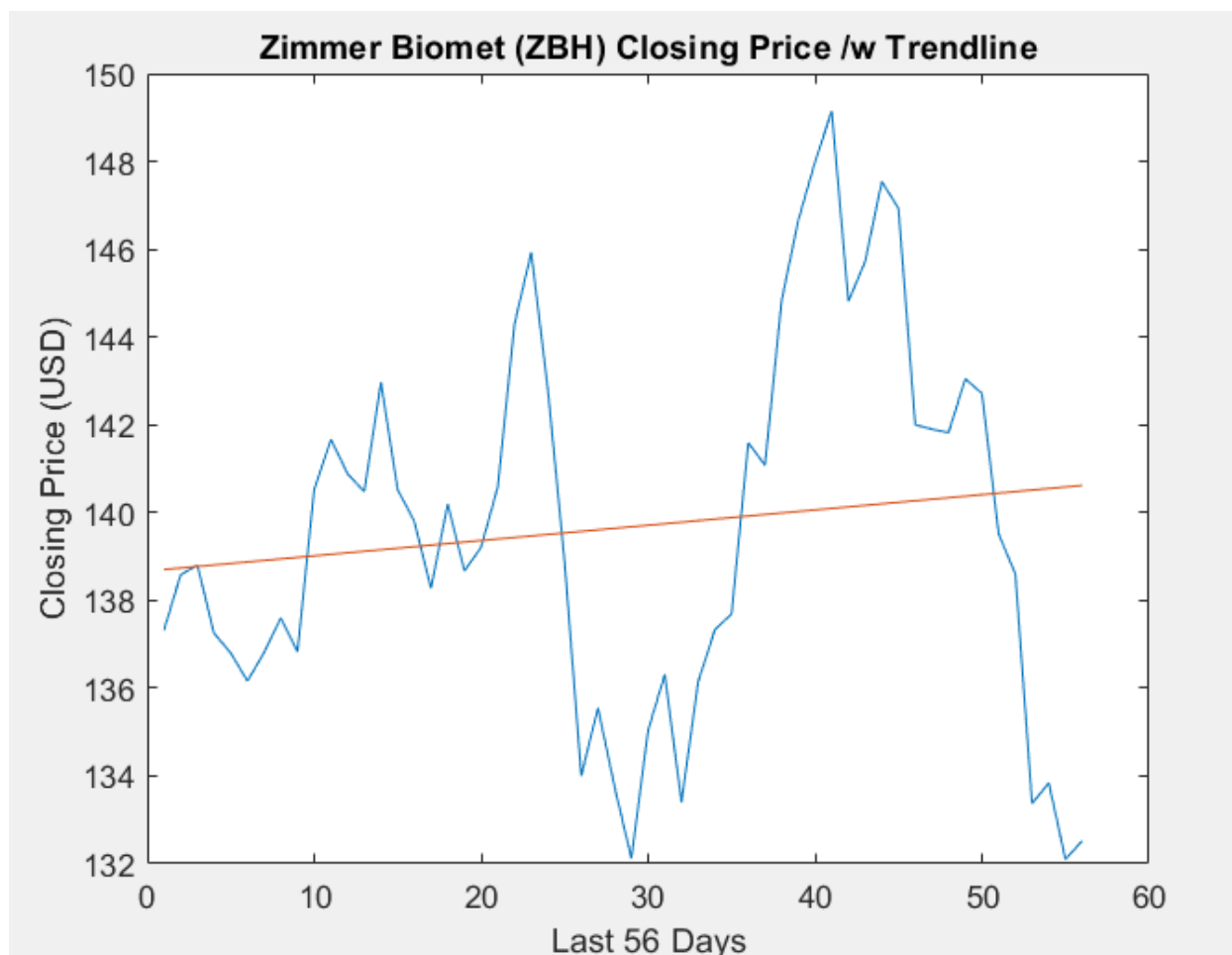


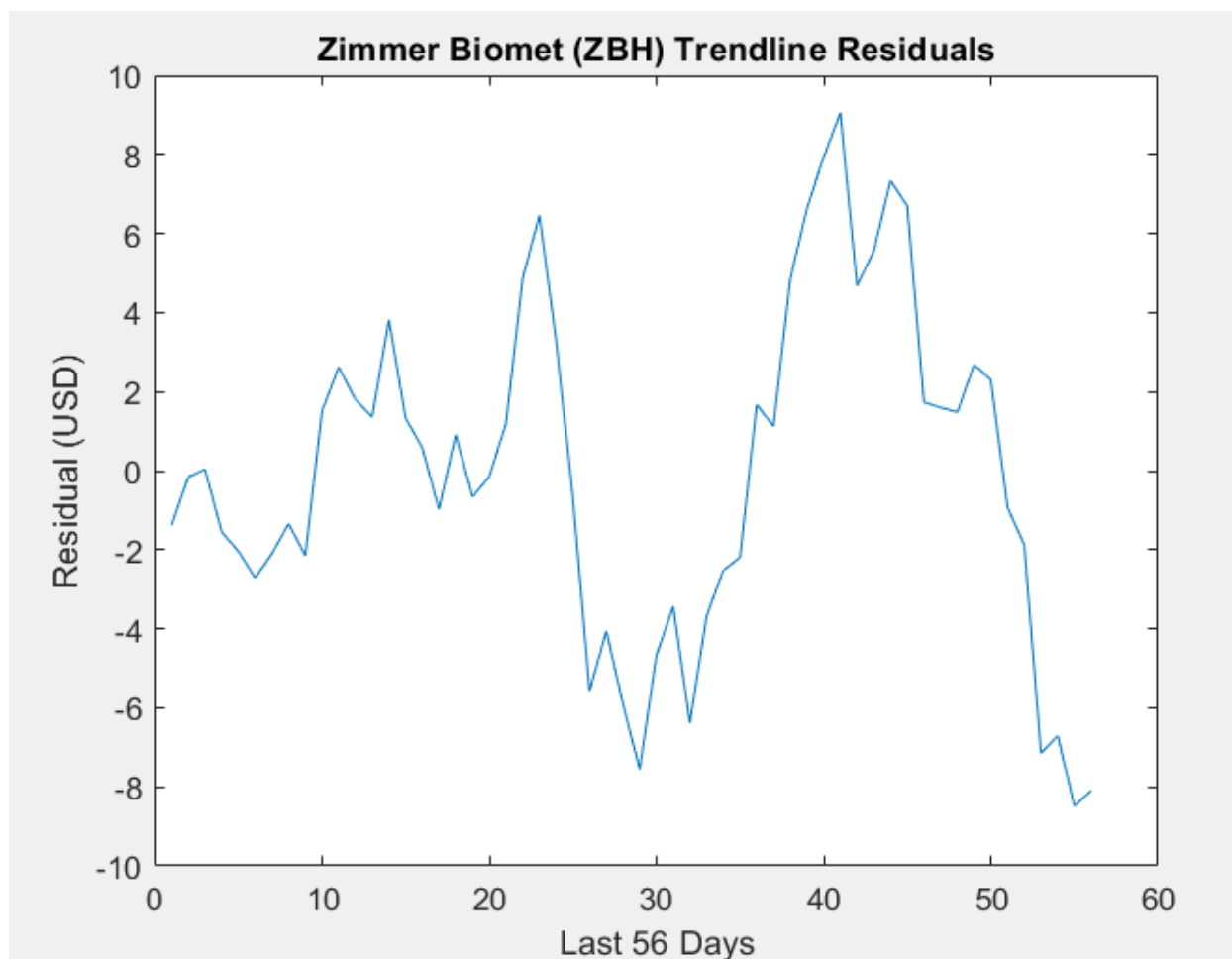


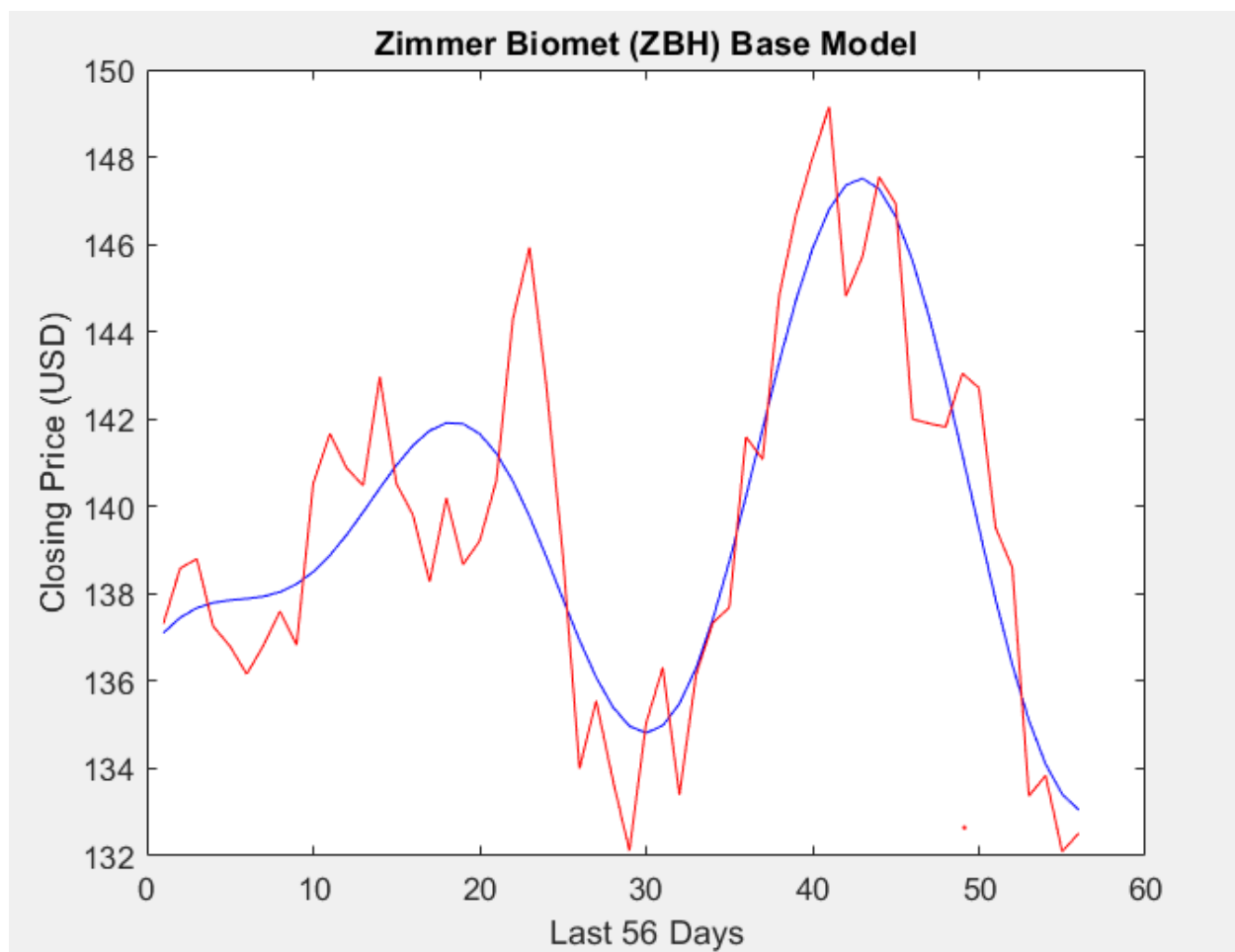


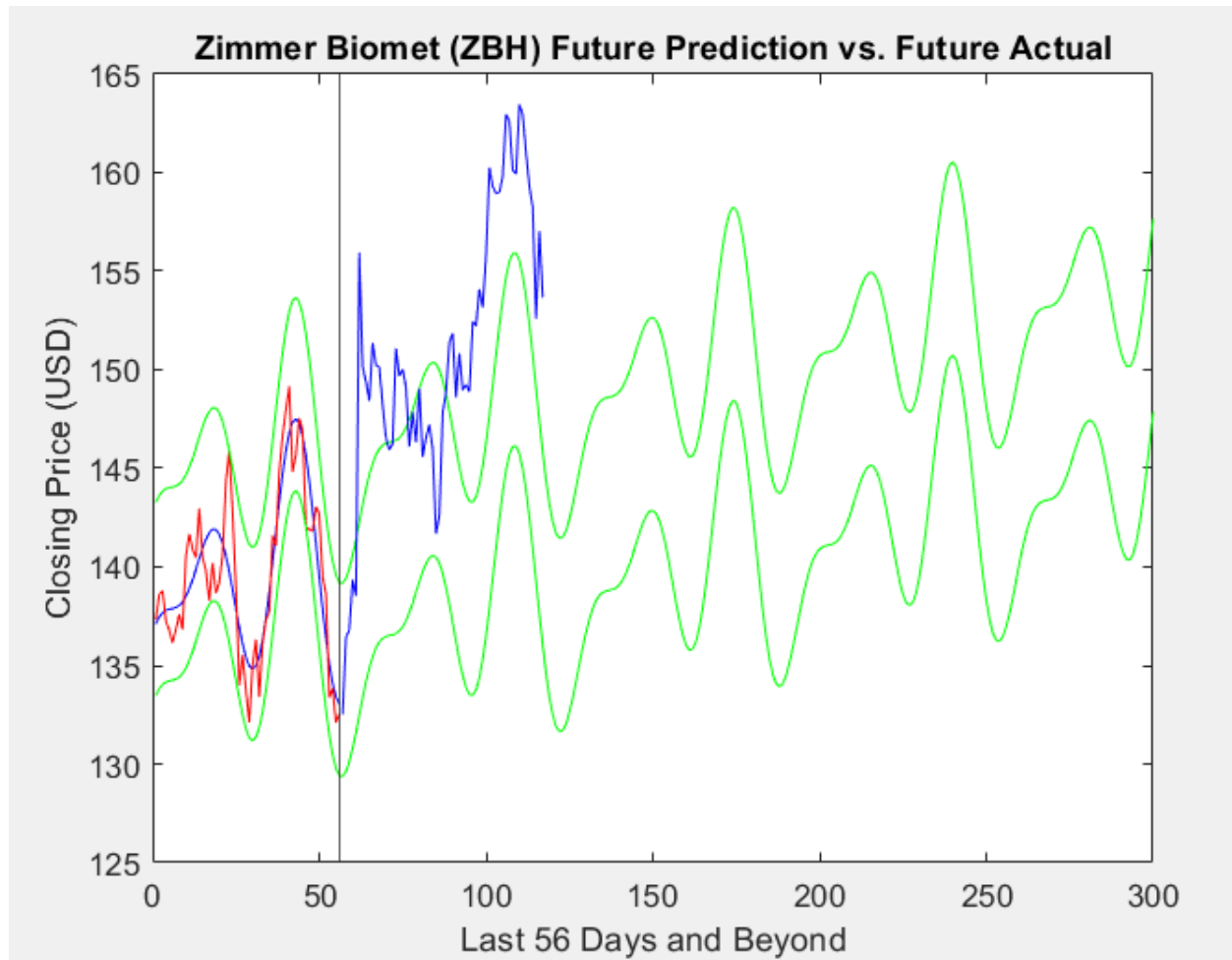












Base Model:

```
load('BDX.csv')
```

```
prclose=BDX(:,5);
```

```
name="Becton Dickinson (BDX)";
```

```
aa="27";
```

```
a=27;
```

```
for i=1:502
```

```
    data(i)=prclose(503-i);
```

```
    historical(i)=prclose(i);
```

```

end

load ('BDXfuture.csv')

prfuture=BDXfuture(:,5);

for i=1:61

    fut(i)=prfuture(i);

end

jj=linspace(a+1,a+61,61);

xx=linspace(1,502,502);

plot(xx,historical)

title(name + ' Closing Prices')

xlabel('Days Since 11/5/2018')

ylabel('Closing Price (USD)')

pause

autocorr(data,501)

title(name + ' Autocorrelation')

xlabel('Lag')

ylabel('Autocorrelation')

pause

RV=prclose(503-a:502);

yy=linspace(1,a,a);

plot(yy,RV)

title(name + ' Relevant Period')

```

```

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

hold

pause

p=polyfit(yy,transpose(RV),1)

for i=1:a

trend(i)=p(1)*i+p(2);

end

[n,m]=size(yy)

[n,m]=size(trend)

plot(yy,trend)

title(name + ' Closing Price /w Trendline')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

hold

pause

prdiff=transpose(RV)-trend;

plot(yy,prdiff)

title(name + ' Trendline Residuals')

xlabel('Last '+aa+' Days')

ylabel('Residual (USD)')

pause

```

```

f=fit(yy',prdiff,'fourier3'); %f will have the coeff of the fourier expansion

for i=1:a

yh(i)=trend(i)+f(i);

end

plot(yy,yh,'b')

hold

plot(yy,RV,'r')

title(name + ' Base Model')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

pause

prdiff2=transpose(RV)-yh;

%plot(yy,prdiff2)%

zz=linspace(1,300,300);

for x=1:300

prd(x)=p(1)*x+p(2)+f(x);

end

%plot(zz,prd)

plot(zz,prd+max(prdiff2),'g')

plot(zz,prd+min(prdiff2),'g')

plot(jj,fut,'b')

title(name + ' Future Prediction vs. Future Actual')

```

```
xlabel('Last '+aa+' Days and Beyond')
```

```
ylabel('Closing Price (USD)')
```

```
xline(a)
```

```
hold
```

Moving Averages Model:

```
load('BDX.csv')

prclose=BDX(:,5);

[n,m]=size(BDX(:,5))

tend=n

for i=10:tend-10

    az=0;

    for j=1:20

        az=az+prclose(i+j-10);

    end

    prsmooth(i)=az/20;

end

%since you are not smoothing the first 10 points and the last 10

%use the original data for these points

for i=1:10

    prsmooth(i)=prclose(i);

    prsmooth(tend-i+1)=prclose(tend-i+1);

end

plot(prsmooth)

pause

name="Becton Dickinson (BDX)";

aa="27";
```



```

a=27;

for i=1:502

    data(i)=prsmooth(503-i);

    historical(i)=prsmooth(i);

end

load ('BDXfuture.csv')

prfuture=BDXfuture(:,5);

for i=1:61

    fut(i)=prfuture(i);

end

jj=linspace(a+1,a+61,61);

xx=linspace(1,502,502);

plot(xx,historical)

title(name + ' Closing Prices')

xlabel('Days Since 11/5/2018')

ylabel('Closing Price (USD)')

pause

autocorr(data,501)

title(name + ' Autocorrelation')

xlabel('Lag')

ylabel('Autocorrelation')

pause

```

```

RV=prsmooth(503-a:502);

yy=linspace(1,a,a);

plot(yy,RV)

title(name + ' Relevant Period')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

hold

pause

p=polyfit(yy,(RV),1)

for i=1:a

trend(i)=p(1)*i+p(2);

end

plot(yy,trend)

title(name + ' Closing Price /w Trendline')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

hold

pause

prdiff=(RV)-trend;

plot(yy,prdiff)

title(name + ' Trendline Residuals')

xlabel('Last '+aa+' Days')

```

```

ylabel('Residual (USD)')

pause

[n,m]=size(yy)

[n1,m1]=size(prdiff)

f=fit(yy',prdiff,'fourier3'); %f will have the coeff of the fourier expansion

for i=1:a

yh(i)=trend(i)+f(i);

end

plot(yy,yh,'b')

hold

plot(yy,RV,'r')

title(name + ' Base Model')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

pause

prdiff2=(RV)-yh;

[n,m]=size(yh)

[n1,m1]=size(prdiff2)

%plot(yy,prdiff2)%

zz=linspace(1,300,300);

for x=1:300

prd(x)=p(1)*x+p(2)+f(x);

```

```
end

%plot(zz,prd)

plot(zz,prd+max(prdiff2),'g')

plot(zz,prd+min(prdiff2),'g')

plot(jj,fut,'b')

title(name + ' Future Prediction vs. Future Actual')

xlabel('Last '+aa+' Days and Beyond')

ylabel('Closing Price (USD)')

xline(a)

hold
```

Volatility-Driven Model:

```
load ('ICUI.csv')

prclose=ICUI(:,5);

aa="116";

name="ICU Medical (ICUI)";

a=116;

for i=1:502

    data(i)=prclose(503-i);

    historical(i)=prclose(i);

end

load ('ICUIfuture.csv')

prfuture=ICUIfuture(:,5);

for i=1:61

    fut(i)=prfuture(i);

end

sd=std(prclose)

jj=linspace(a+1,a+61,61);

xx=linspace(1,502,502);

plot(xx,historical)

title(name + ' Closing Prices')

xlabel('Days Since 11/5/2018')

ylabel('Closing Price (USD)')
```

```

pause

autocorr(data,501)

title(name + ' Autocorrelation')

xlabel('Lag')

ylabel('Autocorrelation')

pause

RV=prclose(503-a:502);

yy=linspace(1,a,a);

plot(yy,RV)

title(name + ' Relevant Period')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

hold

pause

p=polyfit(yy,transpose(RV),1)

for i=1:a

trend(i)=p(1)*i+p(2);

end

[n,m]=size(yy)

[n,m]=size(trend)

plot(yy,trend)

title(name + ' Closing Price /w Trendline')

```

```

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

hold

pause

prdiff=transpose(RV)-trend;

plot(yy,prdiff)

title(name + ' Trendline Residuals')

xlabel('Last '+aa+' Days')

ylabel('Residual (USD)')

pause

f=fit(yy,prdiff,'fourier3'); %f will have the coeff of the fourier expansion

for i=1:a

yh(i)=trend(i)+2.372419255*f(i);

end

plot(yy,yh,'b')

hold

plot(yy,RV,'r')

title(name + ' Base Model')

xlabel('Last '+aa+' Days')

ylabel('Closing Price (USD)')

pause

prdiff2=transpose(RV)-yh;

```

```

%plot(yy,prdiff2)%

zz=linspace(1,300,300);

for x=1:300

prd(x)=p(1)*x+p(2)+2.372419255*f(x);

end

%plot(zz,prd)

plot(zz,prd+max(prdiff2),'g')

plot(zz,prd+min(prdiff2),'g')

plot(jj,fut,'b')

title(name + ' Future Prediction vs. Future Actual')

xlabel('Last '+aa+' Days and Beyond')

ylabel('Closing Price (USD)')

xline(a)

hold

```