## WORCESTER POLYTECHNIC INSTITUTE

# **Sustainable Rooftop Technologies**

A Major Qualifying Project submitted to the Faculty of Worcester Polytechnic Institute in partial fulfillment of the requirements for the Bachelor of Science degree

by

Sebastian Miranda

Ryan Stokes

Ian Taylor

**Date** 

4/26/18

**Report Submitted to** 

Leonard Albano

Civil & Environmental Engineering

## **ABSTRACT**

This project evaluated the feasibility of the installation of sustainable rooftop technologies on selected buildings at Worcester Polytechnic Institute (WPI). This report includes the structural analysis and design of three sustainable rooftop technologies: solar panels, green roofs, and solar collectors. These technologies have the ability to save energy, while contributing to WPI's sustainability plan. Additionally, an economic analysis is prepared to show the simple payback periods of installing these sustainable rooftop technologies.

# **AUTHORSHIP PAGE**

Abstract	Ryan
Capstone Design Statement	Sebastian
Professional Licensure Statement	Ian
Chapter 1: Introduction	All
Chapter 2: Background	All
2.1 Heat Island Effect	Ryan
2.2 Solar Panels	Ryan
2.3 Green Roofs and Stormwater Retention Systems	Sebastian
2.4 Solar Collectors	Ian
2.5 Types of Structural Reinforcements	Sebastian
Chapter 3: Methodology	All
3.1 Identify Buildings for Consideration	Ryan
3.2 Design and Analysis of Solar Panel Technology on Gateway Parking Garage	Ryan
3.3 Design and Analysis of Green Roof Technology on Gordon Library	Sebastian
3.4 Design and Analysis of Solar Evacuated Tubes on Stoddard B	Ian
Chapter 4: Identify Buildings for Consideration	Ryan
Chapter 5: Solar Panel Installation on Gateway Parking Garage	Ryan
5.1 Selected Solar Panel Installation on Gateway Parking Garage	Ryan
5.2 Layout and Construction Process for Solar Panels on Gateway Parking Garage	Ryan
5.3 Structural Analyses and Design for Solar Panels on Gateway Parking Garage	Ryan
Chapter 6: Green Roof Installation on Gordon Library	Sebastian
6.1 Selected Green Roof Technology on Gordon Library	Sebastian
6.2 Layout and Construction Process for Green Roof on Gordon Library	Sebastian
6.3 Structural Analyses and Design for Green Roof on Gordon Library	Sebastian
Chapter 7: Solar Evacuated Tubes Installation on Stoddard B	Ian
Chapter 8: Economic Analysis	All
8.1 Economic Analysis of Solar Panels on Gateway Parking Garage	Ryan
8.2 Economic Analysis of Green Roof Installation on Gordon Library	Sebastian
8.3 Economic Analysis of Solar Evacuated Tubes on Stoddard B	Ian
Chantan O. Canalusians	A 11

References	All
Appendix A: Project Proposal	All
Appendix B: Calculations of Solar Panel Design on Gateway Parking Garage	Ryan
Appendix C: Calculations of Green Roof Design on Gordon Library	Sebastian
Appendix D: Calculations of Solar Evacuated Tube Design on Stoddard B	Ian

#### CAPSTONE DESIGN STATEMENT

To fulfill the requirements of the Capstone Design, our team completed a Major Qualifying Project focused on the plan and design of sustainable rooftop technologies on existing buildings at Worcester Polytechnic Institute (WPI). Structural analyses of different buildings, as well as feasibility of construction and costs were addressed in this project. The Capstone Design constraints expected in this project include: economic, environmental, constructability, sustainability, ethical, and health and safety.

#### Design Problem

As Worcester Polytechnic Institute is committed to a sustainability plan of ecological stewardship, social justice, and economic security, every member of the WPI community should be engaged in this process. Our plan for sustainable rooftop technologies follows the same path of the already existing sustainability plan; it is our job to embrace this mission in the local community.

To approach the problem and support the WPI sustainability plan, our group designed solar panels, green roofs, and solar collectors, for a number of existing buildings on campus. Each proposed system generates a different optimal solution, which includes, but not limited to, energy efficiency, water storage, and building cool-off.

#### **Economic**

The plan of implementing sustainable rooftop technologies comes at a cost. For each alternative that was considered, there was a different design and associated cost. Our group provided costs for implementing each of these systems, which included the actual cost of the system, operational costs, and lifetime. Similarly, the simple payback period of the desired project was determined, and recommendations were provided based on this economic analysis. *Constructability* 

Constructability is one of the most important factors to consider for implementing these sustainable systems. Considerations regarding the type of building (academic/residential/recreational), type of roof (slope/flat), year built, and size of the building are all accounted under this criteria. Similarly, the following factors were analyzed and considered:

• Structural layout of the selected buildings.

- Zoning, permitting, and regulations.
- Construction schedule/time frame for each system.

#### Sustainability

Sustainability in this project consisted of economic, environmental and social aspects. The design and construction of sustainable rooftop technologies includes all of these aspects and brings them together. Solar panels, green roofs, and solar collectors alleviate environmental concerns by implementing new technology in existing buildings at WPI. Sustainable technologies reduce the consumption of energy, and they create more efficient buildings on campus. Implementing sustainable rooftop technologies on buildings at WPI can alleviate the urban heat island effect. This is accomplished by reducing energy usage and decreasing gas emissions with the use of natural sources of energy.

#### **Environmental**

Through the development of this project, another constraint similar to sustainability is environmental. Installing each sustainable rooftop technology requires construction on the WPI campus, which can negatively impact the environment. Noise and dust can emit into the air during the construction process of these rooftop technologies. Our group proposed installation processes, which will have the least amount of impact on noise and air pollution.

# Health and Safety

It is of extreme importance to protect the public and the community of WPI of any possible risks. Health and safety of all the people involved in this project was considered, especially for potential users of the selected buildings. The design and construction of these systems are in accordance with the *International Building Code* and all safety factors. *Ethical* 

Ethical practices played an important role in this project. It was crucial to consider ethical codes for the design and construction of sustainable rooftop technologies. All the appropriate codes and regulations were considered in the implementation of these systems. Furthermore, the team completed confidentiality agreements for the information that was provided by WPI Facilities Department.

#### PROFESSIONAL LICENSURE

Civil engineering has been prevalent in human history since the beginnings of mankind. In addition to gathering food, society's main concern includes building a settlement, which requires civil engineering. Throughout time, civil engineering has advanced into a field, which now contains qualified individuals who have achieved a high level of education. Only a professional licensed civil engineer may prepare, sign, seal and submit engineering plans and drawings to a public authority for approval, or seal engineering work for public and private clients. The purpose of licensure is to protect the health and welfare of the public by regulating requirements to restrict engineering practice to qualified individuals. In order to become licensed, engineers must complete a number of requirements. First, one must complete a four or five-year college undergraduate degree. Following graduation, the individual must work under a professional engineer for at least four years, pass an intensive exam, and earn a license from their state's licensure board. Having a professional engineer's license means acceptance of both the technical and the ethical obligations of the engineering profession. Once a professional engineer is licensed, the individual is free to practice the discipline of civil engineering, and may stamp documents of any kind within their practice and expertise. Licensure is important since it is legally required to be a consulting engineer or a private practitioner. It can also raise prestige and accelerate career development.

The process of preparing a sustainable rooftop technology plan for WPI exposed our group to the concept of structural design and analysis, which is also required by professional licensed civil engineers. Our project explores alternative rooftop technologies that could possibly be employed by the WPI community. These alternative practices consist of installing solar panels, green roofs, and solar collectors to the roofs of chosen buildings at WPI. A structural analysis of the buildings was executed, as well as a proposed sustainable rooftop technology design. In order to install solar panels, green roofs, and solar collectors, one must make sure that the building can carry the loads imposed by these technologies. Additionally, our analysis included how efficient solar panels, green roofs, and solar collectors are.

Solar panels, green roofs, and solar collectors have the ability to deal with the negative impacts of the urban heat island effect by making the problem part of the solution. This project reflects the meaning of a professional licensed civil engineer. There are technical aspects to this

project: designing the layout of solar panels, green roofs, and solar collectors, choosing a building and analyzing the structure's support, and producing an economic evaluation. Finally, our project relates to the nature of a professional licensed engineer by promoting health and welfare in an ethical manner and making the WPI community more sustainable.

# TABLE OF CONTENTS

Chapter 1: Introduction	1
1.1 Problem Statement	1
1.2 Goals and Objectives	1
Chapter 2: Background	3
2.1 The Heat Island Effect	3
2.1.1 Negative Impacts	3
2.1.2 Strategies to Reduce Urban Heat Islands	4
2.2 Solar Panels	4
2.2.1 Solar Panel Properties	5
2.2.2 Solar Panel Process	5
2.2.3 Types of Solar Panel Systems	5
2.2.4 Structural Considerations	7
2.2.5 Wind Design for Solar Panels	8
2.2.6 Seismic Requirements for Solar Panels	10
2.3 Green Roofs and Stormwater Retention Systems	10
2.3.1 The Urban Stormwater Problem	11
2.3.2 Green Roof Stormwater Retention Success	11
2.3.3 Benefits of Green Roofs	11
2.3.4 Structural Considerations	12
2.4 Solar Collectors	13
2.4.1 Solar Collector Process	13
2.4.2 Types of Solar Collector Technologies	13
2.4.3 Structural Considerations	14
2.5 Types of Structural Reinforcements	15
2.5.1 Passive Systems	15
2.5.2 Active Systems	15
3.0 Methodology	17
3.1 Identify Buildings for Consideration	17
3.2 Design and Analysis of Solar Panel Technology on Gateway Parking Garage	18
3.2.1 Layout and Construction Process for Solar Panels on Gateway Parking Garage	18

3.2.2 Structural Analyses and Design for Solar Panels on Gateway Parking Garage	18
3.3 Design and Analysis of Green Roof Technology on Gordon Library	35
3.3.1 Layout and Construction Process for Green Roof on Gordon Library	35
3.3.2 Structural Analyses and Design for Green Roofs	35
3.4 Design and Analysis of Solar Evacuated Tubes on Stoddard B	55
3.4.1 Layout and Construction Process for Solar Collectors on Stoddard B	55
3.4.2 Structural Analyses and Design for Solar Collectors on Stoddard B	55
3.5 Economic Analysis	66
3.5.1 Economic Analysis of Solar Panels on the Gateway Parking Garage	66
3.5.2 Economic Analysis of Green Roof on Gordon Library	71
3.5.3 Economic Analysis of Solar Collectors on Stoddard B	72
Chapter 4: Identify Buildings for Consideration	74
Chapter 5: Solar Panel Installation on Gateway Parking Garage	78
5.1 Selected Solar Panel Technology on Gateway Parking Garage	78
5.2 Layout and Construction Process for Solar Panels on Gateway Parking Garage	79
5.2.1 Layout on Gateway Parking Garage	79
5.2.2 Construction Process for SunPower Polycrystalline Silicon Solar Panels	81
5.3 Structural Analyses and Design for Solar Panels on Gateway Parking Garage	83
5.3.1 Solar Panel Load Calculations	84
5.3.2 Supporting Beam Calculations	85
5.3.3 Laterally Unsupported Beams	86
5.3.4 Supporting Girder Calculations	88
5.3.5 Laterally Unsupported Girders	89
5.3.6 Supporting Column Calculations	91
5.3.7 Second-Order Elastic Analysis	92
5.3.8 Baseplate Design	93
5.3.9 Recalculation of Seismic Load	94
5.3.10 Reinforcement in 2 ft x 2 ft Concrete Columns	95
5.3.11 Supporting Steel Frame Final Results	96
Chapter 6: Green Roof Installation on Gordon Library	98
6.1 Selected Green Roof Technology on Gordon Library	98
6.2 Layout and Construction Process for Green Roof on Gordon Library	99

6.2.1 Layout on Gordon Library	99
6.2.2 Construction Process for Extensive Green Roofs	101
6.3 Structural Analyses and Design for Green Roof on Gordon Library	102
6.3.1 Vertical and Horizontal Load Calculations	102
6.3.2 Basic Load Combinatination Analysis	110
6.3.3 Structural Analysis and Capacity of Building	111
Chapter 7: Solar Collector Installation on Stoddard B	127
7.1 Selected Solar Collector Technology on Stoddard B	127
7.2 Layouts and Construction Process for Solar Collectors on Stoddard B	128
7.3 Research and Estimates	132
7.4 Structural Analysis and Member Designs for Solar Collectors on Stoddard B	133
7.4.1 Solar Evacuated Tubes Load Calculations	133
7.4.1 Slab Design & Calculations	134
7.4.2 Beam Design & Calculations	136
7.4.3 Column Design & Calculations	138
Chapter 8: Economic Analysis	141
8.1 Economic Analysis of Solar Panels on the Gateway Parking Garage	141
8.1.1 Total Cost of Steel Framework	141
8.1.2 Total Cost of Added 2 ft x 2 ft Concrete Columns	142
8.1.3 Total Cost of Reinforcement Within Concrete Columns	143
8.1.4 Total Cost of Solar Panels	143
8.1.5 Economic Analysis Results	144
8.2 Economic Analysis of Green Roof Installation on Gordon Library	145
8.2.1 Material and Labor	145
8.2.2 Stormwater Benefits	147
8.2.3 Energy and Insulation	147
8.3 Economic Analysis of Solar Collectors on Stoddard B	148
8.3.1 Fixed Cost	148
8.3.2 Savings Per Year	149
8.4 Payback Period	150
Chapter 9: Conclusions	151
References	153

Appendix A: Project Proposal	157
Appendix B: Solar Panel Calculations	199
Appendix C: Green Roof Calculations	229
Appendix D: Solar Collector Calculations	286

# LIST OF TABLES

Table 1	9
Table 2	
Table 3	
Table 4	
Table 5	
Table 6	
Table 7	
Table 8	
Table 9.	
Table 10	
Table 11	
Table 12	
Table 13	
Table 14	76
Table 15	79
Table 16	80
Table 17	82
Table 18.	84
Table 19	85
Table 20	85
Table 21	86
Table 22	87
Table 23	89
Table 24	90
Table 25	92
Table 26	92
Table 27	
Table 28	
T. 11. 20	

Table 30	97
Table 31	99
Table 32	101
Table 33	103
Table 34	104
Table 35	
Table 36	
Table 37	
Table 38	
Table 39	
Table 40	110
Table 41	111
Table 42	113
Table 43	113
Table 44	113
Table 45	114
Table 46	114
Table 47	115
Table 48	116
Table 49	117
Table 50	
Table 51	
Table 52	
Table 53	
Table 54	
Table 55	
Table 56	
Table 57	130
Table 58	132
Table 59	134
Table 60	134
Table 61	135

Table 62	137
Table 63	140
Table 64	142
Table 65	142
Table 66	143
Table 67	143
Table 68	144
Table 69	144
Table 70	144
Table 71	146
Table 72	146
Table 73	149
Table 74	149
Table 75	150

# LIST OF FIGURES

Figure 1	13
Figure 2	40
Figure 3	43
Figure 4	43
Figure 5	50
Figure 6	51
Figure 7	54
Figure 8	80
Figure 9	81
Figure 10	82
Figure 11	83
Figure 12	83
Figure 13	87
Figure 14	88
Figure 15	90
Figure 16	
Figure 17	
Figure 18	
Figure 19	
Figure 20	
Figure 21	
Figure 22	
Figure 23	
Figure 24	
Figure 25	
Figure 26	
Figure 27	
Figure 28	
Figure 29	
Figure 30	109

Figure 31	112
Figure 32	118
Figure 33	119
Figure 34	119
Figure 35	121
Figure 36	121
Figure 37	123
Figure 38	126
Figure 39	128
Figure 40	129
Figure 41	130
Figure 42	131
Figure 43	136
Figure 44	137
Figure 45	138
Figure 46	139
Figure 47	140

### **CHAPTER 1: INTRODUCTION**

This chapter contains an introduction to sustainable rooftop technologies, and their ability to mitigate global environmental problems. Additionally, this section lays out the goals and objectives for this project.

#### 1.1 Problem Statement

Climate change, air pollution, and water pollution are a few of many environmental problems that the world is dealing with today. Specifically in urban areas, the heat island effect is another problem, which is increasing temperatures. The negative impacts from the heat island effect in urban cities include an increase in energy usage, increase in gas emissions, impaired water quality, and health risks. It is the responsibility of our generation to explore ways to preserve the environment for future generations. Implementing sustainable rooftop technologies is one practice, which can help reduce some of the environmental problems the world is dealing with today. Sustainable rooftop technologies include solar panels, solar collectors, green roofs, stormwater retention systems, and daylighting systems. All of these systems use the source of the problem, the sun, as a way to reduce environmental problems. Our objective is to explore three rooftop technologies, and investigate the structural impact these systems can have on buildings at Worcester Polytechnic Institute (WPI). The three technologies chosen were solar panels, green roofs, and solar collectors.

# 1.2 Goals and Objectives

The goal of this project is to provide recommendations and improvements for the installation of sustainable rooftop technologies on existing buildings at WPI. Additionally, the impact of these technologies on the net energy demands was investigated. The objectives for this project included:

- 1. Determine WPI's approach to sustainable practices, as well as its current sustainable building practices.
- 2. Identify candidate buildings at WPI for the installation of certain sustainable rooftop technologies.

- 3. Identify energy demand of each building to quantify the needed output for each sustainable rooftop technology.
- 4. Determine the design and construction process for each sustainable rooftop technology on the desired building for installation.
- 5. Identify structural design activities for the selected buildings, which include identifying structural reinforcements needed to withstand sustainable rooftop technologies.
- 6. Conduct an economic analysis to determine whether it is feasible to implement sustainable rooftop technologies at WPI.

## **CHAPTER 2: BACKGROUND**

This chapter provides a brief introduction of the heat island effect, which is an environmental problem, which can be reduced in urban areas through sustainable rooftop technologies. Additionally, this section contains background information on various sustainable rooftop technologies: solar panels, solar collectors, and green roofs.

#### 2.1 The Heat Island Effect

The heat island effect describes urban regions, which become hotter than its rural surroundings due to urban area development of buildings, roads, and other infrastructure, which replaces open land and vegetation. The annual mean temperature of a city with one million people or more can be 1.8°F warmer than its surroundings. However, the temperature difference can be as much as 22°F during the nighttime due to the buildup of heat on infrastructure from the sun during the day, which is slowly released throughout the night. Shaded or moist surfaces in rural areas remain close to air temperatures. Elevated temperatures in urban areas can negatively impact a community's environment and quality of life (United States Environmental Protection Agency, 2017).

#### 2.1.1 Negative Impacts

Some of the negative impacts of the heat island effect include increased energy consumption, elevated emissions of air pollutants and greenhouse gases, compromised human health and comfort, and impaired water quality (United States Environmental Protection Agency, 2017):

- 1. *Increased Energy Consumption:* When the temperature rises in urban areas during the summertime, there is an increase of energy demand for cooling. Starting from 68-77°F, the electricity demand for cooling increases 1.5-2.0% for every 1°F increase in air temperatures (United States Environmental Protection Agency, 2017).
- 2. *Elevated Emissions of Air Pollutants and Greenhouse Gases:* The burning of fossil fuel increases air pollutants and greenhouse gas emissions. Fossil fuel power plants are used to supply electricity, which in turn emit sulfur dioxide, nitrogen oxides, particulate matter, carbon monoxide, mercury, and carbon dioxide. All of these pollutants are

- harmful to human health and contribute to air quality problems including smog, fine particulate matter, acid rain, and global climate change.
- 3. Compromised Human Health and Comfort: High temperatures affect human health and contribute to discomfort, respiratory difficulties, heat cramps and exhaustion, non-fatal heat strokes, and heat-related mortality. The Centers for Disease Control and Prevention estimated from 1979-2003 that excessive heat exposure contributed to more than 8,000 premature deaths in the United States (United States Environmental Protection Agency, 2017).
- 4. *Impaired Water Quality:* High pavement and rooftop surface temperatures can heat stormwater runoff. Tests have shown that 100°F pavement can elevate initial rainwater temperature from 70°F to over 95°F (United States Environmental Protection Agency, 2017). This heated stormwater will eventually runoff into storm sewers and raise the water temperature of streams, rivers, ponds, and lakes. Rapid temperature changes in aquatic ecosystems can be fatal to aquatic life.

#### 2.1.2 Strategies to Reduce Urban Heat Islands

There are various strategies, which help to reduce urban heat islands. One strategy is to increase tree and vegetation cover. This can provide shade and cooling to urban areas, as well as reduce stormwater runoff and protect against erosion. Another strategy is to implement more green roofs in urban areas. By growing a vegetative layer on a rooftop, the roof surface temperature will decrease and stormwater management will improve. Additionally, cool roofs are made of materials or coatings that reflect sunlight and heat away from a building. Cool roofs have the ability to reduce roof temperatures, increase the comfort of building occupants, and reduce energy demand. Vegetation cover, green roofs, and cool roofs are a few of many strategies that have the ability to reduce urban heat islands (United States Environmental Protection Agency, 2017).

#### 2.2 Solar Panels

Solar energy is a renewable source of energy created from the sun. Solar energy produces energy through a process, which is sustainable, inexhaustible, non-polluting, noise-free, and does not emit greenhouse gases (Energy Matters, 2016). Solar panels in the United States should face south to absorb the most sunlight; however, solar panels do not need direct sunlight to produce

electricity. Solar power has the capacity to provide energy for air conditioners, hot water heaters, cooking and electrical appliances, natural gas, electricity, or oil fuels (Solar Power Authority, 2017). Solar technologies can be expensive and require a lot of land area to collect the sun's energy at useful rates; however, solar electricity can pay for itself in the long term, usually five to ten years with tax incentives (Imboden, 2009). When solar panels are purchased, the federal solar tax credit allows the owner to deduct 30% of the cost of installing a solar energy system from the owner's federal taxes. Not only has the cost of solar panels dropped by 80% since 2008 due to its high demand, but maintenance is minimal and returns are high once solar panels have been installed (Solar Power Authority, 2017).

#### 2.2.1 Solar Panel Properties

Solar panel systems (photovoltaic or PV system) are made up of semiconductor materials that convert sunlight into an electric current (Energy Matters, 2016). When sunlight hits the cells of the solar panels, electrons become loose from their atoms and flow through the cell generating electricity (Imboden, 2009). The semiconductor material is covered with an anti-reflective coating and made up of silicon wafers impregnated with impurities; these impurities have the ability to improve electrical properties. The solar cells are joined together by electrical contacts, and located between a superstrate layer on top and a back-sheet layer below (Energy Matters, 2016).

#### 2.2.2 Solar Panel Process

The photovoltaic effect is the process by which light is converted to energy at the atomic level. The majority of energy the solar cells produce goes into a grid-connected inverter, which converts the electric charge from a direct current (DC) into an alternating current (AC). This allows the solar electricity current to flow to and from the grid connect inverter. The solar electricity can power the appliances in a building when needed, and the leftover solar electricity will flow to the grid-connected inverter where it is stored. If more energy is produced than used, then the owner is credited on their electricity bill, making this an incentive for building owners to implement renewable systems (Energy Matters, 2016).

#### 2.2.3 Types of Solar Panel Systems

As the use of technology has increased over the years, different types of solar panels have been created. Of all these, approximately 90% of solar panels are made of silicon photovoltaic

material (Battaglia, Cuevas & De Wolf, 2016). This section describes two different types of solar panel systems: crystalline silicon panels and thin-filmed panels.

Crystalline Silicon (Monocrystalline Silicon & Polycrystalline Silicon)

Crystalline silicon cells are the most common solar cells used in commercially available solar panels, consisting of more than 85% of the world's photovoltaic cell market sales (Battaglia, et. al., 2016). Crystalline silicon panels have two subtypes: Monocrystalline Silicon & Polycrystalline Silicon. The main difference between these types is the production technique. Each technique has its advantages and disadvantages. The cells have laboratory energy efficiencies of 25% for monocrystalline cells and over 20% for polycrystalline cells. However, industrially produced solar modules currently achieve efficiencies ranging from 18%–22% (Battaglia, et. al., 2016).

Monocrystalline solar panels have the highest efficiency rates since they are made out of the highest-grade silicon. Monocrystalline cells are produced from pseudo-square silicon wafers (substrates cut from boules grown by the Czochralski process), the float-zone technique, ribbon growth, or other emerging techniques. These other emerging techniques can have a specific reason for their utilization. For example, if produced using the ribbon growth technique, the production costs as well as the carbon footprint both decrease efficiency. These panels are also space-efficient. Since they yield the highest power outputs, they require less space compared to the other types. They also have a long life expectancy (25+ years) and tend to work better in low-light conditions. This type of panel is the most efficient and has a longer lifespan than other types of panels; however, it is the most expensive type of panel (Battaglia, et. al., 2016).

Polycrystalline silicon solar cells are a newer technology and vary in the manufacturing process. They are traditionally made from square silicon substrates cut from ingots cast in quartz crucibles. Polycrystalline cells are more cost effective to produce due to the fact that many cells can be created from a single block. However, every time silicon is cut, the edges become deformed, which results in a lower operating efficiency. Polycrystalline cells have become the dominant technology in the residential solar panels market because of their operating efficiencies, and the low-cost method by which they can be produced. In terms of efficiency, polycrystalline solar cells are now very close to monocrystalline cells (Battaglia, et. al., 2016).

Since crystalline cells were one of the first technologies, much of the production and manufacturing techniques have been refined to reach their maximum potential. Advantages of

crystalline silicone cells include a high efficiency rate of about 12% to 24.2%, high stability, ease of fabrication, high reliability, and long lifespan. Other benefits include high resistance to heat and lower installation costs. Negatively, these panels are the most expensive, in terms of initial cost, and have a low absorption coefficient (Battaglia, et. al., 2016).

#### Thin-Film Panels

The differences between thin-film and crystalline silicon solar cells are the thin and flexible pairing of layers, and the photovoltaic material: either cadmium telluride or copper indium gallium dieseline instead of silicon. Thin-film solar panels are the least efficient type of solar panel. Depending on the technology, thin-film module prototypes have reached efficiencies between 7–13%, and production modules operate at about 9% (Battaglia, et. al., 2016).

Thin film panels are made by depositing photovoltaic substances (such as glass) into a solid surface. Multiple combinations of substances have successfully and commercially been used for the photovoltaic substance. Typical thin-film solar cells are one of four types, depending on the material used: amorphous silicon (a-Si) and thin-film silicon (TF-Si); cadmium telluride (CdTe); copper indium gallium dieseline (CIS or CIGS); and dye-sensitized solar cell (DSC) plus other organic materials (Battaglia, et. al., 2016).

Despite being the least efficient, thin-film panels have advantages that should be considered when planning for solar roofing. Thin-film material is 100 times thinner than traditional solar panels, provides flexibility, and is lightweight. Thin-film panels are created by combining consecutive thin layers of material together. The result is a single film that is capable of being distributed in rolls or sheets making it easier to handle. Thin-film panels are the lowest cost panels to produce because of their low material costs. However, thin-film panels require the most space for producing the same amount of power as other solar panels, making them less efficient. Additionally, the thin material's durability begins to suffer over time, requiring frequent replacement (Battaglia, et. al., 2016).

#### 2.2.4 Structural Considerations

Placing solar panels on the roof of a building adds various loads to the structure. To perform a structural analysis on the building involves to first define the loads, and then to determine how the loads affect the structure (Wrobel, 2017).

Solar panels add a dead load to the roof of a building. The dead load includes the selfweight of all the physical components of the solar panels. The dead load applied to the roof is a concentrated load located where the roof supports the panels, which is usually located at each corner of the panel (Wrobel, 2017). In geographic regions where snow loads are present on roofs, warm roofs are constructed which can help decrease the snow load. If solar panels are raised above the roof, then they do not receive the benefit of the warm roof to decrease the snow load, which results in an increase of the snow load as well (Wrobel, 2017). The design of snow loads for roofs that include solar panels shall be determined in accordance with ASCE 7-10. Wind loads are also considered as they have the ability to act in various directions, both upward and downward on solar panels. Wind loads also act on different locations of the solar panels depending on which direction the wind is blowing from (Wrobel, 2017). Some of the elements for which wind loads should be considered are: the ultimate design wind speed, risk category, wind exposure, internal pressure coefficient, component and cladding, and seismic concerns for non-structural attachments. Finally, seismic loads should be considered despite the geographic location of Worcester, MA, where earthquakes do not have a large effect on structures. Due to the complexity of wind loads and seismic loads acting on solar panels, these loads should not only be calculated in accordance with the ASCE 7-10, but also in accordance with solar panel related documents provided by the Structural Engineers Association of California. Finally, the size, quantity, and location of solar panels on the roof of a building should be considered. All of these factors will determine the effect of the loads, and the existing structures' capacity for the addition of solar panels.

#### 2.2.5 Wind Design for Solar Panels

A document by the Structural Engineers Association of California titled, *Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs*, provides information on the step-by-step process for calculating wind loads on solar panels. There are many factors to consider when analyzing the effect of wind loads on solar panels. This document provides information on the determination of wind loads for solar photovoltaic arrays, which is not explicitly covered by the methods contained in the ASCE 7-10 (Structural Engineers Association of California, 2012). Steps to determine wind loads on rooftop equipment and other structures are located in Table 29.1-1 in ASCE 7-10. However, in Step 7 of this table, the equation provided needs to be changed for the consideration of solar panels. The design wind pressure for rooftop solar arrays

can be determined using the equation below (Structural Engineers Association of California, 2012).

$p = q_h*(GC_m)$	
$\mathbf{p}$ = wind pressure for rooftop solar arrays	
$\mathbf{q_h}$ = velocity pressure evaluated at mean roof height of the building (lb./ft <sup>2</sup> )	
$GC_m$ = combined net pressure coefficient for solar panels (lb./ft <sup>2</sup> )	

Solar panels mounted on a roof are highly vulnerable to the speed and direction of the wind approaching the panel. There are three distinct regions or zones on a roof where the wind flow characteristics and resulting wind loading on solar panels are different: interior, edge, and corner zones. Wind loads on solar panels located in the corner zones of roofs are much greater than those in the middle of the roof. Higher tilt panels are particularly vulnerable to the vertical component of swirling winds in the corner vortices of the panels. Since solar panels in the northern hemisphere face south, the northeast and northwest corners of the panel create severe loading. The southeast and southwest corners of the panel still create loading, just not as strong as the other two corners (Structural Engineers Association of California, 2012).

Different restricting values for the size, height, spacing, and positioning of solar panels are presented in Table 1. These values will help when designing the roof layout and calculating wind load values. *Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs* provides more detailed information and application for these values.

**Table 1: Solar Panel Design Restrictions** (Structural Engineers Association of California, 2012)

Characteristic	Quantity
Height of gap between panels and roof surface (h <sub>1</sub> )	≤ 2 ft
Maximum height above the roof surface (h <sub>2</sub> ) for panels	4 ft
Panel chord length (l <sub>p</sub> )	≤ 6 ft 8 in
Distance between solar panels and roof edge	≤ 2*h <sub>2</sub>
Space between rows of solar panels	≤ 2*panel characteristic height (h <sub>c</sub> )
Panel tilt angle for typical installations	0-35 degrees

#### 2.2.6 Seismic Requirements for Solar Panels

Similar to the previous section, a document by the Structural Engineers Association of California titled, *Structural Seismic Requirements and Commentary for Rooftop Solar Photovoltaic Array*, provides information on how to calculate and deal with seismic forces when designing solar panels. It is important to understand the effect of seismic forces on solar panels, and prepare for any type of loading. As described in the document, solar arrays can either be attached or unattached to the roof structure of a building (Structural Engineers Association of California, 2012). For our project, attached solar arrays are used, therefore the information obtained has different values and procedures than those for unattached solar arrays.

Solar panels and their structural support systems shall be designed to provide life-safety performance in the design basis earthquake ground motion. Life-safety performance means that solar panels are not expected to create a hazard to life. For example, as a result of breaking free from the roof, sliding off the roof's edge, exceeding the downward load-carrying capacity of the roof, or damaging skylights, electrical systems, or other rooftop features or equipment in a way that threatens life-safety. Solar array support systems that are attached to a roof structure shall be designed to resist the lateral seismic force  $(F_p)$  specified in Chapter 13 of ASCE 7-10. In the computation of  $F_p$ , an evaluation of flexibility and ductility capacity of the support structure is permitted to be used to establish seismic coefficients of component amplification factor  $(a_p)$  and component response factor  $(R_p)$ . These values can be found in Table 13.5-1 of ASCE 7-10 (Structural Engineers Association of California, 2012).

## 2.3 Green Roofs and Stormwater Retention Systems

A green roof is a roof of a building that is covered with vegetation. There are two characterizations of green roofs: extensive green roofs and intensive green roofs. Intensive green roofs use planting mediums that have a greater depth than extensive green roofs; this requires more maintenance because of the larger plant varieties intensive planting mediums can support. An extensive green roof has vegetation ranging from sedums to small grasses, herbs, and flowering herbaceous plants. Extensive green roofs are ideal for efficient stormwater management and low maintenance needs. An intensive green roof has vegetation ranging from herbaceous plants to small trees. Intensive green roofs require professional maintenance and advanced green roof irrigation systems. Rooftop farms fall under the intensive green roof

category. The growing medium for an extensive green roof is 6" or less, while the growing medium for an intensive green roof is greater than six inches (Jörg Breuning & Green Roof Service LLC, 2017). Green roofs have the ability to reduce urban heat islands and can also serve as a stormwater retention system.

#### 2.3.1 The Urban Stormwater Problem

Urban areas generate more stormwater runoff than natural areas due to a greater percentage of impervious roof surfaces and paved surfaces that prevent water infiltration. The United States Environmental Protection Agency (USEPA) concluded that a typical city block generates more than five times as much runoff than a woodlot of the same area. Additionally, urban stormwater runoff carries pesticides, heavy metals, and contaminated nutrients, which have the ability to flow into various bodies of water. According to USEPA, "The most recent National Water Quality Inventory reports that runoff from urbanized areas is the leading source of water quality impairments to surveyed estuaries and the third-largest source of impairments to surveyed lakes (Andresen, Fernandez, Rowe, Rugh, VanWoert & Xiao, 2004)."

#### 2.3.2 Green Roof Stormwater Retention Success

Implementing green roofs in urban areas is a solution to reduce stormwater runoff. The Michigan State University Horticulture Teaching and Research Center conducted a 14-month study in which three simulated roof platforms were constructed. One of the roof platforms contained gravel, the other was vegetated, and the third was non-vegetated. Over a 14-month period, the vegetated roof had the greatest overall rainfall retention at 60.6%, while the non-vegetated roof had rainfall retention of 50.4%, and the gravel roof had rainfall retention of 27.2%. These percentages refer to the amount of rainfall that did not runoff the roof out of total amount of rainfall in the 14-month period. To conclude, vegetated roof platforms retain greater quantities of stormwater than conventional roofs. However, the study stated, "if the objective of a green roof is to maximize rainfall retention, then factors such as slope and media depth must be addressed (Andresen, et. al., 2004)."

#### 2.3.3 Benefits of Green Roofs

Not only do green roofs control stormwater runoff, but their designs also have many other benefits (Andresen, et. al., 2004):

• Insulate buildings, which saves on energy consumption.

- Increase the lifespan of a typical roof by protecting the roof membrane from damaging ultraviolet rays, extreme temperatures, and rapid temperature fluctuations.
- Filter harmful air pollutants.
- Contribute to aesthetically pleasing environment to live and work by controlling the temperature of a building.
- Provide habitat for a variety of living organisms.
- Contribute to reducing the urban heat island effect.

#### 2.3.4 Structural Considerations

Similar to solar panels, green roofs contribute dead loads, live loads, snow loads, rain loads, wind loads, and seismic loads to the roof of a structure. The most contributing factor to the loads on a green roof depends on the size and type of vegetation, which is used. An intensive green roof contributes more load than an extensive green roof due to the larger trees, plants, and sometimes water features that are being used. Additionally, the location of the stormwater storage has an impact on the structure of a building. Depending on the green roof, stormwater can be stored within the green roof itself, in a tank below the building, or drained towards the local watershed.

The structural considerations for green roof design are typically attributed to the different components (layers) of green roofs. A typical, modern, vegetated roof requires a minimum of eight layers: plant level (vegetation), substrate layer, insulation layer, filter fabric, drainage layer, protection fabric, roof barrier, and waterproof layer as shown in Figure 1 (Gartner, 2008). To conclude, the overall design and layers of a green roof determine the effect of the various loads on the structure of a building.

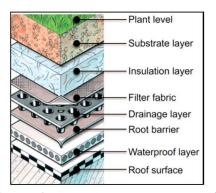


Figure 1: Layers of a Typical Modern Vegetated Roof (Gartner, 2008)

#### 2.4 Solar Collectors

Solar collectors convert energy from the sun into usable heat in a solar water heating system. This energy can be used for hot water heating, pool heating, space heating, or even air conditioning (Apricus Solar Water Company, 2017).

#### 2.4.1 Solar Collector Process

Solar collectors can be mounted on a roof, wall, or the ground. A circulation pump moves liquid through the collector, which then carries heat back to the solar storage tank. Throughout the day, water in the solar storage tank is heated up. When hot water is used, the solar preheated water is fed into the traditional water heater and supplied for its desired usage (Apricus Solar Water Company, 2017).

#### 2.4.2 Types of Solar Collector Technologies

There are three main types of solar collector technologies: evacuated tube solar collectors, flat plate solar collectors, and thermodynamic panels. Each of these technologies has different advantages and can be used for different types of applications.

Evacuated tube solar collectors are the most popular and commonly used solar collector technology. They are light and compact, making them easy to install. The tubes have excellent insulation and are virtually unaffected by air temperature. Out of all the types of solar collector technologies, evacuated tube solar collectors are the most efficient with a rate of efficiency of 70% per cent (Apricus Solar Water Company, 2017). The technology lasts for over 20 years, and the tubes can be replaced individually if one becomes faulty, avoiding the need to replace the whole collector. In terms of material, the tubes are either made out of double glass or a glassmetal combination. Double glass tubes have a reliable vacuum, but reduce the amount of light that reaches the absorber inside. Additionally, they may experience more absorber corrosion due to moisture or condensation forming in the non-evacuated area of the tube. The glass-metal combination tubes allow more light to reach the absorber and reduce the chances of moisture corroding the absorber. In an evacuated tube solar collector, water is heated in the collector and is sent through pipes to the water storage tank, where it is then distributed throughout the building.

Flat plate solar collectors are another type of solar collector technology. This technology has a life expectancy of over 25 years. In an area that produces an average level of solar energy,

the amount of energy a flat plate solar collector generates equates to around one square foot panel generating one gallon of one day's hot water. There are several different types of flat plate solar thermal technologies. The harp design is used in low-pressure thermos-syphon systems or pumped systems. The serpentine design uses a continuous S-shaped absorber and is used in compact hot water only systems, which do not utilize space heating. Flooded and boundary absorber systems use multiple layers of absorber sheet, where the heat is then collected in the boundary layer of the sheets. Polymer flat plate collectors are an alternative to metal plate collectors. Metal plates are more prone to freezing whereas the polymer plates themselves are freeze tolerant so they can dispense with antifreeze and use water as a heat transferring liquid. Polymer plates can be plumbed into an existing water tank, removing the need for a heat exchanger, which increases efficiency.

Thermodynamic panels are a new development in solar thermal technology. These panels are closely related to air source heat pumps in their design, but are deployed on the roof like regular solar collector panels, and do not have to be facing south. These panels can produce up to 100% of domestic heating needs. They also generate energy all year round since they do not rely on having optimal climate conditions to reach their maximum output potential. Thermodynamic panels act as a reverse freezer and do not use solar radiation to heat up heat transferring liquids. The panels have a refrigerant passing through them, which will absorb the heat. The heat that passes through the panel will then, in turn, become a gas. The gas is then compressed which raises its temperature, and it will then be passed on to a heat exchanging coil that is located within a hot water cylinder. The heated water in the cylinder is heated to 55°F and can then be distributed throughout the building.

#### 2.4.3 Structural Considerations

Solar collectors impose similar loads to the roof structure as solar panels: dead loads, snow loads, wind loads, and seismic loads. Solar collectors add dead loads as a result from the weight of the collector, the mounting hardware, and the collector fluid. Typically, the collector has a dead load of approximately three to five pounds per square foot, but the exact weight considerations can be obtained from the manufacturer of the solar collectors (HTP, 2017).

In areas prone to heavy snowfall, such as Massachusetts, snow loads need to be considered in the design of the solar tubes. Ideally, solar collectors should be installed at an angle of 50° or greater to promote snow sliding off the tubes (HTP, 2017). Similarly, when installing

solar tube collectors, wind and seismic resistance needs to be considered as well as the resultant stress on each of the attachment points. It is important to review the roof structure to ensure strength attachments of the solar collectors (HTP, 2017).

## 2.5 Types of Structural Reinforcements

Structural strengthening is used to reinforce structures due to deficiency, and to increase an existing element's capacity to carry new loads, such as sustainable rooftop technologies. As with any structure or method of reinforcement, it is necessary to first identify and establish a good understanding of the existing conditions through a structural condition assessment. The most common techniques to reinforce structural elements are mentioned below and classified into two different categories: passive systems and active systems. When selecting the appropriate strengthening method, it is important to consider the following factors: magnitude of strength increase, size of building and structures, environmental conditions, accessibility, construction, and maintenance and life cycle costs (Shaw, n.d.).

#### 2.5.1 Passive Systems

Passive systems do not introduce any forces to the structure; they contribute to the overall resistance of an element when it deforms. Section enlargement strategies are mostly used to improve strength, stiffness, and to reduce cracks. Some types of section enlargement strategies are: span shortening, externally bonded steel shapes, and epoxy injection (Shaw, n.d.).

Externally bonded fiber reinforced polymer (FRP) reinforcement is a method of reinforcement that involves adhering additional reinforcement to the exterior faces of an element. The success of this strengthening method depends on both the durability and lifespan of the reinforcement material, and the properties of the material used to attach the new reinforcement (usually epoxy material). This method, if adopted correctly and with the appropriate materials, is able to: reduce deflection, increase carrying capacity, increase flexural strength, and increase resistance to shear (Shaw, n.d.).

#### 2.5.2 Active Systems

Active strengthening systems are identified as additional external forces to structural elements, which can increase strength and improve the service performance. Service performance reduces tensile stress and cracking (Alkhrdaji & Thomas, 2017).

A post-tensioning system is an external force method which implements a structural member using high strength cables, bars, and strands. This system usually connects the reinforcement to the existing member at anchor points (typically at the end of the member). The reinforcement is profiled along the span at different locations (Shoultes, 2017).

## 3.0 METHODOLOGY

This chapter provides an overview of how the project was completed. The chapter provides information on how the buildings were selected, as well as the design and structural considerations for each sustainable technology.

## 3.1 Identify Buildings for Consideration

The first step of this project involved identifying buildings at WPI for the application of sustainable rooftop technologies. Online research was conducted to create a list of requirements for buildings to have in support of sustainable rooftop technologies. Additionally, an initial list of all 29 buildings at WPI was created with pertinent information on each building. The two lists were compared to identify the buildings, which satisfied the criteria outlined in the list of requirements for supporting sustainable rooftop technologies. Out of the original 29 buildings, 11 buildings were identified for further analysis for solar panel, green roof, or solar collector installation. Eight of the 11 buildings had the ability to support all types of technologies, while the other three buildings had the ability to support only solar panels and solar collectors, since their roofs are sloped and have no flat section for green roofs.

A meeting with WPI Director of Facilities Operations, Bill Spratt, was used to narrow down the list of 11 buildings. After discussions about energy demand and the availability of design drawings, the list was narrowed down to three buildings: Gordon Library, Stoddard B, and the Gateway Parking Garage. Gordon Library was chosen for the installation of a green roof since the rubber rooftop is flat and was recently renovated. A recently renovated roof provides suitable conditions for the installation of a green roof without concern for failure or maintenance of an old roof. Stoddard B was chosen for the installation of solar collectors since it is a residential building and requires hot water supply for the hospitality of its students. Additionally, the building has separately metered energy consumption and water demand values, which allows for the determination of the number of solar collectors to meet the water demand of the entire building. The Gateway Parking Garage was chosen for the installation of solar panels since the electric bill is lower than other buildings, which allows a sufficient number of solar panels to produce energy for the entire parking garage. Like Stoddard B, the Gateway Parking Garage also

has a separately metered energy consumption value, which allows for the determination for the number of solar panels to meet the energy demand for the entire parking garage.

# 3.2 Design and Analysis of Solar Panel Technology on Gateway Parking Garage

For the Gateway Parking Garage, a solar panel technology was chosen based on online research. First, different types of solar panels were researched, followed by research on different manufacturers of solar panels. A model was chosen based on sufficient energy production, allowing a minimal number of panels to produce energy for the entire garage. Additionally, low cost, low weight, and long lifespan were factors when choosing the solar panel manufacturer and model. Determining the cost of different models involved calling the manufacturer for quantitative information about the model.

# 3.2.1 Layout and Construction Process for Solar Panels on Gateway Parking Garage

Determining the layout of the solar panels involved calculating the number of solar panels needed to meet the energy demand value of the Gateway Parking Garage. The annual energy demand value of the Gateway Parking Garage was given by the WPI Facilities

Department. By dividing the annual energy demand value of the garage by the annual energy production value of one solar panel, the number of panels to produce energy for the entire structure was calculated. A rectangular area was chosen for design based on available space on the top level of the Gateway Parking Garage. The solar panels were designed to be a minimum of 10 ft above the garage floor to allow for clearance of vehicles. Additionally, the panels were proposed to be inclined at 10° above the horizontal which is the minimum and recommended angle for the solar panel model, as well as facing south to absorb the maximum amount of sunlight. The construction process for the panels, including safety precautions, module mounting, mounting configurations, and maintenance and cleaning was found on the manufacturer's website for the chosen solar panel model.

# 3.2.2 Structural Analyses and Design for Solar Panels on Gateway Parking Garage

After determining the layout and quantity of solar panels, a structural steel framework was designed to support all the solar panels. The initial design for the number of beams, girders,

and columns was proposed based on the total solar panel area and existing conditions of the chosen installation area on the top level of the Gateway Parking Garage. Through an iterative process the initial design was changed due to various factors.

#### 3.2.2.1 Solar Panel Load Calculations

The first step of the analysis involved considering all loads acting on the solar panels: dead load, live load, rain load, snow load, wind load, and seismic load. For solar panels, live load and rain load were considered negligible. Due to the 10° angle of the panels, all rain would runoff onto the parking garage floor and no ponding was expected. Live load was neglected since the solar panels are not designed for people to walk and operate on. Calculations for dead load, snow load, wind load, and seismic load are outlined in the sequence of tables below. ASCE 7-10 was used as a reference for these calculations, as well as solar photovoltaic array wind and seismic load documents from the Structural Engineers Association of California (Structural Engineers Association of California, 2012). The calculated design load values were input into the load combination equations outlined in the Step 5 table below. The governing load combination produced the largest load value, which would be used for application when designing the supporting steel framework. All load combination calculations were made in accordance with the Load and Resistance Factor Design (LRFD) method.

Step	Step 1: Dead Load of Solar Panels	
Variable:	Reference/Equation:	
Weight of Panel – lbs.	Obtained from Manufacturer's Website	
Number of Panels	Previously Determined Based on Energy Values	
Overall Weight of Panels – lbs.	Weight of Panel * Number of Panels	
Area of Panels – ft <sup>2</sup>	Determined Based on Dimensions and Number of Panels	
Dead Load – psf	Overall Weight of Panels/Area of Panels	

Step 2: Snow Lo	oad on Solar Panels
Variable:	Reference (ASCE 7-10)/Equation:
Thermal Factor (C <sub>t</sub> )	Table 7-3
Cold Roof Slope Factor (C <sub>s</sub> )	Section 7.4.2 (Fig. 7-2)
i. Roof Slope	Slope of Solar Panels = $10^{\circ}$
Exposure Factor (C <sub>e</sub> )	Table 7-2
Exposure Pactor (Ce)	0.9
: Tamain Catagony	Section 26.7
i. Terrain Category	Category B
Importance Factor (I.)	Table 1.5-2
Importance Factor (I <sub>s</sub> )	1.0
i Diele Catagowy	Table 1.5-1
i. Risk Category	Category II
Cround Snow Loads (a) not	Fig. 7-1
Ground Snow Loads $(\rho_g)$ - psf	50
Elet Doof Snow Load (a) 75f	Section 7.3
Flat Roof Snow Load $(\rho_f)$ - psf	$0.7 * C_e * C_t * I_s * \rho_g$
Slamed Doof Snovy Load (a) not	Section 7.4
Sloped Roof Snow Load (ρ <sub>s</sub> ) - psf	$C_s * \rho_f$

Step 3a: Wind Load on Solar Panels	
Variable:	Reference (ASCE 7-10)/Equation:
Risk Category	Table 1.5-1
	Category II
Basic Wind Speed (V) - mph	Fig. 26.5-1A
	120
Wind Directionality Factor (K <sub>d</sub> )	Table 26.6-1
	0.85
Exposure Category	Section 26.7
	Category B
Topographic Factor (K <sub>zt</sub> )	Section 26.8
Topographic Pactor (Kzt)	1.0
Gust Effect Factor (G)	Section 26.9
Gust Effect Factor (G)	0.85
Velocity Pressure Exposure Coefficient (K <sub>z</sub> )	Table 29.3-1
velocity Hessure Exposure Coefficient (Kz)	0.85
i Height shows ground level ft	Height of Gateway Parking Garage
i. Height above ground level - ft	60
Velocity Pressure (qz) - psf	Section 29.3.2
	$0.00256 * K_z * K_{zt} * K_d * V^2$

Step 3b: Wind Load on Solar Panels	
Reference (Wind Design for Low-Profile Solar P	hotovoltaic Arrays on Flat Roofs):
$A_{pv} \le h$ , therefore $A_{pv} =$	Lower Value of A <sub>pv</sub> and h
: Height of hailding (h) ft	Height of Gateway Parking Garage
i. Height of building (h) -ft	60
ii Width of building on longest side (WI) ft	Width of Gateway Parking Garage
ii. Width of building on longest side (WL) - ft	268
iii. $A_{pv}$ – ft	0.5 * SQRT(h * WL)
Normalized Wind Area (A <sub>n</sub> )	$(1000/A_{pv}^2)$ * Tributary Area of Beam
i. Tributary area of beam – ft <sup>2</sup>	Based on Design
ii. $A_{pv} \ge 15$ ft, therefore $A_{pv} =$	Greater Value of A <sub>pv</sub> and 15 ft
Nominal Net Pressure ((GC <sub>m</sub> ) <sub>nom</sub> )	Average of Two (GC <sub>m</sub> ) <sub>nom</sub> Values
i. Panel angle (ω) - °	Solar Panel Angle = 10°
:: (CC )	Fig. 29.9-1
ii. $(GC_m)_{nom}$ for $15^{\circ} \le \omega \le 35^{\circ}$	1.1
::: (CC )	Fig. 29.9-1
iii. $(GC_m)_{nom}$ for $0^{\circ} \le \omega \le 5^{\circ}$	0.75
Panel Chord Length Factor (V <sub>c</sub> )	$0.6 + (0.06 * l_p)$
: Chard langth of color manel (1) ft	Width of Solar Panel
i. Chord length of solar panel $(l_p)$ - ft	3.275
$V_p \le 1.3$ , therefore $V_p =$	Lower Value of $V_p$ and 1.3
i Mean parapat haight above roof curface (h.) ft	Average Height of Solar Panel Structure
i. Mean parapet height above roof surface $(h_{pt})$ - ft	20.384
ii. For $h_{pt} > 4$ ft, Parapet Height Factor $(V_p)$	$0.25 * h_{pt}$
Characteristic Height (h <sub>c</sub> ) – ft	$h_I + (l_p * SIN((\pi/180) * \omega))$
: Colon manual height shows most at law aday (h.) ft	Minimum Height of Solar Panel Structure
i. Solar panel height above roof at low edge $(h_1)$ - ft	10
ii. $h_1 \le 1$ ft, therefore $h_1 =$	Lower Value of h <sub>1</sub> and 1 ft
Array Edge Factor (E)	Fig. 29.9-1
	1.0
i. Horizontal distance from edge of panel to edge of roof $(d_x)$ – ft	1
ii. $d_x/h_c =$	$d_x/h_c$
Net Pressure Coefficient (GC <sub>m</sub> )	$V_p * E * (GC_m)_{nom} * V_c$
Design Wind Pressure (p) – psf	$q_z * GC_m$

Step 4a: Seismic Load for Solar Panels	
Variable:	Reference (ASCE 7-10)/Equation:
Risk-Targeted Maximum Considered Earthquake	Spectral Response Accelerations (MCE <sub>R</sub> ) - %g
: C 0/-	Fig. 22-1
i. S <sub>s</sub> - %g	18
:: C 0/ c	Fig. 22-2
ii. S <sub>1</sub> - %g	7
Soil Classification	Section 20
Soil Classification	Site D
Site Coefficients	
; [	Table 11.4-1
i. F <sub>a</sub>	1.6
ii. F <sub>v</sub>	Table 11.4-2
II. Fv	2.4
Spectral Response Acceleration Parameters	Section 11.4.3
i. S <sub>MS</sub>	$F_a * S_s$
i. S <sub>M1</sub>	$F_v * S_I$
Design Spectral Acceleration Parameters	Section 11.4.4
i. S <sub>DS</sub>	$2/3 * S_{MS}$
ii. S <sub>D1</sub>	$2/3 * S_{M1}$
Risk Category	Table 1.5-1
Risk Category	II
Seismic Design Category (SDC)	Table 11.6-1
Seisific Design Category (SDC)	B
Seismic Importance Factor (I <sub>e</sub> )	Table 1.5-2
Seisinic Importance Factor (1e)	1.0
Seismic Base Shear (V) - psf	Section 15.4.1.2
Seisinic Dase Shear (v) - psi	$0.3*S_{DS}*W*I_e$
i Type of structure	Section 15.4.1.2
i. Type of structure	Rigid Nonbuilding Structure
ii. Weight of structure (W) - psf	2.07

Step 4b: Seismic Load for Solar Panels	
Variable:	Reference (ASCE 7-10)/Equation:
Fundamental Period (T) – s	Section 12.8.2.1
	$C_t * h_n^x$
i. Type of structural system	Table 12.8-2
	All Other Structural Systems
:: C	Table 12.8-2
ii. C <sub>t</sub>	0.02
iii. x	Table 12.8-2
	0.75
iv Staniotymal haight (b) ft	Average Height of Solar Panel Structure
iv. Structural height (h <sub>n</sub> ) - ft	20.384
Vertical Distribution Factor (C.)	Section 12.8.3
Vertical Distribution Factor $(C_{vx})$	$(W_x * h_x)^k / (W_i * h_i)^k$
i, k	Section 12.8.3
1. K	1.0
ii. Weight of structure (W <sub>x</sub> /W <sub>i</sub> ) - psf	2.07
iii. Structural height (h <sub>x</sub> /h <sub>i</sub> ) - ft	20.384
Lateral Science Force (E.) mof	Section 12.8.3
Lateral Seismic Force $(F_x)$ - psf	$C_{ u x} * V$
Harizantal Cajamia Load Effect (E.) mof	Section 12.4.2.1
Horizontal Seismic Load Effect (E <sub>h</sub> ) - psf	$P*Q_e(Q_e=F_x)$
i. Redundancy Factor (ρ)	Section 12.3.4
	1.0
Vartical Sciencia Load Effect (E.) x-f	Section 12.4.2.2
Vertical Seismic Load Effect (E <sub>v</sub> ) - psf	$0.2*S_{DS}*D$

Step 5: LRFD Load Combinations per ASCE 7-10
1.4D
$1.2D + 1.6L + 0.5(L_r/S/R)$
$1.2D + 1.6(L_r/S/R) + (L/0.5W)$
$1.2D + 1.0W + L + 0.5(L_r/S/R)$
$1.2D + E_v + 1.0E_h + L + 0.2S$
0.9D + 1.0W
$0.9D + 1.0E_h$

#### 3.2.2.2 Supporting Beam Calculations

The second step of the analysis involved sizing the steel beams supporting the solar panels. The steel beams were sized based on the governing load acting on the beams, as well as the size of the area (tributary area) each beam needs to support. The calculation process was completed twice: once to size the interior beams and once to size the exterior beams. Calculations were made to size structural steel members in accordance with the AISC Manual. The beams were sized based on strength requirements, which included choosing an initial beam size based on the required plastic section modulus,  $Z_x$ , and then updating the calculations to include the self-weight of the chosen beam size. This was an iterative process, and the tables below show the calculation process for choosing a beam size. In addition, flange local buckling and web local buckling were checked to ensure no buckling occurs within the chosen beam size.

Step 1:	Step 1: Initial Beam Size	
Variable:	Reference/Equation:	
Tributary Width of Beams - ft	Based on Design	
w <sub>u</sub> - k/ft	Governing Load * Tributary Width * (k/1000 lb.)	
Length of Beam (L) - ft	Based on Design	
Moment (M <sub>u</sub> ) – k*ft	$(w_u * L^2)/8$	
Steel Yield Strength (F <sub>y</sub> ) - ksi	50 (A992 Steel)	
Uncertainty Coefficient (Ø)	0.9	
Plastic Section Modulus (Z <sub>x</sub> ) – in <sup>3</sup>	$M_{u}/(\emptyset * F_{y})$	
Select Beam Size $Z_x \ge$ Calculated $Z_x$	AISC Table 3-2	

Step 2: Check Weigh	Step 2: Check Weight of Selected Beam Size	
Variable:	Reference/Equation:	
Selected Beam Weight - lb./ft	AISC Table 3-2	
$w_u$ - $k/ft$	Step 1 $w_u$ + 1.2 * Beam Weight * ( $k$ /1000 lb.)	
Moment $(M_u) - k*ft$	$(w_u * L^2)/8$	
Plastic Section Modulus $(Z_x) - in^3$	$M_{u}/(\emptyset * F_{y})$	
Check if Calculated $Z_x \le$ Selected Beam $Z_x$	AISC Table 3-2	

Step 3: Flange Local Buckling	
Variable:	Reference/Equation:
$b_{\rm f}/2t_{\rm f}$	AISC Table 1-1
Young's Modulus (E) - ksi	29,000 (A992 Steel)
Steel Yield Strength (F <sub>y</sub> ) - ksi	50 (A992 Steel)
Limit Value	$0.38 * SQRT(E/F_y)$
$b_f/2t_f \le Limi$	t Value

Step 4: Web Local Buckling	
Variable:	Reference/Equation:
h/t <sub>w</sub>	AISC Table 1-1
Young's Modulus (E) - ksi	29,000 (A992 Steel)
Steel Yield Strength (Fy) - ksi	50 (A992 Steel)
Limit Value	$3.76 * SQRT(E/F_y)$
$h/t_w \leq Limit \\$	Value

In addition to strength requirement, the steel beam sizes were selected based on serviceability. The selected beam size was checked for total service load and snow deflection. If the selected beam size did not pass these serviceability requirements, then a different beam size was chosen to satisfy serviceability. The deflection limits for serviceability were set based on the requirements in the International Building Code (IBC) which states: a roof beam supporting a plaster ceiling (similar to solar panels) must have a maximum total deflection = L/240, and a maximum snow load deflection = L/360 or 1" (International Building Code, 2014). The tables below show the calculation process for checking the serviceability of the beam size.

Step 5: Total Service Load	
Variable:	Reference/Equation:
Selected Beam Weight - lb./ft	AISC Table 3-2
w <sub>T</sub> - lb./ft	((DL + SL) * Tributary Width) + Weight of Beam
Young's Modulus (E) - psi	29,000,000 (A992 Steel)
Moment of Inertia $(I_x) - in^4$	AISC Table 3-3
Total Deflection - in	$(5*w_T*L^4)/(384*E*I_x)$
Limit Value - in	(L * 12 in/ft)/240
То	tal Deflection ≤ Limit Value

Step 6: Snow Deflection	
Variable:	Reference/Equation:
w <sub>s</sub> - lb./ft	SL*Tributary Width
Young's Modulus (E) – psi	29,000,000 (A992 Steel)
Moment of Inertia $(I_x) - in^4$	AISC Table 3-3
Snow Deflection – in $ (5 * w_s * L^4)/(384 * E * I_x) $	
Limit Value – in	(L * 12 in/ft)/360 or 1 in
Snow Deflection ≤ Limit Value	

3.2.2.3 Laterally Unsupported Beams

The next step involved checking the laterally unsupported distance of the beams to see if they needed additional support by adding more girders. This step was completed as an investigation for lateral-torsional buckling within the beam member. This process was completed for both the interior and exterior beam sizes, as well as the two different beam spans: 45.69 ft and 28.21 ft. After analysis, it was concluded that the original unbraced length for the beams that span 45.69 ft was too large and had to be decreased. This required changing the design by adding more girders to support the beams and reduce the unbraced length. The calculation process is outlined in the tables below.

Step 1: Unbraced Length Determination	
Variable:	Reference:
Plastic Length (L <sub>p</sub> ) - ft	AISC Table 3-2
Lateral-Torsional Buckling Moment Unbraced Length (L <sub>r</sub> ) - ft	AISC Table 3-2
Actual Unbraced Member Length (Lb) - ft	Distance Between Supporting Girders

Step 2: Calculation of Moment Capacity (M <sub>n</sub> )		
Variable:	Reference/Equation:	
If $L_b \le L_p < L_r$ : Plastic Behavior (Zone 1)		
Moment Capacity (M <sub>n</sub> ) – k*ft	$F_y * Z_x$	
i. Steel Yield Strength (F <sub>y</sub> ) - ksi	50 (A992 Steel)	
ii. Plastic Section Modulus $(Z_x) - in^3$	AISC Table 3-2	
If $L_p < L_b < L_r$ : Inelastic Buckling (Zone 2)		
Moment Capacity (M <sub>n</sub> ) – k*ft	$M_p$ - $(M_p - M_r) * ((L_b - L_p)/(L_r - L_p))$	
i. Plastic Strength (M <sub>p</sub> ) – k*ft	$F_y * Z_x$	
ii. Moment Capacity Between Inelastic and Elastic LTB $(M_r) - k*ft$	$0.7*F_y*S_x$	
iii. Elastic Section Modulus $(S_x) - in^3$	AISC Table 1-1	
If $L_p < L_r \le L_b$ : Elastic Buckling (Zone 3)		
Moment Capacity (M <sub>n</sub> ) – k*ft	$((C_b * \pi^2 * E)/(L_b/r_{ts})^2) * sqrt(1 + (0.078 * (J_c/(S_x * h_o)) * (L_b/r_{ts})^2) * S_x$	
i. $r_{ts}$ , $J_c$ , $S_x$ , $h_o$	AISC Table 1-1	
ii. C <sub>b</sub>	1	
iii. Young's Modulus (E) - ksi	29,000 (A992 Steel)	

Step 3: Unbraced Length Check	
Variable:	Reference/Equation:
$ \emptyset M_n - k*ft $	$0.9*M_n$
Previously Calculated Beam Moment (M <sub>u</sub> ) – k*ft	$(w_u*L^2)/8$
If $M_u \leq \emptyset M_n$	Adequate Unbraced Length
If $M_u > \emptyset M_n$	Decrease Unbraced Length

# 3.2.2.4 Supporting Girder Calculations

The calculation process for determining the girder sizes was the same as the process for determining the beam sizes. Strength and serviceability requirements were checked, and all calculations were made with the assistance of the AISC Manual. All girders were initially chosen to be the same size. Later in the design process, the software RISA was used to perform a structural analysis of the steel framework. A smaller moment value than originally calculated was acting on the girder, allowing for a smaller girder size to be chosen. However, one girder size remained the initial size due to its tributary width, which did not satisfy the snow deflection limit.

# 3.2.2.5 Laterally Unsupported Girders

The calculation process for checking the laterally unbraced length of the girders was the same as the process for checking the laterally unbraced length of the beams. This step was completed as an investigation for lateral-torsional buckling within the girder member. After analysis, it was concluded that the original unbraced length for the girders was too large and had to be decreased. This required changing the design by adding more beams to support the girders and reduce the unbraced length.

#### 3.2.2.6 Supporting Column Calculations

The next step involved determining the supporting steel column sizes. This process was completed with the assistance of the AISC Manual. The size of the column depends on the column's length and the load acting on the column. After analysis, all of the supporting eight columns were sized to be the same. The calculation process for determining the column size is shown in the table below.

Column Size Determination	
Variable:	Reference:
Length of Column (L) - ft	Based on Design of Steel Structure
Available Strength of Axial Compression (Ø <sub>c</sub> P <sub>n</sub> ) - k	AISC Table 4-1a
Load Acting on Column (Pu) - k	Calculated During Analysis
$\emptyset_{c}P_{n} \geq P_{u}$	Adequate Column Size

#### 3.2.2.7 Second-Order Elastic Analysis

The next step involved using the structural analysis software, RISA, to determine member forces and lateral sway  $\Delta H$  for the following LRFD load combination equation for gravity loads:

$$U = 1.2D + 1.6S + 0.5W$$

The horizontal seismic load was also accounted for as the lateral force acting on the steel frame. Dead, snow, and wind loads acting on each column were calculated, as well as the horizontal seismic load. In addition to the given load information, the size of all girders and columns previously calculated were inputted into the software. The design of the frame was checked for stability per Chapter C of *AISC Specification*.

After inputting the appropriate information, the output from the RISA structural analysis was used to perform an approximate second-order analysis to assess the adequacy of the selected column section for the combination of gravity and lateral loads. The approximate second-order analysis was based on Appendix 8 to *AISC Specification*. The calculation process and evaluation for performing an approximate second-order analysis to assess the adequacy of the column size is located in the tables below. This analysis resulted in the use of the interaction equation (AISC Equation H1-1) to check for combined bending and compression of the column member. From the RISA analysis, the moment obtained from the connection of the column and girder was smaller than the moment value used to design the original girder. Therefore, calculations were made to determine a new girder size smaller than the initial girder size.

Step 1: Column Load Effects from RISA Analysis	
Variable:	Units:
Factored Axial Force P <sub>nt</sub> from No-Sway Analysis (Gravity Loads)	k
Factored Axial Force Plt from Sway Analysis (Lateral Loads)	k
Factored Moment M <sub>nt</sub> from No-Sway Analysis (Gravity Loads)	k*ft
Factored Moment M <sub>lt</sub> from Sway Analysis (Lateral Loads)	k*ft

Step 2: Lateral Deflection from RISA Analysis	
Variable:	Units:
Total Story Shear ΣH	k
Lateral Deflection (drift) for Story ΔH	in

Step 3: Amplifier B <sub>2</sub>	
Variable:	Reference/Equation:
Total Elastic Critical Buckling Load for the Story (P <sub>estory</sub> ) – k	
where $R_m = 0.85$ (conservative)	$(R_m * \Sigma H * L)/\Delta H$
L = frame height	
Total Vertical Load Supported by the Story (P <sub>story</sub> ) – k	Calculated from RISA
Amplifier $B_2 \ge 1$	$1/(1-(P_{story}/P_{estory}))$

Step 4: Amplifier B <sub>1</sub>	
Variable:	Reference/Equation:
Smaller Factored Column End Moment due to Gravity Load (No Sway) Analysis: M <sub>1</sub>	Units: k*ft
Larger Factored Column End Moment due to Gravity Load (No Sway) Analysis: M <sub>2</sub>	Units: k*ft
Indicate: Single or Reverse Curvature	Single Curvature: + Reverse Curvature: -
Cm (+ for Single Curvature; - for Reverse Curvature)	$0.6 \pm 0.4 (M_1/M_2)$
Required Second-Order Axial Strength (P <sub>r</sub> ) – k	$P_{nt} + (B_2 * P_{lt})$
Elastic Critical Buckling Load for Column (Pel) - K <sub>1</sub> = 1.0	$(\pi^2 * E * I)/(K_1 * L)^2$
Amplifier $B_1 \ge 1$ ( $\alpha = 1.0$ for LRFD)	$C_m/(1-(\alpha*P_r)/P_{el})$

Step 5: Required Second-Order Strength Values	
Variable:	Equation:
Required Second-Order Axial Strength (Pr) - k	$P_{nt} + B_2 * P_{lt}$
Required Second-Order Moment Capacity (M <sub>r</sub> ) – k*ft	$B_1*M_{nt}+B_2*M_{lt}$

Step 6: Effective Length Factor K for Moment Frame	
Variable:	Reference/Equation:
Rotational Resistance at the Top Joint (G <sub>t</sub> )	$\Sigma (I,I) \Sigma (I,I)$
Rotational Resistance at the Bottom Joint (G <sub>b</sub> )	$\sum (I_c/L_c)/\sum (I_g/L_g)$
Effective Length Factor (K <sub>x</sub> )	AISC Fig. C-A.7.2. Alignment Chart Sidesway
Modified Effective Length Factor (K*x)	$Kx * SQRT(1 + \sum Pleaning / \sum Pstability)$
$\Sigma$ Pleaning/ $\Sigma$ Pstability = 3.5	Kx + SQKI(1 + \(\sigma\)Fstability)

Step 7: Axial Capacity Pc	
Variable:	Reference/Equation:
Slenderness Ratio (x)	$(K^*_x * L)/r_x$
Slenderness Ratio $(y) - K_y = 1.0$	$(K_y * L)/r_y$
Limit Value	$4.71 * SQRT(E/F_y)$
Governing $(K*L)/r \le Limit Value$	Short to Intermediate Column
Governing (K*L)/r > Limit Value	Long Column
Available Axial Strength ( $P_c = \emptyset_c P_n$ )	AISC Table 4-1a
$P_r/P_c \ge 0.2$	AISC Equation H1-1a
$P_r/P_c < 0.2$	AISC Equation H1-1b

Step 8: Bending Moment Capacity & Interaction Equation	
Variable:	Reference/Equation:
Web Local Buckling	$h/t_w \le 90.5$
Flange Local Buckling	$b_f/2t_f \leq 9.2$
Lateral Bracing (Lb) - ft	Column Length
Plastic Length $(L_p)$ – ft	AISC Table 3-2
Lateral-Torsional Buckling Moment Unbraced Length (L <sub>r</sub> ) - ft	AISC Table 3-2
Nominal Flexural Strength $(M_n)$ $L_b \le L_p - k*ft$	AISC Equation F2-1
Nominal Flexural Strength (M <sub>n</sub> ) $L_p \le L_b \le L_r - k*ft$	AISC Equation F2-2
Nominal Flexural Strength $(M_n)$ $L_b > L_r - k*ft$	AISC Equation F2-3
Available Bending Capacity (M <sub>cx</sub> ) – k*ft	$\emptyset * M_n$
i. Uncertainty Constant (Ø)	0.9
AISC Equation H1-1a	$P_r/P_c + (8/9) * (M_{rx}/M_{cx})$
AISC Equation H1-1b	$P_r/2P_c + (M_{rx}/M_{cx})$
If AISC Equation H1-1 ≤ 1	Adequate Column Size

#### 3.2.2.8 Baseplate Design

Baseplates were designed to connect each steel column to a 2 ft x 2 ft concrete column at a height of 3.67 ft. Out of the eight steel columns, three of them already have existing supporting concrete columns on the top level of the Gateway Parking Garage. The design proposal involves constructing five more of these concrete columns to provide support for each steel column. The baseplates were designed based on the load and moment acting on the concrete column. The dimensions and thickness of each A36 baseplate was determined. When determining the thickness of the baseplate, the largest load and moment values acting on the concrete columns from the RISA Analysis were chosen for analysis. This provided a minimum baseplate thickness, which would be suitable for each steel and concrete column connection. All calculations are located in the tables below.

Step 1: Footing Area and Minimum Baseplate Area	
Variable:	Reference/Equation:
Load Acting on Concrete Column (Pu) - k	Previously Calculated $P_u$ + Column Weight * Column Length
Moment Acting on Concrete Column (M <sub>u</sub> ) – k*ft	RISA Analysis
Footing Area $(A_2) - in^2$	Area of Concrete Column
Minimum Baseplate Area (A <sub>1</sub> min) – in <sup>2</sup>	$b_f * d$
i. Column Size b <sub>f</sub> , d	AISC Table 1-1
$sqrt(A_2/A_1 min) \leq 2$	

Step 2: Baseplate Dimensions		
Variable:	Reference/Equation:	
Baseplate Area $(A_1) - in^2$	$P_{u}/(\emptyset_c * 0.85 * f'_c * SQRT(A_2/A_1))$	
i. Concrete Strength (f'c)	Based on Type of Concrete	
ii. Ø <sub>c</sub>	0.65	
$A_1 \ge A_1 \min$		
$\Delta$ - in	$(0.95d - 0.8b_f)/2$	
Baseplate Dimension (N) - in	$SQRT(A_I) + \Delta$	
Baseplate Dimension (B) - in	$A_{I}/N$	
$\mathcal{O}_{c}P_{p}$ - k	$\emptyset_c * 0.85 * f_c * A_1 * SQRT(A_2/A_1)$	
$\mathcal{O}_{c}P_{p} \geq P_{u}$		

Step 3: Moment-Resisting Baseplate Thickness	
Variable:	Reference/Equation:
Eccentricity (e) - in	$(M_u*(12 in/ft))/P_u$
i. Largest Moment from Risa Analysis (M <sub>u</sub> ) - k*ft	18.8
ii. Largest Axial Load from Risa Analysis (Pu) - k	49.36
Strength at Each Flange Edge of Baseplate (f) - ksi	$(-P_u/A) \pm ((P_u * e * c)/I)$
i. Baseplate Area (A) – in <sup>2</sup>	B * N
ii. Variable c - in	0.5 * N
iii. Moment of Inertia (I) – in <sup>4</sup>	$(1/12) * B * N^3$
Moment to Right at Center of Right Flange (Mu) - k*in	$(f_{CRF} * d * (d/2)) + ((f_{-}f_{CRF}) * d * ((2/3) * d))$
i. Strength (f <sub>CRF</sub> ) - ksi	Strength at Center of Right Flange
ii. Distance (d) - in	Distance from Edge of Baseplate to Center of Right Flange
Minimum Thickness (t) - in	$sqrt((6 * M_u)/(\emptyset_b * F_y))$
i. Coefficient Ø <sub>b</sub>	0.9
ii. Yield Strength of Baseplate (F <sub>y</sub> ) - ksi	36 (A36 Steel)
Average Baseplate Strength (fp) - ksi	$(\min f + \max f)/2$
n - in	$(B - 0.8 * b_f)/2$
Bending Moment in Transverse Direction (M <sub>u</sub> ) - k*in	$f_p * n * (n/2)$
Bending Moment in Transverse Direction (M <sub>u</sub> ) < Moment to Right at Center of Right Flange (M <sub>u</sub> )	
Choose Baseplate Thickness Greater than Calculated Minimum Thickness (t)	

#### 3.2.2.9 Recalculation of Seismic Load

At this point in the process, the entire supporting steel structure has been designed and the seismic load was recalculated. According to ASCE 7-10, the superimposed weight of the designed structure must be less than 25% of the current structure weight. This check was done to assess the impact of the designed structure to the existing parking garage structure. The weight of the steel structure as well as the weight of the top floor of the Gateway Parking Garage were calculated to verify this weight requirement. Satisfaction of the weight requirement involved using new equations to calculate the new horizontal and vertical seismic loads. This calculation process is outlined in the tables below. These new seismic load values were plugged into the RISA analysis to check for adequacy of the column sizes. Additionally, the new seismic load values were used to check their effect on the original beam and girder design. After analysis, it was concluded that the updated seismic loads do not have a large impact on the steel framework design, and therefore does not need to be changed for the updated seismic changed for the updated seismic loads.

Step 1: Designed Structure Weight ≤ 25% of Current Structure	
Variable:	Reference/Equation:
Area of Top Floor of Garage – ft <sup>3</sup>	Length * Width * Floor Thickness
Weight of Top Floor of Garage - k	Weight of Concrete * Area
Weight of Selected Beams – lb.	$\sum$ Weight of Beam * Length of Beam
Weight of Selected Girders – lb.	$\sum$ Weight of Girder $*$ Length of Girder
Weight of Selected Columns – lb.	$\sum$ Weight of Column * Length of Column
Combined Weight of Selected Members - k	(Weight of Beams + Weight of Girders + Weight of Columns) * (k/1000 lb.)
Combined Weight of Selected Members ≤ 0.25*Weight of Top Floor of Garage	ASCE 7-10 Section 15.3.1

Step 2: Horizontal Seismic Load (Fp) & Vertical Seismic Load (Fv)	
Variable:	Reference/Equation:
Horizontal Seismic Force (F <sub>p</sub> ) - psf	$((0.4 * a_p * S_{DS} * W_p)/(R_p/I_p)) * (1+(2 * (z/h)))$
i. Spectral Acceleration (S <sub>DS</sub> )	ASCE 7-10 Section 11.4.1
ii. Component Amplification Factor (a <sub>p</sub> )	ASCE 7-10 Table 15.1
iii. Component Importance Factor (I <sub>p</sub> )	ASCE 7-10 Section 13.1.3
iv. Component Operating Weight (W <sub>p</sub> ) - psf	Combined Weight of Selected Members * (1000 lb./k) * (1/Solar Panel Area) + Solar Panel Dead Load
v. Component Response Modification Factor (R <sub>p</sub> )	ASCE 7-10 Table 13.5-1
vi. Height of Attachment Roof (z) - ft	Height of Gateway Parking Garage
vii. Average Roof Height of Structure with Respect to the Base (h) - ft	Average Height of Solar Panel Structure
Lower Limit - psf	$0.3*S_{DS}*I_p*W_p$
Upper Limit - psf	$1.6*S_{DS}*I_p*W_p$
Vertical Seismic Force (F <sub>v</sub> ) - psf	$0.2*S_{DS}*W_p$

#### 3.2.2.10 Reinforcement in 2 ft x 2 ft Concrete Columns

The final step involved designing reinforcement in the 2 ft x 2 ft concrete columns, which support the columns of the steel structure. The size and number of reinforcing steel bars depended on the interaction of axial force and bending moment acting on the concrete columns. Additionally, the size of the steel ties that wrap around the reinforcing steel bars was determined based on the geometry of the concrete column, as well as the diameter and spacing of the reinforcing steel bars. After analysis, it was determined that all eight concrete columns require the same type and size of reinforcement. The calculations are outlined in the tables below.

Step 1: Determination and Evaluation of Reinforcement Ratio pg	
Variable:	Reference/Equation:
Axial Force Acting on Concrete Column (Pu) - k	Risa Analysis
Moment Acting on Concrete Column (M <sub>u</sub> ) – k*ft	Risa Analysis
K <sub>n</sub> Value	$P_{\iota\prime}/(\not O * f_c * A_g)$
R <sub>n</sub> Value	$M_{u}/(\emptyset * f_c * A_g * h)$
p <sub>g</sub> Value	Concrete Column Strength Interaction Diagram
p <sub>min</sub> Value	$(3 * SQRT(f_c))/F_y$
i. Concrete Strength (f'c) - psi	Depends on Type of Concrete
ii. Steel Yield Strength (F <sub>y</sub> ) - psi	Depends on Type of Reinforcing Steel
$p_{\rm max}$ Value	$0.85 * B_1 * (f_o/F_y) * (\varepsilon_u/(\varepsilon_u + 0.004))$
i. B <sub>1</sub> Value	Depends on Type of Concrete
ii. Concrete Strain (ε <sub>u</sub> )	Depends on Type of Concrete
$p_{\min} < p_{ m g} < p_{\max}$	

Step 2: Determination of Steel Reinforcement Bars and Steel Ties	
Variable:	Reference/Equation:
Area of Steel $(A_s)$ – $in^2$	$p_g * A_g$
i. Gross Area of Concrete (A <sub>g</sub> ) – in <sup>2</sup>	Area of Concrete Column
Diameter of Steel Reinforcement Bars (d <sub>b</sub> ) - in	$sqrt(A_s/((\pi/4) * N)$
i. Number of Steel Reinforcement Bars (N)	Based on Chosen Design
Diameter of Steel Ties (d <sub>s</sub> ) - in	$2*Cover + 2*d_s + yb + d_b = h$
i. Cover = Distance from Concrete Edge to Steel Tie - in	Based on Chosen Design (Typically ≥ 1.5 in)
ii. Distance Between Center of Steel Reinforcement Bars (γb) - in	$(\gamma = 0.60) * (b = Length of Concrete Column)$
iii. Width of Concrete Column (h) – in	Based on Concrete Column Width

# 3.3 Design and Analysis of Green Roof Technology on Gordon Library

The Gordon Library was selected to have a green roof technology. A research of the different types of green roofs was done together with the benefits of each technology. An extensive green roof system was chosen based on the structure of the building, the accessibility to the roof, and due to the system's low maintenance costs.

## 3.3.1 Layout and Construction Process for Green Roof on Gordon Library

To determine the layout of the roof garden on the Gordon Library, it was necessary to consider the layout of the roof and all the elements that comprise it. A green roof system is easily implemented on flat roofs that have plenty of open space and a sufficient area. Although much of the roof is open, a penthouse structure is located in the middle of the roof. The garden area chosen includes an area surrounding the penthouse, leaving a path for maintenance in the middle of the roof and leaving the edges of the roof open.

#### 3.3.2 Structural Analyses and Design for Green Roofs

After determining the layout and the total area of the green roof, an analysis of the loads and capacity of the columns and slabs of the building was conducted. The analysis included the feasibility to impose an extra load on the roof of the building without causing any structural damage. This also involved investigating the impact to the building's seismic capacity.

#### 3.3.2.1 Green Roof Load Calculations

Similar to the Solar Panels load calculations, Section 3.2.2, an analysis of the loads acting horizontally and vertically on the Gordon Library was conducted. The analysis considered dead load, live load, rain load, snow load, wind load, and seismic load. Roof live loads and rain loads were not neglected for this case because of their significant load value, and they were calculated with reference to ASCE 7-10 and the *International Building Code* (IBC). Calculations for all these loads are shown in the tables below. Values for all equations and factors are also shown in the tables. ASCE 7-10 and IBC were used as a reference for these calculations, as well as the *Massachusetts Building Code*. The governing load combination produced by the loads acting on the system was used to determine if the strength capacity of the columns and the two-way slab was sufficient. All load combination calculations were made in accordance with the Load and Resistance Factor Design (LRFD) method.

Step 1: Dead Load of Building	
Variable:	Reference/Equation:
Weight of Green Roof- psf.	Obtained from System Selected (Extensive Green Roof)
Overall Weight of Building – lbs.	Determined from Structural and Architectural Drawings of Building (Excel Spreadsheet created to determine weight of each floor)
Weight of Building - psf.	Overall Weight of Building per floor/ area of floor
Mechanical/Electrical/Plumbing (MEP) –psf.	Determined from Research and Assumptions
Dead Load - psf	Sum of all dead loads in pounds per square feet.

Step 2: Live Load on Gordon Library	
Variable:	Reference (ASCE 7-10) / Equation:
Estimated area of occupancy per floor based on usage	Table 4-1
Live Load – psf.	Live load Occupancy Diagram for Building $^{\it l}$

36

<sup>&</sup>lt;sup>1</sup> Live loads will vary for each floor based on occupancy areas (See Appendix C.1 and C.5 for a detailed representation of live loads in Gordon Library)

Step 3: Snow Load on Roof	
Variable:	Reference (ASCE 7-10)/Equation:
Thermal Factor (C <sub>t</sub> )	Table $7-3 = 1.0$
Cold Roof Slope Factor (C <sub>s</sub> )	Section 7.4.2 (Fig. 7-2)
Exposure Factor (C <sub>e</sub> )	Table $7-2 = 0.9$
i. Terrain Category	Section $26.7 = B$
Importance Factor (I <sub>s</sub> )	Table $1.5-2 = 1.10$
i. Risk Category	Table 1.5-1 = III
Ground Snow Loads (pg) - psf	Fig. $7-1 = 50$
Flat Roof Snow Load (ρ <sub>f</sub> ) - psf	Section 7.3
	$\rho_{\rm f} = 0.7 * Ce * Ct * Is * \rho_{\rm g}$
	$\rho_{\rm f} = 34.65 \; \rm psf$

Step 4: Rain Load on Roof	
Variable:	Reference (FM Global Data Sheets) / Equation:
Minimum rain load - psf.	DS 1-54/ Section 2.5.2.8 =32 psf

Step 5: Wind Load Acting Horizontally on Building				
Variable:	Reference (ASCE 7-10)/Equation:			
Risk Category	Table 1.5-1 = III			
Basic Wind Speed (V) - mph	Fig. 26.5-1A/780 CMR 1609 = 134mph			
Wind Directionality Factor (K <sub>d</sub> )	Table $26.6-1 = 0.85$			
Exposure Category	Section $26.7 = B$			
Topographic Factor (K <sub>zt</sub> )	Section 26.8 = 1.0			
Gust Effect Factor (G)	Section $26.9 = 0.85$			
Velocity Pressure Exposure Coefficient (K <sub>z</sub> ) <sup>2</sup>	Table 29.3-1			
i. Height above ground level - ft	Height of Gordon Library from Ground Level = 59.5 ft.			
Velocity Pressure (q <sub>z</sub> ) - psf <sup>3</sup>	Section 29.3.2			
Velocity Flessure $(q_z)$ - psi	$0.00256*K_z*K_{zt}*K_d*V^2=33.13$			
Main Wind Frame Resis	tance System			
Internal Pressure Coefficient (GC <sub>pi</sub> ) <sup>4</sup>	Table $26.11-1 = \pm 0.18$			
External Pressure Coefficient (C <sub>p</sub> )	Figure 27.4-1			
i. Windward Wall	Cp = 0.8			
ii. Leeward Wall (North-South) <sup>5</sup>	Cp = -0.33			
iii. Leeward Wall (East-West)	Cp = -0.5			
Wind Pressure on Parapets	Section 27.4.5			
i. Combined Net Pressure Coefficient (GC <sub>pn</sub> )	+1.5 for windward parapet -1.0 for leeward parapet			
	Equation 27.4-4			
ii. Wind Pressure at Parapet	$p_p = q_p(GC_{pn})$ Equation 27.4-1			
Design Wind Pressure (p)	$p = qGC_p - qi(GC_{pi})$			
Components and Clade				
External Pressure Coefficient (GCp)	Figure 30.4-1 & Figure 30.4-2 <i>ASCE 7-10</i>			
i. Zone 4 <sup>6</sup>				
ii. Zone 5	Figure 30.4-1 <i>ASCE 7-10</i>			
iii. Zone 1				
iv. Zone 2				
v. Zone 3	Figure 30.4-2 <i>ASCE 7-10</i>			
vi. 10 Percent of Least Horizontal Dimension (a)	a = 9.87  ft			

<sup>&</sup>lt;sup>2</sup> Values for K<sub>z</sub> vary along the height of the building, see ASCE 7-10, Table 29.3-1 for values at z height.

<sup>&</sup>lt;sup>3</sup> This velocity pressure value is considered at the top of the parapet of the building. Values at each story level will vary.

<sup>&</sup>lt;sup>4</sup> Negative values indicate pressure acting away from the building <sup>5</sup> Values may be linearly interpolated from ASCE 7-10, Figure 27.4-1

<sup>&</sup>lt;sup>6</sup> Each zone will have a positive and negative value to consider for (GC<sub>p</sub>)

The tables presented below (Table 2 and 3) were created to demonstrate the typical values for each zone of the building as mentioned in Chapter 30 of the ASCE 7-10. These negative and positive values for GCp and GCpi were taken from the different tables in the chapter. In addition, these values were used with the wind force at the leeward side of the building to obtain the maximum force that cladding and components of the building can withstand,

Table 2: GCp Values from ASCE 7-10 for Each Zone in Gordon Library

GCp Table (Figures ASCE 7-10)										
AREA (SF)	ZO	NE 1	ZO	NE 2	ZO	NE 3	ZON	VE 4	ZON	NE 5
AREA (SF)	+	ı	+	-	+	-	+	-	+	-
$\leq 10 \text{ ft}^2$	0.3	-1	0.3	-1.8	0.3	-2.8	1	-1.1	1	-1.4
$\geq 500 \text{ ft}^2 \text{ walls } \&$ $\geq 100 \text{ ft}^2 \text{ roof}$	0.2	-0.9	0.2	-1.1	0.2	-1.1	0.7	-0.8	0.7	-0.8

Table 3: GCpi Values from ASCE 7-10 for Each Zone in Gordon Library

GCp +/- GCpi Table										
AREA (SF)	ZO	NE 1	ZO	NE 2	ZO	NE 3	ZON	VE 4	ZON	NE 5
AREA (SF)	+	1	+	-	+	1	+	-	+	-
$\leq 10 \text{ ft}^2$	0.48	-1.18	0.48	-1.98	0.48	-2.98	1.18	-1.28	1.18	- 1.58
$\geq 500 \text{ ft}^2 \text{ walls &}$ $\geq 100 \text{ ft}^2 \text{ roof}$	0.38	-1.08	0.38	-1.28	0.38	-1.28	0.88	-0.98	0.88	- 0.98

Figure 2 illustrates the wind forces acting on a building with a flat roof, similar to the Gordon Library. For simplicity of calculations for the Main Wind Force Resisting System (MWFRS), it can be assumed that the interior wind forces cancel each other as they have the same value going in opposite directions. This is the influence of factor GCpi in the design of wind pressure equation shown in the table above.

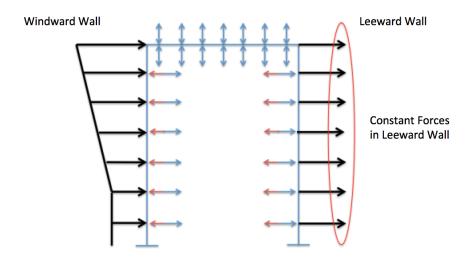


Figure 2: Wind Pressure Diagram for Flat Roof Building

Similarly, Figure 2 above shows the direction of the wind forces and their distribution based on the wall being analyzed. The windward wall, as shown in the figure, has a varying wind force along the height of the building until it reaches a constant wind force at elevations less than 15 feet. The leeward wall has a constant, outward wind force acting along its height. In addition, the weight of the building is different that the actual dead load because the total weight was considered for seismic load purposes as an "effective seismic weight" as illustrated in Step 6 below.

Step 6: Seismic Load Acting Horizontally on Building				
Variable:	Reference (ASCE 7-10)/Equation:			
Risk-Targeted Maximum Considered Earthquak	ke Spectral Response Accelerations (MCE <sub>R</sub> ) - %g			
i. S <sub>s</sub> - %g	Fig. 22-1/ 780 CMR Massachusetts 1609 = 18			
ii. S <sub>1</sub> - %g	Fig. 22-2/ 780 CMR Massachusetts 1609 = 7			
Soil Classification	Section 20			
Site Coefficients				
i. Fa	Table 11.4-1 = 1.6			
ii. F <sub>v</sub>	Table $11.4-2 = 2.4$			
Spectral Response Acceleration Parameters	Section 11.4.3			
i. S <sub>MS</sub>	$F_a*S_s=0.29$			
i. S <sub>M1</sub>	$F_{v}*S_{I}=0.17$			
Design Spectral Acceleration Parameters	Section 11.4.4			
i. S <sub>DS</sub>	$2/3*S_{MS}=0.192$			
ii. S <sub>D1</sub>	$2/3*S_{MI}=0.112$			
Risk Category	Table 1.5-1 = III			

Seismic Design Category (SDC)	Table 11.6-1 = B		
Seismic Importance Factor (I <sub>e</sub> )	Table $1.5-2 = 1.25$		
Effective Weight of Structure (W) <sup>7</sup>	Section 12.7.2		
Response Modification Coefficient (R)	Table $12.2-1 = 3$		
Seismic Base Shear (V) - psf	Section 15.4.1.2		
Scisine Base Shear (v) - psi	Cs*W		
i. Type of structure	Section 15.4.1.2		
ii. Seismic Response Coefficient (Cs)	$S_{DS}/(R*I_e) = 0.08$		
Fundamental Period (T) - seconds	Section 12.8.2.1		
Tundamentar reriod (1) - seconds	$Ct*h_n^x = 0.63$		
i. Type of structural system	Table 12.8-2		
ii. C <sub>t</sub>	Table $12.8-2 = 0.016$		
iii. x	Table $12.8-2 = 0.9$		
iv. Structural height (h <sub>n</sub> ) - ft	Average Height of Building (For Gordon Library mean height is the same as height above ground) = 59.5		
Wasting Distribution France (C.)	Section 12.8.3		
Vertical Distribution Factor $(C_{vx})$	$(W_x*h_x)^k/(W_i*h_i)^k$		
i. k	Section 12.8.3 = 2		
Lataral Cajamia Stary Force (E.)8 mof	Section 12.8.3/Table 4 and 5		
Lateral Seismic Story Force $(F_x)^8$ – psf	$C_{\nu x}*V$		
Shear Force for each story (V <sub>x</sub> )	$\Sigma Fi$		
Harizontal Caiamia Land Effect (E.)	Section 12.4.2.1		
Horizontal Seismic Load Effect (E <sub>h</sub> ) - psf	$p*Q_e$		
i. Redundancy Factor (ρ)	Section 12.3.4 = 1.0		
Wantian Calamia I and Effect (E.)	Section 12.4.2.2		
Vertical Seismic Load Effect (E <sub>v</sub> ) - psf	$0.2*S_{DS}*D$		

Table 4: Values and Base Shear (V) in Gordon Library

Floor	Cvx	Fx (kips)	Vx (kips)
3rd - Roof	0.081	88.99	88.99
2nd - 3rd	0.209	229.40	318.39
1st - 2nd	0.383	420.62	739.01
Ground - 1st	0.327	360.53	1099.54

<sup>&</sup>lt;sup>7</sup> Effective seismic weight is evaluated for all permanent elements above the level of the slab-on-grade, which turn out to be the ground floor of the Gordon Library. Since the roof snow load is greater than 30 psf, 20 percent of snow load is included as part of the effective seismic weight of the building.

<sup>&</sup>lt;sup>8</sup> Fx is a story force. It is applied discretely at each story level.

Table 5: Values and Base Shear (V) with Green Roof

Floor	Cvx	Fx (kips)	Vx
3rd - Roof	0.074	92.11	92.11
2nd - 3rd	0.191	237.43	329.54
1st - 2nd	0.349	435.35	764.90
Ground - 1st	0.385	479.25	1244.15

From comparison of Table 4 and Table 5, the base shear values and forces along the building's height differ when a green roof technology is installed on the building. The forces and base shear have a higher value with a green roof because the effective seismic weight of the building increases when implementing the extra weight of the green roof.

Step 7: LRFD Load Combinations per ASCE 7-10
1.4D
1.2D + 1.6L + 0.5S
1.2D + 1.6S + L
1.2D + 1.6S + 0.5W
$1.2D + 1.0W + L + 0.5(L_r/S/R)$
$1.2D + E_v + 1.0E_h + L + 0.2S$
0.9D + 1.0W
$0.9D + 1.0E_h$

## 3.3.2.2 Factored Design Load of Columns in Gordon Library

The second step of the structural analysis consisted of calculating the factored design load acting on each column of the building. For simplicity purposes, three sections were considered for this analysis. The sections were selected so the calculations could be applied to the rest of the building due to symmetry. Figure 3, represents the sections that were chosen for the building.

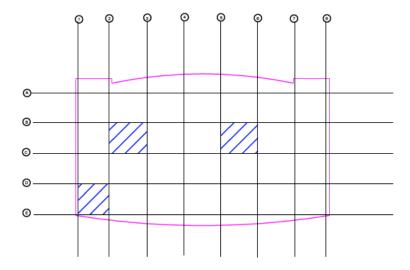


Figure 3: Plan View of Overall Building Sections Analyzed

In addition, the sections included the most critical columns due to the loads acting on the building. A typical section span included four columns arranged as shown in Figure 4.

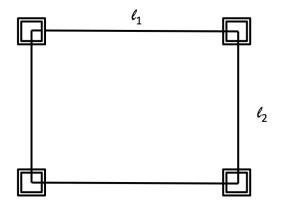


Figure 4: Typical Column Section Gordon Library

The values for  $\ell_1$  and  $\ell_2$  varied according to the section being analyzed. These values were either 21'or 25' for  $\ell_1$  and 20 feet for  $\ell_2$ .

The calculation process for the factored design load (Pu) included all the variables and inputs shown in Table 6. Each column in the building had different factored design load for each floor. The calculation process for (Pu) started by analyzing the first column section in the roof, consequently, the same column section for the third, second and first floor. This analysis had to

take into consideration all the loads for each floor and a sum of the loads above each floor. This means that the factored design load for the column section in the first floor had a higher value than the same section in the roof.

Table 6: Factored Design Load (Pu) Inputs

Variables	Description
Tributary Area (ft^2)	Area that a specific column supports
Tributary Area Drop Panel (ft^2)	Area of the drop panel or solid head of column
Dead Load (kips)	Dead load in pounds per square foot for each floor exclusion drop panels
Dead Load Drop Panel (kips)	Based on the dimensions of the drop panel
Dead Load Total (kips)	Sum of the two dead loads above
Live load (kips)	Live load that is acting on the tributary area of the column being analyzed
Snow Load (kips)	A constant load based on the tributary area of the column

# 3.3.2.3 Axial Load Capacity Calculations

The next step involved calculating the design axial load capacity  $\Phi Pn$  of each column in the building. This was done to determine if the calculated Pu values from the previous step in each column satisfy the condition of:

$$\Phi Pn > Pu$$

The axial load capacity was calculated according to the following formula:

$$\Phi Pn = 0.85\emptyset(0.85f'c(Ag - Ast) + Astfy)$$

This is the formula for a reinforced concrete circular column with spiral, where  $\emptyset = 0.70$  or 0.75 according to the type of column being analyzed. For other cases where the column has ties,  $\emptyset = 0.65$ . This calculation included the variables shown in Table 7 below.

Table 7: Data Required to Obtain Factored Design Load

Variables	Symbol
Axial Capacity	Pn
Gross Column Area	Ag
Area of steel bars	Ast
Steel Strength (psi)	fy
Concrete Strength (psi)	f'c
Reduction Factor	ф

Analyzing the axial capacity of the columns was the first check to determine if the existing building could support the new superimposed load of the green roof. However, it was necessary to include the analysis of the combined axial and flexural effects in each column of the building to have a complete check.

#### 3.3.2.4 Interaction Diagram Columns (Pn-Mn)

Investigation of combined axial and flexural effects consisted of constructing an interaction diagram for each critical column of the Gordon Library building. The interaction diagram was created as a comprehensive check to determine if the columns of the building could support the superimposed loads and the resulting factored design axial force (Pu) and moment (Mu). Tables 8 and 9 below, present the variables and formulas needed to construct an interaction diagram for one particular column. The columns of the building have a mix of rectangular and circular sections, which means that the shape of the column is rectangular but its reinforcement is circular. For calculation purposes, the column was considered as a circular column. Specific input values were updated based on the column being analyzed. Reinforcement and the dimension of the column were the two variables that typically changed within each floor of the building.

**Table 8: Input and Design Summary for Interaction Diagram** 

Input Data & Design Summary				
Variable	Symbol	Description & Formula	Units	
Concrete Strength	f <sub>c</sub> '	Based on Structural Drawings =4	ksi	
Rebar Yield stress	fy	Based on Structural Drawings =60	ksi	
Section Size	Ag	Area of Concrete Colum (b*h)	in^2	
Modulus of Elasticity Steel	Es	29,000	ksi	
Strain Concrete	εс	Max Strain Value = 0.003	-	
Diameter of Column	D	Based on Structural Drawings	in	
Column Vertical Reinforcement	Size	Dowel Size and Quantity	#	
Spiral Reinforcement	Size	Rebar size for spiral	#	
Factored Axial load	Pu	Based on Design	kips	
Factored Magnified Moment	M <sub>u</sub>	Based on Design	ft-kips	
Factored Shear Load	$V_{\rm u}$	Based on Design	kips	

Table 9: Design Summary Formulas and Variables Interaction Diagram

Formula	Symbol	Description
(fy/Es)	εу	Strain Steel
(h)-(cover)-(d. spiral bar) - (d. vertical bar)/2	dt	Distance Vertical bar to edge of concrete
[0.003/(0.003+\varepsilon y)]*dt	Xb	Location of PNA
β1*Xb	ab	Depth of Whitney Stress Block
arcos[((h/2)-ab)/(h/2)]	α	Compression Block Prop.
$((h^2)/2)*[(\alpha rad/2)-(0.25sin2\alpha)]$	A	Area of Compression Block
$[((h^3)/4) * ((\sin\alpha)^3)/3]/A$	X	Centroid of Compression Block
0.85*f'c*A	Cc	Compressive Force in Compression Block
#of bars* As*fy	T1	Area of Tension Steel
#of bars* As*Es*εs3	T2	Area of Tension Steel
#of bars*As*(fy-0.85*f'c)	Cs1	Area of Compression Steel
#of bars*As*(Es*εs2-0.85*f'c)	Cs2	Area of Compression Steel

#### 3.3.2.5 Two-Way Dome Slab

After examining the factored design loads and the combined axial and moment capacity for the columns in the building, an analysis of the two-way dome (or waffle) slab was conducted. The process for this calculation was based on the load factors acting on the entire slab of the building. Each floor of the Gordon Library was analyzed to determine the factored design load (Wu) in pounds/feet based on the load combinations. The process is similar to the method used for calculating the factored design load (Pu) for columns. Similar to Table 7 for the factored design load (Pu), the calculation process included all the loads acting on the slab, but rather than using the tributary area, it used the tributary width of the member being analyzed. The typical building sections for analysis of the waffle slab are the same as those for the columns, Figure 4 above. All manual calculations only considered the gravity loads acting on the building.

#### 3.3.2.6 Two-Way Dome Slab Capacity

The final step of the structural analysis of the Gordon Library consisted of calculating the moments and shear strength of the slab. The moments (Mu) and the shear (Vu) at different points within the slab were compared with the actual concrete capacities  $\emptyset Mn$  and  $\emptyset Vc$  based on the design of the structure. These capacities had to satisfy the following equations:

$$\emptyset Mn > Mu$$

$$\emptyset Vc > Vu$$

In order to determine the two-way dome slab capacity a series of steps were completed. These included determining the drop panel size on the columns, moments at end span and middle columns, moments in the column and middle strip, and the shear strength capacity and load.

#### 3.3.2.7 Determining Drop Panel

In the construction process based on the Concrete Reinforcing Steel Institute (CRSI), the solid heads over the columns are treated as they were drop panels in a conventional flat slab. The use of top and bottom steel bars accounted for the negative and positive moments acting on the slab, and its reinforcement was based on the superimposed loads acting on the slab in each floor. As there were no structural drawings that account for the dimensions of the drop panel for the Gordon Library, the solid heads were calculated using the following specifications.

The solid head shall extend in each direction from the centerline of the column a distance not less than 1/6 the span length center to center, in accordance with the following equation from ACI 318-14.

$$Min. Solid Head = \frac{1}{6}l_1 + \frac{1}{6}l_2$$

# 3.3.2.8 Two-Way Dome Slab Capacity (End Span)

The second step to calculate the capacity of the two-way dome slab consisted of calculating the moments in the column and slab for an end span. The values for the moments for an end span and interior span changed for any building. Similarly, for the Gordon Library the section that consisted of an end span also had different lengths in comparison to a section in the interior of the building. For this reason it was necessary to calculate the moments for an end span and interior span with the change of span length.

Table 10: Moment Distribution within End Span of Column and Slab

Variable	Formula	Description
Total Static Moment (Mo)	$\frac{WuL^2}{8}$	L= length of clear span outside of column supports  Wu= total factored load in k/ft including drop panel
Exterior Column (Negative Factor	ed Moment) ACI 13.6.4.2	
Moment (Mu <sub>EXT</sub> )	0.26Mo	Column Strip resists 100% of Mu
Bottom (Positive Factored Momen	t) ACI 13.6.4.4	
Moment (Mu <sub>BOT</sub> )	0.52Mo	
Column Strip (Mu)	0.60Mu	Column strip resists 60% of Mu
Middle Strip (Mu)	0.40Mu	Middle Strip resists 40% of Mu
Interior Column (Negative Factore	d Moment) ACI 13.6.4.1	
Moment (Mu <sub>INT</sub> )	0.70Mo	
Column Strip (Mu)	0.75Mu	Column strip resists 75% of Mu
Middle Strip (Mu)	0.25Mu	Middle Strip resists 25% of Mu

Figure 5 below illustrate the moment distribution along the slab of the building. This figure helps illustrate how each moment differs for end span and interior span and for column strips and middle strips. This figure was used together with Table 10 above to determine the respective moment (Mu) values according its location.

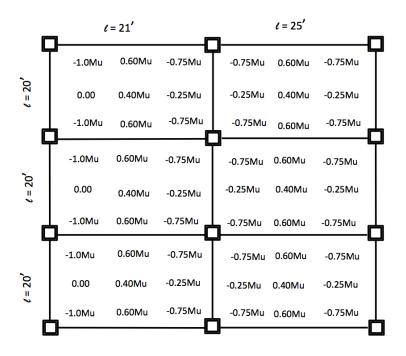


Figure 5: Moment Distribution on Waffle Slab

In the case of determining flexural reinforcement for the slab an additional step was needed. However, as the structural drawings of the Gordon Library already provided details about the reinforcement, this step was not done.

#### 3.3.2.9 Shear Constants & Shear Calculation (End Span)

In order to calculate the factored shear (Vu) of the slab it was necessary to calculate the shear at the exterior column with its appropriate critical section. Figure 6 below illustrates an end span column in the first floor of the Gordon Library and the shear constants needed to obtain the factored shear. The dotted line in Figure 6 represents the critical section of the column to be analyzed.

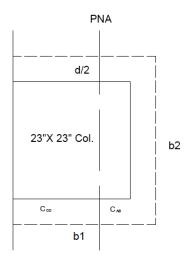


Figure 6: Plan View End Span Column

The following equations were used to calculate the properties of the figure illustrated above.

$$b1 = column \ size \ + \ d/2$$
 
$$b2 = column \ size \ + \ d$$
 
$$b_o = 2 * b1 \ + \ b2$$
 
$$A_c = b_o * d$$
 
$$Jc = \frac{b_1 d^3}{6} + \frac{2d[(C_{AB})^3 + (C_{CD})^3]}{3} + b_2 d(C_{AB})^2$$

These properties of the column were determined manually, however they can also be obtained from Table 11-5 "Peripheral Shear Constants at Columns" from the CRSI. The table from the CRSI provides enough information regarding the shear constants for a corner, edge and interior column with respective column dimensions and slab/drop panel. See Chapter 6, for an overview of Table 11-5 presented by the CRSI.

Calculating the factored shear (Vu) consisted of solving the equations tabulated in Table 11. Ac and C<sub>AB</sub> values are the same as previously calculated.

**Table 11: Factored Shear (vu) Calculations** 

Description/Variable	Formula		
Shear (Vu)	$\frac{wuL}{2} - \frac{Mu}{2}$	$u_{int} - Mu_{ext}$ $L$	
Factored Shear (vu)	$\frac{Vu}{Ac} + \frac{\gamma_v MuC_{AB}}{Jc}$ ACI R11.11.7.2		ACI R11.11.7.2
$\gamma_{v}$	(1	$-\gamma_f)$	ACI Eq. 11-37
$\gamma_f$	$\frac{1}{(1+\left(\frac{2}{3}\right)\sqrt{b_1/b_2}}$		ACI Eq. 13-1
Mu	0.3	ВОМо	ACI 13.6.3.6
	Shear Check at Ext	erior Column	
Shear Capacity (vc)	$(\frac{\alpha_s d}{b_o}$	$+2)\sqrt{f'c}$	ACI Eq. 11-32
$\alpha_s$	30 for ed	ge columns	
	Design Moment Str	rength (ΦMn)	
Area of Steel (As)	# of bars in colum	# of bars in column strip*Area of bars	
a	$\frac{A_s f_y}{0.85 f' cb}$		
Effective width (b)	Half the width of the panel		
ФМп	$\phi Asf_y(d-\frac{a}{2})$		
Reduction Factor $(\phi)$	(	0.9	
	Moment Check at Ex	terior Column	1
	ΦMn > 0.26	$\gamma_f$ Mo	
	$\rho = \frac{As}{ba}$	ī	
$\rho_{max} = 0.011$		ACI	13.5.3.3
	$ ho_{max}$ >	ρ	

# 3.3.2.10 Two-Way Dome Slab Capacity (Interior Span)

**Table 12: Moment Distribution with Interior Span** 

Variable	Formula	Description	
Total Static Moment (Mo)	$\frac{WuL^2}{8}$	Mo is the same as end span	
Panel Moments			
Bottom (Positive Factored Momer	at) ACI 13.6.4.4		
Moment (Mu <sub>BOT</sub> )	0.35Mo		
Column Strip (Mu)	0.60Mu	Column strip resists 60% of Mu	
Middle Strip (Mu)	0.40Mu	Middle Strip resists 40% of Mu	
Top (Negative Factored Moment)	ACI 13.6.4.1	<u> </u>	
Moment (Mu <sub>TOP</sub> )	0.65Mo		
Column Strip (Mu)	0.75Mu	Column strip resists 75% of Mu	
Middle Strip (Mu)	0.25Mu	Middle Strip resists 25% of Mu	

#### 3.3.2.11 Shear Constants & Shear Calculation (Interior Span)

A similar approach was taken to determine the moments (Mu) and the shear (Vu) in the interior span. Some factors varied in value due to the increase in moment and changes in the properties of the column being analyzed. Table 12 was used to calculate the factors, and the same equations under Figure 6 were used to calculate the properties of the column. However, the neutral axis of the column changed, as shown in Figure 7, therefore the equations were altered due to this change.

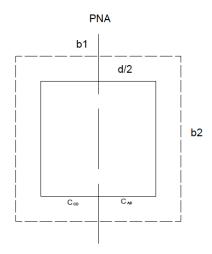


Figure 7: Plan View Interior Span Column

Investigation of the existing two-way dome slab included the analysis of the columns and slab of the first floor of the Gordon Library. This process helped as a guide to determine the capacity of all the columns and slabs in the building, especially the ones in the first floor. In this particular case, only two section of the first floor were analyzed to show its procedure. The section consisted of two edge columns and two interior columns that could fit by symmetry the rest of the floor. As the roof slab has a similar arrange as the slab of the first floor, the slab was not checked to see if it could support the loads of the green roof. It was assumed that the check of the first floor slab would be the most critical of the building. It is important to note that some sections might change depending on the structure of the building.

# 3.4 Design and Analysis of Solar Evacuated Tubes on Stoddard B

For Stoddard B, a solar evacuated tubes model was chosen based on online research. First, different types of solar panels were researched, followed by research on different manufacturers of this particular system. A model was chosen based on the energy production and comparison to the energy consumption of the building. Other factors considered were cost, number of collectors needed, and weight. The information and cost of the considered models were accessible online.

#### 3.4.1 Layout and Construction Process for Solar Collectors on Stoddard B

Determining the layout of the system involved calculating the number of solar collectors needed to meet the energy demand value of Stoddard B. The annual energy demand value of the building was given by the WPI Facilities Department. The number of panels was calculated by dividing the annual energy demand value of the building by the annual energy production value of one solar panel. The two biggest sides of the building were chosen to place the system based on their individual flat roof and ample space. This system is framed with its mounting system and built into the roof.

The solar collectors need an angle of about 40° above the horizontal, the typical angle range for this collector is between 20° and 80°, and need to face south to absorb the maximum amount of sunlight. The process for constructing this system which include safety precautions, module mounting, mounting configurations, and maintenance and cleaning was obtained from the manufacturer's website for the chosen solar panel model.

## 3.4.2 Structural Analyses and Design for Solar Collectors on Stoddard B

After determining the layout and quantity of solar collectors, the building was submitted to a structure analysis to investigate its adequacy to support the added weight. The analysis consisted of designing the minimum member's size and reinforcement to support the added load caused by the solar system. If any of the actual members or reinforcement were smaller than the proposed design, then the structure cannot support the new load. Through trial and error, a final design for each of the members would be constructed.

#### 3.4.2.1 Solar Collectors Load Calculations

The first step of the analysis involved considering all loads acting on the solar collectors: dead load, live load, rain load, snow load, wind load, and seismic load. For the collectors, live load and rain load were considered negligible. Due to the angle of the collectors, all rain not absorbed by the collectors would runoff onto the roof and drain so no ponding was expected. Live load was neglected since the collectors are not designed for people to walk and operate on. Calculations for dead load, snow load, wind load, and seismic load are outlined in the sequence of tables below; the methods for these calculations are very similar to the solar panels (Section 3.2.2) since they are both photovoltaic systems. ASCE 7-10 was used as a reference for these calculations, as well as solar photovoltaic array wind and seismic load documents from the Structural Engineers Association of California (Structural Engineers Association of California, 2012). The calculated design load values were input into the load combination equations outlined in Step 5 below. The governing load combination produced the largest load value that would be used for application when designing the structure's members. All load combination calculations were made in accordance with the Load and Resistance Factor Design (LRFD) method.

Step 1: Dead Load of Solar Collectors	
Variable:	Reference/Equation:
Weight of collectors + Water capacity – lbs.	Obtained from Manufacturer's Website
Number of collectors	Previously Determined Based on Energy Values
Overall Weight of collectors – lbs.	Weight of collectors * Number of collectors
Area of collectors – ft <sup>2</sup>	Determined Based on Dimensions and Number of collectors
Dead Load - psf	Overall Weight of collectors/Area of collectors

Step 2: Snow Load on Solar Collectors	
Variable:	Reference (ASCE 7-10)/Equation:
Thermal Factor (C <sub>t</sub> )	Table 7-3
Evnosura Factor (C.)	Table 7-2
Exposure Factor (C <sub>e</sub> )	0.9
· T	Section 26.7
i. Terrain Category	Category B
Importance Factor (I.)	Table 1.5-2
Importance Factor (I <sub>s</sub> )	1.10
i. Risk Category	Table 1.5-1
	Category II
Ground Snow Loads (ρ <sub>g</sub> ) - psf	Fig. 7-1
	50
Elet Doof Spay Load (a) pof	Section 7.3
Flat Roof Snow Load $(\rho_f)$ - psf	$0.7*C_e*C_t*I_s*\rho_g$

Step 3a: Wind Load on Solar Collectors	
Variable:	Reference (ASCE 7-10)/Equation:
Diels Cotocomy	Table 1.5-1
Risk Category	Category III
Basic Wind Speed (V) – mph	Fig. 26.5-1B
Basic wind Speed (v) – nipii	135
Wind Directionality Factor (K <sub>d</sub> )	Table 26.6-1
wind Directionality Factor (Kd)	0.85
Exposure Category	Section 26.7
Exposure Category	Category B
Topographic Factor (K <sub>zt</sub> )	Section 26.8
Topographic Pactor (Kzt)	1.0
Gust Effect Factor (G)	Section 26.9
Gust Effect Pactor (G)	0.85
Valority Prassura Evrosura Coefficient (V.)	Table 29.3-1
Velocity Pressure Exposure Coefficient (Kz)	0.668
i Haight shove ground level ft	Height of Stoddard B
i. Height above ground level - ft	26
Valacity Processes (a.) mof	Section 29.3.2
Velocity Pressure (q <sub>z</sub> ) - psf	$0.00256 * K_z * K_{zt} * K_d * V^2$

Step 3b: Wind Load on Solar Collectors	
Reference (Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs):	
$A_{pv} \le h$ , therefore $A_{pv} =$	Lower Value of A <sub>pv</sub> and h
	Height of Stoddard B
i. Height of building (h) -ft	26
ii. Width of building on longest side (WL) - ft	Width of Stoddard B, building with collectors
	48
iii. A <sub>pv</sub> - ft	0.5 * SQRT(h * WL)
Normalized Wind Area (A <sub>n</sub> )	$(1000/A_{pv}^2) * Roof area$
i. Tributary area of beam – ft <sup>2</sup>	Based on Design
ii. $A_{pv} \ge 15$ ft, therefore $A_{pv} =$	Greater Value of A <sub>pv</sub> and 15 ft
Nominal Net Pressure ((GC <sub>m</sub> ) <sub>nom</sub> )	(GC <sub>m</sub> ) <sub>nom</sub> Values
i. Panel angle ( $\omega$ ) - $^{\circ}$	Solar Panel Angle = $40^{\circ}$
:: (CC ) for 150 < 0 < 250	Fig. 29.9-1
ii. $(GC_m)_{nom}$ for $15^\circ \le \omega \le 35^\circ$	0.3
Panel Chord Length Factor (Vc)	$0.6 + (0.06 * l_p)$
	Width of Solar collectors
i. Chord length of soalr collectors $(l_p)$ - ft	5.79
Characteristic Height (hc) - ft	$h_1 + (l_p * SIN* \omega)$
: C-1	Minimum Height of Solar Collector
i. Solar panel height above roof at low edge $(h_1)$ - $ft$	6.3
ii. $h_1 \le 1$ ft, therefore $h_1 =$	Lower Value of h <sub>1</sub> and 1 ft
A (E)	Fig. 29.9-1
Array Edge Factor (E)	1.0
i. Horizontal distance from edge of collector to edge of roof $(d_x)$ - ft	3
ii. $d_x/h_c =$	$d_x/h_c$
Parapet Height Factor $(V_p) = 1.0$ if $h_{pt}$ is less than 4 ft	h <sub>pt</sub> =0.25(solar collector height above roof)
	1.0
Net Pressure Coefficient (GC <sub>m</sub> )	$V_p * E * (GC_m)_{nom} * V_c$
Design Wind Pressure (p) - psf	$q_z * GC_m$

Step 4a: Seismic Load for Solar Collectors	
Variable:	Reference (ASCE 7-10)/Equation:
Risk-Targeted Maximum Considered Earthquake	Spectral Response Accelerations (MCE <sub>R</sub> ) - %g
; C 0/ ~	Fig. 22-1
i. S <sub>s</sub> - %g	18
:: S. 0/ a	Fig. 22-2
ii. S <sub>1</sub> - %g	7
Soil Classification —	Section 20
Son Classification	Site D
Site Coefficients	
; E	Table 11.4-1
i. Fa	1.6
:: T	Table 11.4-2
ii. F <sub>v</sub>	2.4
Spectral Response Acceleration Parameters	Section 11.4.3
i. S <sub>MS</sub>	$F_a * S_s$
i. S <sub>M1</sub>	$F_{v} * S_{I}$
Design Spectral Acceleration Parameters	Section 11.4.4
i. S <sub>DS</sub>	2/3 * S <sub>MS</sub>
ii. S <sub>D1</sub>	2/3 * S <sub>M1</sub>
P. I. C.	Table 1.5-1
Risk Category	III
	Table 11.6-1
Seismic Design Category (SDC)	В
	Table 1.5-2
Seismic Importance Factor (I <sub>e</sub> )	1.25
	Section 12.81
Seismic Base Shear (V) - psf	$W^*C_s$
· Tr	Section 15.4.1.2
i. Type of structure	Rigid Nonbuilding Structure
ii. Weight of structure (W) - psf	12.4
Response Modification Factor (R)	Table 12.2-1
1	3.0
Seismic Response Coefficient (C <sub>s</sub> )	Section 12.8.1.1
2000 response Coefficient (Cs)	$S_{DS}/(R/I_e)$

Step 4b: Seismic Load for Solar Collector	
С	Reference (ASCE 7-10)/Equation:
Evandomental Davie d (T)	Section 12.8.2.1
Fundamental Period (T) – s	0.1 * Stories above base
: True of atmostratel arratement	Table 12.8-2
i. Type of structural system	All Other Structural Systems
Ventical Distribution Factor (C.)	Section 12.8.3
Vertical Distribution Factor (C <sub>vx</sub> )	$(W_x * h_x)^k / (W_i * h_i)^k$
: 1-	Section 12.8.3
i. k	1.0
ii. Weight of structure (W <sub>x</sub> /W <sub>i</sub> ) - psf	12.4
iii. Structural height (h <sub>x</sub> /h <sub>i</sub> ) - ft	26
Lataral Saissaia Farra (F.) and	Section 12.8.3
Lateral Seismic Force (F <sub>x</sub> ) - psf	$C_{\nu_X} * V$
Horizontal Sciencia Lood Effect (E.) mof	Section 12.4.2.1
Horizontal Seismic Load Effect (E <sub>h</sub> ) - psf	$P*Q_e(Q_e=F_x)$
i Dadundanay Faatan (a)	Section 12.3.4
i. Redundancy Factor (ρ)	1.0
W (* 10 * * 1 1E66 (/E)	Section 12.4.2.2
Vertical Seismic Load Effect (E <sub>v</sub> ) - psf	$0.2 * S_{DS} * D$

Step 5: LRFD Load Combinations per ASCE 7-10
1.4D
$1.2D + 1.6L + 0.5(L_r/S/R)$
$1.2D + 1.6(L_r/S/R) + (L/0.5W)$
$1.2D + 1.0W + L + 0.5(L_r/S/R)$
$1.2D + E_v + 1.0E_h + L + 0.2S$
0.9D + 1.0W
$0.9D + 1.0E_h$

#### 3.4.2.2 Slab Calculations and Design

The second step of the analysis involved designing the minimum slab requirements for the new imposed loads plus any loads acting on top of the slab as dead loads. For this procedure, the slab was assumed to be a continuous one-way slab with interior supports. The design of this member included the minimum thickness of the slab as well as its minimum required reinforcement. This step was completed twice, once for the roof slab and another for the first-floor slab. The remaining slabs are assumed to be the same as the first floor since they have smaller loads acting on them making the design of the first-floor slab adequate for their loads. Calculations were made to design the slabs with the *Reinforced Concrete* book that is in accordance with the ACI 318-11 code. Using the ACI code, the self-weight of the slab can be calculated and then it is designed by adding this new weight to all the loads acting on top of the member; the self-weight includes a metal deck, which is a permanent formwork, as well as MEP which weight were estimated after research. The end result of the design consists of the thickness, reinforcement size and spacing, and the maximum allowed moment. The tables below show the calculation process for choosing a thickness and rebar number & spacing. Finally, the moment capacity  $\Phi M_n$  is calculated and compared to the design moment acting on the slab.

Step 1: Slab Thickness, Constants, and Actual Moment	
Variable:	Reference/Equation:
Spacing between supports (l) - ft	Assumed
Steel Yield Strength (Fy) - ksi	60 (A432 Steel)
Concrete Yield Strengh (F'c) -ksi	3
Thickness (h) - inches	V24
Self Weight (S <sub>w</sub> ) psf	h(150 psf)
w <sub>u</sub> - psf	Governing Load including self weight and any weight on system
Design Moment (M <sub>u</sub> ) – k*ft	$(w_u * L^2)/9$
Steel Ratio design (pdes)	$0.85\beta_1(F'c/F_y)(\epsilon_u/\epsilon_u+0.005)$
Max Steel Ratio( ρ <sub>max</sub> )	$0.75[0.85\beta_1(F'c/F_y)(87/87+F_y)]$
$\beta_1$	0.85
Minimum steel ratio (ρ <sub>min</sub> )	0.0018

<sup>&</sup>lt;sup>9</sup> MacGregor, James, and James Wight. *Reinforced Concrete: Mechanics and Design.* Fourth ed., 2005.

Step 2a: Trial Design	
Variable:	Reference/Equation:
Uncertainty Coefficient Φ	0.9
Cover- inches	0.75
Unit width (b)- inches	12
Depth (d <sub>design</sub> )- inches	h-cover-0.25
Whitney's stress block (a assumed)- inches	1
Area of steel (A <sub>s</sub> ) per unit width@ max moment	$M_u/\Phi F_v(d_{design}-a/2)$

Once step two is done, the reinforcement can be chosen from table A-9  $^{10}$  (Reinforced Concrete, 2005). With the new area of steel, step two is repeated utilizing this new information to get the actual design specification. Following step two, the actual steel ratio is calculated and checked to be sure it is within parameters. In the final step, the shear and moment capacities are calculated and compared to the design load values  $V_u$  and  $M_u$ .

Step 2b: Final Design	
Variable:	Reference/Equation:
Actual Depth (d)-inches	h-cover-half bar diameter
Design Steel Ratio (ρ)	A <sub>s</sub> /bd
Unit Width (b)- inches	12
Actual Whitney's stress block (a)- inches	$A_s F_y$ ./0.85*F'c*b

Step 3: Shear & Moment	
Variable:	Reference/Equation:
	Φ in shear=0.75
Shear Capacity (ΦV) -kips	$\Phi^*(SQRT(F'c))^*b^*d$
Design Shear (V <sub>u</sub> ) -kips	$1.15(W_u*l)(1/2)+dW_u$
Moment Capacity (ΦM <sub>n</sub> ) –kip*ft	$\Phi A_s * F_y * (d-a/2)$

-

<sup>&</sup>lt;sup>10</sup> Areas of Bars in a Section 1ft Wide, Annex 9

## 3.4.2.3 Beam Calculations and Design

The third step of the analysis is designing the member beneath the slab; in this case the beams. Much like the slab, the proposed design is the minimum requirements for the beam to support the new loads created by the solar collectors. The calculations for this design were conducted following the steps in the book (Reinforced Concrete, 2005). The beams were estimated as best as possible since no dimensions were provided in the drawings. The design of these members resulted in the required reinforcement and the allowed moment. This procedure was done once for the 1<sup>st</sup> floor and all other beams are assumed to be the same. The first floor's loading exceeds that of the roof with the solar collectors, making this design adequate for all other floors. For this design, an initial assumption is made that the steel stress is equal to the yield stress. If this assumption is correct, the steel ratio is less than the balanced steel ratio having no need to check it. The tables below show the calculation steps in order to choose reinforcement and calculate the allowed moment.

Step 1: Known Values and Constants	
Variable:	Reference/Equation:
Length (l) – ft	Assumed
Steel Yield Strength (F <sub>y</sub> ) - ksi	60 (A432 Steel)
Concrete Strength (F'c) -ksi	3
Area (b x h) –in <sup>2</sup>	$(8 \times 10) = 80$
Self-Weight (S <sub>w</sub> ) psf	Area(1)(150 psf)
Factored Load (W <sub>u</sub> )- psf	Governing Load including self-weight and any acting on system
Allowed area of steel (A <sub>s</sub> )- in <sup>2</sup>	Same as the slab= 0.7
$\beta_1$	0.85
Modulus of elasticity of steel (E <sub>s</sub> ) -psi	29,000,000

Following step one, a bar size was chosen for reinforcement. Given the area of the bar, different values can be calculated in order to make sure that the initial assumption is correct. The assumption is acceptable if the net tensile strain in the reinforcement is larger than its yield strain. If the net tensile strain is equal or larger than 0.005, then the beam is tension controlled and the uncertainty coefficient is equal to 0.9.

Step 2: Assumption Check	
Variable:	Reference/Equation:
Design Depth (d)-inches	h-cover-half bar diameter
Design Whitney's Stress Block (a)- inches	A <sub>s</sub> *Fy/0.85*F'c*b
С	$a/\beta_1$
Net tensile strain $(\varepsilon_t)$	0.003[(d-c)/c]
Yield strain in tension $(\varepsilon_y)$	$F_y/E_s$
Uncertainty Coefficient Φ	0.9

Step 3: Moment Check	
Variable:	Reference/Equation:
Design Moment (M <sub>u</sub> ) –kip*ft	$(W_u*l^2)/8$
Moment Capacity (ΦM <sub>n</sub> ) –kip*ft	$\Phi A_s * F_y * (d-a/2)$

## 3.4.2.4 Column Calculations and Design

The fourth and final step for the structural analysis was to design the minimum size and reinforcement for the columns. Similar to the slab and beams, this process was conducted following the column chapter in the book (Reinforced Concrete, 2005). The cross sections of the columns were measured using a measuring tape and the height was given in the drawings. Different columns in the first floor were measured to be more accurate (all measured columns had the same area). With these known values and the imposed load, an adequate design can be proposed. The analysis starts by calculating the imposed load acting on the columns, like all the other members. For this design, the member is assumed to be governed by axial forces since the lateral force resisting system was assumed to be shear walls. The axial load depends on the tributary area of each column resulting in three types, each with a different tributary area. The column that was analyzed for design purposes is the column with the biggest tributary area, given that this one will have the largest axial load. All other columns are assumed to have the same reinforcement. The design of the column was completed following the steps below.

Step 1: Known Values and Constants	
Variable:	Reference/Equation:
Height of columns (H) - ft	8.67
Steel Yield Strength (F <sub>y</sub> ) - ksi	60 (A432 Steel)
Concrete Strength (F'c) -ksi	3
Area of entire column (b x h) (A <sub>g</sub> ) -in <sup>2</sup>	$(12 \times 12)=144$
Self-Weight (S <sub>w</sub> ) psf	Area(l)(150 psf)
Factored Load (Wu)- psf	Governing Load including self-weight and any load acting on system
Largest tributary area –ft <sup>2</sup>	15.67 x 15.67
Uncertainty Coefficient Φ	0.65
Tie size	Bar # 3

Step 2: Point Load and Steel Area	
Variable:	Reference/Equation:
Design Axial Load (Pu)- kips	W <sub>u</sub> *Tributary Area
Axial Load Capacity (ΦP <sub>n</sub> )	$0.80\Phi(A_sF_y+0.85*F^*c*(A_g-A_s))$
Area of Steel (A <sub>s</sub> ) –in <sup>2</sup>	$[P_u/(0.80\Phi^*(F_y-0.85^*F'c))]-[(0.85^*F'c^*A_g)/(F_y-0.85^*F'c)]$
Steel Ratio (ρ)	$ m A_s/A_g$
Allowed Steel Ratio (ρ)	1-2%

Step 3: Tie Spacing	
Variable:	Reference/Equation:
Spacing of ties is equal to smallest number of the following equations	16*bar diameter
	48*tie diameter
	Smallest column dimension

# 3.5 Economic Analysis

This section contains information on the economic analysis to determine whether it is feasible to implement the chosen sustainable rooftop technologies. The simple payback period will be evaluated by calculating the total installation cost, as well as the net annual energy savings of the sustainable rooftop technology. This evaluation will result in a recommendation to WPI on if they should invest in the proposed designs on the three structures. When determining the total installation cost of the technology, the unit cost values for labor, material, and equipment were considered using the *Building Construction Costs* source created by R.S. Means Company. This section outlines the calculation process to perform the economic analysis for each sustainable rooftop technology.

#### 3.5.1 Economic Analysis of Solar Panels on the Gateway Parking Garage

When determining the overall installation cost of the proposed solar panel design elevated above the Gateway Parking Garage, many factors were accounted for. These factors included total cost of the steel framework, added 2 ft x 2 ft concrete columns, reinforcement within the concrete columns, and solar panels. The total cost for each factor was added together to produce the overall cost of the proposed solar panel design. This value was compared to the annual energy demand cost of the Gateway Parking Garage to determine how many years it would take to pay off the solar panel design and begin making a profit. These were compared since the chosen number of solar panels can produce the annual energy demand of the Gateway Parking Garage.

#### 3.5.1.1 Total Cost of Steel Framework

The steel framework total cost was determined by first calculating the total weight of the steel members. The overall weight of the miscellaneous items in the framework, which includes steel, plates, studs, and connections was estimated by taking 10% of the total steel member weight (R.S. Means Company, 2017). This calculation process is shown in the tables below.

Step 1: Total Weight of Steel Members	
Variable:	Reference/Equation:
Member Weight – lb./ft	Based on Chosen Member Size
Member Length – ft	Based on Structural Layout
Member Quantity	Based on Structural Layout
\( \sumber Weight * Member Length * Member Quantity * (tons/2000 lb.) - tons	

Step 2: Total Weight of Miscellaneous Items	
Variable:	Reference/Equation:
Overall Weight of Miscellaneous Items - tons	RS Means Building Construction Costs
i. Steel	
ii. Plates	100/*T-1-1W-1-1
iii. Studs	10%*Total Weight of Steel Members
iv. Connections	

Once the weight of the steel framework was determined, the total cost was calculated using the construction cost data and equation shown in the table below. The costs include unit cost values for labor, materials, and equipment. Labor rate accounts for the workers constructing and installing the steel framework, material rate accounts for the steel members and miscellaneous items, and equipment rate accounts for the tools used to construct the steel framework (R.S. Means Company, 2017). These rates are represented in \$/ton.

Step 3: Total Cost of Steel Framework	
Variable:	Reference/Equation:
Labor Unit Cost - \$/ton	RS Means Building Construction Costs
i. Steel Members	400
ii. Misc. Steel/Plates/Studs/Connections	400
Material Unit Cost - \$/ton	RS Means Building Construction Costs
i. Steel Members	3,000
ii. Misc. Steel/Plates/Studs/Connections	3,400
Equipment Unit Cost - \$/ton	RS Means Building Construction Costs
i. Steel Members	200
ii. Misc. Steel/Plates/Studs/Connections	200

 $(Total\ Steel\ Member\ Weight + Total\ Miscellaneous\ Weight)*[Labor\ Unit\ Cost + Material\ Unit\ Cost + Equipment\ Unit\ Cost] - \$$ 

#### 3.5.1.2 Total Cost of Added 2 ft x 2 ft Concrete Columns

As a portion of the solar panel design, five 2 ft x 2 ft concrete columns were proposed to support the columns of the steel framework. The total construction cost of the added concrete columns was calculated using the unit costs and equation shown in the table below. The cost elements accounted for are the same as for the steel framework (labor, material, and equipment);

however, each has different values and are represented for 24" x 24" cast-in-place concrete columns (R.S. Means Company, 2017).

Total Cost of Added 24" x 24" Concrete Columns	
Variable:	Reference/Equation:
Number of Added Concrete Columns	5
Labor Unit Cost - \$	RS Means Building Construction Costs
	400
Material Unit Cost - \$	RS Means Building Construction Costs
	241
Equipment Unit Cost - \$	RS Means Building Construction Costs
	32
Number of Added Concrete Columns*[Labor Unit Cost + Material Unit Cost + Equipment Unit Cost] - \$	

#### 3.5.1.3 Total Cost of Reinforcement Within Concrete Columns

Proposed reinforcement within the concrete columns included 6 #9 steel bars. This was proposed within all eight concrete columns supporting the steel framework columns, including the three concrete columns that already exist. Since no structural drawings were provided for the Gateway Parking Garage, it was assumed that 6 #9 steel rebar does not exist within the three existing concrete columns. Therefore, the total cost for the reinforcement included all eight concrete columns. The first step required determining the material cost, labor cost, and equipment cost of the #9 steel rebar, which is outlined in the Step 1 table below (R.S. Means Company, 2017). The second step required calculating the total cost of the steel rebar, which is outlined in the Step 2 table below.

Step 1: Material Cost, Labor Cost, and Equipment Cost of #9 Steel Rebar	
Variable:	Reference/Equation:
Material Unit Cost - \$	RS Means Building Construction Costs
	64.50
Labor Unit Cost - \$	RS Means Building Construction Costs
	60.50
Equipment Unit Cost - \$	RS Means Building Construction Costs
	15.35

Step 2: Total Cost of Steel Rebar	
Variable:	Reference/Equation:
Number of Concrete Columns	8
Number of #9 Steel Rebar per Column	6
Number of Concrete Columns*Number of #9 Steel Rebar per Column*[Material Unit	

Cost + Labor Unit Cost + Equipment Unit Cost] - \$

#### 3.5.1.4 Total Cost of Solar Panels

The total cost of solar panels was based on the chosen SPR-P17-350-COM model from the manufacturer SunPower. The total cost was calculated in the table below based on the unit cost of the technology and unit installation cost for the Northeast region of the United States provided by SunPower (SunPower Corporation, 2017).

Total Solar Panel Cost	
Variable:	Reference/Equation:
Number of Solar Panels	272
Cost of Solar Panels - \$	Unit Technology Cost*Number of Solar Panels
i. Unit Cost of Technology (\$/panel)	SunPower Corporation
	635.50
Unit Installation Cost (\$)	Panel Energy Production*Unit Installation Cost*Number of Solar Panels
i. Panel Energy Production (watt/panel)	SunPower Corporation
	350
ii. Unit Installation Cost (\$/watt)	SunPower Corporation
	4.00
Cost of Solar Panels + Unit Installation Cost - \$	

#### 3.5.1.5 Simple Payback Period of the Proposed Solar Panel Design

The construction costs of the steel framework, added concrete columns, steel rebar, and solar panels were summed together to produce the overall cost of the proposed solar panel design. The next step involved determining the net annual energy savings by installing solar panels on the Gateway Parking Garage. This was calculated in the table below using the annual energy demand and energy operational cost values obtained from the WPI Facilities Department, as well as the total annual solar panel energy production value. For this design, the total annual solar panel energy production is greater than or equal to the annual energy demand of the

Gateway Parking Garage, therefore, the total annual solar panel energy production is multiplied by the energy operational cost.

Step 1: Net Annual Energy Savings			
Variable:	Reference/Equation:		
Annual Energy Demand & Wh	WPI Facilities Department		
Annual Energy Demand - kWh	137,207		
Energy Operational Cost \$/I/Wh	WPI Facilities Department		
Energy Operational Cost - \$/kWh	0.14		
Total Annual Panel Energy Production - kWh	Number of Solar Panels*Annual Panel		
Total Filmai Faller Bhergy Froduction - Kvvn	Energy Production		
i. Number of Solar Panels	272		
ii. Annual Panel Energy Production – kWh/panel	511		
Energy Operational Cost*Total Annual Panel Energy Production - \$			

The next step involved determining the number of years to pay off the installation of the proposed solar panel design. The annual operational cost and lifespan of the solar panels, provided by SunPower, were multiplied together and added to the overall installation cost of the proposed solar panel design. This was calculated to give the total installation cost of the solar panel design over a 25-year span (the lifespan of the solar panels). Dividing this value by the net annual energy savings of the Gateway Garage would produce the simple payback period of the solar panel system. This calculation process is outlined in the table below.

Step 2: Simple Payback Period of the Proposed Solar Panel Design				
Variable: Reference/Equation:				
Annual Operational Cost of Solar Panels - \$	SunPower Corporation			
Allitual Operational Cost of Solar Paliets - \$	2,593			
Lifegrap of Color Danals, years	SunPower Corporation			
Lifespan of Solar Panels - years	25			

(Overall Cost of Solar Panel System + Annual Operational Cost\*Lifespan)/(Net Annual Energy Savings) - years

#### 3.5.2 Economic Analysis of Green Roof on Gordon Library

The costs of installation and materials for the green roof had a more simplistic approach in comparison to the solar panels on Gateway Garage. The main factors that were included in this economic analysis were:

- Total cost of green roof per square foot (includes labor and material)
- Annual maintenance of green roof per square foot
- Energy reduction savings per square foot for implementing a green roof technology on Gordon Library (annually)
- Stormwater net savings per square foot (annually)

The total cost of all these factors was added together to determine the overall cost of the proposed green roof on the Gordon Library and the possible savings on an annual basis. In addition, the added cost of implementing a roof garden was compared to the costs of installing a conventional roof.

#### 3.5.2.1 Cost of Green Roof Technology

The cost of the green roof on consisted of calculating the area of the technology on the roof of the Gordon Library. Not all the roof was used for this technology, therefore the cost of installation and maintenance of the green roof depended solely on its total area. The calculation for this cost consisted of multiplying the gross area of the green roof times the cost per square foot. For the calculation of the annual maintenance of the green roof, a similar approach was taken. It consisted of multiplying the annual maintenance cost per square foot times the gross area of the green roof.

The results of these calculations are shown in Chapter 8, Economic Analysis of Sustainable Roofing Technologies.

# 3.5.2.2 Energy Savings of Green Roof Installation on Gordon Library

Part of the economic analysis of the green roofs consisted on calculating the total savings of installing this technology on the building. The savings included the overall energy reduction due to the benefits of roof gardens and stormwater savings. These costs were estimated using a national average consumption for college buildings, as specific information regarding energy consumption of the Gordon Library was not obtained.

#### 3.5.3 Economic Analysis of Solar Collectors on Stoddard B

When determining the overall installation cost of the proposed solar collector design on Stoddard B, a simple approach was employed. The result of this analysis is the number of years the solar collectors will take to pay itself off. This was completed by estimating the fixed cost of the proposed systems as well as the amount of money it will save WPI per year in the future.

#### 3.5.3.1 Fixed Cost

The first step in the analysis was to determine the fixed cost, which are costs that do not change with an increase or decrease in the amount of goods or services provided. In this case, the fixed cost referred to the price of technology and its installation cost. The table below provides the steps to determine this.

Step 1: Fixed Cost			
Variable: Reference/Equation:			
Cost of Solar Panels - \$	Unit Technology Cost*Number of Solar Panels		
Installation Cost (\$)  Collector installation cost per hour*(time required for installation) + Tank installation cost			
Cost of Solar Panels + Installation cost -\$			

#### 3.5.3.2 Annual Savings

To determine the annual savings, a number of variables that change with time were considered. These variables are the current spending of WPI in water heating, the annual savings provided by the collectors, and any maintenance fee. The WPI facilities departments and the technology's webpage provided this information. The table below shows the procedure to calculate these variables.

Step 2: Annual Savings			
Variable: Reference/Equation:			
Number of Collectors*Savings per panel			
Obtained from Website			
Annual Savings – Maintenance Cost -\$			

# 3.5.3.3 Payback Period

The calculation of the amount of years the technology will take to pay itself off is fairly simple. The annual savings from the technology is divided from the cost of technology plus its installation, or fixed cost, as seen in the equation below.

$$Payback\ Period = \frac{Fixed\ Cost}{Annual\ Savings}$$

# CHAPTER 4: IDENTIFY BUILDINGS FOR CONSIDERATION

Through online research, a list of requirements for buildings to have for supporting sustainable rooftop technologies was created. This list was categorized into the following sections: age of building, exposure to sun, slope of roof, and existing sustainable rooftop technology. A description of each category and its corresponding requirement for sustainable rooftop installation is located in Table 13.

Additionally, an initial list of all 29 buildings at WPI was created. The list contains the following information related to each building: type of building, year constructed, number of stories, trees or buildings blocking south side of roof, type of roof, and existing sustainable rooftop technology. The number of stories does not include the basement because the basement does not affect the elevation of the building above ground. Solar panels and solar collectors must be angled facing south, therefore sloped roofs facing south or flat roofs are sufficient for the installation of these technologies. Green roofs can only be constructed on flat roofs. A list of the buildings at WPI and their respective information is located in Table 14.

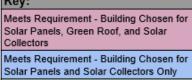
By comparing Table 13 and Table 14, 11 buildings were identified, out of the initial 29 buildings, for further analysis for solar panel, green roof, or solar collector installation. The 11 buildings are identified and highlighted in Table 14. Eight out of the 11 buildings have the ability to support solar panels, green roofs, and solar collectors. Three out of the 11 buildings have the ability to support only solar panels and solar collectors, since their roofs are sloped and have no flat section for green roofs. The next step involved bringing the list of 11 buildings to WPI Facilities Department for further examination and analysis.

Table 13: List of Requirements for Buildings to have for Supporting Sustainable Rooftop Technologies

Category	Description	Requirement	
1) Age of Building	Depending on the material, roofs typically last anywhere from 20-50 years before maintenance needs to occur.	For maintenance purposes, the building must have been constructed within the last 50 years (1967).	
2) Exposure to Sun	In order for solar panels, green roofs, and solar collectors to produce the most energy, they need to have the greatest exposure	Physical Observation: make sure there are no surrounding trees or buildings which block the roof's exposure to the sunlight (south side of roof).	
to the sunlight. Green roofs also need exposure to rainf		The building must be greater than two stories tall. This does not include if there is a basement.	
	According to the geographic location of Worcester, MA, solar	The roof of the building must be flat.	
3) Slope of Roof	panels and solar collectors have the greatest exposure to sunlight when they are faced south. Green roofs can only be placed on a flat roof; solar panels and solar collectors can be placed on a sloped or flat roof.		
4) Existing Sustainable Roofing Technology	Sustainable roofing technology includes a roof which contains any type of solar panel, green roof, or solar collector system.	The building must not already have an existing sustainable roofing technology.	

Table 14: Initial List of Buildings at WPI

Building	Type of Building	Year Constructed	Number of Stories (Not Including Basement)	Trees or Buildings Blocking South Side of Roof	Type of Roof	Sustainable/ Type
Gateway Park I	Academic	2007	4	No	Flat	No
Gateway Park II	Academic	2013	4	No	Flat	No
Alden Hall	Academic	1940	Varies (>2)	No	Slope - Not Facing South	No
Atwater Kent	Academic	1907	3	No	Slope/Flat	No
Bartlett Center	Administration	2006	3	No	Slope - Facing South	No
Boynton Hall	Administration	1868	3	No	Slope - Facing South	No
Daniels Hall	Residential	1963	4	No	Flat	No
East Hall	Residential	2008	5	No	Flat	Green Roof
Ellsworth Apartments	Residential	1972	2	No	Slope - Facing South	No
Faraday Hall	Residential	2013	4	No	Flat	No
Founders Hall	Residential	1984	4	No	Slope - Facing South	No
Fuller Laboratories	Academic	1990	4	No	Flat	No
Gateway Parking Garage	Parking	2010	5	No	Flat	No
Gordon Library	Academic	1967	4	No	Flat	No
Goddard Hall	Academic	1965	4	No	Flat	No
Harrington	Athletic	1968	3	No	Slope - Facing South	No
Higgins Laboratories	Academic	1941	3	No	Slope/Flat	No
Higgins House	Administration	1923	2	No	Slope - Facing South	No
Institute Hall	Residential	1989	3	No	Flat	No
Kaven Hall	Academic	1954	2	No	Slope - Facing South	No
Morgan Hall	Residential	1958	4	No	Flat	No
Olin Hall	Academic	1958	2	No	Slope/Flat	No
Project Center	Academic	1902	2	Yes (Building)	Slope - Not Facing South	No
Rubin Campus Center	Academic	2001	2	Yes (Building)	Flat	No
Salisbury Laboratories	Academic	1889	4	No	Flat	No
Sanford Riley Hall	Residential	1926	4	No	Slope - Facing South	No
Sports & Recreational Center	Recreational	2012	4	No	Flat	Solar Collectors
Stoddard Complex	Residential	1969	3	No	Flat	No
Stratton Hall	Academic	1894	4	No	Flat	No
Washburn Shops	Academic	1868	3	No	Slope/Flat	No



Meets Requirement - Building Not Chosen

A meeting was scheduled with the Director of Facilities Operations, Bill Spratt, on Thursday, October 26<sup>th</sup>, 2017. The beginning of the meeting involved describing the objectives and goals of the project. The list of 11 buildings chosen for further consideration was then given to Mr. Spratt. After discussion about energy consumption and available design drawings, the list was narrowed down to three buildings: Gordon Library, Stoddard B, and the Gateway Parking Garage. Additionally, it was discovered that Washburn Shops is the powerhouse which produces and distributes energy to all of the buildings on the WPI campus. Because of this, there is an overall energy consumption value for the campus, and only certain buildings have a separately metered energy consumption value.

Gordon Library was chosen for the installation of a green roof since the rubber rooftop is flat and was recently renovated. Stoddard B was chosen for the installation of solar collectors on its flat stone rooftop. Stoddard B provides an application for the installation of solar collectors since it is a residential building and requires hot water supply for the hospitality of its students. Additionally, this building has a separately metered energy consumption value. The Gateway Parking Garage was chosen by Mr. Spratt for the installation of solar panels. It was chosen since the electric bill is lower than other buildings, which allows a sufficient number of solar panels to produce energy for the entire parking garage. For this application, the solar panels would be elevated above the top level of the parking garage, slanted at an angle facing south. Since the Gateway Parking Garage is not on the main campus, there is a separately metered energy consumption value for this structure.

To conclude, Mr. Spratt informed us that roofs require maintenance every 25-30 years, and he said that the cost of energy consumption is \$0.14 per kW. This cost value will be helpful for performing an economic evaluation of each building; calculating the current cost of energy for the building and determining how much money the sustainable rooftop technology would save over time. Finally, Mr. Spratt said he would be able to provide us with design drawings for each of the considered buildings.

# CHAPTER 5: SOLAR PANEL INSTALLATION ON GATEWAY PARKING GARAGE

This chapter contains information on the specific type of solar panel technology chosen for the Gateway Parking Garage. The technology was chosen based on ease of installation, energy production, and cost. Additionally, this chapter contains information about the rooftop layout and construction process for the installation of solar panels. Pertinent information includes the number of solar panels, dimensions of the technology, as well as the specific location on the roof where the technology should be installed. Finally, this chapter contains associated structural analyses and design information for the steel frame supporting the solar panels above the Gateway Parking Garage.

# 5.1 Selected Solar Panel Technology on Gateway Parking Garage

For the application of solar panels on the Gateway Parking Garage, polycrystalline silicon solar panels were chosen because they are a more economic option than monocrystalline solar panels for larger scaled applications (Battalia, et. al., 2016). SunPower is a manufacturer of solar panel technologies which has been leading global solar innovation since 1985. After researching their products, the SPR-P17-350-COM model was chosen for the application of polycrystalline silicon solar panels. This model minimizes white space between solar cells, eliminates reflective metal lines on the cells, and lowers electrical resistance between cells which increases efficiency (SunPower Corporation, 2017). Additionally, each panel produces a large amount of power, approximately 350 W, which is beneficial for the application on the Gateway Parking Garage (SunPower Corporation, 2017). Our plan was to design a solar panel system which was elevated above the top level of the parking garage. This involved designing a framework of steel columns and beams to support the solar panels. Based on a previous SunPower solar panel application on a parking garage, the panels will be installed directly next to each other, angled facing south, on top of the designed steel structure. Table 15 below contains information on the type, size, weight, energy production, lifespan, and costs of the chosen SunPower polycrystalline silicon solar panel.

**Table 15: Type of Solar Panel Technology Information (SunPower Corporation, 2017)** 

Building	Gateway Parking Garage	
Sustainable Rooftop Technology	Polycrystalline Silicon Solar Panel	
Manufacturer	SunPower	
Model	SPR-P17-350-COM	
Panel Dimensions	81.4" x 39.3" x 1.8"	
Panel Gross Area	22.25 ft <sup>2</sup>	
Panel Weight	51 lbs.	
Panel Energy Production	350 W	
Estimated Panel Lifespan	25 years	
Unit Cost of Technology <sup>11</sup>	\$635.50/panel	
Unit Installation Cost	\$4.00/Watt	
Annual Unit Operational/Maintenance Cost	\$9.53/panel	

# 5.2 Layout and Construction Process for Solar Panels on Gateway Parking Garage

This section contains information on the layout and construction process for the installation of solar panels on the Gateway Parking Garage.

#### 5.2.1 Layout on Gateway Parking Garage

To determine the layout of the solar panels, the number of solar panels to produce the energy consumption demand of the Gateway Parking Garage was calculated. Given by WPI Facilities Department, the annual energy consumption of Gateway Parking Garage is 137,207 kWh. The chosen SunPower polycrystalline silicon solar panel produces 511 kWh of energy per year. By dividing the annual energy consumption demand of Gateway Parking Garage by the annual energy production capacity of one solar panel, it was determined that at least 269 panels would be needed to meet the energy consumption demand of the Gateway Parking Garage. Table 16 contains information on energy, cost, number of panels, and total area of panels. To produce a distributed rectangular area, 272 solar panels were proposed for design. Excess energy produced can be distributed to other surrounding buildings, or sold to a local electrical company. All panels are angled at 10° above the horizontal and facing south. The angle of 10° above the

<sup>&</sup>lt;sup>11</sup> Unit Cost of Technology does not include installation cost; Unit Cost of Technology only accounts for the panel.

horizontal was chosen since this value is the minimum and recommended angle for the chosen SunPower solar panel model. The panels will be elevated on top of a framework of steel columns, beams, and girders. Figure 8 below displays an overhead visual of the top level of the Gateway Parking Garage with the proposed solar panel location, and Figure 9 displays an overhead visual of the solar panel layout.

Table 16: Installation of Solar Panels on Gateway Parking Garage Information

GATEWAY PARKING GARAGE	Current Installation of SunPower Polycrystalline Silicon Solar Pane		
<b>Annual Energy Demand/Production</b>	137,207 kWh	511 kWh/panel	
Annual Cost of Energy Paid/Saved	\$19,209 \$71.54/panel		
Number of Panels	272 panels		
Total Area of Panels	6,052 ft <sup>2</sup>		

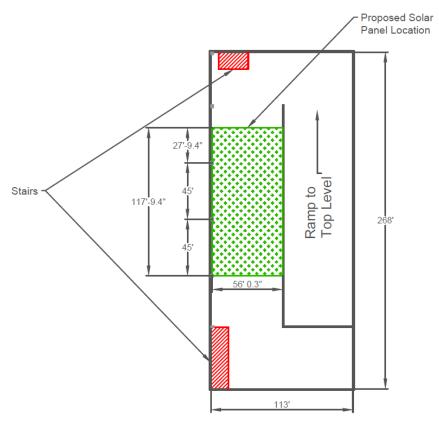


Figure 8: Plan View of Top Level of Gateway Parking Garage with Proposed Solar Panel Location

# 17 Rows x 16 Columns 272 Solar Panels

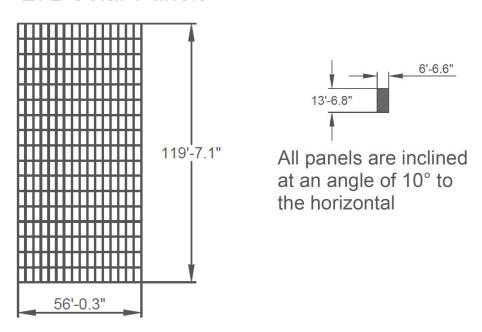


Figure 9: Plan View of Solar Panel Layout

# 5.2.2 Construction Process for SunPower Polycrystalline Silicon Solar Panels

Table 17 contains information on the construction process for SunPower Polycrystalline Silicon Solar Panels. This information from the manufacturer includes safety precautions, module mounting, mounting configurations, and maintenance and cleaning. Figure 10 below displays the orientation, dimensions, and mounting location of the selected SunPower solar panel model. Figure 11 below shows the clamp force location and how the clamp force must be applied. These figures aided when designing the layout of the solar panel configuration by providing dimensions and the orientation of the solar panel model.

Table 17: Construction Process for SunPower Polycrystalline Silicon Solar Panels (SunPower Corporation, 2016)

Safety Precautions	Module Mounting	Mounting Configurations	Maintenance and Cleaning
1) Installations should be performed in compliance with the National Electrical Code (NEC) and local codes	For 96 cell solar panel model on Gateway Parking Garage:      a. Silver frame type     b. Pressure clamps  2) Load ratings:	1) Panels must be installed in landscape orientation at a minimum angle of 10° above the horizontal  2) Minimum of 4" of clearance between the module frames and the	1) Trained SunPower support personnel should inspect all modules annually
	a. Wind load = 2400 Pa	structure 3) Required clearance	
2) Installation of panels should be	b. Snow load = 5400 Pa	between installed modules is a minimum of 1/4" distance	2) Periodic cleaning of module glass results in
performed by qualified personnel	c. Cyclonic wind load = 7500 Pa  3) Mounting location should be 398 mm from the edge of panel (Figure 10)	4) Clamp force location is located in Figure 11	improved performance levels

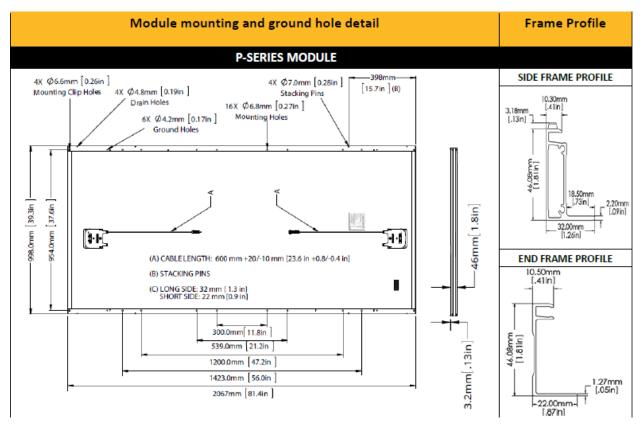


Figure 10: Selected SunPower Module Design (SunPower Corporation, 2016)

Force must not deform top frame flange or glass may break

Force can be applied in line with

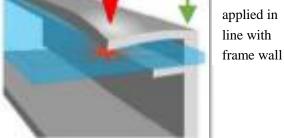


Figure 11: Clamp Force Locations (SunPower Corporation, 2016)

# 5.3 Structural Analyses and Design for Solar Panels on Gateway Parking Garage

After determining the layout and quantity of solar panels, a structural steel framework was designed to support all 272 solar panels. A plan view of the original framework design is shown below in Figure 12. For this original proposal, Table 18 contains information on the number of steel members to support the panels. After continuing the structural analysis, this initial design was changed due to various factors. The original proposed design is also shown on Page 1 of Appendix B.1.

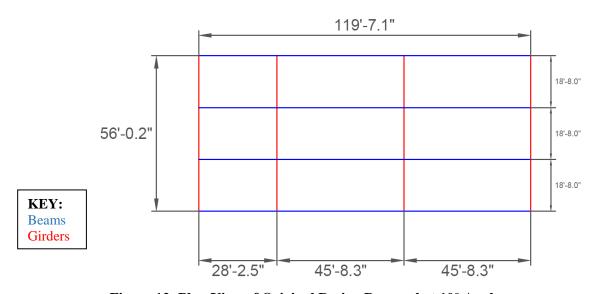


Figure 12: Plan View of Original Design Proposal at 10° Angle

**Table 18: Number of Steel Members for Original Proposal Design** 

Member Type	Quantity
Beam	12
Girder	4
Column	8

#### 5.3.1 Solar Panel Load Calculations

The first step in our analysis involved considering all loads acting on the solar panels: dead load, live load, rain load, snow load, wind load, and seismic load. For solar panels, live load and rain load were considered negligible. Due to the 10° angle of the panels, all rain would runoff onto the parking garage floor and no ponding was expected. Live load was neglected since the solar panels were not designed for people to walk and operate on. Dead load was calculated by using the weight, area, and number of panels. Finally, snow load, wind load, and seismic load were calculated in accordance with the ASCE 7-10. In addition to the ASCE 7-10, wind and seismic load were calculated in accordance with documents from the Structural Engineers Association of California, which provided information specifically to solar photovoltaic arrays (Structural Engineers Association of California, 2012). All calculated design loads are shown below in Table 19, and all calculations can be found in Appendix B.1. Provided in the ASCE 7-10, there are seven load combinations which were considered when determining the governing load acting on the panels. These combinations accounted for both gravity and lateral loads. All load combination calculations were made in accordance with the Load and Resistance Factor Design (LRFD) method. The calculated load combinations are displayed in Table 20.

**Table 19: Calculated Design Loads Acting on Solar Panels** 

Loads	Value <sup>12</sup> (psf)
Dead (D)	2.07
Snow (S)	28.98
Wind (W)	25.62
Seismic Horizontal (E <sub>h</sub> )	0.12
Seismic Vertical (E <sub>v</sub> )	0.079
Roof Live (L <sub>r</sub> )	0
Live (L)	0
Rain (R)	0

Table 20: Calculated LRFD Load Combinations per ASCE 7-10

	Value <sup>12</sup> (psf)	
	1.4D	2.9
	1.2D + 1.6L + 0.5(L/S/R)	16.97
Gravity Loads	$1.2D + 1.6(L_r/S/R) + (L/0.5W)$	61.61
	$1.2D + 1.0W + L + 0.5(L_r/S/R)$	42.48
	$1.2D + E_v + L + 0.2S$	8.36
I atomal I anda	0.9D + 1.0W	1.86
Lateral Loads	$0.9D + 1.0E_{h}$	1.98

#### 5.3.2 Supporting Beam Calculations

Different beam sizes were calculated for the exterior and interior beams due to different supporting tributary widths. Steel beam sizes were determined by checking for strength and serviceability requirements. Serviceability included both total deflection and snow deflection. The total deflection limit and snow deflection limit are based on the International Building Code (IBC) which states: a roof beam supporting a plaster ceiling (similar to solar panels) must have a maximum total deflection = L/240, and a maximum snow load deflection = L/360 or 1" (International Building Code, 2014). All calculations were made with the assistance of the AISC Manual. Table 21 shows the process for determining the final member sizes, and Appendix B.2 shows all supporting calculations for both the exterior and interior beam sizes.

85

<sup>&</sup>lt;sup>12</sup> Pounds per square foot (psf) refers to the total area of the solar panels at the 10° angle above the horizontal

**Table 21: Beam Member Sizes** 

Beam Size			Span Length (ft)	Required Plastic Section Modulus Z <sub>x</sub> (in <sup>3</sup> )	Available Plastic Section Modulus Z <sub>x</sub> (in <sup>3</sup> )	Total Deflection = L/240 (in)	Deflection Limit (in)	Snow Defection (in)	Snow Deflection Limit = L/360 or 1" (in)	Commentary
	1.	W14 x 26	45.69	42.4	40.2	-	-	-	-	Failed to Support Self-Weight (Strength)
Exterior Beam	2.	W14 x 30		44.7	47.3	3.72	2.28	-	-	Failed Deflection Performance (Serviceability)
	3.	<u>W24 x 55</u>		<u>46.8</u>	<u>134</u>	<u>0.86</u>	<u>2.28</u>	<u>0.68</u>	<u>1</u>	<u>Satisfied Strength and</u> <u>Serviceability</u>
Interior Beam	1.	W21 x 44	45.69	83.7	95.4	2.5	2.28	-	-	Failed Deflection Performance (Serviceability)
	2.	<u>W24 x 68</u>		<u>89.4</u>	<u>177</u>	<u>1.2</u>	<u>2.28</u>	<u>1</u>	<u>1</u>	Satisfied Strength and Serviceability

# 5.3.3 Laterally Unsupported Beams

Figure 13 is an updated plan view of the original design; it has been updated to include member sizes. As displayed, the beams have a laterally unsupported distance of 45.69 ft or 28.21 ft, which also represents the spacing of the supporting girders. With the concern for lateral-torsional buckling, the next step involved checking to see if the selected beam sizes could withstand this laterally unbraced length  $L_b$  without failing. It was determined that the unbraced length  $L_b = 45.69$  ft was too large for the design loads, and therefore needed to be decreased. Additional lateral support to the beams was proposed by adding girders to reduce the unbraced length  $L_b$ . Table 22 shows the process for determining appropriate unbraced length  $L_b$  values for the W24 x 55 and W24 x 68 beams. Figure 14 shows the new design of the steel members. All supporting calculations are shown in Appendix B.3.

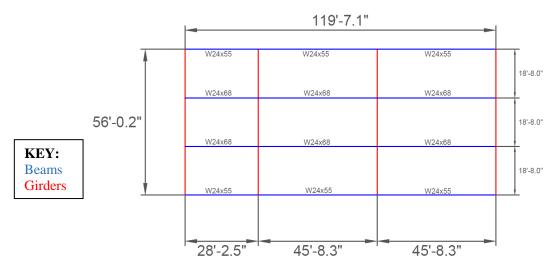


Figure 13: Plan View of Original Design with Beam Sizes

Table 22: Determination of Revised Beam Layout Based on Design for Lateral-Torsional Buckling

Member Size	Length of Member (ft)	Unbraced Length (ft)	Zone	Beam Moment Mu (k-ft)	Moment Capacity ØM <sub>n</sub> (k-ft)	Commentary
	45.60	45.69	Elastic Buckling (Zone 3)	175 427	51.38	Exceeds Moment Capacity
W24 x 55 (Exterior Beams)	45.69	<u>15.23</u>	Elastic Buckling (Zone 3)	175.437	256	Unbraced Length Satisfies Moment Capacity
	28.21	<u>28.21</u>	Elastic Buckling (Zone 3)	66.85	96.93	Unbraced Length Satisfies Moment Capacity
	45.69	45.69	Elastic Buckling (Zone 3)	335.217	106.16	Exceeds Moment Capacity
W24 x 68 (Interior Beams)		<u>15.23</u>	Inelastic Buckling (Zone 2)		482.1	Unbraced Length Satisfies Moment Capacity
	28.21	<u>28.21</u>	Elastic Buckling (Zone 3)	127.83	209.7	Unbraced Length Satisfies Moment Capacity

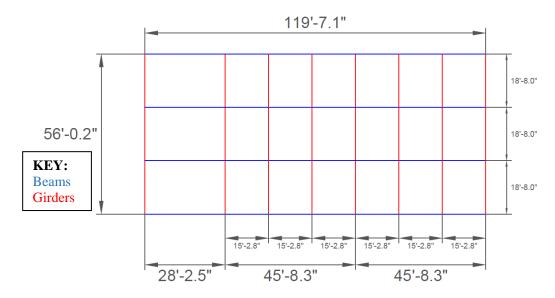


Figure 14: Plan View of Revised Design to Address Lateral-Torsional Buckling in Beams

## 5.3.4 Supporting Girder Calculations

Similar to the beam calculations, a girder size was calculated for all girders within the frame. Steel girder sizes were determined by checking for strength and serviceability requirements. Serviceability included both total deflection and snow deflection, with limits the same as the beam analysis. All calculations were made with the assistance of the AISC Manual.

Later in the design process, the software Risa was used to perform a structural analysis of the steel framework. It was determined that a smaller moment value than originally calculated was acting on the girder, allowing for a smaller girder size to be chosen. However, one girder remained the initial size of W30 x 108 since its tributary width did not satisfy the snow deflection limit. Displayed in Appendix B.8, a new lighter girder size was calculated, despite the one girder with the larger tributary width. Table 23 shows the process for determining the final member size, and Appendix B.4 shows all supporting calculations for the initial supporting steel girder size.

**Table 23: Girder Member Sizes** 

G	irder Size	Span Length (ft)	Required Plastic Section Modulus Z <sub>x</sub> (in <sup>3</sup> )	Available Plastic Section Modulus Z <sub>x</sub> (in <sup>3</sup> )	Total Deflection (in)	Deflection Limit = L/240 (in)	Snow Deflection (in)	Snow Deflection Limit = L/360 or 1" (in)	Commentary
1.	W21 x 68	56.02	154.7	160	7.79	2.8	-	-	Failed Deflection Performance (Serviceability)
2.	2. W30 x 108	56.02	159.7	346	2.66	2.8	Tributary Width ≤ 15.23 ft: 0.75	1	Smaller Size can be Selected Based on Smaller Moment from Risa Analysis (Appendix B.8)
2. W 3	W 30 X 108						Tributary Width = 21.72 ft:	1	
	3. <u>W30 x 90</u>	<u>56.02</u>	<u>141.2</u>	<u>283</u>	<u>2.68</u>	<u>2.8</u>	Tributary Width ≤ 15.23 ft: <u>0.93</u>	<u>1</u>	Satisfied Strength and Serviceability
3.							Tributary Width = 21.72 ft: 1.3	1	Failed Snow Deflection: Remains W30 x 108

## 5.3.5 Laterally Unsupported Girders

The current design is shown below in Figure 15, which remains the same as the previous design shown in Figure 14, however, now has labeled girder sizes. As displayed, the girders have a laterally unsupported length  $L_b$  of 18.67 ft, which also represents the spacing of the beams. With concern for lateral-torsional buckling, the next step involved checking to see if the selected girder size could sustain this unbraced length without failing. It was determined that the unbraced length  $L_b = 18.67$  ft was too large for the design loads, and therefore needed to be decreased. Table 24 shows the process for determining appropriate unbraced length  $L_b$  for the initial W30 x 108 girders. Figure 16 shows the new design of the steel members. All supporting calculations are shown in Appendix B.5.

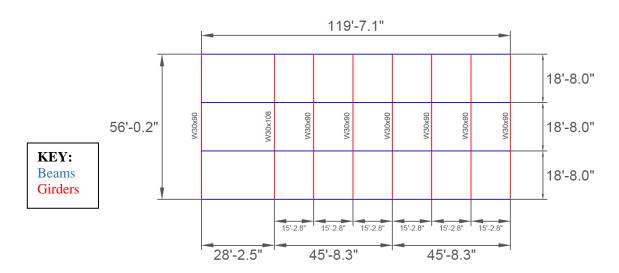


Figure 15: Plan View of Current Design with Girder Sizes

Table 24: Determination of Revised Girder Layout Based on Design for Lateral-Torsional Buckling

Member Size	Length of Member (ft)	Unbraced Length (ft)	Zone	Beam Moment M <sub>u</sub> (k-ft)	Moment Capacity ØM <sub>n</sub> (k-ft)	Commentary
	56.0167	18.67	Inelastic Buckling	598.98	391	Exceeds Moment Capacity
W30 x 108		<u>9.335</u>	Inelastic Buckling		1236	Unbraced Length Satisfies Moment Capacity

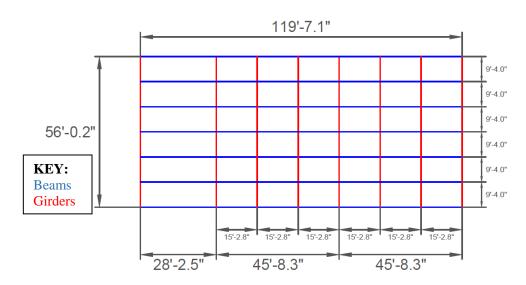


Figure 16: Plan View of Final Beam and Girder Layout

# 5.3.6 Supporting Column Calculations

Figure 17 displays a plan view of the locations and labels of each column supporting the beam and girder frame. Located on the west side (outer edge) of the parking garage are three existing 2 ft x 2 ft concrete columns which are at a height of 3.67 ft above the parking garage floor. These existing columns are located 45 ft apart, and have proposed steel columns placed on top of them to support the solar panel steel frame. Originally, the steel column sizes were designed for the existing floor conditions of the parking garage. Using the AISC manual, the designed steel column's axial strength was checked to satisfy the axial strength capacity of the member size and length. The designed steel column's axial strength was the same for all column members since each column supports the same tributary width, which is equal to half of the girder length. Likewise, all girders were designed to support the area of loads imposed by the beams, and the beams were designed to support the area of loads from the solar panels. To conclude, the column's axial strength and design is based on the imposing girder supported by the column. The initial steel column sizes chosen are displayed in Table 25.

After consideration, the recommendation is to place a 2 ft x 2 ft concrete column with a height of 3.67 ft under each of the five remaining steel columns (C1, C2, C3, C4, C8), which were currently designed to extend to the garage floor. This would allow each steel column across from each other to be identical, having the same length. The new selected steel column sizes are displayed in Table 26. Figure 18 displays an elevation view of the columns placed on top of the 2 ft x 2 ft concrete columns. All column calculations are shown in Appendix B.6.

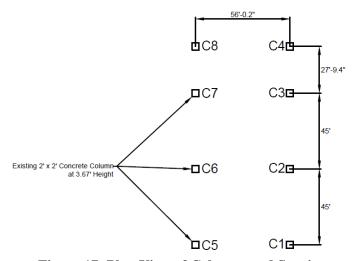


Figure 17: Plan View of Columns and Spacing

**Table 25: Initial Chosen Column Sizes** 

Column Number	Member Size	Member Length (ft)	Column Axial Strength P <sub>u</sub> (k)	Axial Strength Capacity Ø <sub>c</sub> P <sub>n</sub> (k)
1	W8 x 31	10	48.35	317
2	W8 x 31	17.93	48.35	178
3	W8 x 31	25.87	48.35	86.5
4	W8 x 31	30.77	48.35	61
5	W8 x 31	6.33	48.35	362
6	W8 x 31	14.26	48.35	230
7	W8 x 31	22.2	48.35	111
8	W8 x 31	30.77	48.35	61

**Table 26: Final Chosen Column Sizes** 

Column Number	Member Size	Member Length (ft)	Column Axial Strength P <sub>u</sub> (k)	Axial Strength Capacity Ø <sub>c</sub> P <sub>n</sub> (k)
1	W8 x 31	6.33	48.35	362
2	W8 x 31	14.26	48.35	230
3	W8 x 31	22.20	48.35	111
4	W8 x 31	27.10	48.35	74.5
5	W8 x 31	6.33	48.35	362
6	W8 x 31	14.26	48.35	230
7	W8 x 31	22.20	48.35	111
8	W8 x 31	27.10	48.35	74.5

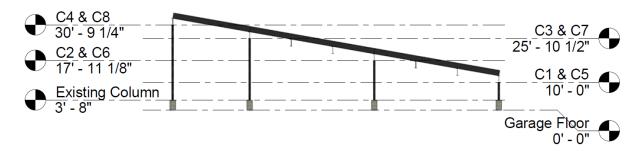


Figure 18: Elevation View of Columns Placed on 2 ft x 2 ft Concrete Columns

# 5.3.7 Second-Order Elastic Analysis

An approximate, second-order elastic analysis was performed to ensure that the columns were sufficiently designed to satisfy the stability requirements of Chapter 3 of the *AISC*Specification for Structural Steel Design. The first step of this process involved inputting both

gravity and lateral loads, acting on the designed rigid frame, into the structural analysis software, Risa. Moment values due to gravity and lateral loads were obtained, from Risa, for the top and bottom of the column. The next step involved inputting these moment values into a created Excel sheet to go through the approximate second-order elastic analysis calculation outlined in Appendix 8 of the AISC Specification. The outcome of this analysis involves obtaining a value from the AISC Chapter H interaction equation. If the outcome value is less than or equal to one, then the column is adequate. If the outcome value is greater than one, then a new column or girder size must be chosen, and the analysis must be repeated. For this analysis, all of the selected column sizes satisfied the interaction equation and were considered adequate. The input for the Risa analysis and the outline for the second-order elastic analysis are displayed in Appendix B.7. Table 27 shows various results from the second-order elastic analysis for each column.

From the Risa analysis, the moment obtained from the connection of the column and girder was smaller than the moment value used to design the original girder. Therefore, calculations were made to determine a new girder size smaller than the original girder size. This girder size, W30 x 90, is located above in Table 23. The calculation process for the new girder size is located in Appendix B.8.

Table 27: Results from Approximate Second-Order Elastic Analysis and Interaction of Flexure and Compression

Column Number	Member Size	Multiplier B <sub>1</sub>	Multiplier B <sub>2</sub>	P <sub>r</sub> (k)	M <sub>rx</sub> (k-ft)	$P_{c}(k)$	M <sub>cx</sub> (k-ft)	Interaction Value	Interaction Limit
1 & 5	W8 x 31	1	1	13.17	33.39	370	114	0.31	1
2 & 6	W8 x 31	1	1.03	26.39	41.11	243.32	97.2	0.48	1
3 & 7	W8 x 31	1	1.12	37.73	44.31	117	78.36	0.83	1
4 & 8	W8 x 31	1	1.11	24.53	25.66	80.5	64.69	0.66	1

## 5.3.8 Baseplate Design

Baseplates were designed to connect the steel columns to the supporting 2 ft x 2 ft concrete columns. The length, width, and thickness of each baseplate were determined using the load and moment acting on the concrete column from the steel column. The moment was found at the bottom of the steel column using the Risa analysis. To determine the moment-resisting thickness of the baseplate, the largest moment and load values out of all the columns were used

to determine the largest minimum thickness required for the baseplates. After analysis, it was concluded that all baseplates will have the same length, width, and thickness. The results of the baseplate design are shown in Table 28. Figure 19 displays the design of the baseplate connecting the steel column from the rigid frame to the 2 ft x 2 ft concrete column. All supporting calculations are shown in Appendix B.9.

Column Number	Baseplate Material	Width-B (in)	Length-N (in)	Thickness $t_{req}$ (in)
1	A36 Steel	9	9	0.5
2	A36 Steel	9	9	0.5
3	A36 Steel	9	9	0.5
4	A36 Steel	9	9	0.5
5	A36 Steel	9	9	0.5
6	A36 Steel	9	9	0.5
7	A36 Steel	9	9	0.5
8	A36 Steel	9	9	0.5

**Table 28: Baseplate Design Results** 

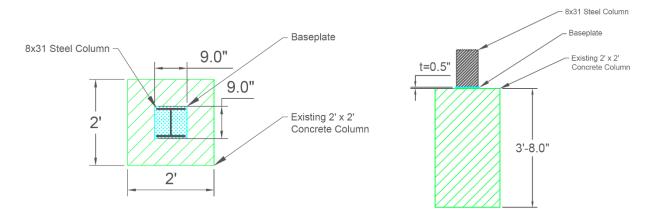


Figure 19: Overhead and Side Elevation of Baseplate Design

### 5.3.9 Recalculation of Seismic Load

Now that the steel frame has been designed to support the solar panels, the seismic load was recalculated. From the ASCE 7-10, it is required that the designed structure weight is 25% less than the current structure weight. This check was done to assess the impact of the designed structure to the existing parking garage structure. Based on this, new horizontal and vertical

seismic loads were calculated. The recalculation of the new horizontal seismic load equals 1.28 psf, compared to the original 0.12 psf. The recalculation of the new vertical seismic load equals 0.64 psf, compared to the original 0.079 psf. These new seismic load values were plugged into the Risa analysis to check for the adequacy of the column sizes. Additionally, the new seismic load values were used to check their effect on the original beam and girder design. After analysis, it was concluded that the updated seismic loads do not have a large impact on the steel framework design, and therefore does not need to be changed for the updated seismic loads. Calculations for the new seismic load are contained in Appendix B.10.

### 5.3.10 Reinforcement in 2 ft x 2 ft Concrete Columns

The last step involved designing the reinforcement needed to be placed inside of the 2 ft x 2 ft concrete columns supporting the steel frame. This involved determining the number and type of steel reinforcing rebar, as well as the thickness of the ties wrapped around the steel rebar. The design of the reinforcement is based on axial force and bending moment acting on the concrete columns from the steel frame. Due to the small axial force and bending moment values, the smallest reinforcement ratio value,  $\rho_g$  equal to 0.01, was chosen for each concrete column based on the concrete column strength interaction diagram. The minimum and maximum reinforcement ratio values,  $\rho_{min}$  and  $\rho_{max}$ , were calculated the same for each concrete column based on their concrete properties. After ensuring that the reinforcement ratio  $\rho_g$  satisfied the calculated minimum and maximum values,  $\rho_g$  was used to determine the area of the reinforcing steel rebar. Table 29 displays the results from the concrete reinforcement calculations. Figure 20 shows a cross section of the 2 ft x 2 ft concrete column with the designed reinforcement. All supporting calculations are located in Appendix B.11.

**Table 29: Concrete Reinforcement Results** 

Required Steel Area (in²)	5.76	
Reinforcing Steel Rebar Area (in²)	5.96	
Calculated Minimum Reinforcement Ratio ρ <sub>min</sub>	0.003	
Reinforcement Ratio ρ <sub>g</sub>	0.01	
Calculated Maximum Reinforcement Ratio ρ <sub>max</sub>	0.021	
Bar Diameter (in)	9/8	
Number of Bars	6	
Tie Diameter (in) 2		
6 #9's with 2" ties in existing 2' x 2' concrete		

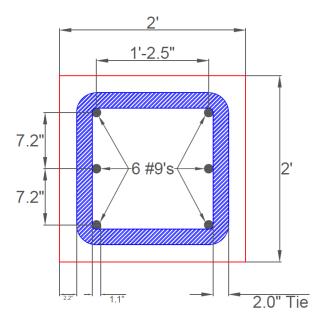


Figure 20: Designed Reinforcement in 2 ft x 2 ft Concrete Column

# 5.3.11 Supporting Steel Frame Final Results

To conclude, a steel frame containing beams, girders, and columns was designed to support solar panels above the top level of the Gateway Parking Garage. It was recommended that the columns of the steel frame be placed on top of 2 ft x 2 ft concrete columns at a height of 3.67 ft. Three out of eight of these concrete columns already exist, however, reinforcing steel was designed for each concrete column. Baseplates were designed to connect the steel columns to the concrete columns. Table 30 displays the size, length, and number of steel members needed for the steel frame. A 3-D perspective of the overall steel design is shown below in Figure 21.

**Table 30: Steel Frame Member Properties** 

Type of Member	Member Size	Member Length (ft)	Quantity
Entonion Domes	W24 x 55	45.69	4
Exterior Beams	W 24 X 33	28.21	2
Interior Beams	W24 x 68	45.69	10
Interior Beams	W 24 X 68	28.21	5
Girders	W30 x 90	56.02	7
Giraers	W30 x 108	30.02	1
		6.33	2
Calaman	W8 x 31	14.26	2
Columns		22.20	2
		27.10	2



Figure 21: Overall Steel Design 3-D Perspective

# CHAPTER 6: GREEN ROOF INSTALLATION ON GORDON LIBRARY

This chapter contains information on the specific type of green roof chosen for the Gordon Library. The type of green roof was chosen based on ease of installation, energy reduction, and cost. Additionally, this chapter contains information about the rooftop layout and construction process for the installation of a green roof. Pertinent information includes the dimensions of the green roof, as well as the specific location on the roof for its installation. Finally, this chapter contains associated structural analyses and design information.

# 6.1 Selected Green Roof Technology on Gordon Library

For the application of a green roof on Gordon Library, an extensive green roof was chosen. An extensive green roof was selected, over an intensive green roof, since extensive green roofs are less expensive, have a lower overall weight, and require less maintenance. Since there is no public access to the Gordon Library rooftop, a green roof with sidewalks, benches, and tables for human interaction was not designed. Instead, the technology was designed over an area with the purpose of reducing the building's energy consumption. In addition, the low cost of an extensive green roof can make this system cost-effective, feasible for construction, and easy to implement on the sustainable plan of WPI. The green roof will have small pathways along its sides only for maintenance use. Roof and gutter checks for extensive green roofs are required twice a year. Additionally, extensive green roofs require weeding three times a year and the application of fertilizer once a year (Green Roof Guide, n.d.). Table 31 contains information on the type, weight, energy reduction, lifespan, and costs of an extensive green roof.

Table 31: Information about Green Roof Installation<sup>13</sup>

Building	Gordon Library
Sustainable Rooftop Technology	Extensive Green Roof
Dimensions	80' x 167'-85'8" x 30'8"
Gross Area	10,732.89 ft <sup>2</sup>
Weight	20-35 psf (4-6" soil depth)
Energy Reduction	12% overall energy reduction
Lifespan	50 years
Cost of Technology & Installation	\$15 psf
Annual Operation & Maintenance Cost <sup>14</sup>	\$0.27 psf

This table presents an overall description of the selected technology for the Gordon Library. All the information that is presented in the table was specifically selected to suit the dimensions of the roof and energy consumptions of the building. Likewise, it is shown that the lifespan of the roof extends up to 50 years, reducing maintenance, repairs and restoration costs of the roof.

# 6.2 Layout and Construction Process for Green Roof on Gordon Library

This section contains information on the layout and construction process for the installation of a green roof on Gordon Library.

# 6.2.1 Layout on Gordon Library

Based on rooftop drawings of Gordon Library provided by WPI Facilities Department, a roof garden design, which will reduce the overall energy of the building by approximately 12% was proposed (Urban Design Tools, 2017). The proposed design produces an overall area of 10,733 square feet with a six-inch soil depth. The extensive green roof that was chosen will contain vegetation including sedum, herbs, perennials, and shrubs. Additionally, the roof garden

<sup>&</sup>lt;sup>13</sup> (Urban Design Tools, 2017)

<sup>&</sup>lt;sup>14</sup> http://www.epdmroofs.org/attachments/sproul-et-al economic-comparison-of-white-green-and-blackflat-roofs-in-the-us.pdf

will contain drainage plates to collect all water absorbed by the vegetation. Water is retained within pockets on the upper sides of the drainage plates. Excess water will spill over the edges of the plates and funnel towards the existing drainage system on the roof. Figure 22 illustrates the proposed layout of the green roof on Gordon Library and the appropriate path for maintenance. It is clear that most of the roof is composed of the green roof technology. This is because the benefit of a roof garden is noticeable with a larger area. The proposed design is quite simple due to the flat surface of the roof. This is beneficial for construction and design purposes.

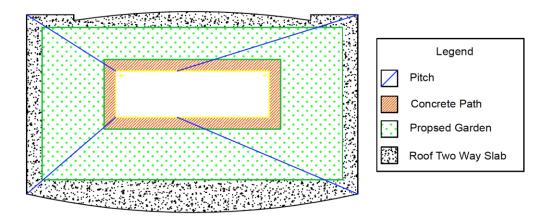


Figure 22: Green Roof Design and Layout on Gordon Library

# 6.2.2 Construction Process for Extensive Green Roofs

The steps for the installation process of an extensive green roof are displayed in Table 32.

A visual of the different layers of an extensive green roof is provided in Figure 23.

Table 32: Steps for Installation of Extensive Green Roof<sup>15</sup>

Step 1	Install a waterproof membrane that possesses monolithic properties. It could be made of plastic or rubber,
	and it needs to fit on top of a traditional roof decking.
Step 2	Place one sheet of plastic with a maximum thickness of 6 millimeters over the already installed
	waterproof membrane.
Step 3	Install one or more sheets of foam insulation with a <sup>3</sup> / <sub>4</sub> " thickness over the plastic sheet. This layer
_	provides proper contact with the damp soil.
Step 4	If the space directly below the green roof does not have proper conditioning, some protection needs to be
	provided to the waterproof membrane. The protection can be made up of fan –board-type insulation or can
	be a layer of building felt.
Step 5	Add one drainage mat with capillary spaces at the top portion of the insulation, after the protective layer.
	To prevent soul from clogging over the mat, place the mat in a manner that the felt side faces upward.
Step 6	Install framing around the perimeter of the green roof. This can be done with wood, mesh gutter-type
	guards, or some other type of edging material that can hold soil with more strength to keep it in the right
	place. Intermediate angle-type support, over vertical edging, might be required to support or improve
	sturdiness.
Step 7	The horizontal leg in the support system can be slipped under a drainage mat that is weighted with a
_	specific amount of topping soil so that overturning can be avoided.
Step 8	Once the structure is ready, add soil to the sections.
Step 9	Once soil is added, set plants in specific locations.
Step 10	Water the area to allow for proper settling of plants.

101

<sup>&</sup>lt;sup>15</sup> (My Rooff, 2017)

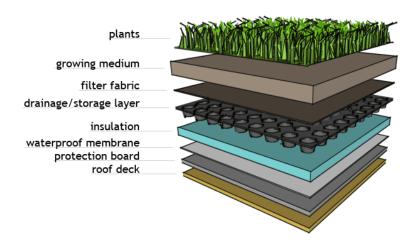


Figure 23: Layers of an Extensive Green Roof (My Rooff, 2017)

6.3 Structural Analyses and Design for Green Roof on Gordon Library

After obtaining a proper design and layout for the roof garden on Gordon Library, a structural anlysis was made to determine all the loads acting on the existing building (vertically and horizontally), the capacity of the existing roof to support the loads, and the economic cost of implementing a new system into the building. The structural analyses evaluated the existing roof of the building, and its capability to sustain a green roof based on the design provided.

### 6.3.1 Vertical and Horizontal Load Calculations

One of the first stages to complete the structural analysis of the building was to obtain all the loads that are acting on the building. This include, Live, Dead, Rain, Snow, Wind and Seismic loads. For this case, the analysis of the loads was done in two different ways. One, for the existing building as it is, and the second one for the green roof layout. The purpose of this is to show how some of the loads differ when they have an extra applied oad on the roof, in this case the roof garden. Each load that is acting on the building had its own characteristics in accordance with ASCE 7-10, FM-Global and the *International Building Code* (IBC). It is important to state that the analysis for the gravity loads acting on the building is different than the one for lateral loads. Calculating the load combinations manually can be very complex when the combination requires both vertical and lateral loads. For that reason, the use of the software packages RISA 2D and RISA 3D was necessary in the analysis. This software allows the user to compute all the loads acting on the building while using as many load combinations as needed.

6.3.1.1 Live Loads

Live loads of the 1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup> and roof floor were based on occupancy and architectural designs of the building. The American Society of Civil Engineers 7-10 (ASCE 7-10) Chapter 4, was used to get this occupancy loads. Live loads in each floor are going to differ, as each floor has a different area for specific live loads. Some assumptions were made to select this area, as there are no specific details in the drawings that determine where each live load will be acting in each floor. The live loads that were considered in this building for calculation are shown in Table 33 below.

Table 33: Live Loads in Accordance with ASCE 7-10

Description	Load (psf)
Roof 16	20
Meeting Room	40
Office Room	50
Reading Room	60
Corridor Above 1st Floor	80
Corridor 1st Floor	100
Mechanical Room	100
Stairs	100
Library Stacks	150

The application areas for live loads shown in Table 33 were determined using AutoCAD Software and a sample prototype of the second floor of the library is illustrated in Figure 24 below. For the design of each floor and its occupancy live loads, see Appendix C.1.

103

<sup>&</sup>lt;sup>16</sup> ASCE 7-10 specifies a roof used for roof garden to have a live load of 100 psf: however, a live load of only 20 psf is more appropriate in roof gardens that do not need high maintenance and do not allow public access to it.

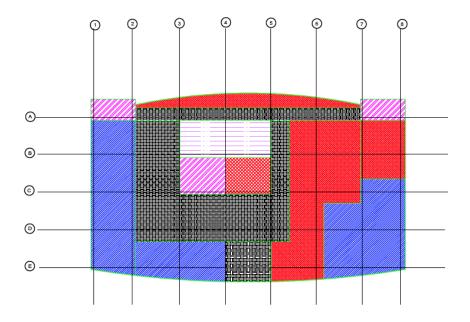


Figure 24: Live Loads Occupancy Area on 2nd Floor of Gordon Library

# 6.3.1.2 Dead Loads

The dead load was calculated by doing an analysis of the weight for each floor of the building. The loads for each floor includes the weight of the two-way dome slab, internal and external concrete walls, exit stairs, and roof penthouse. The dead load also included the designed green roof. An approximate weight per floor is shown in Table 34; see Appendix C.1 for extended dead load calculations.

Table 34: Weight per floor Gordon Library

Weight Library Results		
Floor	Weight (kips)	
Ground - 1st	3,734.31	
1st - 2nd	3,597.36	
2nd - 3rd	3,479.40	
3rd- Roof	2,818.64	
Weight of Library (kips)	13,629.71	

A more approximate approach to the weight of the two-way dome slab is shown in Table 35 below. These values are given by the CRSI according to the slab thickness and dome depth for a waffle slab. The weight of two-way dome slab is given in pounds per square feet.

Table 35: Weight of Two-Way Dome Slab in Accordance with CRSI<sup>17</sup>

Two-Way Dome Slab Dimensions			
Slab Thickness	Dome Depth	Weight (psf)	
3 inches	10 inches	91	
4 inches	10 inches	103	

### 6.3.1.3 Rain Loads and Snow Loads

Rains and snow loads did not vary by implementing a green roof on the building. These loads were determined in accordance with FM Global and ASCE 7-10 Chapter 7 respectively.

# 6.3.1.4 Seismic Loads and Wind Loads

Seismic and wind loads were calculated in accordance with ASCE 7-10 and by using two step-by-step code masters. These loads were first calculated without considering the roof garden as shown in Table 36. After this calculation was done, some steps were re-done but this time including the weight of the green roof on the building, Table 37.

Table 36: Calculated Loads without Green Roof Technology

Loads	Value (psf)
Dead (D)	Table
Snow (S)	34.65
Wind (W)	Figure 27 and Figure 28
Seismic	Figure 30
Roof Live (L <sub>r</sub> )	20
Live (L)	0
Rain (R)	32

Table 37: Total Weight of Gordon Library per Floor

Weight Library Results						
Floor Weight (kips)						
Ground - 1st	3734.31					
1st - 2nd	3597.36					
2nd - 3rd	3479.39					
3rd- Roof	2818.64					
Weight of Library (kips)	13629.71					

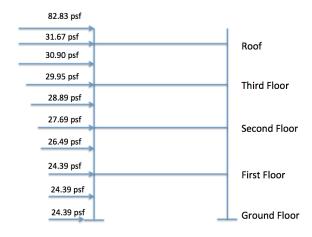
<sup>&</sup>lt;sup>17</sup> Concrete Reinforcing Steel Institute

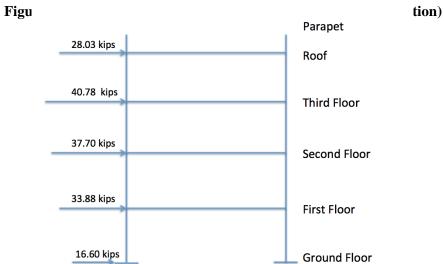
A simple calculation was done to determine the total weight of the roof garden on Gordon Library. It was assumed that the weight of the green roof technology was 35 pounds per square feet. This value was obtained in accordance to the depth of the soil, the type of green roof installed, and the layers used. Table 38 shows the overall weight of an extensive green roof with a six inch soil-depth.

**Table 38: Total Weight of Green Roof** 

Green Roof System							
<b>Description</b> Value							
Weight of Green Roof	35	psf					
Gross Area	10,733.00	$ft^2$					
Weight of Green Roof System	375.66	kips					

The entire analysis and results of the seismic and wind load procedures are illustrated in Figures 25-30 below. These figures represent the total force in kips acting on the building laterally along its height. The figures represent wind forces in the North-South and East-West directions, the total resultant per floor for each direction, and seismic forces. For the wind load analysis, the forces also changed for the parapet on the roof of the building. As can be seen in Figure 27, the parapet has a distributed load of 82.83 pounds per square feet in the North-South direction, which drastically changed with respect to the other floors of the building. The parapet has a separate analysis and equation, causing this value to increase.





**Figure 26: Resultant Wind Forces (North-South Direction)** 

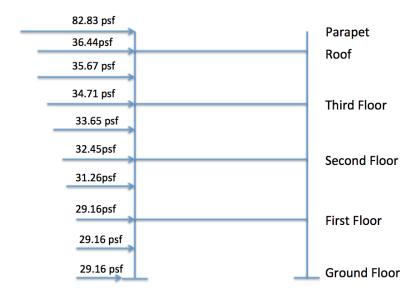
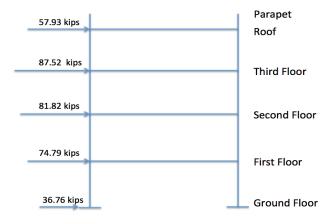


Figure 27: Wind Load Distribution per Floor (East-West Direction)



**Figure 28: Resultant Wind Forces (East-West Direction)** 

As shown in the figures above, the resultant wind forces in the East-West direction are more critical than the wind forces in the North-South direction. For this reason, the resultant wind forces used for analysis were the ones from the East to West direction.

In addition to the resultant wind forces acting laterally on the building, a Components and Cladding analysis was done to understand how building components need to resist the wind forces. Table 39 shows the results for each zone in the building as stated in Chapter 30 of the ASCE 7-10. This table was generated with the guidance of Table 2 and 3 from Section 3.3.2.1, and the wind pressure at the roof.

Table 39: Wind Components and Cladding Results for Gordon Library

Results Components and Cladding										
ADEA (SE)	ZO	NE 1	ZONE 2		ZONE 3		ZONE 4		ZONE 5	
AREA (SF)	+	-	+	-	+	-	+	-	+	-
$\leq 10 \text{ ft}^2$	15.83	-38.91	15.83	-65.30	15.83	-98.28	38.91	-42.21	38.91	-52.10
$\geq$ 500 ft <sup>2</sup> walls & $\geq$ 100 ft <sup>2</sup> roof	12.53	-35.61	12.53	-42.21	12.53	-42.21	29.02	-32.32	29.02	-32.32

A similar approach was taken for the seisimc analysis of the building. Figures 29 and 30 represent the lateral loads in kips acting at each floor of the Gordon Library.

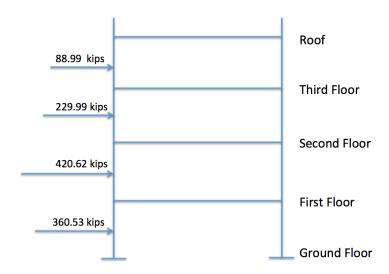


Figure 29: Seismic Forces Acting on Building

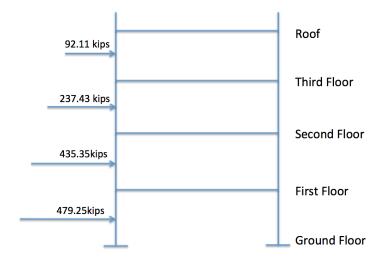


Figure 30: Seismic Forces Acting on Building with Green Roof Technology

# 6.3.2 Basic Load Combinatination Analysis

An assessment was performed for each floor of the structure with all the basic load combinations and with customized combinations that could be useful. All basic combinations were in accordance to ASCE 7-10, Chapter 2, However, some of the combinations used are not going to be stipulated in the ASCE 7-10 as they were modified to suit the structure more accurately (based on the more significant loads). See Table 40 for load combinations that were used in this structure and their values in pounds per square foot.

**Table 40: Basic Load Combinations** 

<b>Load Combinations</b>						
	1.4D					
	1.2D + 1.6L + 0.5(L/S/R)					
Gravity Loads	1.2D + 1.6S + L					
	1.2D + 1.6S + 0.5W					
	$1.2D + 1.0W + L + 0.5(L_r/S/R)$					
	$1.2D + E_v + L + 0.2S$					
Lateral Loads	0.9D + 1.0W					
	$0.9D + 1.0E_h$					

By obtaining the values of all load combinations, the most significant combination was selected and therefore the most conservative load in pounds per square feet. This assessment was performed for each floor of the building as the loads accumulated from the roof to the first floor.

# 6.3.3 Structural Analysis and Capacity of Building

In order to determine if the building could resist the new loads imposed on its roof, a structural analysis was performed. The columns and the waffle slabs of each floor of the building were analyzed and then compared to their actual capacity.

### 6.3.3.1 Overturning Moment of the Building

Overturning moment of the structure relates to the capacity of the system to resist lateral loads due to seismic. For this structure, the overturning moment was not analyzed because the green roof technology imposes additional weight to the existing structure, and the overturning moment should not be a concern for the design.

# 6.3.3.2 Factored Design Load of Column (Axial Capacity $\Phi Pn$ )

The first check consisted of simply analyzing the reinforced concrete capacity of each of the columns in the building. This calculation involved the following:

- Dimensions and shape of the column,
- Reinforcement properties (dowels<sup>18</sup> and spirals),
- Total area of concrete and steel in the column
- Concrete and steel strength.

**Table 41: Concrete and Steel Strength Properties Gordon Library** 

Concrete and Steel Properties							
Steel Yield Strength (psi) fy 60,000							
Concrete Strength (psi)	f'c	4,000					
Reduction Factor	ф	0.7					

It was assumed that the steel strength is approximately 60,000 psi. This value was obtained through research of historic requirements of AISC for old buildings. Figure 31 below, illustrate

111

<sup>&</sup>lt;sup>18</sup> A "dowel" refers to the vertical steel bars inside of the column.

the requirements per year of the AISC and the values for steel. The book titled, *Iron and Steel Beams 1873 to 1952*<sup>19</sup> also provides a table for structural steel specifications.

Table 1 ASTM and AISC History								
		AISC						
Year	Standard	<b>T.S.</b> (ksi)	<b>Y.P.</b> (ksi)	Basic Working Stress				
1901	A9 Buildings	60-70	0.5 T.S.	_				
1909	A9 Buildings	55-65	0.5 T.S.	_				
1923	A9 Buildings	55-65	0.5 T.S.	18				
1924	A9 Buildings	55-65	0.5 T.S.	18				
1933	A9 Buildings	60-72	0.5 T.S. (not less than 33)	18				
1936	A9 Buildings	60-72	0.5 T.S. (not less than 33)	20				
1939	A7 Buildings (and Bridges)	60-72	0.5 T.S. (not less than 33)	20				
1942		Emergency	/ Standards	24				
1960	A7	60-72	0.5 T.S. (not less than 33)	20				
	A36 (Supp.)	58-80	36	22				
	A7	60-72	0.5 T.S. (not less than 33)	20				
1963	A36	58-80	36	$0.6F_{v}$				
1703	A440	varied	varied	$0.6F_{v}$				
	A441	varied	varied	$0.6F_{v}$				
	A242	varied	varied	$0.6F_y$				
1967		7 discontin						
	A36	58-80	36	$0.6F_y$				
1968	A572	varied	varied	$0.6F_y$				
	A588	varied	varied	$0.6F_y$				

Figure 31: Typical Steel Standards for Old Buildings<sup>20</sup>

The following results were calculated for the axial capacity of the columns. The results are tabulated for each floor of the building and based on the column size and the reinforcement properties. The columns that have the most axial capacity, as illustrated in Table 42, are typically the most critical columns in the building. For this reason, the structural analysis was based on these columns to have a realistic idea of how the entire structure will behave when the new load of the green roof is imposed on the building.

 $https://www.aisc.org/global assets/modern-steel/steelwise/30762\_steelwise\_reno.pdf$ 

 $<sup>^{19}\</sup> https://www.aisc.org/globalassets/aisc/publications/out-of-print/iron-and-steel-beams-1873-1952.pdf$ 

<sup>&</sup>lt;sup>20</sup> Gustafson, Kurt. "Evaluation of Existing Structures." *Steel Solutions Center*, https://www.giga.org/globalessats/modern.steel/steelwiga/20762.steelwiga.rope.

Table 42: Axial Capacity of Columns Ground Floor with 60 Grade Steel Reinforcement

Ground to First Floor								
Column Size (in x in)	Ag (in²)	# of Bars	Size of Bar	Ast (in <sup>2</sup> )	Pn <sub>max</sub> (kips)	φPn <sub>max</sub> (kips)		
24x24	576	6	11/9	7.68	2034	1423		
24x24	576	6	10	7.62	2031	1421		
24x24	576	8	10	10.16	2153	1507		
24x24	576	8	11	12.48	2265	1586		
24x24	576	6	9	6	1953	1367		
24x18	432	6	9	6	1537	1076		
29x29	841	8	11	12.48	3030	2121		

Table 43: Axial Capacity of Columns First Floor with 60 Grade Steel Reinforcement

First Floor							
Column Size (in x in)	<b>Ag</b> ( <b>in</b> <sup>2</sup> )	# of Bars	Size of Bar	Ast (in <sup>2</sup> )	Pn <sub>max</sub> (kips)	φPn <sub>max</sub> (kips)	
16x16	256	8	10	10.16	1229	860	
18x18	324	6	9/11	7.68	1306	914	
23x23	529	8	11	12.48	2129	1490	
24x24	576	6	9	6	1953	1367	
24x18	432	6	9	6	1537	1076	

Table 44: Axial Capacity of Columns Second Floor with 60 Grade Steel Reinforcement

Second Floor							
Column Size (in x in)	Ag (in²)	# of Bars	Size of Bar	Ast (in²)	Pn <sub>max</sub> (kips)	φPn <sub>max</sub> (kips)	
16x16	256	8	10	10.16	1229	860	
18x18	324	8	10	10.16	1425	998	
18x18	324	8	11/10	11.32	1481	1037	
18x18	324	6	9/8	5.37	1195	836	
18x18	324	6	8	4.74	1164	815	
23x23	529	8	11/10	11.32	2073	1451	
23X23	529	8	10/7	7.48	1889	1322	
23x23	529	8	10	10.16	2018	1412	

Table 45: Axial Capacity of Columns Third Floor with 60 Grade Steel Reinforcement

	Third Floor							
Column Size (in x in)	Ag (in²)	# of Bars	Size of Bar	Ast (in <sup>2</sup> )	Pn <sub>max</sub> (kips)	φPn <sub>max</sub> (kips)		
12x12	324	8	10/6	6.84	1265	886		
12x12	144	8	9	8	801	561		
12x12	144	6	8	4.74	644	451		
12x18	216	6	8	4.74	852	597		
17x17	289	8	10/9	9.08	1272	890		
17x17	289	8	7/5	3.64	1010	707		
18x18	324	6	8	4.74	1164	815		

As shown in the table above, the axial capacity of the columns  $\phi Pn_{max}$  increases with increasing distance from the roof level. The strongest column is located in the lowest (first) floor of the building because that specific column needs to resist the entire load of the upper floors, plus the loads on that same floor. This table provides the values for Grade 60 Steel<sup>21</sup>. The axial capacities of each column would slightly change if the Grade of the steel changes. See Table 46 and Table 47 for an example of axial capacities  $\phi Pn$  with a different Grade of steel in the first floor of the Gordon Library.

Table 46: Axial Capacities of Columns with 50 Grade Steel Reinforcement

First Floor								
Column Size (in x in)	Ag (in²)	# of Bars	Size of Bar	Ast (in²)	Pn <sub>max</sub> (kips)	φPn <sub>max</sub> (kips)		
16x16	256	8	10	10.16	1142	799		
18x18	324	6	9/11	7.68	1241	868		
23x23	529	8	11	12.48	2023	1416		
23x23	529	8	10	10.16	1931	1352		
23x23	529	6	9	6	1766	1237		
24x24	576	6	9	6	1902	1332		
24x18	432	6	9	6	1486	1040		

<sup>&</sup>lt;sup>21</sup> Grade of steel determine the yield strength of the steel, (e.g. Grade 60 Steel; fy=60,000 psi)

Table 47: Axial Capacities of Columns with 40 Grade Steel Reinforcement

First Floor								
Column Size (in x in)	<b>Ag</b> ( <b>in</b> <sup>2</sup> )	# of Bars	Size of Bar	Ast (in <sup>2</sup> )	Pn <sub>max</sub> (kips)	φPn <sub>max</sub> (kips)		
16x16	256	8	10	10.16	1056	739		
18x18	324	6	9/11	7.68	1175	823		
23x23	529	8	11	12.48	1917	1342		
23x23	529	8	10	10.16	1845	1291		
23x23	529	6	9	6	1715	1201		
24x24	576	6	9	6	1851	1296		
24x18	432	6	9	6	1435	1005		

Tables 46 and 47 show the difference in axial capacities when lower yield strength steel is used. This is important to consider, as come columns have a higher change due to this factor, and it can affect in the overall design of a building or the structural analysis.

As a result of the calculations of the axial capacity of the concrete columns, Table 45 was created. This table illustrates the three sections chosen in the building for analysis. The columns in the three sections were the most critical columns in the building and also the most appropriate columns to work with for symmetry purposes. Some axial capacities are repeated because their properties (dimension and reinforcement) were similar.

**Table 48: Column Axial Capacities per Sections** 

Grade 60 Steel				
Column No.	3rd Floor	2nd Floor	1st Floor	Ground
Column No.	ΦPn (kips)	ΦPn (kips)	ФРп (kips)	ΦPn (kips)
B5	890	1451	1490	1586
C5	707	1322	1490	1586
В6	890	1451	1490	2122
C6	707	1322	1490	1586
Column No.	3rd Floor	2nd Floor	1st Floor	Ground
Column No.	ΦPn (kips)	ΦPn (kips)	ΦPn (kips)	ΦPn (kips)
D1	890	997	1412	1422
E1	560	1413	1412	1422
D2	560	1036	1490	1507
E2	560	1451	1490	1507
Column No.	3rd Floor	2nd Floor	1st Floor	Ground
Column No.	ΦPn (kips)	ΦPn (kips)	ΦPn (kips)	ΦPn (kips)
B2	890	1451	1490	1507
C2	560	1036	1490	1507
В3	560	836	1367	1367
C3	451	1251	1272	1367

A similar table was created with the actual factored design loads (Pu) acting on each column section of the building. Table 46 provides the values of (Pu) calculated with the respective load combinations and superimposed loads acting on the building. See Appendix C.4 for procedure of the calculation.

Table 49: Factored Design Loads (Pu) on Different Sections

Grade 60 Steel				
Column No.	3rd Floor	2nd Floor	1st Floor	Ground
Column No.	Pu (kips)	Pu (kips)	Pu (kips)	Pu (kips)
B5	160	333	459	665
C5	160	329	459	665
В6	160	329	459	626
C6	160	303	459	626
Column No	3rd Floor	2nd Floor	1st Floor	Ground
Column No.	Pu (kips)	Pu (kips)	Pu (kips)	Pu (kips)
D1	53	116	177	266
E1	26	58	88	133
D2	115	253	387	581
E2	72.949775	159.07565	243.9240125	366.2244375
Column No.	3rd Floor	2nd Floor	1st Floor	Ground
Column No.	Pu (kips)	Pu (kips)	Pu (kips)	Pu (kips)
B2	115.4885	265.57394	388.0166	581.65878
C2	115.4885	260.53394	388.0166	388.0166
В3	160.0177	317.36975	470.214225	630.0147
C3	160.0177	329.36975	466.214225	639.2147

From an axial load point of view, implementing a green roof technology on Gordon Library is not going to have critical conditions on the columns of the building. Structural reinforcement for the columns or additional reinforcement methods is not needed.

### 6.3.3.3 Combined Axial and Moment Capacities

Part of the structural analysis of the building included analyzing the most critical columns under a combined axial  $\Phi Pn$  and moment  $\Phi Mn$  capacities. Even though the columns satisfy the condition  $\Phi Pn > Pu$ , it was necessary to determine the effects and the capacity of the moments generated at the column due to the acting loads on the building. Interaction diagrams were created in accordance with the most critical column of the building, Column B5. The interaction diagrams for this column depend on the floor that is being analyzed. This was the only column selected for the analysis, and it would act as a basis for other critical columns in the building. Figures 32 to 34 illustrated below show the interaction diagram for column B5 for the first, second and third floor of the Gordon Library. The blue line in the figure represents the combined

axial and moment capacity without the reduction factor  $\Phi$ , while the green line represents the same axial and moment capacity including the reduction factor.

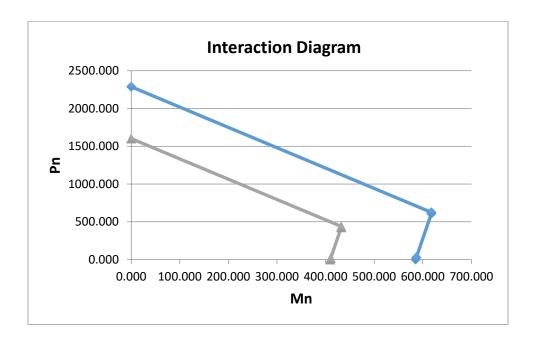


Figure 32: Interaction Diagram Column B5 First Floor

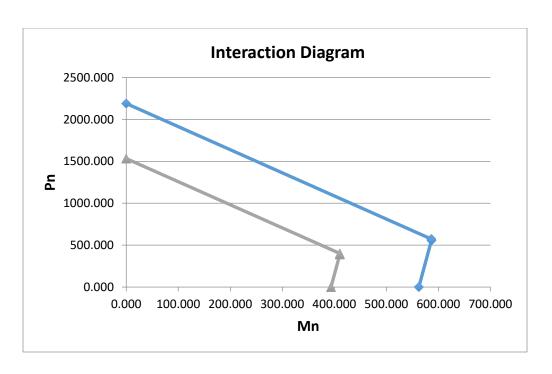


Figure 33: Interaction Diagram Column B5 Second Floor

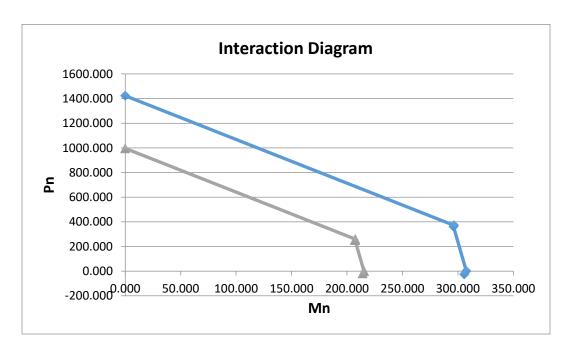


Figure 34: Interaction Diagram Column B5 Third Floor

In addition, the diagram was graphed by obtain five different points as previously noted in the methodology section. Table 47, displays an example of the interaction diagram points for the column in the first floor.

Table 50: Interaction Diagram Points Column B5 First Floor

Interaction Diagram Points					
a	Pn	Mn	ФРп	ФМп	
inches	kips	kips*ft	kips	kips*ft	
23.00	2287	0.0	1601	0.0	
10.35	625	618	438	432	
10.21	607	618	425	432	
6.47	267	587	19	411	
6.33	0.0	585	0.0	410	

It is clear than by doing an axial and moment combined analysis of the columns of the building, the extra load of the green roof is not going to generate any structural damages. This column is assumed to be the most critical in the entire building, so satisfying the conditions for this particular column should make the system appropriate for the Gordon Library.

# 6.3.3.4 Two-Way Dome Waffle Slabs

The construction of waffle flat slabs allows a substantial reduction of the dead load of a building. The advantages of this type of slab construction include the overall weight reduction of a system while providing the building with an architecturally desirable structure. Ease of construction is another advantage of this type of slab, as a typical two-way dome slab is symmetric for the entire floor and it allows a building to be designed without any type of beams.

Table 51: Average Live Loads for each Floor

Live Loads			
Floor Average (psf)			
Roof	20		
3rd	73		
2nd	63.1		
1st	102.2		

The calculated minimum solid head over the columns of the Gordon Library was based on the minimum solid head equation, where the values of  $l_1$  and  $l_2$  were 25 feet and 20 feet respectively. The minimum solid head calculated was 7'6", and the actual value of the solid head for the building was taken as 8'6" as a conservative value. This calculation was done, as the structural drawings did not provide specific details and dimensions for the actual solid head. The 8'6" value it is assumed based on specifications in accordance to the CRSI and its dimension is the same for all drop panels in the building. Figure 35, shows the side view of a column-to-column span for the slab on each floor of the Gordon Library. Each floor is going to have an exact arrangement of the slab except for the roof floor for which the slab will decrease in one inch. Figure 36 below shows a main section of the building that includes an edge, corner and interior column. The distribution of the domes in the slab is as illustrated in the figure, while the sections that do not include any domes are considered the drop panels.



Figure 35: Side View of Waffle Slab on Gordon Library

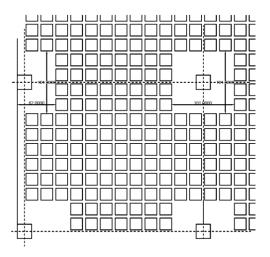


Figure 36: Plan View of Waffle Slab and Drop Panel Distribution

By obtaining the appropriate dimensions of the two-way dome slab and all the loads acting on the building, an analysis of the slab was done. This analysis included the calculations of the load combinations to obtain the most critical (Wu) values. Tables 52 and 53 below show the most critical values in kips per foot for each floor slab. The two tables differ in values for a 20'x25' section and a 20'x21' section. In addition, the (Wu) values increase for each floor, as additional weight has to be resisted. For this reason, the most critical slab is the one in the first floor as it is the one who has to support most of the loads of the building. The Factored Design Load (Wu) for the slab on the fist floor is the highest value for the entire building because the slab has to support the accumulated dead loads of the floors on top.

Table 52: Factored Design Load (Wu) 20'x25' Section

20'x25' Section				
Floor Wu (kips/ft)				
Roof	8.42			
Third	16.89			
Second	24.25			
First	33.00			

Table 53: Factored Design Load (Wu) 20'x21' Section

20'x21' Section			
Floor Wu (kips/ft)			
Roof	7.18		
Third	14.40		
Second	20.73		
First	28.19		

With the calculations of the (Wu) values on the floor slab the strength capacity of the slab was obtained.

Table 54 provides the distributed moments on the waffle slab. As the slabs for each floor of Gordon Library are two-way dome slabs, the distribution of moment is going to be different for

interior, exterior, and edge columns. This table was used as a guideline to obtain the moments on the slab based on the Total Factored Moment (Mo) calculated<sup>22</sup>.

Table 54: Distribution of Total Factored Moment (Mo) on Waffle Slab

	Exterior Edge Unrestrained	Slab Without Beam Between Interior Supports	Exterior Edge Fully Restrained
Interior (Negative factored Moment)	0.75	0.70	0.65
Positive Factored  Moment	0.63	0.52	0.35
Exterior (Negative Factored Moment)	0	0.26	0.65

The calculations for the moment distribution on the slab and the appropriate shear and moment checks were done manually and are shown in Appendix C.6. The process for calculating the moment values for the slab can also be done by obtaining the shear constants from Table 11-5 from the CRSI Handbook as shown in Figure 37 below. The full table with different column sizes and slab dimensions can be obtained from the CRSI Handbook. The calculations and results for an end and interior span for the waffle slab of the first floor are shown Tables 51-54.

TABLE 11-5 PERIPHERAL SHEAR CONSTANTS AT COLUMNS										
		Co	Corner Column Edge Column			Inte	rior C	olumn		
Square Column (in.)	Slab or Drop* (in.)	C <sub>AB</sub> = y <sub>t</sub> (in.)	$A_c = b_o d$ (in.2)	<i>J<sub>c</sub></i> (in.⁴)	C <sub>AB</sub> = y <sub>t</sub> (in.)	$A_c = b_o d$ (in.2)	<i>J<sub>c</sub></i> (in.⁴)	C <sub>AB</sub> = y <sub>t</sub> (in.)	$A_c = b_o d$ (in.2)	<i>J<sub>c</sub></i> (in.⁴)
22	6 7 8 9 10 11 12	6.03 6.16 6.28 6.41 6.53 6.66 6.78	205 259 314 372 431 493 556	12,600 16,600 21,200 26,200 31,900 38,100 45,100	7.81 7.93 8.04 8.16 8.27 8.39 8.51	317 402 491 584 681 782 887	20,800 27,600 35,400 44,100 53,900 64,900 77,100	13.13 13.63 14.13 14.63 15.13 15.63 16.13	446 572 706 848 998 1,156 1,322	51,600 71,500 95,100 122,800 155,100 192,300 235,000

Figure 37: Shear Constants for Distributed Moment Calculations

<sup>&</sup>lt;sup>22</sup> Appendix C.6 shows the calculation for the waffle slab and the Total Factored Moment (Mo)

**Table 55: End Span Moment Distribution** 

Variable	Formula	Values		
Total Static Moment (Mo)	$\frac{WuL^2}{8}$	1282.81 k*ft		
Exterior Column (Neg	gative Factored Moment) ACI	13.6.4.2		
Moment (Mu)	0.26Mo	333.53 k*ft		
Bottom (Positive	e Factored Moment) ACI 13.6.	4.4		
Moment (Mu)	0.52Mo	667.06 k*ft		
Column Strip (Mu)	0.60Mu	400.24 k*ft		
Middle Strip (Mu)	0.40Mu	266.82 k*ft		
Interior Column (Negative Factored Moment) ACI 13.6.4.1				
Moment (Mu)	0.70Mo	897.97 k*ft		
Column Strip (Mu)	0.75Mu	673.48 k*ft		
Middle Strip (Mu)	0.25Mu	224.49 k*ft		

**Table 56: End Span Shear Calculations** 

	Factored Shear (vu) Calculations	
Description/Variable	Formula	Values
Shear (Vu)	$\frac{wuL}{2} - \frac{Mu_{int} - Mu_{ext}}{L}$	239.35 kips
Factored Shear (vu)	$\frac{Vu}{Ac} + \frac{\gamma_v MuC_{AB}}{Jc}$	0.255 ksi
$\gamma_v$	$(1-\gamma_f)$	0.38
$\gamma_f$	$\frac{1}{(1+\left(\frac{2}{3}\right)\sqrt{b_1/b_2}}$	0.623
Mu	0.30Mo	384.84 k*ft
	Shear Check at Exterior Column	
Shear Capacity (vc)	$(\frac{\alpha_s d}{b_o} + 2)\sqrt{f'c}$	0.382 ksi
$\alpha_s$	For edge columns	30
	Design Moment Strength (ΦMn)	
Area of Steel (As)	# of bars in column strip*Area of bars	6.60 in^2
a	$\frac{A_s f_y}{0.85 f' cb}$	2.28 in
Effective width (b)	Half the width of the panel	51 in

ФМп	$\phi Asf_y(d-\frac{a}{2})$	344.82
N	Moment Check at Exterior Column	
0	207.79 k*ft	
ФМп	344.82 > 207.79	
	0.010	
	0.011	
ρ	$_{max} > \rho$	0.011 > 0.010

**Table 57: Interior Span Moment Distribution** 

Variable	Formula	Values
Total Static Moment (Mo)	$\frac{WuL^2}{8}$	1282.81 k*ft
Panel Moments		
Bottom (Positive Factored Moment) ACI 1	3.6.4.4	
Moment (Mu)	0.35Mo	448.98 k*ft
Column Strip (Mu)	0.60Mu	269.39 k*ft
Middle Strip (Mu)	0.40Mu	179.59 k*ft
Top (Negative Factored Moment) ACI 13	.6.4.1	•
Moment (Mu)	0.65Mo	833.83 k*ft
Column Strip (Mu)	0.75Mu	625.37 k*ft
Middle Strip (Mu)	0.25Mu	208.46 k*ft

**Table 58: Interior Span Shear Calculations** 

Factored Shear (vu) Calculations		
Description/Variable	Formula	Values
Shear (Vu)	$\frac{wuL}{2} - \frac{Mu_{int} - Mu_{ext}}{L}$	298.52 kips
Factored Shear (vu)	$\frac{Vu}{Ac} + \frac{\gamma_v MuC_{AB}}{Jc}$	0.164 ksi
Shear Check at Exterior Column		
Shear Capacity (vc)	$(\frac{\alpha_s d}{b_o} + 2)\sqrt{f'c}$	0.264 ksi
$\alpha_{\scriptscriptstyle S}$	For edge columns	40

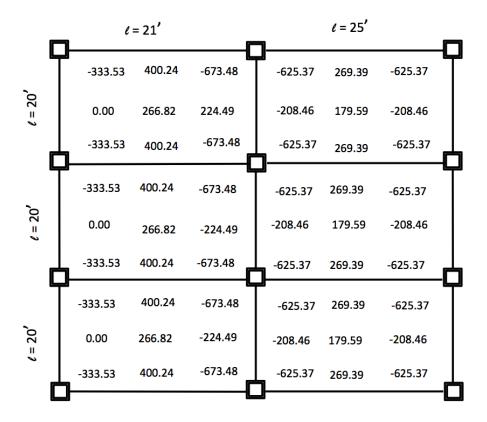


Figure 38: Moment Distribution Along Waffle Slab First Floor<sup>23</sup>

Figure 38 represents the moment distribution along the spans of the first floor waffle slab. These moments are distributed throughout the entire slab of the first floor of the building based on symmetry.

With the results of these calculations and with the appropriate checks for the slab and columns it was determined that both the waffle slabs and the concrete columns on the building would be able to support the additional load of the green roof. Appendix C.5 show the resulted moment calculations on the slab and the appropriate check based on its capacity.

It is important to notice that the seismic loads acting on the building do not affect the existing structure. As an additional load is imposed on the roof of the Gordon Library, the extra load is going to make the effective seismic weight to increase.

<sup>&</sup>lt;sup>23</sup> Moment values in Figure are in kips\*feet.

## CHAPTER 7: SOLAR COLLECTOR INSTALLATION ON STODDARD B

This chapter contains information on the specific type of solar collector technology chosen for Stoddard B. The technology was chosen based on ease of installation, energy production, and cost. Additionally, this chapter contains information about the rooftop layout and construction process for the installation of solar collectors. Such information includes the number of solar collectors, dimensions of the technology, as well as the specific location on the roof where the technology should be installed. Finally, this chapter contains associated structural analyses and minimum design specifications for the building's members. Since no blueprint with dimensions was obtained, a number of assumptions were made for the structural analyses as well as external research.

## 7.1 Selected Solar Collector Technology on Stoddard B

For the application of solar collectors on Stoddard B, evacuated tube solar collectors were chosen because of their efficiency, ease of installation, and insulation properties. Apricus is a leading designer and manufacturer of solar hot water and hydronic heating products. After researching their products, the ETC-30 model was chosen for the application of evacuated tube solar collectors. This model contains 30 double-glass solar tubes and is often used for commercial, rather than residential, projects (Apricus, 2016). For flat roofs, like Stoddard B, the solar collectors must be angled facing south in order to absorb the most amount of sunlight. The ETC solar collector converts sunlight into usable heat, heating the liquid in the header pipe. If the temperature in the header pipe is measured to be hotter than the water in the bottom of the solar tank, then the pump turns on. The liquid is slowly circulated through the header pipe in the collector, heating by approximately 13°F during each pass. Gradually throughout the day, the water in the solar tank is heated up, since hot water is less dense than cold water, the water at the top of the solar tank is distributed out to either a boost tank, or directly to the user (Apricus, 2016). Figure 39 displays the ETC solar system operation. Table 55 contains information on the type, size, weight, energy production, lifespan, and costs of the chosen Apricus evacuated tube solar collector.

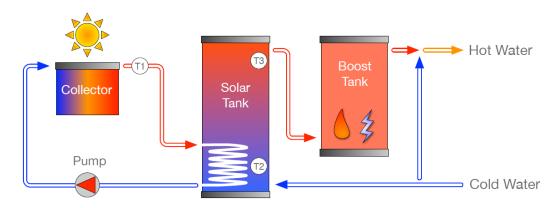


Figure 39: Evacuated Tube Solar Collector (ETC-30) Operation (Apricus, 2016)

**Table 59: Type of Solar Collector Technology Information (Apricus, 2016)** 

Building	Stoddard B
Sustainable Rooftop Technology	Evacuated Tube Solar Collectors
Manufacturer	Apricus Solar Hot Water
Model	ETC-30
Dimensions	78.9" x 86.4" x 5.3"
Gross Area	47.34 square feet
Weight	209 lbs
Energy Production	12 kW/day (1kW = 7.5 gallons)
Lifespan	25 years
Cost of Technology	\$3,080/collector (includes pump and solar tank)
Installation Cost	\$1,000 (plumbing/tank installation)
installation Cost	\$70/hour (collector installation)
Annual Operational/Maintenance Cost	\$50

## 7.2 Layouts and Construction Process for Solar Collectors on Stoddard B

This section contains information on the layout and construction process for the installation of solar collectors on Stoddard B. To determine the layout of the solar collectors, the number of solar collectors to produce the water consumption value of Stoddard B was calculated. According to the WPI Facilities Department, the annual water consumption of Stoddard B is

991,419 gallons. The chosen Apricus evacuated tube solar collector produces 32,850 gallons of water per year. By dividing the annual water consumption value of Stoddard B by the annual water production value of one solar collector, it was determined that Stoddard B would require at least 31 collectors to produce enough water for the entire building. All collectors will be angled at 40° above the horizontal and facing south. Table 56 contains information on energy, water, cost, number of collectors, and total area of collectors. Stoddard B contains two rectangular sections on its roof. The proposed design has 15 collectors on one section, and 16 collectors on the other section as seen in Figure 40.

Table 60: Installation of Solar Collectors on Stoddard B Information

STODDARD B	Current	Installation of Evacuated Tube Solar Collectors
Annual Energy Consumption/Production	232,800 kWh	4,380 kWh/panel
Annual Water Consumption/Production	991,419 gallons	32,850 gallons/panel
Annual Cost of Energy Paid/Saved	\$32,592	\$613.20/panel
Number of Collectors	31 collectors	
Total Area of Collectors	1,467.54 square feet	

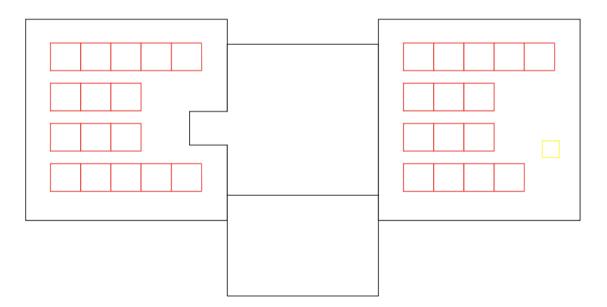


Figure 40: Solar Collectors Roof Layout

Table 57 contains information on the construction process for Apricus Evacuated Tube Solar Collectors. Figure 41 displays the mount's anchor that connects to the roof itself and some design requirements. Figure 42 shows the design of the mounting frame (as well as assembly instructions), maintenance and safety precautions.

**Table 61: Construction Process for Apricus Solar Collectors (Apricus, 2008)** 

System Design	Mounting Frame	Maintenance and Safety
		Precautions
1) Installed at an angle between	1) All Apricus solar collectors are supplied with	2) Under no conditions, the Apricus
20° and 80° above the horizontal	a standard frame	ETC-30 system is maintenance free
2) Installed facing south with a	2) Figure 41 below displays the roof attachment	2) Draining of the manifold is
deviation of up to 10°	that should be followed for a flat roof.	required for maintaining the system
3) Collector should be positioned as close to the storage cylinder as possible	3) Flat roofs require a high angle frame, which provides adjustments from 30° to 50° above the horizontal	3) Leaves should be removed regularly to ensure optimal performance and prevent life hazard
	4) Figure 41 displays the Apricus solar collector	
	high angle frame kit, including safety	
	considerations	

# Mount on Flat Roof using Round Feet

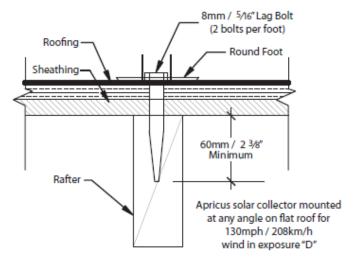


Figure 41: Attachment of Mounting Frame of Apricus ETC-30 (Apricus, 2008)

## Apricus Solar Collector High Angle Frame Kit

Part #: FR-XX-HIGH-RFOOT

The components contained in this package combine with the standard frame to form the complete frame assembly shown below.

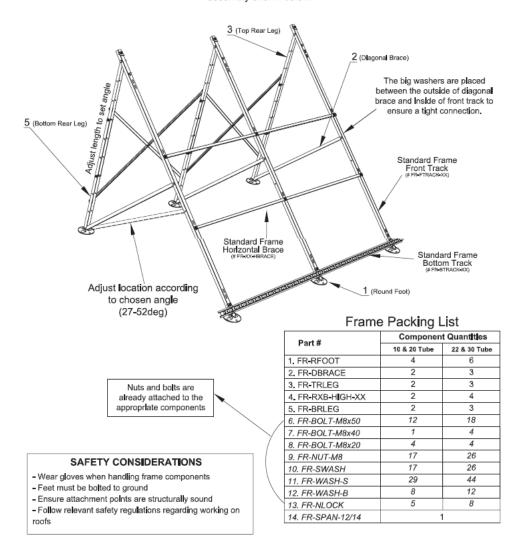


Figure 42: Round Foot High Angle Frame Kit Assembly Diagram (Apricus, 2008)

## 7.3 Research and Estimates

In order to complete a structural analysis, the proper information about the building is required. This information requires a set of structural drawings with proper dimensions; unfortunately, the acquired drawings were not complete nor did they contain sufficient dimensions. In order to fill in the gaps as much as possible, extra research was conducted. This research involved reading relevant documents in WPI archives named *Stoddard Residence Center: Specifications* <sup>24</sup> as well as conducting as much measurements as possible in the actual building. Table 58 contains all the information obtained from this research.

**Table 58: Information Obtained from Research** 

Stoddard Specifications		Measurements	
Concrete strength	3 Ksi	Columns Area	Base= 12inches
Steel yield strength	60 Ksi	(Measured)	Height = 12 inches
Concrete cover	<sup>3</sup> ⁄ <sub>4</sub> inch	External Building Area	Base= 48 feet
Slabs	Contain wire mesh	(Measured)	Height = 48 feet
		Beam Area	Base= 10 inches
		(Eye estimate)	Height= 8 inches

This collected information was not sufficient to completely fill in the gaps, and estimates and assumptions had to be done to fill in the gaps in order to do a structure analysis. These estimates were done as objectively and as accurately as possible and the assumptions are the limitation of this aspect of the project. The assumptions made are regarding the building's members as well as their layout. The slabs were assumed to be a continuous one-way slab and have a metal deck weighting 3.5 psf and a MEP of 5psf; the beams were estimated to be 10 inches by 12 inches; the ties used for concrete were #3's; the columns are governed by axial forces; all members are the same as the ground's floor, with the exception of the roof slab; finally, the layout of the column and beam drawn and estimated as best as possible. All of these assumptions are found in Annex D.2.

132

<sup>&</sup>lt;sup>24</sup> This book contains specifications for three dormitories for WPI to be known as the Stoddard Residence Center, Worcester, MA, O.E. Nault & Sons, Inc., Architects, May 1969 – includes Addendum Nos. 1, 2, and 3.

## 7.4 Structural Analysis and Member Designs for Solar Collectors on Stoddard B

After determining the layout and quantity of the Solar Collectors and compiling all the possible information on the building, the structure's analysis began. It started with determining the new loads acting on the flat roof. For the calculations, the side of the building with 16 collectors was chosen since it will introduce the largest load. After the new imposed load is a calculated, different member of the building are designed with all the loads acting on them, and these designs will establish the minimum requirement for each of the members. If any of the actual members are below these designs, the analysis is not adequate. The members designed consist of the first-floor slab, columns, beams, and the roof slab. The second and third floor members are assumed to have the same dimensions as the first floor for this analysis. The design of each member was done in the order that the weight is distributed along the building. To start, the new imposed load is directly above the roof slab, and then it is distributed into the beams. From the beams, the weight is distributed along the columns. The columns in turn rest on the first-floor slab.

#### 7.4.1 Solar Evacuated Tubes Load Calculations

The first step in our analysis involved considering all loads acting on the solar panels: dead load, live load, rain load, snow load, wind load, and seismic load. For this system, the rain loads were considered negligible. Due to the 40° angle of the panels, all rain would runoff onto the roof and simply be drained. Live load was neglected since the system was not designed for people to walk on. Dead load was calculated by using the wet weight, area, and number of panels. Finally, snow load, wind load, and seismics load were calculated in accordance with the ASCE 7-10. In addition to the ASCE 7-10, wind and seismic load were calculated in accordance with documents from the Structural Engineers Association of California, which provided information specifically to solar photovoltaic arrays (Structural Engineers Association of California, 2012). All calculated design loads are shown below in Table 59, and all calculations can be found in Appendix D.1. Provided in the ASCE 7-10, there are seven load combinations that were considered when determining the governing load acting on the panels. These combinations accounted for both gravity and lateral loads. All load combination calculations were made in accordance with the Load and Resistance Factor Design (LRFD) method. The

calculated load combinations are displayed in Table 60; the governing load for gravity effects is formula number three with a value of 81.55 psf.

**Table 59: Calculated Design Loads for Solar Collectors** 

Loads	Value (psf)
Dead (D)	5.47
Snow (S)	34.65
Wind (W)	39.09
Seismic Horizontal (E <sub>h</sub> )	0.9.92
Seismic Vertical (E <sub>v</sub> )	0.21
Roof Live (L <sub>r</sub> )	10
Live on technology (L)	0
Rain (R)	0

Table 60: Calculated LRFD Load Combinations per ASCE 7-10

	Load Combinations	
	1.4D	7.66
	1.2D + 1.6L + 0.5(L/S/R)	39.89
Gravity Loads	$1.2D + 1.6(L_r/S/R) + (L/0.5W)$	81.55
	$1.2D + 1.0W + L + 0.5(L_r/S/R)$	72.98
	$1.2D + E_v + L + 0.2S$	23.7
T . 1T 1	0.9D + 1.0W	44.01
Lateral Loads	$0.9D + 1.0E_{h}$	14.84

## 7.4.1 Slab Design & Calculations

To begin the slab design, a sum of all the loads on top of the member is done and plugged into the governing load combination to get the factored load. This sum of forces includes the self-weight of the member. The next step is calculating maximum moment acting on the slab. In this case, for a continuous one-way slab with inner supports, the maximum moment occurs at the interior support. This moment represents the actual moment acting on the slab. From here on, different aspects of the slab were designed. Given the actual moment, an estimate of the effective depth, the allowed area of steel, and Whitney's stress block were made. This step can be thought of as a trial design. With the allowed area of steel, a bar is chosen with its required spacing using a book table<sup>25</sup>. This bar and spacing represent the actual area of steel per unit width. Given the actual area of steel, the effective depth and Whitney's stress block are recalculated to be more

\_

<sup>&</sup>lt;sup>25</sup> Table A-9 found in the annex

accurate. The steel ratio is calculated and compared to the min and max to make sure that the reinforcement will yield before the concrete fails in compression. Finally, having a member design with every variable, the bending capacity  $\Phi M_n$  of such slab is calculated. The moment capacity is compared to the design moment Mu and if it is larger than Mu, then the design for the slab can withstand the imposed load. Very similar to the moment, the shear Capacity  $\Phi V_c$  and design shear Vu are calculated and compared. If all of these parameters are complied with, the proposed design is adequate to hold all of the loads acting on it.

This design was done twice, one for the roof slab as well as the first-floor slab. The slabs are very similar; the only difference is the reinforcement size and spacing. It is important to always have in consideration that this calculation is the minimum required design to withstand the load. Table 61 shows the design calculations for both slabs, and Figure 43 illustrates a cross section for the slab on the 1<sup>st</sup> floor. All calculations are found in Appendix D.2.

**Table 61: Slab Values & Minimum Design** 

Roof Slab		1 <sup>ST</sup> Floor Slab	
Design specification	Value	Design specification	Value
d-in	6.86	d-in	6.67
Thickness-in	8.0	Thickness-in	7.8
Area of steel- in <sup>2</sup>	0.2	Area of steel- in <sup>2</sup>	0.7
Bar number	3	Bar number	6
Spacing between bars-in	6.5	Spacing between bars-in	7.5
Min Steel Ratio (ρ <sub>min</sub> )	0.0018	Min Steel Ratio (ρ <sub>min</sub> )	0.0018
Design Steel Ratio (ρ)	0.0024	Design Steel Ratio (ρ)	0.009
Max Steel Ratio (ρ <sub>max</sub> )	0.016	Max Steel Ratio (ρ <sub>max</sub> )	0.016
Design Moment Mu- kips *ft	5.69	Design Moment Mu- kips *ft	18.33
Moment Capacity ØM <sub>n</sub> - kips *ft	6.0	Moment Capacity ØMn - kips *ft	18.9
Design Shear (Vu) -kips	1.76	Design Shear (Vu) -kips	5.67
Shear Capacity ΦV-kips	6.7	Shear Capacity ΦV-kips	6.7
Whitney's Stress Block (a) -in	0.39	Whitney's Stress Block (a) -in	1.37

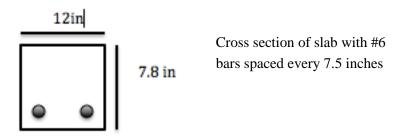


Figure 41: Slab Cross-Section for 1st Floor

## 7.4.2 Beam Design & Calculations

After completing the slabs designs, the next members to be looked were the beams. For this section, it is important to remember that the beam measurements were estimated by eye since there was no way of measuring it properly. The layout of the beams is shown in Figure 44, with the X being the columns and the beams being the light blue rectangles. Similar to the slab design process, the factored load was calculated by summing all of the dead loads and live loads acting on it, including self-weight, and plugging them into the governing factored load combination. For a simply supported beam, the maximum moment formula is known. The area of steel is assumed to be close to the slab's so a proper bar placement can be taken out from a book table<sup>26</sup>. For this procedure, the steel stress is assumed to equal the specified minimum yield stress, meaning that the steel ratio is within parameters. After choosing the bar number and actual area of steel, the effective depth and Whitney's stress block are calculated. With the entire dimensions at hand, the initial assumption is checked to make sure that the beam is tensioncontrolled to prevent brittle effects. After making sure the assumptions are correct, the final step is to calculate the moment capacity  $\Phi M_n$  and make sure it is larger than the design moment  $M_u$ . Having done this whole procedure, the design for a simply supported beam is adequate if the allowed moment and net tensile strain are larger than the actual moment and yield strain in tension, respectively.

This design was done once for the first-floor beams and assumed all other beams were the same. If the actual beams have other dimensions and bars, the design should be redone in

٦

<sup>&</sup>lt;sup>26</sup> Table A-8 of the annex.

order to get the allowed moment. Table 62 shows the design values and Figure 45 illustrates a cross section of the designed beam. All of the calculations are found in Appendix D.2.

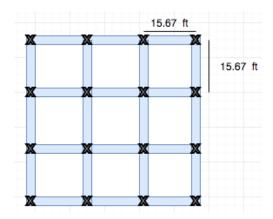


Figure 42: Beam Layout

Table 62: Beam Values and Minimum Design

First floor beams		
Design specification	Value	
Factored Load (W <sub>u</sub> ) -psf	13.6	
Area of steel (A <sub>s</sub> )- in <sup>2</sup>	0.79	
Bar number	8	
Thickness-in	10	
Width (b) -in	8	
Whitney's Stress Block (a) -in	2.3	
Net tensile strain $(\epsilon_t)$	0.0.0074	
Steel Yield strain in tension (ε <sub>y</sub> )	0.00207	
Moment Capacity (ΦM <sub>n</sub> ) –kips*ft	24.3	
Design Moment (M <sub>u</sub> )- kips *ft	9.78	
Safety Factor (Φ)	0.9	
Steel Ratio (ρ)	0.0123	

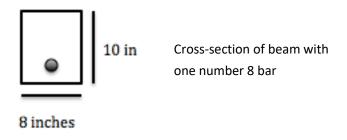


Figure 43: Beam Cross-Section for 1st Floor

## 7.4.3 Column Design & Calculations

The last members to be considered for design purposes were the columns. For this design, the layout of the columns is estimated to be 15.67 feet away from one another. Figure 46 shows the assumed layout with the tributary area. The columns were measured by hand to be 1foot by 1 foot. For the design of this member, the columns are considered to be governed by axial forces. Similar to the other members, the first step is calculating the factored load. Summing all the forces acting on the member, including self-weight, and plugging them in to the governing load combination gave the calculation. The design accounts for the column load effects from other floors. The layout of this column results with three different types of columns (Edge, Corner, and Middle), the difference being in the tributary area. The different columns are shown as E, C, and M in the layout. The column with the largest axial load Pu acting on it will be the governing one and the one that will be designed. The axial load is easily calculated by multiplying the factored load by the tributary area; the middle columns had the largest axial load acting on it. For the next step of the design, the axial load is considered to be equal to the axial load capacity  $\Phi P_n$ . This results in a formula that allows the calculation of the required area of steel. Next, the layout of the reinforcement is chosen from the table A-8 of the book found in the annex. The chosen area of steel has to be similar to the required one; this selection will also provide the number of bars and quantity of bars in the column. In this case, two reinforcement arrays were selected which are acceptable: four # 7 bars, and two # 9 bars. After selecting the reinforcement, the steel ratio has to be checked to be within parameters. This ratio has to have a minimum of one to two percent. If it is within this range, the proposed design is acceptable. To finish the design, the ties

and spacing were calculated. This step is fairly simple since the tie number is known and the spacing is the minimum of three straightforward equations.

This design was done once for the first floor columns and assumed all the others were the same. If the columns in any of the floors have other dimensions and reinforcement, the design should be redone in order to get the minimum size and reinforcement. Table 63 shows the design values and Figure 47 illustrates a cross section of the designed beam for the design with the # 7 bars. All of the calculations are found in Appendix D.2.

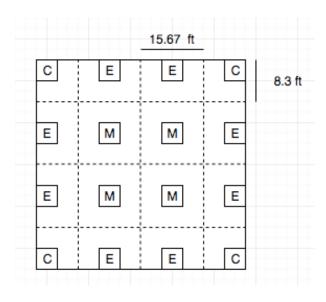


Figure 44: Assumed Column Layout

Table 63: Column Values & Minimum Design

First floor columns		
Design specification	Value	e
Area (b x h)- ft <sup>2</sup>	1	
Factored Load (W <sub>u</sub> ) -psf	544.6	2
Governing Axial Load -kips	133.7	7
Area of steel required (A <sub>s</sub> )- in <sup>2</sup>	1.92	
Bar number 7	Layout Area of Steel (A <sub>s</sub> )-in <sup>2</sup>	4 bars 2.40
Bar number 9	Layout Area of Steel (A <sub>s</sub> )-in <sup>2</sup>	2 bars 2.0
Steel Ratio (ρ) bar number 7	0.016	7
Steel Ratio (ρ) bar number 9	0.014	
Minimum steel ratio (ρ) -%	1-2	
Ties	#3	
Ties Spacing -in	12	
Safety Factor (Φ)	0.8	

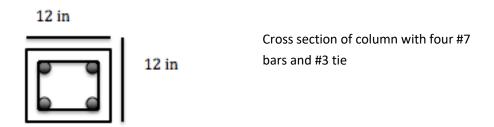


Figure 45: Column Cross-Section for 1st Floor

## **CHAPTER 8: ECONOMIC ANALYSIS**

This chapter contains information on the economic analysis to determine whether it is feasible to implement the chosen sustainable rooftop technologies. This chapter provides the values and results obtained from the calculation process outlined in section 3.5 of the Methodology chapter.

## 8.1 Economic Analysis of Solar Panels on the Gateway Parking Garage

The overall cost of the proposed solar panel design was calculated by adding the total cost of the following variables: steel framework, added 2 ft x 2 ft concrete columns, reinforcement within the concrete columns, and solar panels. The overall cost of the proposed solar panel design as well as the operational cost were compared to the net annual energy savings of the Gateway Parking Garage to determine how many years it will take to pay off the solar panel design and begin making a profit. These were compared since the chosen number of solar panels can produce the annual energy demand of the structure.

#### 8.1.1 Total Cost of Steel Framework

The total weight of the primary steel members was calculated, as well as the total weight of the miscellaneous items in the framework, which includes steel plates, studs, and connections. The total weight of the miscellaneous steel was equal to 10% of the total weight of the primary members. The total weight of the steel members and miscellaneous items are shown in Table 64 below. The total cost of the steel framework was calculated using the unit costs provided in Table 65 below. The costs include unit cost values for labor, materials, and equipment. Labor rate accounts for the workers constructing and installing the steel framework, material rate accounts for the steel members and miscellaneous items, and equipment rate accounts for the tools used to construct the steel framework.

Table 64: Total Weight of Steel Members and Miscellaneous Items

Member Size	Member Weight (lb./ft)	Member Length (ft)	Quantity	Total Weight (tons)
W24 55	55	45.69	4	5.03
W24 x 55	55	28.21	2	1.55
W24 60	<b>C</b> 0	45.69	10	15.53
W24 x 68	68	28.21	5	4.80
W30 x 90	90	T.C. 0.0	7	17.65
W30 x 108	108	56.02	1	3.03
		6.33	2	0.20
W/O 21	21	14.26	2	0.44
W8 x 31	31	22.2	2	0.69
		27.1	2	0.84
	TOTAL WEIGHT OF STEEL MEMBERS = 49.75 tons			

**Table 65: Total Steel Framework Cost** 

ESTIMATED TOTAL WEIGHT OF MISC. STEEL/PLATES/STUDS/CONNECTIONS = 4.97 tons

49.75	4.97
400	400
3,000	3,400
200	200
3,600	4,000
179,100	19,880
	3,000 200 3,600

## 8.1.2 Total Cost of Added 2 ft x 2 ft Concrete Columns

The total cost of the five added 2 ft x 2 ft concrete columns was calculated by multiplying the number of added concrete columns by the labor, material, and equipment unit costs for the installation of 24" x 24" concrete columns. Table 66 displays the cost data and total cost of the added concrete columns.

**Table 66: Total Concrete Column Cost** 

<b>Number of Added Concrete Columns</b>	5
Labor Unit Cost (\$)	400
Material Unit Cost (\$)	241
<b>Equipment Unit Cost (\$)</b>	32
Total Unit Cost (\$)	673
TOTAL CONCRETE COLUMN	N COST = \$3,365

### 8.1.3 Total Cost of Reinforcement Within Concrete Columns

In order to support the steel framework columns, 6 #9 steel rebar was recommended to be placed within all eight concrete columns, including the three existing concrete columns. The material cost, labor cost, and equipment cost were determined and added together to produce the total cost of reinforcement within the concrete columns. The results are shown in Table 67 below.

**Table 67: Total Cost of Reinforcement Within Concrete Columns** 

Number of Concrete Columns	8
Number of #9 Steel Rebar per Column	6
Material Cost (\$)	64.50
Labor Cost (\$)	60.50
<b>Equipment Cost (\$)</b>	15.35
TOTAL STEEL REBAR COST = \$6,736.80	

### 8.1.4 Total Cost of Solar Panels

The total cost of solar panels was based on the SPR-P17-350-COM model from the manufacturer SunPower. The total cost is displayed in Table 68 below, which is based on the unit cost of the technology and unit installation cost provided by SunPower. The unit cost of the technology and unit installation cost are values based on the Northeast region of the United States.

**Table 68: Total Cost of Solar Panels** 

Number of Solar Panels	272
Cost of Solar Panels (\$)	172,856
i. Unit Cost of Technology (\$/panel)	635.50
<b>Unit Installation Cost (\$)</b>	380,800
i. Panel Energy Production (watt/panel)	350
ii. Price per Watt (\$/watt)	4.00
TOTAL SOLAR PANEL COST = \$553,656	

### 8.1.5 Economic Analysis Results

The total cost of the steel framework, added concrete columns, steel rebar, and solar panels were added together to produce the overall construction cost of the proposed solar panel design. This is outlined in Table 69 below.

Table 69: Overall Cost of Proposed Solar Panel Design

Total Steel Framework Cost (\$)	198,980
Total Concrete Column Cost (\$)	3,365
Total Steel Reinforcing Rebar Cost (\$)	6,736.80
Total Solar Panel Cost (\$)	553,656
TOTAL COST = \$762,738	

The net annual energy savings of the Gateway Parking Garage was calculated using the total annual solar panel energy production value as well as the energy operational cost obtained from the WPI Facilities Department. The simple payback period of the proposed solar panel design was calculated to determine if it is economically feasible for WPI to invest in this sustainable rooftop technology. The simple payback period of the proposed solar panel design is shown in Table 70 below.

Table 70: Simple Payback Period of the Proposed Solar Panel Design

Net Annual Energy Savings (\$)	19,459	
i. Annual Energy Demand (kWh)	137,207	
ii. Annual Panel Energy Production (kWh)	138,992	
iii. Cost per kWh of Energy (\$/kWh)	0.14	
Annual Operational Cost of Solar Panels (\$)	2,593	
Lifespan of Solar Panels (years)	25	
Total Installation Cost of Design (\$)	762,738	
NUMBER OF YEARS TO PAY OFF DESIGN= 42 years and 7 months		

Based on this result, it is not economically feasible for WPI to invest in the proposed solar panel design. The number of years to pay off the design is much higher than originally expected. In addition, the lifespan of the solar panels is 25 years, which is over 15 years prior to when WPI would begin making a profit. This would require a new added solar panel cost, in addition to operational costs, taking it even longer for WPI to become profitable. The main contributing factor to the large cost of the design is the price of the solar panels. The cost for one solar panel is \$635.50, and our proposed design contains 272 panels to produce energy for the entire parking garage.

## 8.2 Economic Analysis of Green Roof Installation on Gordon Library

#### 8.2.1 Material and Labor

Implementing green roof systems can have many benefits on a building, including an overall energy reduction. However, the main concern comes when comparing the estimated costs of a normal flat roof and a green roof system on a structure. Even though green roofs have a vast quantity of benefits for the building and the environment, owners are not ready to assume such a high extra cost to build up this technology. A typical built-up flat roof can be extremely inexpensive versus a green roof. RS Means Software estimates the cost of a commercial roof without green technology to be around \$5- \$7 per square feet of construction. On the other hand, the estimate cost of a green roof ranges from \$14 -\$15 per square foot, in national averages. The additional \$10 per square foot that this system costs includes, materials, installation process and labor.

A green roof system for a building such as the Gordon Library would have the estimated costs of construction and maintenance as shown in Table 71. This table illustrates the cost for the installation of a green roof on Gordon Library, assuming an area of 10,733 square feet. For the first days of green roof installation, some additional costs may be incurred due to the extra labor

needed for an establishment period<sup>27</sup>. The annual maintenance of green roofs typically includes fertilization, weeding, drain inspection and removal of debris. <sup>28</sup>

Table 71: Costs of Installation and Maintenance for Green Roofs

Description	Unit Cost (per square foot)	Cost of System
Material & Installation	\$15	\$160,995.00
Maintenance/Annual	\$0.27	\$2,897.91
Total First Year	\$15.27	\$163,892.91

The typical costs for installation and maintenance of a conventional roof needed for the Gordon Library are shown in Table 72 below. This cost is given because at some point in time the building will need to have a full roof reconstruction, typically in 15-20 years (average service life of a roof). The area of the roof for the Gordon Library is 172'0"x 92'10", which is equal to 14,002.38 square feet<sup>29</sup>. This roof area is different than the area of the green roof because not all the roof will include the green roof technology.

Table 72: Costs of Installation and Maintenance Gordon Library Roof

Description	Unit Cost (per square foot)	Cost of System
Material & Installation	\$7	\$98,016.66
Maintenance/Annual	\$0.13	\$1,820.31
Total First Year	\$7.13	\$99,836.97

This cost is assuming that there is a good and constant maintenance of the roof. If maintenance of the roof is not constant the price in the table can decrease but also the overall service life of the roof would decrease. The following conditions can be applied:

1. If the roof has no maintenance, the service life that is typically around 20 years can be reduced in half. This at the end will require an additional cost of the roof

<sup>&</sup>lt;sup>27</sup> When vegetation of the green roof is in place and roots of plant start growing and adapting

<sup>&</sup>lt;sup>28</sup> https://facilityexecutive.com/2017/10/greening-the-roof/

<sup>&</sup>lt;sup>29</sup> The area of the roof does not include the penthouse system located on top of the roof.

- 2. If some maintenance is done, the roof will last a little less than 20 years, however the cost for maintenance is going to decrease as well.
- 3. If full maintenance is done, the average service life of the roof will be around 20 years, and its maintenance cost will be as shown in Table 72. At year 20 or less, there needs to be a full corrective and maintenance of the entire roof, which due to inflation and change in prices, it will typically cost more than the original cost of the roof shown in Table 72.

In addition, the cost of a commercial roof can change based on local contractor prices, type of labor used and other conditions. There is not an actual price for the reconstruction of a roof, but an average can be obtained from these values.

The main benefit of a green roof technology is the ability to increase twice the service life of a conventional roof. This would allow WPI to save some costs on full corrective and maintenance of the roof at year (20), which at the end is the biggest saving.

#### 8.2.2 Stormwater Benefits

Some other savings and benefits occur as part of installing a roof garden on the Gordon Library, including stormwater benefits. Based on the building type (commercial) for Gordon Library, an estimate of \$0.004 per square foot per year can be used for utility benefits for stormwater retention systems. This would be the best case-scenario for this particular saving due to stormwater retention. This value is not much and is not going to be used in cost reduction of the system. However, if this value can increase due to future technology, savings might be considerable high.

## 8.2.3 Energy and Insulation

The most significant cost benefit of a roof garden is the ability to reduce the overall energy consumption of a building by temperature control. For the Gordon Library, the green roof technology is going to act as an additional insulator of the roof and not as a replacement for insulation, creating energy savings for the building. As the information regarding annual energy consumption of the Gordon Library was not provided, an exact analysis of the savings was not done.

Implementing a green roof technology on the Gordon Library will reduce annual energy consumption by 12% for all types of structures (Andresen, et. al., 2004). The average cost of

energy in Massachusetts is approximately 13.84 cents per kWh. With a 12% reduction of this the cost of energy would be around 12.18 cents per kWh.

On average, college and universities in the United States consume 18.9 kWh of electricity per square foot annually ("Managing Energy Costs in College and Universities"). This means than on average Gordon Library is consuming over 1,200,000 kWh annually, with an approximate cost of \$156,921. Assuming an energy reduction of 12%, the annual savings for the building will be around \$15,000 to \$20,000. This is assuming that a constant energy reduction of 12% is applied for every month of the year. However, as this may not be true for certain months, a conservative value for annual savings would be around \$10,000 to \$12,000 a year. Based on these numbers it will take around 12 to 15 years to payback the actual cost of the green roof. However, this is only assuming the energy reduction savings by installing a green roof technology. If all the factors are considered, the payback period can be between 5 to 7 years. This is assuming that the reconstruction of the current roof of the Gordon Library includes the green roof technology. This value was obtained by concluding that at some point a full reconstruction of the roof is needed, and implementing a roof garden will be more expensive but it will increase the service life of the roof.

## 8.3 Economic Analysis of Solar Collectors on Stoddard B

This economic analysis results in the number of years required for the technology to pay itself off. The steps for this calculation is simply dividing the initial cost that WPI will have to spend by the annual savings that the technology will provide.

#### 8.3.1 Fixed Cost

The first step in this analysis is determining the fixed cost of the system, which is the installation cost plus the price of each solar collector. The installation cost for the tank is known and the installation cost for the panels is \$70 an hour. A period of two weeks is assumed for installation purposes and an estimate was calculated. The price of technology was fairly simple: multiplying price of panels times number of panels needed. These two values were added to get the fixed cost. The formulas and process for this process is listed in Table 73.

**Table 73: Initial Cost of Solar Collectors** 

Step 1: Fixed Cost	
Variable:	Reference/Equation:
Number of Solar Panels	31
Cost of Solar Panels - \$	Unit Technology Cost*Number of Solar Panels
i. Unit Cost of Technology (\$/panel)	SunPower Corporation
	3,080
Installation Cost (\$)	Panel Energy Production*Unit Installation Cost*Number of Solar Panels
i. Tank installation	Apricus Corporation
	1,000
ii. Collector installation (per hour)	Apricus Corporation
	70
	80 hours assumed
Cost of Solar Panels + Installation cost -\$	

## 8.3.2 Savings Per Year

After having the fixed cost, the next step is calculating the total savings per year of WPI. The first step involved calculating the annual savings by subtracting the amount saved per year from energy by the maintenance cost per year. Finally, the payback period was calculated by adding the overall cost and the installation cost and dividing it by the annual savings amount. The formulas and process for this process is listed in Table 74.

**Table 74: Annual Savings of WPI with Solar Collectors** 

Step 2: Annual Savings		
Variable:	Reference/Equation:	
Annual Energy Demand – kWh	WPI Facilities Department	
	232,800	
Energy Operational Cost - \$/kWh	WPI Facilities Department	
	0.14	
Annual cost of energy	Annual Energy Demand* Energy Operational Cost	
Annual Savings of system - \$/ panel	613.20	
Annual Total Savings of collectors	Number of Collectors*Savings per panel	
Annual Maintenance Cost-\$	50	
Annual Total Savings of System – Annual Maintenance Cost		

## 8.4 Payback Period

To get the simple payback period, the annual savings of WPI is divided from the fixed cost. This value represents the number of years that the technology will take to pay itself off in savings. This number is compared with the remaining lifespan of the technology to finalize economic feasibility. The formulas and process for this process is listed in Table 75.

**Table 75: Payback Period of Solar Collectors** 

Step 3: Simple Payback Period of the Proposed Solar Collector		
Variable:	Reference/Equation:	
Fixed Cost -\$	Following step 1	
	102,080	
Savings per year -\$	Following step 2	
	18,959.3	
Fixed Cost/Annual Savings - years		

The proposed technology will take 5.3 years to pay itself off and has a lifespan of 25 years. Meaning that the technology has a little less than 20 years to continue helping WPI saving a lot of money that is currently spending annually. This proposed system is very feasible and could aid WPI with its feasibility plan. All calculations are found in Appendix D.3.

## **CHAPTER 9: CONCLUSIONS**

Our recommendation would be to redesign the solar panel system with less solar panels to reduce the overall cost. However, by doing this would not produce energy for the entire structure and a portion of the annual \$19,209 of energy demand would have to be paid in addition to the cost of the solar panel design. A cost analysis would have to be done to determine how to gain a profit in the shortest time period. This would require analyzing how many solar panels would be needed to produce a certain percentage of energy demand required by the Gateway Parking Garage. Our second recommendation would be to choose a different model and manufacturer of solar panels, which are sold at a lower cost. However, the quality and energy production of these panels might not compare to the chosen SunPower model. For large-scale applications, such as the Gateway Parking Garage, it might not be economically feasible to install solar panels to produce energy to the entire structure.

As shown in this analysis, it would be economically feasible to implement a green roof on the Gordon Library, although many factors need to be considered. It is expected that the price of construction for green roofs is going to decrease throughout the years. As this technology becomes more popular in the country, material and labor costs will decrease. This will make the cost per square foot of the system more affordable and possibly get around the cost of a conventional roof. In addition, it will be more appropriate to implement the green roof technology when full corrective roof maintenance is needed in the building. This will reduce the additional cost of installing a green roof over a roof that is still working and in good shape and will increase the service life of the entire roof.

Like the green roof technology, it is economically feasible to invest in solar collectors for Stoddard B. According to calculations, the payback period of this technology is roughly 5.4 years, meaning that after that period the technology will start saving money for WPI until it reaches the lifespan. Annually, this system could save WPI nearly \$19,000 after the payback period.

It is important to note that all these sustainable technologies are not extremely common in the United States. Even though their installation has increased dramatically in the last couple of years, the price for each technology is expected to decrease in the near future. This would reduce the overall cost for each sustainable rooftop technology: solar panels, solar collectors, and green roofs. In addition, tax incentives for implementing sustainable technologies should be determined to get the most approximate cost of installation. Each State will have a different tax credit for the installation of sustainable technologies, as well as a federal tax credit which can be applied. For example, for Massachusetts, the tax credit for implementing green roofs is 9.5%. However, WPI is tax exempt so tax incentives would not apply for sustainable rooftop technologies at WPI. All of these factors contribute to the overall price of the technology and whether or not it is feasible for implementation. Future work for this MQP would involve redesigning the solar panels on Gateway Parking Garage to make the installation economically feasible. This would require reducing the number of solar panels, or choosing a different solar panel manufacturer. Since the roof of the Gordon Library was recently reconstructed, it would be recommended to wait a couple of years until the roof begins to deteriorate to install a green roof, since a green roof will protect and increase the service life of the roof. Finally, in order to properly install the solar collector system, an analysis by a licensed professional structural engineer has to be done with adequate structural drawings.

## REFERENCES

- Alkhrdaji, T., & Thomas, J. (2017). Structural Strengthening Using External Post-Tensioning Systems. *Structure Magazine*. Retrieved from https://www.structural.net/article/structural-strengthening-using-external-post-tensioning-systems. Accessed 29 Oct. 2017.
- Andresen, Fernandez, Rowe, Rugh, VanWoert & Xiao. (2004). Effects of Roof Surface, Slope, and Media Depth. *Green Roof Stormwater Retention*, *34*(3), 1036-1044. Retrieved from https://dl.sciencesocieties.org/publications/jeq/articles/34/3/1036?highlight=&searchresult=1. Accessed 20 Sept. 2017.
- Apricus (2008). *Apricus Solar Collector Installation and Operational Manual*. Retrieved from http://www.buildsite.com/pdf/mainegreen/Apricus-AP-30-Solar-Collector-Installation-Instructions-380583.pdf. Accessed 30 Nov. 2017.
- Apricus. (2016). ETC Solar Collector Product Overview. Retrieved from http://www.apricus.com/upload/userfiles/downloads/ETC\_Collector\_Overview\_USA.pdf Accessed 4 Dec. 2017.
- Apricus Solar Water Company. (2017). *Evacuated Tube Solar Collectors*. Retrieved from http://www.apricus.com/html/solar collector.htm. Accessed 1 Nov. 2017.
- Battaglia, C., Cuevas, A., & De Wolf, S. (2016). High-efficiency crystalline silicon solar cells: status and perspectives. *Energy & Environmental Science*, 9th ser., 1552-1576. doi:10.1039/c5ee03380b
- Carter, Timothy, and Andrew Keeler. *Journal of Environmental Management*. vol. 87, www.sciencedirect.com/science/article/pii/S0301479707000436
- Energy Matters. (2016). Solar Power Educational Information: Renewable Energy. Retrieved from http://www.energymatters.com.au/education/. Accessed 20 Sept. 2017.

- Gartner. (2008). Structural Implications of Green Roofs, Terraces, and Walls. Retrieved from http://mgase.weebly.com/uploads/6/1/1/3/6113816/paper\_5\_-\_2008\_seaoc\_convention\_\_structural\_implications\_of\_green\_roofs\_terraces\_and\_walls\_by\_seaosc\_sdc\_7-7-08.pdf. Accessed 25 Oct. 2017.
- Green Roof Guide. n.d. *Maintenance*. Retrieved from www.greenroofguide.co.uk/maintenance. Accessed 15 Dec. 2017.
- HTP. (2017). Evacuated Tubes Solar Collectors. Retrieved from http://www.htproducts.com/literature/lp-220.pdf. Accessed 10 Oct. 2017.
- Imboden, P. B. (2009). Solar Power Has Benefits as a Source of Alternative Energy. Retrieved from http://www.nationalgeographic.com/environment/global-warming/solar-power/.

  Accessed 15 Sept. 2017.
- International Code Council (2014). 2015 International Building Code. Retrieved from https://codes.iccsafe.org/public/document/IBC2015/copyright. Accessed 29 Mar. 2018.
- Jörg Breuning & Green Roof Service LLC. (2017). Consultancy, Design, Engineering, Project Management and Expert Witness of Green Roofs and Green Walls since 1980. Retrieved from http://www.greenrooftechnology.com/. Accessed 20 Sept. 2017.
- "Managing Energy Costs in College and Universities." *Managing Energy Costs in Colleges and Universities Business Energy Advisor*, OUC, 2 Mar. 2015, https://ouc.bizenergyadvisor.com/colleges-and-universities
- MacGregor, James, and James Wight (2005.). *Reinforced Concrete: Mechanics and Design*. Fourth ed., Accessed 20 Mar. 2018
- My Rooff. (2017). *Green Roof Construction*. Retrieved from https://myrooff.com/green-roofing construction. Accessed 5 Dec. 2017.
- Nault & Sons, Inc., Architects (May 1969) *Stoddard Residence Center: Specifications*. Retrieved from WPI's Archives. Accessed 15 Mar. 2018
- R.S. Means Company. (2017). *Building Construction Costs*. Norwell, MA: Construction Publishers & Consultants.

- Shaw, M. (n.d.). Structural Strengthening With External Plate Bonding. Retrieved from http://www.bath.ac.uk/cwct/cladding\_org/icbest97/paper24.pdf. Accessed 23 Sept. 2017.
- Shoultes, S. (2017). Post-Tensioning. Retrieved from http://kcwardco.com/concrete-repair services/structural-strengthening/post-tensioning. Accessed 22 Oct. 2017.
- Solar Power Authority. (2017). 25 Interesting Facts About Solar Power. Retrieved from https://www.solarpowerauthority.com/25-facts-about-solar-power/. Accessed 19 Sept. 2017.
- Structural Engineers Association of California. (2012). Structural Seismic Requirements and Commentary for Rooftop Solar Photovoltaic Arrays. Retrieved from SEAOC\_Solar\_PV\_Seismic\_document\_2012\_08\_Final.pdf. Accessed 21 Oct. 2017.
- Structural Engineers Association of California. (2012). Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs. Retrieved from SEAOC\_Solar\_PV\_wind\_document\_2012\_08\_Final.pdf. Accessed 21 Oct. 2017.
- SunPower Corporation. (2016). *Safety and Installation Instructions*. Retrieved from https://us.sunpower.com/sites/sunpower/files/media-library/manuals/mn-sunpower-solar-panels-safety-installation-guide-na.pdf. Accessed 4 Dec. 2017.
- SunPower Corporation. (2017). SunPower Performance Series, P17. Retrieved from https://us.sunpower.com/sites/sunpower/files/media-library/data-sheets/ds-sunpower-p17-355-commercial-solar-panels.pdf. Accessed 7 Dec. 2017.
- United States Environmental Protection Agency. (2017). Learn About Heat Islands. Retrieved from https://www.epa.gov/heat-islands/learn-about-heat-islands. Accessed 10 Sept. 2017.
- Urban Design Tools. (2017). *Green Roofs*. Retrieved from http://www.lidstormwater.net/greenroofs.htm. Accessed 28 Nov. 2017.
- WPI Sustainability Plan. (2017). Retrieved from https://web.wpi.edu/Images/CMS/Facilities/WPI\_Sustainability\_Plan.pdf. Accessed 22 Oct. 2017.

Wrobel, C. A. (2017). Structural Effect of Solar Arrays on an Existing Structure. Retrieved from http://spi17.mapyourshow.com/7\_0/collateral\_redirect.cfm?CollateralID=8. Accessed 8 Oct. 2017.

## APPENDIX A: PROJECT PROPOSAL

## WORCESTER POLYTECHNIC INSTITUTE

## **Sustainable Roofing Practices**

A Major Qualifying Project submitted to the Faculty of Worcester Polytechnic Institute in partial fulfillment of the requirements for the Bachelor of Science degree

by

Sebastian Miranda Ryan Stokes Ian Taylor

**Date** 

10/12/17

**Proposal Submitted to** 

Leonard Albano

Worcester Polytechnic Institute

## **Abstract**

This project will evaluate the feasibility of the installation of sustainable roofing practices on selected buildings at Worcester Polytechnic Institute (WPI). This report includes the structural analysis and design of three sustainable rooftop technologies: solar panels, green roofs, and solar collectors. These methods have the ability to alleviate the urban heat island effect, while contributing to WPI's sustainability plan. Additionally, an economic evaluation using a life-cycle cost analysis will be prepared to show the incentives for installing these sustainable rooftop technologies.

### 1 The Problem

This section contains an introduction to sustainable rooftop technologies, and their ability to mitigate global environmental problems. Additionally, this section lays out the goals and objectives for this project.

#### 1.1 Problem Statement

Climate change, air pollution, and water pollution are a few of many environmental problems that the world is dealing with today. Specifically in urban areas, the heat island effect is another problem which is increasing temperatures. The negative impacts from the heat island effect in urban cities include an increase in energy usage, increase in gas emissions, impaired water quality, and health risks. It is the responsibility of our generation to explore ways to preserve the environment for future generations. Implementing sustainable rooftop technologies is one practice which can help reduce some of the environmental problems the world is dealing with today. Sustainable rooftop technologies include solar panels, solar collectors, green roofs, stormwater retention systems, and daylighting systems. All of these systems use the source of the problem, the sun, as a way to reduce environmental problems. Our objective is to explore three rooftop technologies, and investigate the structural impact these systems can have on buildings at Worcester Polytechnic Institute (WPI). The three technologies we have chosen are solar panels, green roofs, and solar collectors.

### 1.2 Goals and Objectives

The goal of this project is to provide recommendations and improvements for the installation of sustainable rooftop technologies on existing buildings at WPI. Additionally, we will investigate the impact of these technologies on the net energy demands. The objectives for this project include:

- 7. Determine the approach WPI has towards sustainable practices, as well as its current sustainable building practices.
- 8. Identify candidate buildings at WPI for the installation of certain sustainable rooftop technologies.
- 9. Perform an engineering analysis of the selected buildings.
- 10. Perform an energy analysis to determine the sustainable rooftop system which will result in the greatest reduction of energy usage.

- 11. Outline structural design activities for the selected buildings, which includes identifying structural reinforcements needed to withstand sustainable rooftop technologies.
- 12. Conduct a life-cycle cost analysis to determine whether it is economically feasible to implement sustainable rooftop technologies at WPI.

## 2 Background

This section provides information on the heat island effect, which is an environmental problem. The heat island effect can be reduced in urban areas through sustainable roofing practices. Additionally, this section contains background information on various sustainable rooftop technologies: solar panels, solar collectors, green roofs, stormwater retention systems, and day lighting systems.

#### 2.1 The Heat Island Effect

The heat island effect describes urban regions which become hotter than its rural surroundings due to urban area development of buildings, roads, and other infrastructure which replaces open land and vegetation. The annual mean temperature of a city with one million people or more can be 1.8°F warmer than its surroundings. However, the temperature difference can be as much as 22°F during the nighttime due to the buildup of heat on infrastructure from the sun during the day, which is slowly released throughout the night. Shaded or moist surfaces in rural areas remain close to air temperatures. Elevated temperatures in urban areas can negatively impact a community's environment and quality of life (United States Environmental Protection Agency, 2017).

### 2.1.1 Negative Impacts

Some of the negative impacts of the heat island effect include increased energy consumption, elevated emissions of air pollutants and greenhouse gases, compromised human health and comfort, and impaired water quality (United States Environmental Protection Agency, 2017):

- 5. *Increased Energy Consumption:* When the temperature rises in urban areas during the summertime, there is an increase of energy demand for cooling. Starting from 68-77°F, the electricity demand for cooling increases 1.5-2.0% for every 1°F increase in air temperatures (United States Environmental Protection Agency, 2017).
- 6. *Elevated Emissions of Air Pollutants and Greenhouse Gases:* The burning of fossil fuel increases air pollutants and greenhouse gas emissions. Fossil fuel power plants are used to supply electricity, which in turn emit sulfur dioxide, nitrogen oxides, particulate matter, carbon monoxide, mercury, and carbon dioxide. All of these pollutants are

- harmful to human health and contribute to air quality problems including smog, fine particulate matter, acid rain, and global climate change.
- 7. Compromised Human Health and Comfort: High temperatures affect human health and contribute to discomfort, respiratory difficulties, heat cramps and exhaustion, non-fatal heat strokes, and heat-related mortality. The Centers for Disease Control and Prevention estimated from 1979-2003 that excessive heat exposure contributed to more than 8,000 premature deaths in the United States (United States Environmental Protection Agency, 2017).
- 8. *Impaired Water Quality:* High pavement and rooftop surface temperatures can heat stormwater runoff. Tests have shown that 100°F pavement can elevate initial rainwater temperature from 70°F to over 95°F (United States Environmental Protection Agency, 2017). This heated stormwater will eventually runoff into storm sewers and raise the water temperature of streams, rivers, ponds, and lakes. Rapid temperature changes in aquatic ecosystems can be fatal to aquatic life.

#### 2.1.2 Strategies to Reduce Urban Heat Islands

There are various strategies which help to reduce urban heat islands. One strategy is to increase tree and vegetation cover. This can provide shade and cooling to urban areas, as well as reduce stormwater runoff and protect against erosion. Another strategy is to implement more green roofs in urban areas. By growing a vegetative layer on a rooftop, the roof surface temperature will decrease and stormwater management will improve. Additionally, cool roofs are made of materials or coatings that reflect sunlight and heat away from a building. Cool roofs have the ability to reduce roof temperatures, increase the comfort of building occupants, and reduce energy demand. Vegetation cover, green roofs, and cool roofs are a few of many strategies that have the ability to reduce urban heat islands (United States Environmental Protection Agency, 2017).

#### 2.2 Solar Panels

Solar energy is a renewable source of energy created from the sun. Solar energy produces energy through a process which is sustainable, inexhaustible, non-polluting, noise-free, and does not emit greenhouse gases (Energy Matters, 2016). Solar panels in the United States should face south to absorb the most sunlight; however, solar panels do not need direct sunlight to produce

electricity. Solar power has the capacity to provide energy for air conditioners, hot water heaters, cooking and electrical appliances, natural gas, electricity, or oil fuels (Solar Power Authority, 2017). Solar technologies can be expensive and require a lot of land area to collect the sun's energy at useful rates; however, solar electricity can pay for itself in the long term, usually five to ten years with tax incentives (Imboden, 2009). When solar panels are purchased, the federal solar tax credit allows the owner to deduct 30% of the cost of installing a solar energy system from the owner's federal taxes. Not only has the cost of solar panels dropped by 80% since 2008 due to its high demand, but maintenance is minimal and returns are high once solar panels have been installed (Solar Power Authority, 2017).

#### 2.2.1 How Solar Panels are Made

Solar panel systems (photovoltaic or PV system) are made up of semiconductor materials that convert sunlight into an electric current (Energy Matters, 2016). When sunlight hits the cells of the solar panels, electrons become loose from their atoms and flow through the cell generating electricity (Imboden, 2009). The semiconductor material is covered with an anti-reflective coating and made up of silicon wafers impregnated with impurities; impurities have the ability to improve electrical properties. The solar cells are joined together by electrical contacts, and located between a superstrate layer on top and a backsheet layer below (Energy Matters, 2016).

### 2.2.2 How Solar Panels Work

The photovoltaic effect is the process by which light is converted to energy at the atomic level. The majority of energy the solar cells produce goes into a grid connect inverter which converts the electric charge from a direct current (DC) into an alternating current (AC). This allows the solar electricity current to flow to and from the grid connect inverter. The solar electricity can power the appliances in a building when needed, and the leftover solar electricity will flow to the grid connect inverter where it is stored. If more energy is produced than used, then the owner is credited on their electricity bill, making this an incentive for building owners to implement renewable systems (Energy Matters, 2016).

## 2.2.3 Types of Solar Panel Systems

As the use of technology has increased over the years, different types of solar panels have been created. Of all these, approximately 90% of solar panels are made of silicon photovoltaic

material (Battaglia, Cuevas & De Wolf, 2016). This section describes two different types of solar panel systems: crystalline silicon panels and thin-filmed panels.

Crystalline Silicon (Monocrystalline Silicon & Polycrystalline Silicon)

Crystalline silicon cells are the most common solar cells used in commercially available solar panels, consisting of more than 85% of world photovoltaic cell market sells. Crystalline silicon panels have two subtypes: Monocrystalline Silicon & Polycrystalline Silicon. The main difference between these types is the production technique. Each technique has its advantages and disadvantages. The cells have laboratory energy efficiencies of 25% for monocrystalline cells and over 20% for polycrystalline cells. However, industrially produced solar modules currently achieve efficiencies ranging from 18%–22% (Battaglia, et. al., 2016).

Monocrystalline solar panels have the highest efficiency rates since they are made out of the highest-grade silicon. Monocrystalline cells are produced from pseudo-square silicon wafers (substrates cut from boules grown by the Czochralski process), the float-zone technique, ribbon growth, or other emerging techniques. These other emerging techniques can have a specific reason for utilizing. For example, if produced using the ribbon growth technique, the production costs as well as the carbon footprint both decrease efficiency. These panels are also space-efficient. Since they yield the highest power outputs, they require less space compared to the other types. They also have a long life expectancy (25+ years) and tend to work better in low-light conditions. This type of panel is the most efficient and has a longer lifespan than other types of panels; however, it is the most expensive type of panel (Battaglia, et. al., 2016).

Polycrystalline silicon solar cells are a newer technology and vary in the manufacturing process. They are traditionally made from square silicon substrates cut from ingots cast in quartz crucibles. Polycrystalline cells are more cost effective to produce due to the fact that many cells can be created from a single block. However, every time silicon is cut, the edges become deformed, which results in a lower operating efficiency. Polycrystalline cells have become the dominant technology in the residential solar panels market because of their low operating efficiencies, and the cheap method by which they can be produced. In terms of efficiency, polycrystalline solar cells are now very close to monocrystalline cells (Battaglia, et. al., 2016).

Since crystalline cells were one of the first technologies, much of the production and manufacturing techniques have been refined to reach their maximum potential. Advantages of crystalline silicone cells include a high efficiency rate of about 12% to 24.2%, high stability, ease

of fabrication, high reliability, and long lifespan. Other benefits include high resistance to heat and lower installation costs. Negatively, these panels are the most expensive, in terms of initial cost, and have a low absorption coefficient (Battaglia, et. al., 2016).

### Thin-Film Panels

The differences between thin-film and crystalline silicon solar cells are the thin and flexible pairing of layers, and the photovoltaic material: either cadmium telluride or copper indium gallium dieseline instead of silicon. Thin-film solar panels are the least efficient type of solar panel. Depending on the technology, thin-film module prototypes have reached efficiencies between 7–13%, and production modules operate at about 9% (Battaglia, et. al., 2016).

Thin film panels are made by depositing a photovoltaic substance onto a solid surface, such as glass. Multiple combinations of substances have successfully and commercially been used for the photovoltaic substance. Typical thin-film solar cells are one of four types, depending on the material used: amorphous silicon (a-Si) and thin-film silicon (TF-Si); cadmium telluride (CdTe); copper indium gallium dieseline (CIS or CIGS); and dye-sensitized solar cell (DSC) plus other organic materials (Battaglia, et. al., 2016).

Despite being the least efficient, thin-film panels have advantages that should be considered when planning for solar roofing. Thin-film material is 100 times thinner than traditional solar panels, provides flexibility, and is lightweight. Thin-film panels are created by combining consecutive thin layers of material together. The result is a single film that is capable of being distributed in rolls or sheets making it easier to handle. Since they are becoming the lowest cost panels to produce because of their low material costs for thin film, they are quickly becoming the most economically efficient panel types. Some of thin-film panels' disadvantages include low efficiency, and they require the most space for producing the same amount of power as other solar panels. Additionally, the thin material's durability begins to suffer over time, requiring frequent replacement (Battaglia, et. al., 2016).

Table 1: Energy Output and Cost of Different Types of Solar Panel Systems

Type of Panel	Output (w)	Singular Panel Cost (\$)
Monocrystalline	150	165
Polycrystalline	165	165
Thin-Film	100	135

#### 2.2.4 Structural Considerations

Placing solar panels on the roof of a building adds various loads to the structure. To perform a structural analysis on the building involves to first define the loads, and then to determine how the loads affect the structure (Wrobel, 2017).

Solar panels add a dead load to the roof of a building. The dead load includes the self-weight of all the physical components of the solar panels. The dead load applied to the roof is a concentrated load located where the panels are supported by the roof, which is usually located at each corner of the panel (Wrobel, 2017).

In geographic regions where snow loads are present on roofs, warm roofs are constructed which can help decrease the snow load. If solar panels are raised above the roof, then they do not receive the benefit of the warm roof to decrease the snow load, which results in an increase of the snow load as well (Wrobel, 2017). The design of snow loads for roofs that include solar panels shall be determined in accordance with ASCE 7-10.

Wind loads are also considered as they have the ability to act in various directions, both upward and downward on solar panels. Wind loads also act on different locations of the solar panels depending on which direction the wind is blowing from (Wrobel, 2017). Some of the elements for which wind loads should be considered are: the ultimate design wind speed, risk category, wind exposure, internal pressure coefficient, and component and cladding.

Not only must we consider the various loads acting on the structure of a building, but we must also take into consideration the size, quantity, and location of solar panels on the roof of a building. All of these factors will determine the effect of the loads, and the existing structures' capacity for the addition of solar panels.

### 2.2.5 Wind Design for Solar Panels

A document by the Structural Engineers Association of California titled, *Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs*, provides information on the step-by-step process for calculating wind loads on solar panels. There are many factors to consider when analyzing the effect of wind loads on solar panels. This document provides information on the determination of wind loads for solar photovoltaic arrays, which is not explicitly covered by the methods contained in the ASCE 7-10 (Structural Engineers Association of California, 2012). Steps to determine wind loads on rooftop equipment and other structures is located in Table 29.1-1 in ASCE 7-10. However, in Step 7 of this table, the equation provided needs to be

changed for the consideration of solar panels. The design wind pressure for rooftop solar arrays can be determined by the formula below (Structural Engineers Association of California, 2012).

$$p = q_h*(GC_m)$$

$$\label{eq:posterior} \begin{split} \boldsymbol{p} &= \text{wind pressure for rooftop solar arrays} \\ \boldsymbol{q_h} &= \text{velocity pressure evaluated at mean roof height of the building (lb/ft^2)} \\ \boldsymbol{GC_m} &= \text{combined net pressure coefficient for solar panels (lb/ft^2)} \end{split}$$

Solar panels mounted on a roof are highly vulnerable to the speed and direction of the wind approaching the panel. There are three distinct regions or zones on a roof where the wind flow characteristics and resulting wind loading on solar panels are different: interior, edge, and corner zones. Wind loads on solar panels located in the corner zones of roofs are much greater than those in the middle of the roof. Higher tilt panels are particularly vulnerable to the vertical component of swirling winds in the corner vortices of the panels. Since solar panels in the northern hemisphere face south, the northeast and northwest corners of the panel create severe loading. The southeast and southwest corners of the panel still create loading, just not as strong as the other two corners (Structural Engineers Association of California, 2012).

Different restricting values for the size, height, spacing, and positioning of solar panels are located in Table 2. These values will help when designing the roof layout and calculating wind load values. Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs provides more detailed information and application for these values.

**Table 2: Solar Panel Design Restrictions** (based on Structural Engineers Association of California, 2012)

Characteristic	Quantity
Height of gap between panels and roof surface (h <sub>1</sub> )	≤ 2 feet
Maximum height above the roof surface (h <sub>2</sub> ) for panels	4 feet
Panel chord length (l <sub>p</sub> )	≤ 6 feet 8 inches
Distance between solar panels and roof edge	$\leq 2*h_2$
Space between rows of solar panels	≤2*panel characteristic height (h <sub>c</sub> )
Panel tilt angle for typical installations	0-35 degrees

## 2.2.6 Seismic Requirements for Solar Panels

Similar to the previous section, a document by the Structural Engineers Association of California titled, *Structural Seismic Requirements and Commentary for Rooftop Solar Photovoltaic Array*, provides information on how to calculate and deal with seismic forces when designing solar panels. It is important to understand the effect of seismic forces on solar panels, and prepare for any type of loading. As described in the document, solar arrays can either be attached or unattached to the roof structure of a building (Structural Engineers Association of California, 2012). For our project, we plan on using attached solar arrays, therefore the information obtained has different values and procedures than that of unattached solar arrays.

Solar panels and their structural support systems shall be designed to provide life-safety performance in the design basis earthquake ground motion. Life-safety performance means that solar panels are expected not to create a hazard to life. For example, as a result of breaking free from the roof, sliding off the roof's edge, exceeding the downward load-carrying capacity of the roof, or damaging skylights, electrical systems, or other rooftop features or equipment in a way that threatens life-safety. Solar array support systems that are attached to a roof structure shall be designed to resist the lateral seismic force  $(F_p)$  specified in Chapter 13 of ASCE 7-10. In the computation of  $F_p$ , an evaluation of flexibility and ductility capacity of the support structure is permitted to be used to establish seismic coefficients of component amplification factor  $(a_p)$  and component response factor  $(R_p)$ . These values can be found in Table 13.5-1 of ASCE 7-10. Additionally, friction is permitted to contribute in combination with the design lateral strength of attachments to resist the lateral force  $F_p$  (Structural Engineers Association of California, 2012).

## 2.3 Solar Collectors

Solar collectors convert energy from the sun into usable heat in a solar water heating system. This energy can be used for hot water heating, pool heating, space heating, or even air conditioning (Apricus Solar Water Company, 2017).

#### 2.3.1 How Solar Collectors Work

Solar collectors can be mounted on a roof, wall, or the ground. A circulation pump moves liquid through the collector, which then carries heat back to the solar storage tank. Throughout the day, water in the solar storage tank is heated up. When hot water is used, the solar preheated

water is fed into the traditional water heater and supplied for its desired usage (Apricus Solar Water Company, 2017).

#### 2.3.2 Structural Considerations

Solar collectors impose similar loads to the roof structure as solar panels: dead loads, snow loads, wind loads, and seismic loads. Solar collectors add dead loads as a result from the weight of the collector, the mounting hardware, and the collector fluid. Typically, the collector has a dead load of approximately three to five pounds per square foot, but the exact weight considerations can be obtained from the manufacturer of the solar collectors (HTP, 2017).

In areas prone to heavy snowfall, such as Massachusetts, snow loads need to be considered in the design of the solar tubes. Ideally, solar collectors should be installed at an angle of 50° or greater to promote snow sliding off the tubes (HTP, 2017). Similarly, when installing solar tube collectors, wind and seismic resistance needs to be considered as well as the resultant stress on each of the attachment points. It is important to review the roof structure to ensure strength attachments of the solar collectors (HTP, 2017).

## 2.4 Green Roofs and Stormwater Retention Systems

A green roof is a roof of a building that is covered with vegetation. There are two characterizations of green roofs: extensive green roofs and intensive green roofs. Intensive green roofs use planting mediums that have a greater depth than extensive green roofs; this requires more maintenance because of the larger plant varieties intensive planting mediums can support. An extensive green roof has vegetation ranging from sedums to small grasses, herbs, and flowering herbaceous plants. Extensive green roofs are ideal for efficient stormwater management and low maintenance needs. An intensive green roof has vegetation ranging from herbaceous plants to small trees. Intensive green roofs require professional maintenance and advanced green roof irrigation systems. Rooftop farms fall under the intensive green roof category. The growing medium for an extensive green roof is 6" or less, while the growing medium for an intensive green roof is greater than 6" (Jörg Breuning & Green Roof Service LLC, 2017). Green roofs have the ability to reduce urban heat islands and can also serve as a stormwater retention system.

#### 2.4.1 The Urban Problem

Urban areas generate more stormwater runoff than natural areas due to a greater percentage of impervious roof surfaces and paved surfaces that prevent water infiltration. The United States Environmental Protection Agency (USEPA) concluded that a typical city block generates more than five times as much runoff than a woodlot of the same area. Additionally, urban stormwater runoff carries pesticides, heavy metals, and contaminated nutrients which have the ability to flow into various bodies of water. According to USEPA, "The most recent National Water Quality Inventory reports that runoff from urbanized areas is the leading source of water quality impairments to surveyed estuaries and the third-largest source of impairments to surveyed lakes (Andresen, Fernandez, Rowe, Rugh, VanWoert & Xiao, 2004)."

#### 2.4.2 Green Roof Stormwater Retention Success

Implementing green roofs in urban areas is a solution to reduce stormwater runoff. The Michigan State University Horticulture Teaching and Research Center conducted a 14-month study in which three simulated roof platforms were constructed. One of the roof platforms contained gravel, the other was vegetated, and the third was non-vegetated. Over a 14-month period, the vegetated roof had the greatest overall rainfall retention at 60.6%, while the non-vegetated roof had a rainfall retention of 50.4%, and the gravel roof had a rainfall retention of 27.2%. These percentages refer to the amount of rainfall which did not runoff the roof out of total amount of rainfall in the 14-month period. To conclude, vegetated roof platforms retain greater quantities of stormwater than conventional roofs. However, the study stated, "if the objective of a green roof is to maximize rainfall retention, then factors such as slope and media depth must be addressed (Andresen, et. al., 2004)."

### 2.4.3 Benefits of Green Roofs

Not only do green roofs control stormwater runoff, but their designs also have many other benefits (Andresen et. al., 2004):

- Insulate buildings, which saves on energy consumption.
- Increase the lifespan of a typical roof by protecting the roof membrane from damaging ultraviolet rays, extreme temperatures, and rapid temperature fluctuations.
- Filter harmful air pollutants.

- Contribute to aesthetically pleasing environment to live and work by controlling the temperature of a building.
- Provide habitat for a variety of living organisms.
- Contribute to reducing the Urban Heat Island Effect

### **2.4.4 Structural Considerations**

Similar to solar panels, green roofs contribute dead loads, live loads, snow loads, rain loads, wind loads, and seismic loads to the roof of a structure. The most contributing factor to the loads on a green roof depend on the size and type of vegetation which is used. An intensive green roof contributes more load than an extensive green roof due to the larger trees, plants, and sometimes water features that are being used. Additionally, the location of the stormwater storage has an impact on the structure of a building. Depending on the green roof, stormwater can be stored within the green roof itself, in a tank below the building, or drained towards the local watershed.

The structural considerations for green roof design are typically attributed to the different components (layers) of green roofs. A typical modern vegetated roof requires a minimum of eight layers: plant level (vegetation), substrate layer, insulation layer, filter fabric, drainage layer, protection fabric, roof barrier, and waterproof layer as shown in Figure 1 (Gartner, 2008). To conclude, the overall design and layers of a green roof determine the effect of the various loads on the structure of a building.

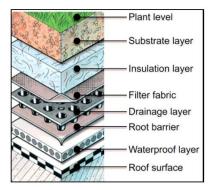


Figure 1: Layers of a Typical Modern Vegetated Roof (Gartner, 2008)

## 2.6 Types of Structural Reinforcements

Structural strengthening is used to reinforce structures due to deficiency, and to increase an existing element's capacity to carry new loads; new loads such as sustainable rooftop

technologies. As with any structure or method of reinforcement, it is necessary to first identify and establish a good understanding of the structure through a structural condition assessment. The most common existing techniques to reinforce structural elements are mentioned below and classified into two different categories: passive systems and active systems. When selecting the appropriate strengthening method, it is important to consider the following factors: magnitude of strength increase, size of building and structures, environmental conditions, accessibility, concrete strength, construction, and maintenance and life cycle costs (Shaw, n.d.).

## 2.6.1 Passive Systems

Passive systems do not introduce any forces to the structure; they contribute to the overall resistance of an element when it deforms. Section enlargement strategies are mostly used to improve strength, stiffness, and to reduce cracks. Some types of section enlargement strategies are: span shortening, externally bonded steel shapes, and epoxy injection (Shaw, n.d.).

Externally bonded fiber reinforced polymer (FRP) reinforcement is a method of reinforcement which includes adhering additional reinforcement to the exterior faces of an element. The success of this strengthening method depends on both the durability and lifespan of the reinforcement material, and the properties of the material used to attach the new reinforcement (usually epoxy material). This method, if adopted correctly and with the appropriate materials, is able to: reduce deflection, increase carrying capacity, increase flexural strength, and increase resistance to shear (Shaw, n.d.).

## 2.6.2 Active Systems

Active strengthening systems are identified by adding external forces to structural elements, which can increase strength and improve the service performance. Service performance reduces tensile stress and cracking (Alkhrdaji & Thomas, 2017).

A post-tensioning system is an external force method which implements a structural member using high strength cables, bars, and strands. This system usually connects the reinforcement to the existing member at anchor points (typically at the end of the member). The reinforcement is profiled along the span at different locations (Shoultes, 2017).

# 3 Scope of Problem

After background research, the sustainable rooftop technologies we will further analyze are solar panels, green roofs, and solar collectors. We plan on analyzing one or more buildings at WPI for the application of each of these practices. This section includes the project activities as well as the range of topics and parameters that will be investigated for the chosen sustainable roofing practices.

### 3.1 Solar Panels

This section includes the range of topics and parameters that will be investigated for using solar panels as the sustainable rooftop technology on buildings at WPI. Information is defined for the following considerations: ease of construction, loads, structural analysis, energy output, and economic costs.

#### 3.1.1 Ease of Construction

When investigating the structural impact solar panels have on buildings at WPI, we must first determine how solar panels are constructed and installed on roofs. We will be investigating multiple types of panel systems and assess their ease of installation. Many variables must be considered during the construction and installation process of solar panels. One variable is determining the type, size, and weight of the solar collectors. Additionally, the number of solar panels needs to be evaluated, which may vary per building based on the available space and the required energy output.

A second variable which needs to be considered is the safety of construction. We must determine the safety measures which must be taken when installing solar panels. Furthermore, we must figure out the time period for constructing and installing solar panels, which will vary depending on the quantity.

A third variable is the location on the roof where the solar panels need to be installed. This depends on the slope and shape of the roof, as well as the side of the roof which has the best exposure to the sun's rays. Another variable is how the panels will be installed at their desired location. Installation includes the blocking behind the roof, which supports the panels, and the process of mounting the panels. The position of the panels offset from the roof, the angle of the panels, and how the panels will be secured must also be considered (Radiantec Company, n.d.).

Finally, the last variable is figuring out where the energy will be supplied throughout the building. We must determine how the energy produced from the solar panels will be stored and distributed throughout the building. Depending on the functionality of the building, distributed amounts of energy will be required for various purposes.

### **3.1.2 Loads**

There are many loads associated with installing solar panels on the roof of a building. These loads include dead loads, wind loads, snow loads, and seismic loads.

Dead load includes the self-weight of all the physical components of the solar panels. The dead load applied to the roof is a concentrated load located where the panels are supported by the roof; which is usually located at each corner of the panel (Wrobel, 2017). The dead load also depends on the size, type, and number of solar collectors placed on the roof.

Wind loads, snow loads, and seismic loads should be calculated in accordance with the guidelines provided in the ASCE 7-10. The reference chapters for these loads are displayed in Table 3. The following information related to wind load should be considered when performing an analysis: ultimate design wind speed, risk category, wind exposure, internal pressure coefficient, and component and cladding. For each selected wind direction at which the wind loads are to be evaluated, the exposure of the building should be determined for the two upwind sectors extending 45 degrees either side of the selected wind direction.

**Table 3: Reference Chapters for Wind, Snow, and Seismic Load Information** (Solar World, 2014, & Structural Engineers Association of California, 2012)

Chapter in ASCE 7-10:	Information Provided:
Chapter 7	Snow load calculations
Chapter 13	Seismic load calculations
Chapter 16	Determination of wind resistance using an effective wind area, based on dimensions of a single unit frame
Chapter 26-36	Determination and calculations of wind loads

## 3.1.3 Structural Analysis

An assessment of the buildings at WPI needs to be performed in order to determine whether the existing building can support the loads from solar panels, or if structural reinforcements need to be added to the building. To begin the structural analysis, the type, dimensions, gross area, and mass of the solar panels needs to be determined. Next, we must identify if the building has a flat or pitched roof, and the angle of the pitched roof. We will then need to analyze the material and dimensions of the roof structure and building frame. Once these variables have been identified, load combinations can be calculated using dead, wind, snow, and seismic loads with the guidelines outlined in ASCE 7-10 (Ridal, Garvin, Chambers, & Travers, 2010).

Based on a risk assessment of structural impacts on buildings of solar panels: "In order to establish a straightforward method of assessing, critical or affected members should not be loaded to more than 100% of their design capacity as a consequence of increased loading from solar collector products (Ridal, et. al., 2010)." To conclude, a structural analysis of the buildings can be performed by first determining the solar panel requirements, then using the resources and plans of the building to assess the adequacy of the structural load path, and finally decide whether the building can withstand the loads from the solar panels.

## 3.1.4 Energy Output

The number of solar panels to provide a desired amount of energy needs to be calculated. The number of solar panels correlates with total solar panel area. The global formula to estimate the energy generated in output of a photovoltaic system is (Photovoltaic Software, 2017):

$$E = A * r * H * PR$$

 $\mathbf{E} = \text{Energy (kWh)}$ 

 $\mathbf{A} = \text{Total solar panel area } (\text{m}^2)$ 

r =Solar panel yield or efficiency (%)

 $\mathbf{H} = \text{Annual average solar radiation on tilted panels (kWh/m}^2)$ 

**PR** = Performance ratio (range of values: 0.5 - 0.9; default value: 0.75)

The value '**r**' is equal to the electrical power (kWp) of one solar panel divided by the area of one panel. The value '**H**' is a global radiation value, found online, which reflects seasonal effects and varies per geographic location. The value '**PR**' is an important value to evaluate the quality of a photovoltaic installation because it gives the performance of the installation independent of the orientation and inclination of the panel. The '**PR**' value is essentially a coefficient for losses (Photovoltaic Software, 2017).

We must determine the energy requirement of the building in order to calculate the total solar panel area. The energy value will vary depending on the purpose of the building. For example, recreational and residential buildings at WPI will most likely require more energy than an academic building. This information can be found from the WPI Facilities Department, but might not be given for each building. The energy requirements are most likely tracked for newer buildings, rather than the older ones. If this information is not available, we will research standard energy requirement values for recreational, residential, or academic buildings.

When the energy requirement for the building is obtained, we can use the global energy formula to calculate the required solar panel area. By calculating the required solar panel area, the number of solar panels for the building can be determined.

### 3.1.5 Economic Costs

Based on the energy output analysis described above, we will determine whether it is economically feasible to install and use solar panels on the chosen building. Using the required energy value of the building, we can either calculate or use available resources (WPI Facilities Department) to figure out the energy cost for the building. Then, from the design, the cost for installation of the solar panels can be calculated. The economic evaluation will not only include the initial product and construction costs, but will also include any costs that are incurred over time, such as maintenance costs. Additionally, we will need to figure out the lifetime of solar panels to see how long they will be able to effectively produce energy. Finally, a short-term and long-term financial analysis can be made to show the return of this investment over time.

For the life cycle cost analysis, we will also need to evaluate the time value of money. For example, something worth \$200 in 40 years could be equivalent to \$100 today. With that in mind, the energy cost of buildings will most likely increase in the future. The initial cost for the installation of solar panels will not be affected by the time value of money. However, the time

value of money could have an effect on the maintenance costs of solar panels years after installation.

# 3.2 Green Roofs

This section includes the range of topics and parameters that will be investigated for using green roofs as the sustainable roofing practice on buildings at WPI. Information is defined for the following considerations: ease of construction, loads, structural analysis, energy output, and economic costs.

#### **3.2.1** Ease of Construction

When investigating the structural impact green roofs have on buildings at WPI, we must first determine how they are constructed. Many variables come into hand for the installation of green roofs. One variable is determining the type of green roof that will be constructed. There are two main types of green roofs: intensive roofs and extensive roofs. Intensive roofs have a thick base and can support a wide variety of plants; however they are heavy and require maintenance. Extensive roofs have a shallow base, are light, and require minimal maintenance. Extensive roofs can support 10-25 pounds of vegetation per square foot and intensive roofs can support 80-150 pounds of vegetation per square foot. Some green roof designs incorporate both intensive and extensive elements. Comprehensive green roofs support plant varieties typically seen in intensive green roofs, but have the depth and weight of an extensive green roof system. A comparison of extensive and intensive green roofs is shown in Figure 2.

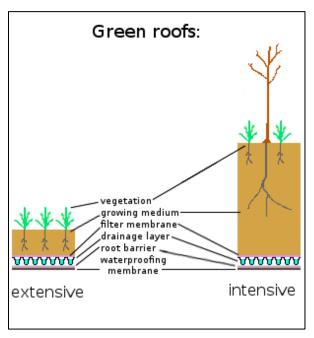


Figure 2: Extensive vs. Intensive Green Roofs (MGASE, 2008)

A second variable to consider when installing green roofs is location. Location of the green roof plays an important role in the design process. The height of the roof above grade, its exposure to wind, the roofs' orientation to the sun, and shading by surrounding buildings during parts of the day will all have an impact when deciding the location of the green roof. The general climate of the area and the specific microclimate on the roof must also be considered.

Another variable to consider is the type of plants that will be used. While most plants do well during the summer, they will likely die during the winter. Therefore, plants that thrive in winter should be highly considered. The last variable that should be considered is figuring out the amount of heating and cooling cost that will be saved. After the implementation of green roofs, the soil mixture and vegetation act as insulation, which reduces these costs by approximately 20%. This percentage varies depending on the type of green roof and amount of vegetation used.

#### **3.2.2 Loads**

There are many loads associated with green roofs. These loads include dead loads, live loads, transient live loads, snow loads, wind loads and seismic loads. A thorough analysis on how to determine these loads can be found in: ASTM E2397-05 Standard Practice for Determination of Dead Loads and Live Loads Associated with Green Roof Systems.

The dead loads associated with a green roof have the greatest contribution to the structure of the building. Dead loads include the weight of the roof system, all layers between the vegetation and roof, the capture water, and the vegetation itself. A 15% increase in the specified depth is recommended to account for future additions of growth media.

The live loads should be determined based on the type of occupancy and local building code requirements. It is recommended by FM Global that extensive green roofs be designed for no less than 12 psf when considering live load reduction, and a minimum of 20 psf for intensive green roofs. We will need to assess the adequacy of these values based on the range of parameters considered in our design. The live loads of green roofs include the weight of transient water contained in the drainage materials. This is the quantity of water that is required to completely fill the drainage layer of a green roof system.

The snow loads are based on the local jurisdictions building code requirements. In Worcester, buildings should be designed to withstand a snow load of 55 psf. For wind loads, the local building code requirements has to be followed, and roofs should be designed for the envelope of wind uplift on a bare roof and a saturated green roof. Seismic loads need to be calculated, in accordance with Chapter 13 of ASCE 7-10, since retained stormwater in the green roof produces a weight that is an inertia force.

## 3.2.3 Structural Analysis

The structural analysis of green roofs is similar to the structural analysis of solar panels. The structural implications of augmented loads on WPI buildings need to be analyzed to see whether additional reinforcements are needed to support the loads of green roofs.

The first step for this analysis is to determine the type of green roof that is going to be implemented. This is of extreme importance as different green roofs will generate different loads on a building. For example, extensive roofs usually require only minimal changes to the structural system of a building, while semi-intensive and intensive green roofs require a more detailed analysis and a need for a stronger building structure. Similarly, the layer design of a green roof will determine the exact load that the system will have on the structure. The layers of a green roof include, but are not limited to: roof barrier, protection fabric, drainage layer, filter fabric layer, insulation layer, substrate layer, and plant level (MGASE, 2008). Documents such as the 2002 Guideline for the Planning, Executing and Upkeep of Green-Roofs Sites, and Property Loss Prevention Data Sheet 1-35, provide a comprehensive way on how to design

green roof structures. These documents also indicate: "If a green roof assembly is not tested per ASTM standards, then the design load should be based on a saturated density of no less than 100 pcf (MGASE, 2008)." It is also important to consider several structural notes for green roof design:

- 1. Maintenance of the green roof and plant growth control to prevent structural overload.
- 2. Loading maps regarding different locations where a green roof is implemented.
- 3. Weights and thickness of all components.
- 4. Drainage plan and storage tank.
- 5. Specific tree data with weights and sizes.
- 6. Fabricate and test a mockup of the final green roof design (tested with ASTM E2397 and ASTM E2399).

When the design of the green roof is completed and all the necessary layers are determined, an analysis of the loads can be done to the selected buildings. The selected buildings will require to hold the different loads mentioned above in addition to the design dead load of the green roof.

### 3.2.4 Energy Saved

Green Roofs do not generate energy like solar panels, but its energy output is measured by the amount of energy saved after its implementation. Green roofs work as a form of insulation, thus improving the thermal performance of a roof. This allows buildings to better retain their heat during the cooler winter months while reflecting and absorbing solar radiation during the hotter summer months, allowing buildings to remain cooler. The insulated properties reduce energy demand for both heating and cooling; this reduced energy demand also reduces building energy costs. This means that energy requirements of the building are reduced year-round which allows the building temperature to be controlled at a lower cost.

There are only a small number of studies focused on quantifying the saved energy from green roofs. There is a study developed by Quantec that modeled the heating and cooling benefits of a green roof used in Portland, Oregon. The study found that a green roof reduced energy demand by 12%, with an annual cooling savings of 0.17 kWh/SF for electricity, and a heating savings of 0.02 therms/SF for natural gas. Roughly, the building saved around \$1,500 a

year. Other studies show similar results to this one; the reduction in the total energy demand for buildings ranges from 5-15%. If a green roof were to be implemented at WPI, then the energy requirements of that building should be expected to reduce around the same percentage as the studies. After choosing an appropriate location for the green roof at WPI, we will be able to determine an estimate of how much energy and money will be saved.

#### 3.2.5 Economic Costs

While the average cost of installing a green roof can run two or three times more than a conventional roof, it's likely to be a lower cost approach in the long run, due to energy savings. The growth medium and plantings of a green roof help protect the roof's waterproof membrane from ultraviolet radiation, extreme temperature fluctuations, and damage from use or maintenance. This protection may extend the life of the roof by two to three times that of a conventional roof. Conventional roofs have a life expectancy of around 20 years, while studies have found that the life expectancy of a green roof is close to 40 years. These studies were made in the United States, where green roofs are a fairly new practice. In Europe, where the development of green roofs has gone on for decades, some research shows that green roofs can protect the roof membrane upward of 50 years. For example, there are green roofs in Berlin that show a lifespan of more than 90 years before important repairs or replacement may be required (MGASE, 2008).

The study developed by Quantec, described in the previous Energy Saved section, also performed a cost and benefit report. In it, the cost and benefit analysis for a green roof is developed at different years after implementations (5 years, 20 years, and 40 years). The key findings from the analysis are: at five years, benefits accrued by a developer for green roof construction would only account for approximately half the cost of the green roof. Benefits do not appear to exceed costs until year 20 when an avoided cost of conventional roof replacement would be accrued. By forty years after development, the calculated economic benefits exceed costs by approximately \$700,000. In both the five-year and forty-year time period, the public benefit of the green roof is positive.

### 3.3 Solar Collectors

Solar collectors convert energy from the sun to heat water. The construction process for installing solar collectors is similar to that for solar panels; however, the loads on the roof

structure are different since solar collectors store water in their system. This affects the weight of the overall solar system, which contributes to the dead and seismic loads on the roof structure. Loads include dead, wind, snow, and seismic. Based on the calculated loads, proper structural reinforcements can be analyzed for the building. Additionally, it must be considered where to put the storage tank for the heated water. In order to install solar collectors, the hot water consumption value of the building and the amount of hot water the solar collectors can supply needs to be determined. Once the hot water consumption value of the building is collected, then the number of solar collectors can be calculated based on how much hot water each solar collector can produce. The cost to install solar collectors can be researched, followed by a life cycle cost analysis to determine whether it is worthwhile to install solar collectors on the roofs of specific buildings. For our project, we will look to install solar collectors on residential buildings, rather than academic buildings, since residential buildings consume more hot water than academic buildings. The athletic building at WPI has solar collectors on the roof, which heat the pool water. This saves more than \$50,000 in operating costs and reduces carbon dioxide emissions by 4,400 pounds per year, as compared with conventional pool heating (WPI Sustainability Plan, 2017). Solar collectors will be an important technology for the application of our project.

# 4 Capstone Design

To fulfill the requirements of the Capstone Design, the team will complete a Major Qualifying Project focused on the plan and design of sustainable roofing practices on existing buildings at Worcester Polytechnic Institute (WPI). Structural analysis of different buildings, as well as feasibility of construction and costs will be addressed in this project. The Capstone Design constraints expected in this project include: economic, environmental, constructability, sustainability, ethical, and health and safety.

## 4.1 Design Problem

As Worcester Polytechnic Institute is committed to a sustainability plan of ecological stewardship, social justice, and economic security, every member of the WPI community should be engaged in this process. Our plan for sustainable rooftop technologies follows the same path of the already existing sustainability plan; it is our job to embrace this mission in the local community.

To approach the problem and support the WPI sustainability plan, our group will design sustainable rooftop technologies, solar panels, green roofs, and solar collectors, for a number of existing buildings on campus. Each proposed system has the ability to generate energy efficiency, water storage, and building cool-off.

## 4.2 Economic

The plan of implementing sustainable rooftop technologies comes at a cost. For each alternative that is considered, there is going to be a different design and therefore a different cost. Our group is going to provide costs for implementing each of these systems, which will include the actual cost of the system, maintenance costs, lifetime, and long-term net savings. Similarly, we are going to determine the return on investment of the desired project, and we will provide recommendations based on budget and costs.

# 4.3 Constructability

Constructability is one of the most important factors to consider for implementing these sustainable systems. Considerations regarding the type of building (academic/residential/recreational), type of roof (slope/flat), year built, and size of the building are all addressed under this criterion. Similarly, the following factors need to be analyzed and considered:

Structural layout of the selected buildings.

- Zoning, permitting, and regulations.
- Construction schedule/time frame for each system.

# 4.4 Sustainability

Sustainability in this project consists of economic, environmental and social aspects. The design and construction of sustainable rooftop technologies includes all of these aspects and brings them together. Solar panels, green roofs, and solar collectors alleviate environmental concerns by implementing new technology in existing buildings at WPI. Sustainable practices reduce the consumption of energy, and they create more efficient buildings on campus.

#### 4.5 Environmental

Through the development of this project, another constraint similar to sustainability is environmental. Implementing sustainable rooftop technologies on buildings at WPI can alleviate the urban heat island effect. This is accomplished by reducing energy usage and decreasing gas emissions with the use of natural sources of energy, such as the sun. However, installing each sustainable technology requires construction on the WPI campus, which can negatively impact the environment. Noise and dust can emit into the air during the construction processes for these systems. Our group will propose installation processes which will limit the impact on noise and air pollution.

### 4.6 Health and Safety

It is of extreme importance to protect the public and the community of WPI of any possible risks. Health and safety of all the people involved in this project is going to be considered, especially for potential users of the selected buildings. The design and construction of these systems will be in accordance with the *International Building Code* and all safety factors.

### 4.7 Ethical

Ethical practices play an important role in this project. It is crucial to consider ethical codes for the design and construction of sustainable rooftop technologies. All the appropriate codes and regulations are to be considered in the implementation of these systems. Furthermore, the team will complete confidentiality agreements for the information that it is going to be provided by WPI Facilities Department.

# **5 Professional Licensure**

Civil engineering has been prevalent in human history since the beginnings of mankind. In addition to gathering food, society's main concern includes building a settlement, which requires civil engineering. Only a professional licensed civil engineer may prepare, sign, seal and submit engineering plans and drawings to a public authority for approval, or seal engineering work for public and private clients. The purpose of licensure is to protect the health and welfare of the public by regulating requirements to restrict engineering practice to qualified individuals that have obtained a professional license. In order to get licensed, engineers must complete a number of requirements. First, one must complete a four or five-year college undergraduate degree. Following graduation, the individual must work under a professional engineer for at least four years, pass an intensive exam, and earn a license from their state's licensure board. Having a professional engineer's license means you have accepted both the technical and the ethical obligations of the engineering profession. Once a professional engineer is licensed, the individual is free to practice the discipline of civil engineering, and may stamp documents of any kind within the practice and expertise. This licensure is important since it is legally required to be a consulting engineer or a private practitioner. It can also raise prestige and accelerate career development.

The process of preparing a sustainable roofing plan for WPI will expose our group to the concept of structural design and analysis, which is also required by professional licensed civil engineers. Our project explores alternative rooftop technologies that could possibly be employed by the WPI community. These alternative systems consist of installing solar panels, green roofs, and solar collectors to the roofs of chosen buildings at WPI. A structural analysis of the buildings will be executed, as well as a proposed sustainable roofing plan which will be given to the school. In order to install solar panels, green roofs, and solar collectors, one must make sure that the building can carry the loads imposed by these technologies. Additionally, our analysis will include how efficient solar panels, green roofs, and solar collectors are, and how much money they can save the school in the long run.

Solar panels, green roofs, and solar collectors have the ability to deal with the negative impacts of the urban heat island effect by making the problem part of the solution. This project reflects the meaning of a professional licensed civil engineer. There are technical aspects to this project: designing the layout of solar panels and green roofs, choosing a building and analyzing

the structure's support, and producing an economic evaluation. Finally, our project relates to the nature of a professional licensed engineer by promoting health and welfare in an ethical manner and making the WPI community more sustainable.

# 6 Methodology

The methods section outlines the criteria for completing our MQP project and accomplishing our objectives. Each criteria contains information relating to steps, specific tasks, references, and person responsible for completing the task. The following criteria are defined in this section: identify buildings to begin analyzing, meet with WPI Facilities Department, identify type of solar panel, green roof, and solar collector systems to install, define solar panel, green roof, and solar collector layout, structural analysis and design, and evaluation and recommendation.

# **6.1 Identify Buildings for Consideration**

The goal for this criteria is to make a list of potential buildings at WPI for consideration. This involves starting with a list of all the buildings at WPI, categorizing these buildings based on different criteria, and then narrowing down the list. An outlined list of requirements for buildings to have in order to support solar panels, green roofs, and solar collectors will be outlined, as well as the initial list of all the buildings at WPI with information pertaining to the requirements. By comparing the list of buildings and seeing if they meet the requirements outlined, we will be able to make a narrowed down list of buildings to begin analyzing. Table 4 shows a breakdown of steps and tasks for identifying buildings for consideration.

## **6.2** Meet with WPI Facilities Department

The goal for this criteria is to narrow down the list even further, and identify one or more buildings for each of the three technologies for our final analysis. This involves getting in contact with a representative within the WPI Facilities Department to obtain information about the buildings identified in the previous criteria. Our plan during the meeting is to give the representative the list of buildings we currently believe can support solar panels and/or green roofs, and explain the process and requirements for identifying these buildings. Once the representative understands and approves of this process, we will attempt to obtain different information on the energy consumption and design drawings for each building. Our objective is to choose the final buildings which have available design drawings, and have available energy consumption values. If we are not able to obtain energy consumption for the buildings, then we will use researched standard energy consumption values. Table 5 shows a breakdown of steps and tasks for meeting with WPI Facilities Department.

Table 4: Steps and Tasks for Identifying Buildings for Consideration

Steps	Specific Tasks	References	Person(s) Responsible
	a. Categorize list into following sections:		Ryan
	i. Age of building		
Outline list of requirements for buildings to have in order to support solar panels, green roofs, and solar collectors	ii. Exposure to sun	Online research	
to support solar pariols, groom roots, and solar concetors	iii. Slope of roof		
	iv. Existing sustainable roofing practice		
	a. List all of the buildings at WPI	Online research: WPI website	Sebastian and lan
	b. Categorize buildings into academic, residential, recreational, or administrative		
	c. Identify year the building was constructred		
	d. Identify the number of stories the building has (not including basement)		
Begin categorizing and observing buildings at WPI	e. Physical observation: identify if there are any trees or buildings which block the roof's exposure to the sunlight (south side of roof)		
	f. Identify type of roof on building:		
	i. Flat or sloped		
	ii. If sloped, identify if a portion of the sloped roof is facing south		
	g. Identify buildings which currently use sustainable practices:		
	i. Buildings that have solar panels, green roofs, or solar collectors		
3) Make list of potential buildings at WPI for consideration	a. See which buildings in Step 2 meet the requirements outlined in Step 1 (steps above)	Step 1 + Step 2	All

 Table 5: Steps and Tasks for Meeting with WPI Facilities Department

Steps	Specific Tasks	References	Person(s) Responsible
Get in contact with someone within WPI Facilities Department	a. Potential contact: William Paul Spratt - Director of Facilities	Email: wpspratt@wpi.edu	All
1) Get in contact with someone within WP11 achines Department	a. Potential contact. William Paul Spratt - Director of Facilities	Phone: 508-831-5904	All
	a. Energy consumption of building:		
	i. If cannot obtain information, will have to research standard values depending on type of building		All
	b. Cost of energy consumption of building:	Obtain from interview	
	i. If cannot obtain information, will have to research standard values depending on type of building		
	c. Design drawings (plans) of building		
3) Narrow down list even further for buildings to analyze	a. Identify final buildings:		
	i. Design drawings must be available for the building	Obtain from interview	All
	ii. Energy consumption values must be available for the building		

## 6.3 Identify Types of Solar Panels, Green Roofs, and Solar Collectors to Install

The goal for this criteria is to choose two types of solar panel systems, one type of green roof system, and one type of solar collector system to use for our analysis. This requires researching different types of solar panel, green roof, and solar collector systems, and choosing the types based on ease of installation, low weight to reduce loads, sufficient energy production, and low cost of installation. Table 6 shows a breakdown of steps and tasks for identifying types of solar panels, green roofs, and solar collectors to install.

### 6.4 Define Solar Panel, Green Roof, and Solar Collector Layout

The goal for this criteria is to calculate the number of solar panels or solar collectors for each building, choose the specific location on the roof for solar panel, green roof, solar collector installation, outline the construction process, and consider safety of construction. Calculating the number of solar panels or solar collectors will depend on the energy production for each building, and the type of solar panel or solar collector system used. By calculating the number of solar panels or solar collectors, we can determine the location on the roof by assessing the available space of proper size. Similarly for green roofs, we will need to use the energy consumption of the building to determine what size green roof will save energy greater than or equal to the building's energy consumption value. Then we can determine the location on the roof by assessing the available space of proper size. Table 7 shows a breakdown of steps and tasks for defining the solar panel, green roof, and solar collector layout.

## 6.5 Structural Analysis and Design

This criteria is a major portion of our project. The goal is to perform a structural analysis for each considered building, and determine whether it is feasible to install solar panel, green roof, or solar collector system on the roof of the building. If the current structure of the building cannot support the solar panels, green roof, or solar collectors, then structural reinforcements will be designed for the supporting elements of the building. Table 8 shows a breakdown of steps and tasks for the structural analysis and design.

#### **6.6 Evaluation and Recommendation**

The goal of this criteria is to determine whether it is both structurally and economically feasible to install solar panels, green roofs, or solar collectors on the roof of each building. After the structural analysis is performed in the previous criteria, we will need to perform an economic

evaluation by comparing current energy consumption cost values for the building and cost values for the installation and long term maintenance of solar panels, green roofs, and solar collectors. Whichever value is greater will determine whether or not it is economically feasible to install solar panel, green roof, or solar collector system on the building. There is also a revenue source due to production of electricity or increased insulation that reduces energy demand for cooling. Table 9 shows a breakdown of steps and tasks for the evaluation and recommendation.

Table 6: Steps and Tasks for Identifying Types of Solar Panels, Green Roofs, and Solar Collectors to Install

Steps	Specific Tasks	References	Person(s) Responsible
1	Choose two types of solar panel systems, one type of green roof system, and one type of solar collector system:		Sebastian
	i. Ease of installation		
A) December 1997 and the second secon	ii. Low weight to reduce loads		
Research different types of solar panel, green roof, and solar collector systems	iii. Suffecient energy production	Online research	
Solidates systems	iv. Low cost of installation		
	b. Identify size (dimensions, gross area) and weight for each type of solar panel, green roof, and solar collector system		
	i. Will need to identify type of vegetation used for green roof system		
Determine cost for installation of solar panel, green roof, and solar collector systems	a. Determine installation costs for each type of solar panel, green roof, and solar collector system	Online research	lan
3) Determine lifetime of each type of solar panel, green roof, and solar collector system	a. Determine the maintenance costs overtime	Online research	Ryan

Table 7: Steps and Tasks for Defining the Solar Panel, Green Roof, and Solar Collector Layout

Steps	Specific Tasks	References	Person(s) Responsible
1) Using global energy output formula, calculate number of solar panels	a. Based on energy consumption of building and type of solar panel or solar collector system used	Global energy output formula	Ryan
and solar collectors for each building	b. Number of solar panels or solar collectors will vary per building and for each type of solar system	Giobal energy output lorniula	
	a. Identify the building's energy consumption value	Information from interview	Ryan
2) Identify size of green roof system for each building	<ul> <li>b. Identify size of green roof which will produce energy greater than or equal to the building's energy consumption value</li> </ul>	Online research	
	a. Calculate area of different sections of roof to determine if solar panels, green roof, or solar collectors can be installed:		Sebastian
Determine available space on roof for calculated number of solar panels,	i. Will require calculating total area of all solar panels or solar collectors	Online research and design	
solar collectors, or size of green roof system	ii. Total area of solar panels or solar collectors will depend on type of solar system	drawings	
	iii. Compare to size of green roof determined in previous step (Step 2)		
	b. Needs to be completed for each chosen building		
	a. Identify safety measures needed to be considered when installing solar panels, green roofs, and solar collectors		lan
4) Consider safety of construction	b. Time it will take to install solar panels, green roofs, and solar collectors	Online research	
	i. When can they be installed (season dependent)?		
	ii. Depends on number of solar panels, solar collectors, or size of green roof being installed		
5) Choose specific location on roof where solar panels, green roof, or solar collectors will be installed	a. Solar panels and solar collectors depend on pitch of roof		
	b. Solar panels and solar collectors must be positioned to face south	Design drawings	All
	c. Roof must be flat for green roof		
Outline construction process of installing solar panels, green roof, or solar collectors	a. Database research on step by step construction process for installing solar panel, green roof, or solar collector system	Online research	Ryan

Table 8: Steps and Tasks for the Structural Analysis and Design

Steps	Specific Tasks	References	Person(s) Responsible
Set up Excel sheet which will calculate dead loads, wind loads, snow loads, and seismic loads of solar panels, green roofs, and solar collectors	a. Identify calculation process in accordance with ASCE 7-10	ASCE 7-10	Sebastian and lan
	a. Depends on type of solar panel, green roof, or solar collector system, dimensions, weight, and number of solar panels and solar collectors	Excel sheet from Step 1	Ryan
	b. Calculate for each building and type of solar panel, green roof, or solar collector system		
	a. Identify material and dimensions of roof structure and building frame	Design drawings & design	
Analyze structure of each building to determine feasibility of installing solar panels, green roof, or solar collectors on roof of building	b. Benchmark the capacity of the exisiting roof structure and supporting elements (columns)	specifications (AISC, ACI, NDS)	All
	c. Use design drawings of building to perform analysis		
	a. Identify which structural reinforcements should be applied to the building	Online research	All
	b. Design added structural reinforcements	Online research	All

# **Table 9: Steps and Tasks for the Evaluation and Recommendation**

Steps	Specific Tasks	References	Person(s) Responsible
1) Determine the current cost of energy requirement of the building	a. Will vary per building	Obtain from interview	All
	b. Previously determined from meeting with WPI Facilities Department	Obtain from interview	
	a. Cost values include:		
	i. Current cost of energy consumption of the building		
	ii. Cost for installation of solar panels, green roofs, and solar collectors		
Compare cost values to determine if it is economically feasible to install solar panels, green roofs, and solar collectors	iii. Lifetime of solar panels, green roofs, and solar collectors: maintenance costs overtime	Obtain from interview and online research	All
mistali solali paliolo, groon rooto, ana solali sollottoro	b. Compare values i and ii+iii above and see which is greater to determine feasibility		
	i. Will involve life-cycle cost analysis with time value of money		
	c. Determine for each chosen building		
	a. Comprehensive proposal handbook:	Microsoft Word	Ryan
	i. Outline plan for implementing sustainable roofing practices		
3) Create deliverables	ii. Type of solar panel, green roof, or solar collector system		
	iii. Roof layout		
	iv. Structural reinforcements		
	v. Economic evaluation		
	b. Engineering design drawings	AutoCAD and Revit	Sebastian and lan

## 7 Deliverables

Our deliverables will include recommendations for the WPI Facilities Department on ways they can implement sustainable rooftop technologies on a defined set of buildings at WPI. The vision of WPI's sustainability plan states: "We at WPI will demonstrate our commitment to the preservation of the planet and all its life through the incorporation of the principles of sustainability throughout the institution (WPI Sustainability Plan, 2017)." We can contribute to this vision by providing the school with a set of recommendations for the implementation of sustainable rooftop technologies.

The recommendations given to WPI will be in the form of a proposal handbook, which will outline a plan for implementing sustainable rooftop systems on specific buildings at WPI. The handbook will outline a plan for implementing a sustainable roofing practice on one or more buildings at WPI. The plan will contain information on the type of solar panel, green roof, or solar collector system, the roof layout, structural reinforcements, and an economic evaluation which will identify how much money is saved for the building overtime. By providing WPI Facilities Department with a handbook outlining a plan for sustainable rooftop technologies on different buildings, the Department has the opportunity to further contribute to the vision outlined in WPI's sustainability plan.

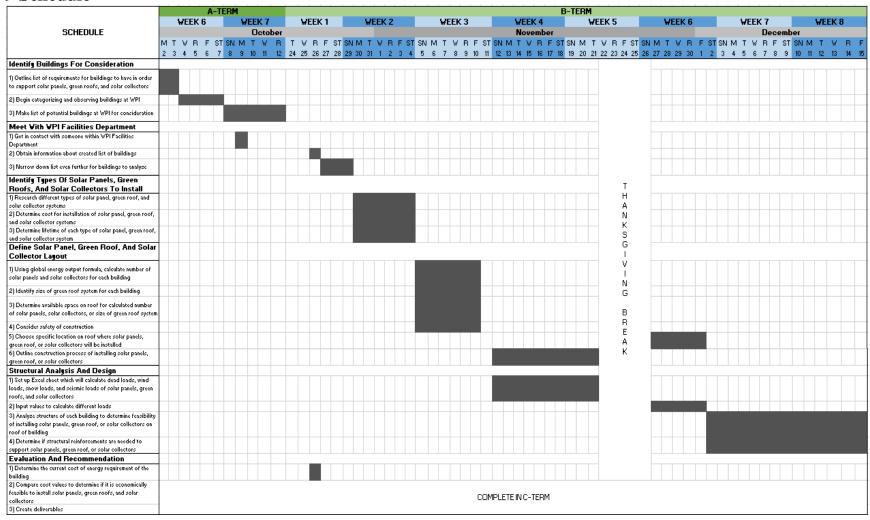
Additionally, we will create engineering drawings using Revit and/or AutoCAD to present and document the proposed sustainable roofing practice on each of the buildings. This will include the location and dimensions of the sustainable roofing practice, as well as any structural reinforcements on the columns or roof structure of the building. These drawings will be created in accordance with the actual design drawings of the building.

As described, the products of our project will include a handbook and engineering drawings. By producing these deliverables, we can provide WPI Facilities Department with a comprehensive outlined plan for implementing sustainable roofing practices on different buildings at WPI. Our MQP provides an opportunity for WPI to further enhance its sustainability plan, and commit to the vision they have set out in the plan.

# **8 Conclusions**

The expectation of this project is to identify buildings at WPI where an analysis will be performed for the installation of solar panels, green roofs, and solar collectors. The analysis will be completed on one or more buildings for the installation of solar panels, green roofs, and solar collectors. A structural analysis and economic evaluation will be performed to determine the feasibility of installing the sustainable roofing system for each building. Finally, a comprehensive proposal handbook and engineering design drawings will outline and display the process for installing solar panels, green roofs, and solar collectors on each of the chosen buildings. These deliverables will be given to the WPI Facilities Department at the end of the project. By completing this project, we will contribute to WPI's sustainability plan and serve the community in an environmental, economic, and ethical way.

# 9 Schedule



## 10 References

- Alkhrdaji, T., & Thomas, J. (2017). Structural Strengthening Using External Post-Tensioning Systems. Structure Magazine. Retrieved from https://www.structural.net/article/structural-strengthening-using-external-post-tensioning-systems
- Andresen, Fernandez, Rowe, Rugh, VanWoert & Xiao. (2004). Effects of Roof Surface, Slope, and Media Depth. *Green Roof Stormwater Retention*, *34*(3), 1036-1044. Retrieved from https://dl.sciencesocieties.org/publications/jeq/articles/34/3/1036?highlight=&searchresult=1
- Apricus Solar Water Company. (2017). Evacuated Tube Solar Collectors. Retrieved from http://www.apricus.com/html/solar\_collector.htm
- Battaglia, C., Cuevas, A., & De Wolf, S. (2016). High-efficiency crystalline silicon solar cells: status and perspectives. *Energy & Environmental Science*, 9th ser., 1552-1576. doi:10.1039/c5ee03380b
- City of Portland. (2008). Cost Benefit Evaluation of Eco-Roofs. Retrieved from www.portlandonline.com/bes/index.cfm?a=261053&c=50818.
- Energy Matters. (2016). Solar Power Educational Information: Renewable Energy. Retrieved from http://www.energymatters.com.au/education/
- Gartner. (2008). Structural Implications of Green Roofs, Terraces, and Walls. Retrieved from http://mgase.weebly.com/uploads/6/1/1/3/6113816/paper\_5\_-\_2008\_seaoc\_convention\_\_structural\_implications\_of\_green\_roofs\_terraces\_and\_walls\_by\_seaosc\_sdc\_7-7-08.pdf
- GSA. (n.d.). GSA Green Roof Benefits and Challenges. *Challenges to Green Roof Construction*.

  Retrieved from

  https://app\_gsagov\_prod\_rdcgwaajp7wr.s3.amazonaws.com/Challenges\_to\_Green\_Roof

  \_Construction.pdf
- HTP. (2017). Evacuated Tubes Solar Collectors. Retrieved from http://www.htproducts.com/literature/lp-220.pdf

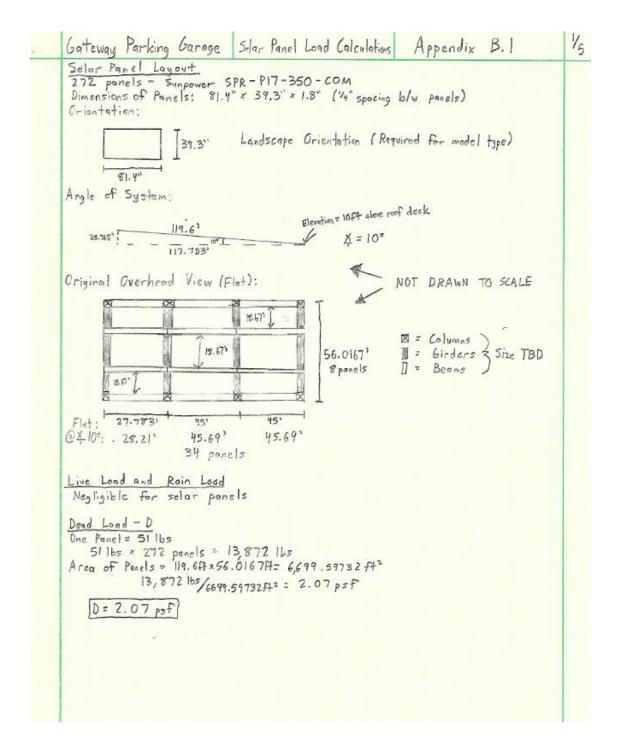
- Huffington Post. (2009). Green Roofs: All You Need to Know. Retrieved from http://www.huffingtonpost.com/2009/01/14/green-roofs-all-you-need\_n\_157935.html
- Imboden, P. B. (2009). Solar Power Has Benefits as a Source of Alternative Energy. Retrieved from http://www.nationalgeographic.com/environment/global-warming/solar-power/
- Jörg Breuning & Green Roof Service LLC. (2017). Consultancy, Design, Engineering, Project Management and Expert Witness of Green Roofs and Green Walls since 1980. Retrieved from http://www.greenrooftechnology.com/
- Kosareo, L., & Ries, R. (2007). Comparative Environmental Life Cycle Assessment of Green Roofs. *Building and Environment*, 42(7), 2606-2613. doi:https://doi.org/10.1016/j.buildenv.2006.06.019
- Leslie. (2003). Capturing the Daylight Dividend in Buildings: Why and How? *Building and Environment*, 38(2), 381-385. doi:https://doi.org/10.1016/S0360-1323(02)00118-X
- MGASE. (2008). Structural Implications of Green Roofs, Terraces, and Walls. Retrieved from http://mgase.weebly.com
- National Geographic (2017). Green Roofs. Retrieved from http://ngm.nationalgeographic.com/2009/05/green-roofs/klinkenborg-text
- Photovoltaic Software. (2017). How to calculate the annual solar energy output of a photovoltaic system? Retrieved from http://photovoltaic-software.com/
- Radiantec Company. (n.d.) Solar Construction Manual. Retrieved from http://www.radiantsolar.com/pdf/construction.pdf
- Ridal, J., Garvin, S., Chambers, F., & Travers, J. (2010). Risk assessment of structural impacts on buildings of solar hot water collectors and photovoltaic tiles and panels final report.

  Retrieved from 
  http://www.solarthermalworld.org/sites/gstec/files/solar\_thermal\_collector\_building\_load s.pdf
- Shaw, M. (n.d.). Structural Strengthening With External Plate Bonding. Retrieved from http://www.bath.ac.uk/cwct/cladding\_org/icbest97/paper24.pdf

- Shoultes, S. (2017). Post-Tensioning. Retrieved from http://kcwardco.com/concrete-repair services/structural-strengthening/post-tensioning
- Solar Power Authority. (2017). 25 Interesting Facts About Solar Power. Retrieved from https://www.solarpowerauthority.com/25-facts-about-solar-power/
- Solar World. (2014). Determining Wind and Snow Loads for Solar Panels. *America's Authority on Solar*. Retrieved from https://www.solarworld-usa.com/
- Structural Engineers Association of California. (2012). Structural Seismic Requirements and Commentary for Rooftop Solar Photovoltaic Arrays. Retrieved from SEAOC\_Solar\_PV\_Seismic\_document\_2012\_08\_Final.pdf
- Structural Engineers Association of California. (2012). Wind Design for Low-Profile Solar Photovoltaic Arrays on Flat Roofs. Retrieved from SEAOC\_Solar\_PV\_wind\_document\_2012\_08\_Final.pdf
- Sustainable Facilities Tool General Services Administration. (2017). Retrieved from https://sftool.gov/explore/green-building/section/76/planted-roof/system overview#planted-roof/stormwater-management
- United States Environmental Protection Agency. (2017). Learn About Heat Islands. Retrieved from https://www.epa.gov/heat-islands/learn-about-heat-islands
- WPI Sustainability Plan. (2017). Retrieved from https://web.wpi.edu/Images/CMS/Facilities/WPI\_Sustainability\_Plan.pdf
- Wrobel, C. A. (2017). Structural Effect of Solar Arrays on an Existing Structure. Retrieved from spi17.mapyourshow.com/7\_0/collateral\_redirect.cfm?CollateralID=8

#### APPENDIX B: SOLAR PANEL CALCULATIONS

#### **Appendix B.1: Solar Panel Load Calculations**



```
3/5
                                                           Appendix B. 1
Snow Load - S
Sloped Roof Snow Loads (Section 7.4)
Thermal Factor (Table 7-3)
                   for all structures except indicated below
       (t = 1.0
Lold Roof Slope Factor (Section 7.4.2)
       Since Ce = 1.0
        => Dashed line on Fig. 7-2a
       Using 10° roof slope
Cs = 0.92
Exposure Factor (Table 7-Z)
    => Terrain Lategory B (Section 26.7)
       Fully Exposed Roof
     . Ce = 0.9
Importance Factor (Table 1.5-2; Table 1.5-1)
Risk Category II
       Is = 1.00
Ground Snow Loads (Figure 7-1)
       Worcester, MA:
Flat Roof Snow Load (Section 7.3)
        Pf = 0.7 Ce C+ Ispg
        p== 0.7 (0.9)(1.0)(1.0)(50psf)
        PF = 31.5 psf
.. Ps = Cs pf
   Ps = (0.92)(31.5 psf)
                                S = 28,98 psf
   Ps = 28.98 psf
Wind Load - W
From ASCE 7-10:
  1) Risk Category (Table 1.5-1)
  Risk Lategory II.
2) Basic Wind Speed (Fig. 26.5-1A)
        Worcester, MA:
         V=120mph
  3) Wind Directionality Factor (Table 26.6-1)
        Structure Type - Buildings
Ka = 0.85
     Exposure Cotegory (Section 26.7)
        Terrain Category B
     Topographic Factor (Section 26.8)
No topographic effects
Kzt = 1.0
Gust Effect Factor (Section 26.9)
          6= 0.85
  4) Velocity Pressure Exposure Coefficient (Table 29.3-1)
          Height above ground level = 60ft
          Exposure Lategory B
            Kz = 0.85
```

```
1/5
                                                          Appendix B. 1
   9) Calculate Design Wind Pressure
         P= 9266m
         p = (26.63 psf)(0.962)
         P = 25.618 psf
                                         W= 25.618 psf
Scismic Load - E
Risk-Targeted Maximum Considered Earthquake Spectral Response Accelerations
    5s: (Fig. 22-1)
      Warcoster, MA: MCER = 18 % 9
    Si: (Fig. 22-2)
       Worcester, MA: MCER = 7%, 9
Seismic Design Category
    Soil Classification (Section 20)
       Site D - Details unknown
    Design Spectral Acceleration Parameters (Section 11.4.4)
        505 = 35ms
        500 = 35MI
    Spectral Response Acceleration Parameter (Section 11.4.3)
        Sms = Fass
        Smi = Fus,
     Site Coefficients
        For Site D and Js = 0.25
          Fo = 1.6 (Table 11.4-1)
        For Site D and S1 = 0.1
          Fv = 2.4 (Table 11.4-2)
     :. 5Ms = (1.6)(0.18) 5M1 = (2,4)(0.07)
        Sus = 0.288
                            5m1 = 0.168
     1. So5 = = (0.288)
                            501 = = (0.168)
        Sps = 0.192
                             501 = 0.112
     Risk Category (Table 1.5-1)
     Risk Catagory II
Seismic Design Entegory (Toble 11.6-1)
         For 0.167 : 505 4 0.33 and Risk Cotegory II
            SDC = B
Seismic Importance Factor (Table 1.5-2)
     For Risk Lategory II
         Te = 1.00
Jeismic Bose Shear (Section 15.4.1.7)
     V= 0.30500 WIE
                      For rigid nonbuilding structures
     V= 0.30 (0.192)(2.07psf)(1.00)
     V= 0.119232 psf
Fundamental Period (Scotion 12.8.2.1.)
     Ta = Cthi
        Ct = 0.02 - All other structural systems'
x = 0.75 - (Table 12.8-2)
        ha= 10f+ + 30.768f+ = 20.384f4 - Structural height
     Ta = (0,02) (20.384 ft) 0.75
```

Ta = 0.195 = T

```
5/5
                                                            Appendix B. 1
Vertical Distribution Factor (Section 12.8.3)
       Cvx = Wx hx k

it with k

Wx = 2.07 psf - weight
          hx = 20.384 Ft
k = 1 - since T ≤ 0.55
                                        (T= 0.195)
      Cux = (2.07 psf)(26.384F4)"
              (2.07 psf) (20,384 ft)
       Lvx = 1.0
Lateral Seismic Force (Section 12.8.3)
       Fx = LynV
       Fx = (1.0)(0.119232 psf)
       Fx = 0,119232 psf
Seismic Load Effect (Section 12.4.2)
       E = En + Er
     Horizontal Scismic Load Effect (Section 12.4.2.1)
          En= pas
            p - Redundancy Factor (Section 12.3.4)
              p=1.0 - Seismic Design Category B
          QE = 0.119232 psf = Fx
          En = (1.0)(0.119232 psf)
          En = 0. 119232 psf
     Vertical Science Load Effect (Section 12,4.2.2)
          Ev = 0.25050
          Ev = 0.2(0.192)(2.07psf)
         1 Ev = 0.079 psf
Summary
 D= 2.07 psf
 5= 28.98 psf
 W= 25.618 PSF
 En= 0.119232 psf Ev = 0.079psf
 L= 0 psf
 R = 0 psf
Load Combinations:
 1. 1.4 D
 2. 1.2 D + 1.6L + 0.5(Lr or 5 or R)
3. 1.2 D + 1.6(Lr or 5 or R) + (L or 0.5 W)
4. 1.2 D + 1.6 W + L + 0.5(Lr or 5 or R)
                                                   & Gravity Loads
  5. 1.2D+ Ev+ L+0.25
  6. 0.90 + 1.0 W
  7. 0.90 + 1.0 Eh
```

### **Appendix B.2: Beam Calculations**

Gater	lay Parking	Garage	Beam Ca	lculations	Appendix	B. 2	1/
1.4D = 1.ZD+1 1.2D+1 1.ZD+1 1.ZD+	.6 L + 0.5 .6 (L-/5/R) .6 W + L + Ev + L 1.0 W = 0	5f)= 7.90 (L-/5/R)= )+(L/0.5W 0.5(L-/5/F + 0.25	1.2(2.07psf)=1.2(2.07ps 2)=1.2(2.07ps 2)=1.2(2.07 =1.2(2.07 =8.36ps 4)+1.0(6	sf) + 1.6(28.98p psf) + 1.0(28.61 17psf) + 0.079ps sf 0 osf) = 1.88	.5(28.98psf)= 11 sf) + 0.5(25.618 8psf)+ 6psf+ 0.5(2 f + 0psf + 0.2( psf sf) = 1.98psf	psf)= 61.61 psf 8.98;sf)= 42.48psf 28.98ps F)	
Exter	ion Bear	nad = 61.6					
Wy = 6 Max. B	1.61psf,	, 9.335 A h = 45.6	9++	) + + = 0.58 k/f+ = 156.073 k	. 64		
1	8	8		= 40.0103			
AISC 1	able 3-Z	: W14×	26 => Zx	= 40.2in3 ≥	40.0in3		
Mu =	0.58 WELL	0.606k/f+	(45.69++)	= 0.606 k/f+ = 158.214 l = 42.2in3	e · f+		
AISC 7	able 3-7	2: WZ4×	55 => Z×	= 134 in 3 2 4	2. Zin 3 /		
Mu = 0. $Mu = w$	606 k/ft	+ 1.2(55)	+ = 55 b/f+ b/f+) (b/600 b 15.69 F+) = +) (12:0/F+) =	) = 0.672 <sup>k/</sup> F 175.437 k 46.8in <sup>3</sup> ≤ 1	7,5+ 34in 3		
Flange l	ocal Buch	eling (FLB			Fable 1-1 . bf 24255 : Zér	= 6.94	
h/f	al Buckli u ≤ 3.76 ≤ 90.6	ng (WLB): \( \frac{E}{F_u} = 3.76 \)	129,000kg;	AISC Ta	ble 1-1: hy =	54.6	

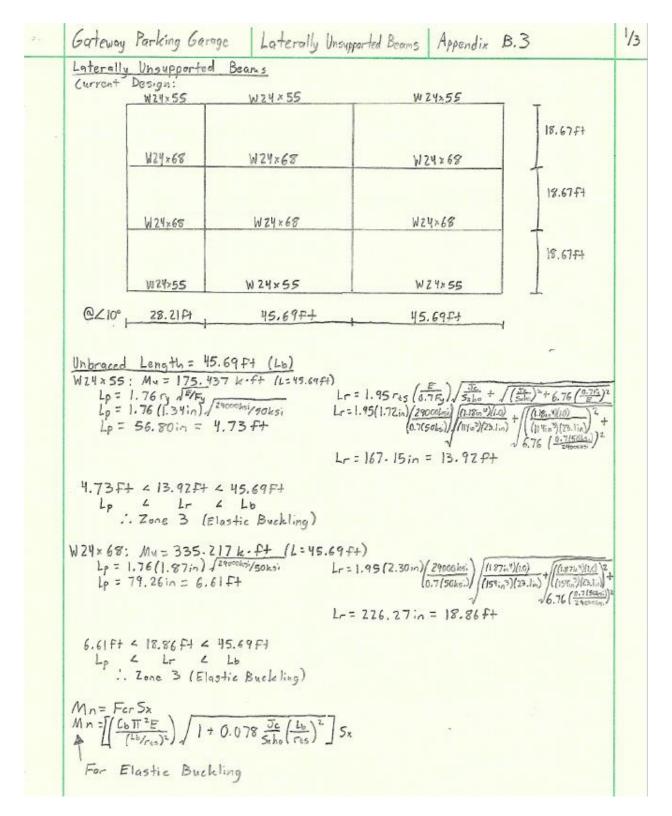
```
2/3
                                                             Appendix B.Z
Total Service Load:
                               WT = (D+S) Tributary Width + Weight of Beam
    A= 50-L4
         384 FI>
                               WT = (2.07 psf + 28.98 psf) (9.33 5F+) + 5516+
    A= 5(344.857 1/4+) (45.694)4
                               WT = 344.857 WA
       384(29×10°05)(1350in4)
       x 1728in3
                               Ix: from AISC Table 3-3 for beam size
            53
                              Linit = 1/240 = (45.69 Ft) (1211/FT) = 2.2819
   A= 0.86 in
     0.86in< 2,28in V
Snow Deflection:
    D= 5 ws L"
                                Wa = 5 x Tributary Width
        384 EIX
                                Ws = (28.98 psf) 9.335f4
   D3 = 5(270 528 1424) (45.6984)4
                                Vs= 270,528 13/5+
        384 (29×106 ps.) (1350 mx)
                                Limit = 1/360 or 1" = (45.69f+)(1219/54) = 1.5in
       x 1728 in3
            P.1-3
   As= 0.68 in
                                Limit = lin
    0.68 in 4 1 in
Due to satisfication of FLB, WLB, Total Service Load, Snow Deflection:
       Exterior Beam Size = WZ4 x 55
Interior Beams
Governing Load = 61.61 psf
Tributary Width = 18.67ft
Wy = 61.61psf x 18.67ft x (*/100016) = 1.15 */++
Max Beam Length = 45.69ft
Mu = wul2 = (1.15 WFL) (45.69ft) = 300.145 K.ft
Zx = Mu = (300.145 k.f+)(12in/f+) = 80.0in3
AISC Table 3-2: WZIX 44 => Zx= 95.4 in 3 2 80.0 in 3 /
New Scleeted Beam Weight = 44 14/5+
Wy = 1.15 k/F+ + 1.2(441b/F+)(1/100510) = 1.203 k/F+
My = WUL" = (1.203 WFF) (45.69 FF) = 313.923 k.ft
Zx= Mu = 313.923 k-f+(12"/4+) = 83.7in3 = 95.4in3 => However Deflection

DFy (0.9)(50lesi) Performence Not Sotio
                                                                    Performance Not Satisfied
AISC Table 3-2: W24x68 => Zx= 177 in3 = 83,7in3 /
New Selected Beam Weight = 6819/5+
Wu = 1.203 Mp+ + 1.2(68 Mp+) ( Wiccom) = 1.285 Mp+
Mu = Wul2 = (1.285 Wex) (45.69 Fx) = 335.217 k. A
```

```
3/3
                                                      Appendix B.Z
Zx = Mw = 335.217 k. P+ (12:0/A) = 89.4:n 3 4 177:n3 V
Flange Local Buckling (FLB):
                                 AISC Table 1-1: b1/24= 7.66
    by 26 6 6.38 馬
                                 for W24×68
   7.66 4 9.15 /
Web Local Buckling (WLB):
                                 ALSC Table 1-1: 1/4 = 52
    We = 3.76 Fy
                                 for W24×68
    52 = 90.6
Total Service Load:
   Δτ = 5/647.714 16/4+) (45.69ft) 1/28/2 1/2 647. 714 16/4

Δτ = 1.20 in
                                 Ix: From AISC table 3-3 For bean size
    AT = 1.20 in
                               Limit = 1/240 = (45.6991)(1210/4-)/240 = 2.28:0
    1.20in < 2.28in
Snow Deflection:
   As = 5 wal4
                                 Ws = 5 x Tributary Width
                                 Ws = (28.98psf)(18.67f4)
   Δs = 5(541.057 10/4)/45.69F+) × 178 Ws = 541.057 10/5+
                                 Limit= 4300 or 1"= 145.69 F4) (1814) = 1.5 in
    As = 1.00in
    1.00in & 1.00in
                                Limit = lin
Due to satisfaction of FLB, WLB, Total Service Load, Snow Deflection:
      Interior Beam Size = W24x68
```

### **Appendix B.3: Laterally Unsupported Beam Calculations**



```
Appendix B.3
For W24x55: Elastic Buckling
    Mn= [((1.0) 172 (24000 ks.) / 1 + 0.078 (1.181 m/n) (45.69 ft x 127) 2] (1141 m) (15 m)
     Mn = 57 k.ft
    DMn = 10.9) 157 k. F+) = 51.38 k. F+
     175. 437 k. ft 4 51.38 k. ft
             My & bun
                . Decrease Lb
For WZ4x68: Elastic Buckling
    Mn = 118 k.f+
    bmn = (0.9)(118k.F+) = 106, 16 k.F+
      335.217 k-ft & 106.16 k-ft
           Mu A tMn. Decrease Lb
Changed Unbraced Length = 15.23A(16)
W24x55: Mu= 175, 437 k.f+ (L= 45.69 f+)
       Lp = 4.73++ Lr = 13.92++
       Lp & Lr & Lb .. Zone 3 (Elastic Buckling)
WZ4x68: Mu = 335.217 k.f+ (L=45.69f+)
        Lp = 6.61F+ Lr = 18.86F+
        Lp 4 Lb 4 Lr . . Zone Z (Inclustic Buckling)
For WZ4x55: Elastic Buckling
     M_{n} = \left[ \left( \frac{(1.0) \prod^{2} (29000ks_{1})}{(15.23f+212^{3/2}/1.72in)^{2}} \right) \sqrt{1 + 0.078} \frac{(1.18in^{3})(1)}{(114in^{3})(23.1in)} \left( \frac{15.23f+212^{3/2}}{1.72in} \right)^{2} \right] (114in^{3}) \left( \frac{f+1}{12in} \right)^{2} 
      Mn = 284 4 k.f+
    OMn = (0.9)(284,4k.f+) = 256k.f+
         175.437k-ft 4 256 k-ft
                  My & OMA
For WZ4 × 68: Inelastic Buckling
     M_n = C_b \left[ M_p - (M_p - 0.7 F_y S_b) \left( \frac{L_b - L_p}{L_b - L_p} \right) \right]
     Mn = (1.0) \left[ (177 in^3) (50ksi) - ((177 in^3) (50ksi) - 0.7 (50ksi) (157 in^3) \right] \left( \frac{15.23 F + (1^{10} \%_1) - 6.61 F + (1^{10} \%_2)}{18.86 F + (1^{10} \%_1) - 6.61 F + (1^{10} \%_2)} \right)
     Mn= 6428k·in (品)
     Mn = 535.67 k.ft
    OMn = (0.9) (535.67 k.f+) = 482.1 k.f+
        335.217 k-ft 4 482.1 k-ft
                                                      For WZYx55 and WZYx68 member
                                                      @ L= 45.69 F4 => Lb = 15.23 F+
```

# **Appendix B.4: Girder Calculations**

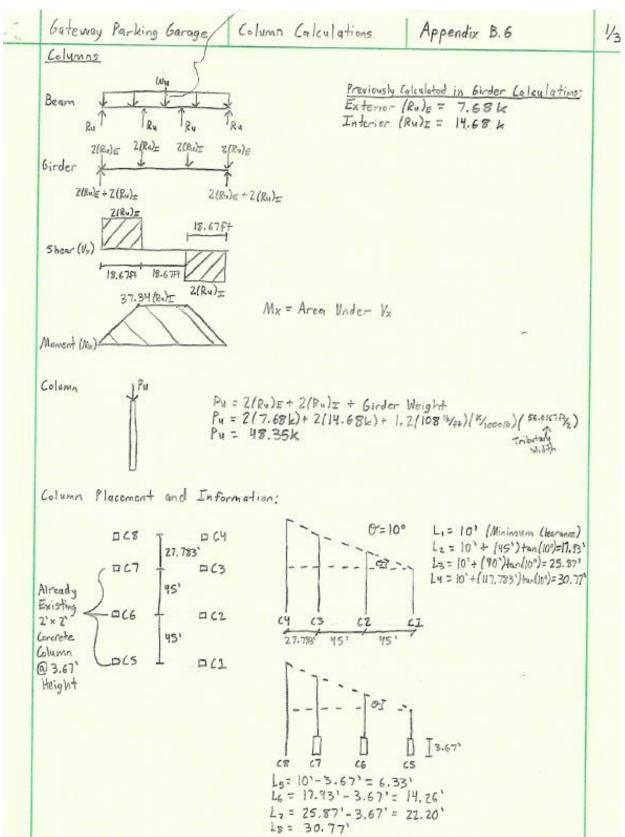
terior (Ru) = =   (0.6 4	ч
(Ru)E = 7.68  k Herior $(Ru)E = (100) \pm L = 11.3$ (Ru)E = 14.68  k	ч
(Ru)= 14.68 k	4 (45.69F+)
ea Under Vx	
ea Under Vx	
Mu=37.34(Ru)= Mu=37.34(14.68k) Mu=548.15 k.ft	-
146.17in3	
= 160 n3 ≥ 146.17 m3 /	
	f+
+)2 = 580.16 k.f+	
154.7 in 3 < 160 in 3 =>	However Deflection Performance Not Satisfied
346 in 3 ≥ 146.17 in 3	
(A) 598.98 K-FF	
59.7in3 4 346 in3	
ATSC Table 1-1. bf/ for W30 x 108. 245	= 6.89
	146.17:n3 $= 160:n^{3} \ge 146.17.n^{3} $ theorem of Girden = 56.0167. $\frac{4}{1} = 580.16 \text{ k.ft}$ $154.7:n^{3} \le 160:n^{3} = 3$ $346:n^{3} \ge 146.17:n^{3} $

		Appendix B.4
We	b Local Buckling (WLB):	7,11
	N 33 F	AISC Table 1-1 h.
	h/fw = 3.76 /=	AJSC Table 1-1 . N/Lw = 49.6
	49.6 ± 90.6	
7.1	al Service Load:	
103	AT = Mu L2	( - 100 F 1:
	6. Ix	(1 = 158 for acting point leads
	AT = (598.99 K. F+) (56.016	TX: From AISC Table 3-3 For girder size
	(158)(4470;n")	
	$\Delta \tau = 2.56$ in	Limit = 1/240 = (56.0167 Ft) (12:0/p+) = 2.80in
	366 . 386	240
	2.66 in < 2.80 in	
Sno	w Deflection:	
	15 = 5 W5 L4	W= S * Tributary Width
	384EIm	Ws = (28, 980sf)(15, 23f+)
	A5=5(441.57 VA)(56.01++)4	Ws = 441.37 10/#1
	384(29×106,5;)(44,70;4	1: 11 - ht 11 /5( a) a /5   12
	x 1728 in 3	Limit = 1/360 or 1" = (56.01 F+XIZin/F+) = 1.9 in
	As= 0.75in	Limit = lin 360
		dentification at the second
	0.75 in 4 lin /	
=	One girder has Tributa	W:1+1 = 21 72 C1
300	Ws = (28.980sf)(Z)	72-1)
	Ws = (28.98psf)(21. Ws = 629.45 1b/ff	
	1 - 51100 Up lb	1/50 - 1 - 1
	384/29×106	1) (56.01f+) " × 1728 in 3 si) (4470 in 4) × F+3
	Ds= lin	SINCIA TO IN O FEE
	- A	
	lin & lin V	
Due	to satisfaction of FI	B, WLB, Total Service Load, Snow Deflection:
	The second secon	
	Girder Size = W	30 × 108

# **Appendix B.5: Laterally Unsupported Girders**

1 atomal	y Parking Garage	Laterally Di	nsupported Girdens	Appendix 1	3.5
rair al	ly Unsupported	Girders			
Unbrace W30x1	d length = 18.67 08 => Lp = 7.59 Lp < Lb < Lr	ft (Lb) ft Lr = 22.1 Zone 2 (I)	Ft My = 59 nelastic Buckling	8.98k-ft	
	[Mp-(Mp-0.				
	.0) [(346i,3)(50ksi)			-11/18.67f+-7.5	59.51\7
Mn = 4	134,94k.++ 10,9)(434,94k	7.5		7)/( 22.1f+-7.5	9 F+ /]
7.000	598.98k.ft	4 391 k · F+			
C) 1	., Decre				
W30×10	Unbraced Length 18 => Lp = 7.59 Lp 4 Lb 4 Lr	1 = 4.335F4 (L F4 Lr = 22.1 Zone 2 (I	-b) f+ Mu=598. inclastic Buck	986-Ft ling)	-
$M_0 = I$	0)[6	//3116: 31/6-: 1	1 3/m 3/ 3	1/9 33501-	1.59617
	0)[(346in3)(50ksi)-	((346in 3)(50ksi)-	0.7850ks:/(299in	22.1++-7.5	9F+
	173 k · f+ (0, 9)(1373k · f+	)= 123CL .E4			
OMn =	(0,7)(12/3k+++	1-1579K-LL			
	598.98k-ft 6	1236k . Ft V	_		
For W	598.98k-ft 6			9.335ft]	
28 0000	30 × 108 member			9.335Ft]	
FOR W	30 × 108 member			9.335Ft	
8 000	30 × 108 member			9.335Ft]	9.72.60
28 0000	30 × 108 member			9.335Ft]	9. 335f <del>†</del>
28 0000	30 × 108 member			9.335Ft]	9. 335ft 9. 335ft
2000	30 × 108 member				
28 0000	30 × 108 member				9. 335 f4
8 000	30 × 108 member				9, 335 f4 9,335 f4
8 000	30 × 108 member				9. 335 f+ 9. 335 f+ 9. 335 f+
B 0.00	30 * 108 member	- @ L= 56.01	f+ => L6 =		9. 335 f+ 9. 335 f+ 9. 335 f+
2000	30 * 108 member		f+ => L6 =		9. 335 f+ 9. 335 f+ 9. 335 f+
2000	30 × 108 member	- @ L= 56.01	F+ => L6 =		9. 335 f+ 9. 335 f+ 9. 335 f+

### **Appendix B.6: Column Calculations**



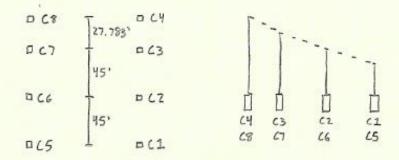
100000000000000000000000000000000000000			Appendi	х В.6
	Table 4-la:		g/2 // // // // // // // // // // // // /	
C1:	L, = 10'		65: L5 = 6.33' → 7	
	A=Pn = 317k > 48.35 ∴ W8×31	ok /	\$c Pn = 362 k > 4	8.35 k
	L2 = 17.93' -> 18'		1. W8×31 (6: L6 = 14.26' → 15	9
U1 1/2 (15 1.1)	Dc Pn = 178 k > 48.35 k	/	Oc. Pr = 230 k > 4	
	'. W8×31	2.2	W8 × 31	
	L3 = 25.87' → 26'		67: L7 = 27.70' → 2	3,
	cpn= 86.5 k > 48.35 1	× /	be Pn = 111k > 48	35k/
CH :	. M8×31		W8×31	
	4 = 30.77° → 31° 2Pn = 61.0K > 48.3		C8: Same as 64	
	". W8x 31	2 K P	W1 x 51	
	Column Number	Member Size	Member Length	
	2	W 8×31	10 FF	
	2 3 4 5 6 7	W 8×31	17.93 ft	
	u u	W 8 × 31	25.87 ft 30.77 ft	
	5	W8×31	6.33 f+	
	6	W 8×31	14.26 Ft	
	7	W 8×31	22.20 ft	
	8	W 8×31	30.77 Ft	

3/3

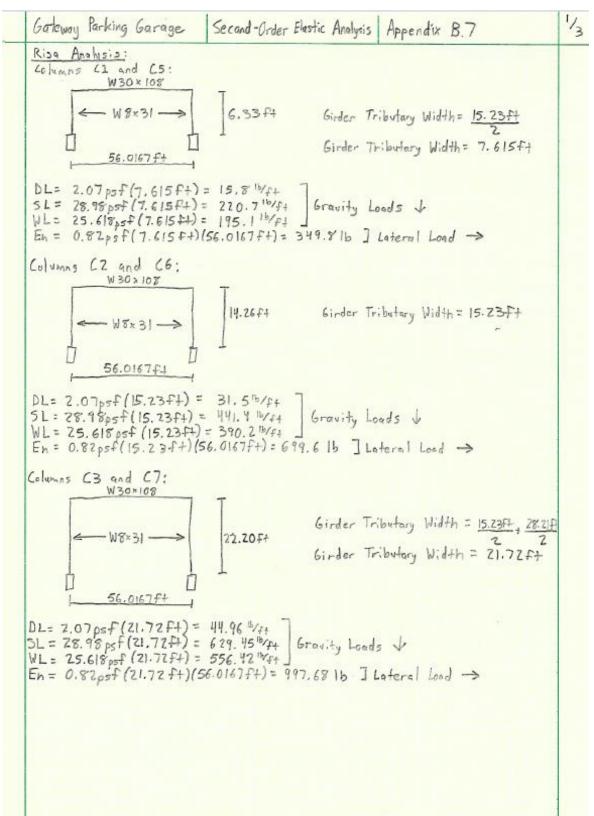
=> For convenience, we recommend placing 2ft x 2ft concrete columns with a height of 3.67 ft under the following columns: (1, C2, C3, C4, C8. By doing this, C1, C2, C3 will be the exact same as C5, C6, C7, respectively, since there are already existing 2ft x 2ft anasks columns under C5, C6, C7. C4 will be the same as C8, causing each to be resized because neither has an existing concrete column under them. Resizing of the columns is shown below:

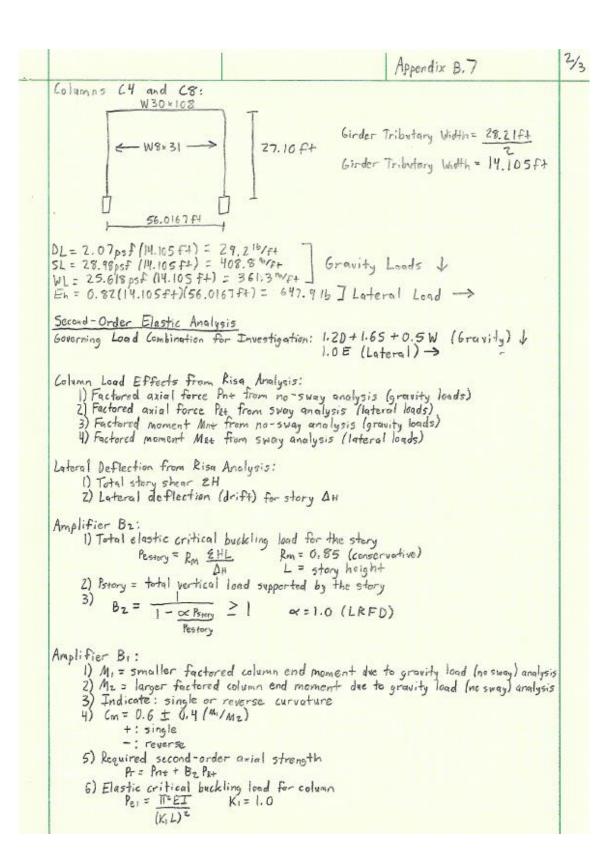
C4 and (8: L= 30.77ft - 3.67ft = 27.10 ft → 28ft ØcPn = 74.5k > 18.35 k ∴ W8×31

Column Number	Member Size	Member Length
1	W8×31	6.33FF
2	W8×31	14.26F+
3	W8×31	22.20 ft
4	W8 x31	27.10 ft
5	W8x31	6.33ft
6	W8×31	14. 26 F1
7	W8×31	22.20 Ft
8	W 8x 31	27. 10 FH



### **Appendix B.7: Second-Order Elastic Analysis**





	Appendix B.7	3/3
7) $B_1 = \frac{Cm}{1 - \frac{\omega Pr}{Per}} \ge 1$ $\omega = 1.0 (LRFD)$		
Required Second-Order Strength Values: 1) Pr = Pn+ + BzPe+ 2) Mr = B, Mn+ + BzMe+		
Effective Length Factor K:  1) Rotational resistance at joints $G = \underbrace{\mathbb{E}(^{Te}V_{L})}_{\Xi(^{Te}J_{L}g)}$ Gb: bottom joint  2) AISC Fig. C-A.7.2.  Determine Kx		
Axial Capacity Pc  1) $\frac{K_x L}{F_x}$ $\frac{K_y L}{F_y}$ $(K_y = 1.0)$ Larger value governs  2) $\frac{K_L}{F}$ $< 4.71\sqrt{F_y}$ $=>$ short to intermediate	-	
3) AISC Table 4-1a  - Vsing column length and size => OPn  Pc = PPn	Column	
Bending Capacity Mex  1) Web Local Buckling  1) Web Local Buckling  1) Flange Local Buckling  1) Flange Local Buckling  1) Lateral Torsional Buckling  1) Lateral Torsional Buckling  1) Lateral Torsional Buckling		
Mn = Mp = FyZx	Cb = 1.0	
Lp $L$ Lr $L$	2012	
5) $\frac{P_{r}}{P_{e}} \ge 0.2 \left  \frac{P_{r}}{P_{e}} + \frac{8}{9} \left( \frac{M_{rx}}{M_{ex}} \right) \le 1.0 \right  (HI - I)$		

### **Appendix B.8: New Girder Calculations**

Gataway Parking Garage New Gi	rder Calculation Appendix B. 8	
New (Lighter) Girder Sizes From Risa		_
New Max. Moment = 487, 14 4. Ft		
	120.0:3	
$Z_{x} = \frac{M_{y}}{\sigma_{Fy}} = \frac{(487.14 \text{ k·ft})(12^{\text{in}}/s_{t})}{(0.9)(50 \text{ k·si})} =$	. 164. 4 in	
1874 PART PART PART PART PART PART PART PART		
AISC Table 3-2: WZIX62 => Zx =	144in3 ≥ 129.9in3	
Solostal Girden Weight = 62 /2/c.		
Selected Girder Weight = 62 15/f+ Wu = 1.2(6215/f+) × (1/100016) = 0.0744 16/f+		
Mu = 487, 14k + f+ + wylz		
Mu - 487 141 - FL + 10 0744 Was 1/51	(K7C+)2 FIG 321 Et	
Mu = 487, 14k + + 10.0744 h/f+ ) 156	- 310.32k /	
Zx = Mu = (516.32k.f+)(12in/f+) =	137.7: 3 4 144 in 3 => However Deflection	
φFy (0.9)(50ksi)	Performance Not Satisfic	d
AISC Table 3-2: W30 x 90 => Zx=	283in3 ≥ 129.9in3	
	- Marketines - Tark Charles (Marketines	
Selected Girder Weight = 9016/F+ Wu = 1.219016/F+)(Wiscons) = 0.108 k/F+		
Wi = 482-148 t+ + (0.108x2+)/26	0K7FH2 5795 b-EL	
8	-CAR-CO 1995 1995 - CAR-1995 - PART - 4-	
$\frac{Z_x = M_u}{DF_y} = \frac{(529.5 \text{ f.f.})(12^{\text{in}}/_{f+})}{(0.9)(50 \text{ f.s.})} =$	141.21n3 4 283in3	
Dry (0.9)(50ks)	2000 C C C C C C C C C C C C C C C C C C	
Flange Local Buckling (FLB):	Web Local Buckling (WLB):	
bf/26 ≤ 0.38 /=	May ≤ 3.76 JE	
8.57 £ 9.15	57.5 = 49.6	
	332 102	
Total Service Loud:	1 11.	
$\Delta T = \frac{M_{\rm W}L^2}{C_1 I_X}$ $C_1 = 158$ For (	acting point loads	
AT = (487, 14 k. F+) (56.0167++)2	Limit = 1/246 = (56.0167 FA)(12/0/fa)	
(158)(3616104)	240	
At= 2.68 in < 2.80 in	= 2,80 in	
Snow Deflection	ese versió fres per eserv	
$\Delta s = \frac{5 \text{ Ws L}^4}{2}$	Ws = 5 x Tribytary Width	
384EIX As = 5(441,37 WA)(56.01 Ft) 4	45 = (28,98 psf) (15,23 ft) W5 = 441, 37 16/ft	
384 (29×106 psi) (3610:04)		
× 1728 in3	Limit= 1/360 or 1" = 156.0157)(12m/st) - 1	9:4
As = 0.93 in	Limit = lin	
	F144/1 - 1/14	
0.93 in < 1 in /		

2/2 => One girder has Tributary Width = 21.72 ft
Ws = (28.98psf)(21.72 ft)
Ws = 629.95 15/ft  $\Delta s = \frac{5(629.45 \, \text{lb/f+})(56.01 \, \text{f+})^4}{384(29 \times 10^6 \, \text{ps.})(3610 \, \text{in}^4)} \times \frac{1728 \, \text{in}^3}{\text{f+}^3}$ As = 1.3 in 1.3in & 1in ... Girder with Tributary Width = 21.72ft => W30×108 Due to satisfaction of FLB, WLB, Total Service Load, Snow Deflection: All Other Girder Size = W30 x 90

# Appendix B.9: Baseplate Design

C2 and C5: W8x31 L= Pv = (Proviously Calculated	Pa) + (Column Weight) (Column	na Leneth)
Pu = 48.35 k + 1.2(3110). Pu = 48.59 k	f+)(6.33f+)(Wiocosb)	Mu= 13.3 k . f+ (Risa Analysis)
$A_1 = (8in)(8in) = 64in^2$ $\sqrt{\frac{A_1}{A_1}} = \sqrt{\frac{576in^2}{64in^2}} = 3 \ge 3$	$x^{(2in/p_+)}(2F+x 2^{(n/p_+)}=576$ $\Leftarrow$ bed (A <sub>1</sub> min) 2	in "
$\int \frac{A_L}{A_1} = 2$		
A1 = PM PE (0.85Fe) JAVA, = (0. A1 = 11.0 in2	48.59 k .55)(0.85)(4ks.)(2)	
A, min = 64:n2 -> A = 64:n2		
A = 0.95d - 0.8bf - 0.9	15 (8in) - 6.8 (8in) = 0.6 i	n -
N = JA: + D = J64 +	0.6in = 8.6in	
B = 810 = 79in B = 810 = 79in	. I in	
φερρ = φε 0.85 f'e A, JAYA be Pρ = (0.65)0.85 (4ksi)(9in φερρ = 358.02k > 48.59)	* 9in)(Z)	
$M = \frac{N - 0.95d}{2} = \frac{9in}{2}$	-0.95(8in) = 0.7in	
$h = \frac{B - 0.8b\varepsilon}{2} = \frac{gi_0 - gi_0}{2}$	0.8(8in) = 1.3in	
$V_1 = \frac{\sqrt{4pt}}{h} = \frac{\sqrt{(8in)(8in)}}{h} = \frac{1}{\sqrt{(8in)(8in)}}$		
L= 7.0in (largest of		. 30
tree = g 2Pu = (2.0).		. 5014
A36 Baseplate = 9	in × 9in	

	Appendix B.9	
CZ and CG: W8×31 L=14.26ft  Pu = 48.35kc + 1.2(31 12/ft)(14.26ft)(14.26ft)  Pu : 48.88k  => Since Pu is similar to CI and CS Pu	Mu= 18.6 k. ft (Risa Analysis)	
48.88k & 48.59k  [A36 Steel Beseplate = 9in × 9in]  C3 and C7: W8×31 L= 22.20ft		
Pu= 48.35 k + 1.2 (3116/4+) (22.26f+) (16/100000) Pu= 49.18 k => Since Pu is similar to C1 and C5 Pu 49.18 k 2 48.59 k  A36 Steel Baseplate = 9in x 9in	Mu=18.8K-F+ (Risq Analysis)	
C4 and C8: W8x31 L= 27.10f+ Pu = 48.35k + 1.2(3/16/f+)(27.10f+)(K/100016) Pu = 49.36k	Mu = 10.3k.ft (Risa Analysis)	
Az = 576 in 2 (2f+ x2f+) A1 = (8in)(8in) = 64 in 2		
$A_{i} = \frac{P_{u}}{\phi_{c}(0.85F'c)\sqrt{A_{c}/A_{i}}} = \frac{49.36k}{(0.65)(0.75)(4k5.)(2)}$ $A_{i} = 11.17in^{2}$ $A_{i} = 64.0in^{2}$ $= 7 A_{i} = 64.0in^{2}$		
Δ = 0.95d - 0.86f = 6.95(8.00in) - (0.8)(8.00in)	_ 0.60 in	
$N = \sqrt{A_1} + \Delta = \sqrt{64.0 \text{ in}^2} + 0.60 \text{ in} = 8.60 \text{ in}$ $N = 9 \text{ in}$ $B = 41/n = 64.0 \text{ in}^2 7_{9 \text{ in}} = 7.11 \text{ in}$ $B = 8 \text{ in} = > 9 \text{ in}$	Φερο = Φεδ 85 f'e Aι JAZA, Φερο = (0.65)(0.85)(4165)/910 900/2) Φερο = 358.02W > 49.36 kV	
$M = \frac{N - 0.95d}{2} = \frac{9in - 0.95(8.00in)}{2} = 6.70in$ $N = \frac{B - 0.8bs}{2} = \frac{9in - 0.8(8.00in)}{2} = 1.30in$		
$n = \frac{8 - 0.8bF}{2} = \frac{9in - 0.8(8.00in)}{2} = 1.30in$ $n' = \frac{\sqrt{dbr}}{4} = \frac{\sqrt{(8.00in)(8in)}}{4} = 2.0 in$ $\ell = 2.0in$		
$treq = 1 \sqrt{\frac{2P_q}{0.9F_{yBN}}} = (2.00 \text{ in}) \sqrt{\frac{2(49.36\text{k})}{0.9(36\text{k} \div)(9\text{in})(9\text{in})}} = 0$	.39in	
A36 Steel Baseplate = 9in x 9in		

	Appendix B.9	3/2
Moment - Resisting Thickness: E = Mu = 18.82. ft (1210/ft) = 4.57in 49.36k		
$f = -\frac{Pu}{A} \pm \frac{Puec}{\pm} = -\frac{49.36k}{(9in)(9in)} \pm \frac{(49.36k)}{412}$ $f = -0.6(ks) \pm 1.86ksi = 1.25ksi$ $-2.47ksi$	(4.57in)(4.5in) (9in)(9in)3	
0.72" 7.565" 0.72"		
$N = 9^{n-1}$ 1.25ks: $N = 9^{n-1}$ $-2.77ks: -2.47ks:$ $M_{11} = (2.17ks:)(0.72i_{11})(0.72i_{22}) + (2.47ks: -2.17ks:)(0.72i_{22})$	1.72: \\\\ 43 × 0.72: \)	
$M_{\rm W} = 0.67k \cdot in$ $t \ge \sqrt{\frac{6M_{\rm W}}{\phi_{\rm b} F_{\rm b}}} = \sqrt{\frac{6(6.67k \cdot in)}{(0.9)(36k \cdot in)}}$ $t \ge 0.35in$		
Average $F_p = -\frac{2.47 \text{ks}}{1.25 \text{ks}}$ Avg. $F_p = -0.6 \text{lks}$ ;		
$M_u = f_F \cap (N_2) = 0.61 k_B : (1.3 in)(1.3 in/2)$ $M_u = 0.52 k_B < 0.67 k_B = 0.67 k_B$		
(All Baseplates will have a thickness (t) =	0.5 in	
4		
		1

				Appendix B.9	4/
	A36 5	teel Baseplat	e		
	Column Number	BN	trey		
	12345678	B N Gin Gin Gin Gin Gin Gin Gin Gin	0.5 in 0.5 in 0.5 in 0.5 in 0.5 in 0.5 in 0.5 in		
	2	9in 9in	0.5in		
	u o	9in 9in	0.5 (0)		
	5	gin gin	0.5 in		
1	6	gin gin	0.5 10		
	7	9in 9in	0.5in		
	8	9in 9in	0.5in		
			- With - Art Cardi		
				0,00	
- 1					
1					
	,				
1					

### Appendix B.10: Recalculation of Seismic Load

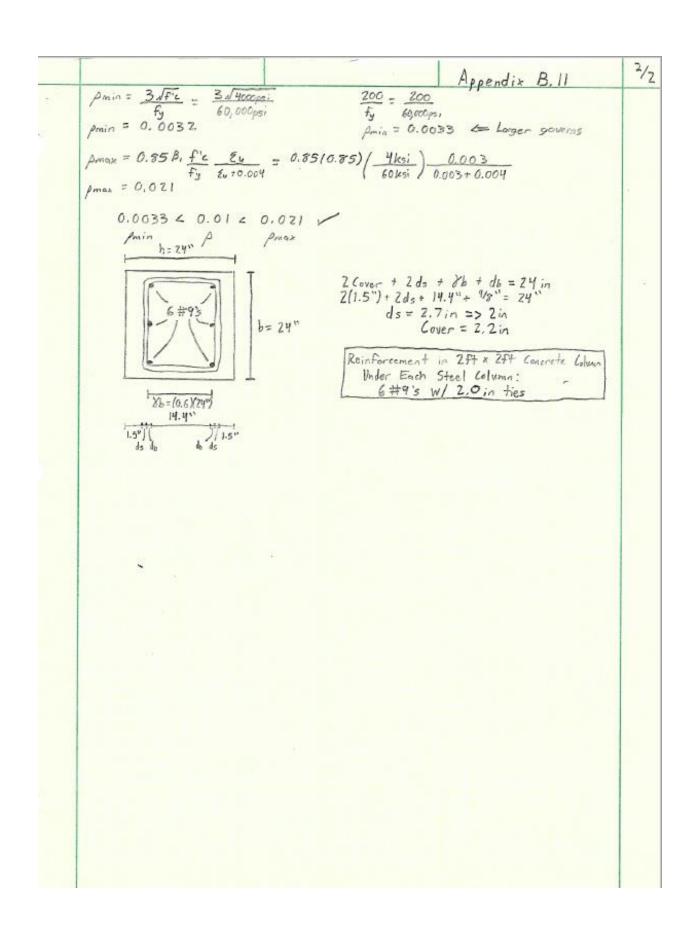
```
Recalculation of Seismic Load Appendix B. 10
                                                                                              1/2
 Gatewood Parking Garage
Recalculation of Science Load
Check to see if designed structure weight & 25% of current structure weight
     Area of Top Floor of Garage = (Length) (Width) (Thickness)
                                   = (268++)(113++)(4++)
                                   = 121,136 ft3
     Weight of Top Floor of Garage = (Neight of Concrete) (Area)
                                    = (150 16/4+3) (121, 136 ft3) (K/100016)
                                    = 18,170 kips
     Weight of Selected Beams = 4[(5516/4+)(45.694+)]+ 2[(5516/4+)(28.21++)]+
                                  10[(68 WA)(45.69 PA)] + 5[(68 W/F+)(28.21 F+)]
    Weight of Selected Girders = 8[(90 1/4+)(56.0167 Ft)]
                                  = 40,332.0216
     Weight of Selected Columns = 31 1/4 (216.33ft)+ 2(14.26Ft)+ 2(22.20ft)+
                                            2(27.10++))
                                  = 4,333.18 lb
    Combined Weight of Selected Members = [53, 815.51b + 40,332.021b + 4,333.1814] (4) Members = [53, 815.51b + 40,332.021b + 4,333.1814]
                                        = 98.48 Kips
           98.48 kips $ 0.25 (18,170 kips)
98.48 kips $ 4,542.5 kips \ (Section 15.3.1)
Therefore, horizontal design force (Fp):
     Fp = 0.4 ap Sos Wp (1+2 = ) (Section 13.3.1)
     Sos = 0.192 = previously calculated (Section 11.4.1) - Spectral Acceleration
     ap = 1.0 (Table 15.1 - Other Rigid Components) - Component Amplification Factor

Ip = 1.0 (Section 13.1.3) - Component Importance Factor
  Component
 Operating Weight
                                Solar Panel Area Solar Panel Weight
     Wp = 16.77 psf
     Ro = 2.5 (Table 13.5-1) - Component Response Medification Factor
     i = 60ft - Height of Attachment Roof
     h = 10f+ 30,77f+ = 20.384f+ + 60f+ = 80.384f+ - Average Roof Height of Structure With Respect
     h = 80.384ft
                                                                    to the Base
     Fp = 0.4(1.0)(0.192)(16.77psf) (1+ 2 60ft (2.5/1.0)
    Fp = 1,28 psf
Lower Limit: 0.3505 IpWp = 0.3(0.192)(1.0)(16.77 +54) = 0.97 psf
Upper Limit: 1.650s IAWp= 1.6(0.192)(1.0)(16.77psf)= 5.15psf
  0.97psf = 1.28psf = 5.15 psf
```

	Appendix B.10	2
Vertical science force (FV):		
Fv=0.2505Wp=0.2(0.192)(16.77psf) [v=0.64psf]		
Horizontal Seismic Load (Fp) = 1.28psf Vertical Seismic Load (Fv) = 0.64psf		
	J	

### **Appendix B.11: Concrete Reinforcement**

```
Gateway Parking Garage Concrete Reinforcement
                                                                       Appendix B.11
Reinforcement in 2ft x 2ft Concrete Columns
Columns (1 and (5:
    Pu = 13.15k
    Pu = 13.15k (Axial Force acting on concrete column) } Risq Analysis
Mu = 32.857 k. Ft (Moment acting on concrete column) } Risq Analysis
  K_n = \frac{P_V}{\Phi f' c A_g} = \frac{13.15 k}{(0.9)(4 kei)(24 in \times 24 in)} = 0.006
R_n = \frac{M_V}{\Phi f' c A_g h} = \frac{32.857 k \cdot f +}{(0.9)(4 kei)(24 in \times 24 in)(2 f +)} = 0.608
Columns CZ and C6:
     Pu = 26.30k
     M== 18.568k.f+
  Kn = 26,30k = 0.013
  Rn = 18.568 k.ft
         10.9)(4ksi)(24in+24in)(2ft) = 0.004
Columns 63 and 67.
     Pu= 37.51k
     Mu= 18,794 6. ft
  K_n = \frac{37.51 \, \text{k}}{(0.9)(4 \text{ksi})(24 \text{in} - 24 \text{in})} = 0.018
  Rn = 18,794 k - F1
(0.9)(4k5)/(24in x 24in)(2At) = 0.005
Columns C4 and C8:
     Pu = 24.36 k
     My = 10. 299 k . Fx
  Kn = 74.36 k
(0.9)(4 ks) (24 in = 24 in) = 0.012
  Rn = 10.299 K.ft
         (0.9)(4ks)(21in+24in)(2+4) = 0.002
For All Columns:
    pg < 0.01 => pg = 0.01 (min. volue)
As = pg Ag
As = (0.01)(24in × 24in)
    As = 5.76 in 2
    N("/4 db2) = As
6("/4 db2) = 5.76 in 2
         db=1.1in => 6 井9's (As=5.96in2)
```



# **APPENDIX C: GREEN ROOF CALCULATIONS**

### **Appendix C.1: Live, Dead, Snow and Rain Load Calculations**

Live Loads (per floor) ASCE 7-10 chapter A
Root = 100 pst root gordens or 12 pst (EN Global, Green roof system)
1st, 2nd, and 3d = stack rooms = 150 pst
reading rooms = 60 psf
Corridors = 80 psf (fint Floor= 100 psf)
stans and exit ways = 100 pst
meeting reams = 50 pst
Live loads will vary per each floor on library regarding
the mage of each floor.
A live load of so put its assumed for meeting come in library or as we call them "tech suites".
Dead Loads
· For 6" soil appth . (How. you)
D= 35 pst -> captured and retained water part of load
. Green not dead look will be added to additional clear loads
obtained from Excel spreadiheat collistions for effective
weight of building
. Other dead loads will be neglicted
· Flow dood load (pst): (past) = 91 pst
· Floor dead load (pst): (for 1t, 2nd and 3th floor)
- Dome size = 19in
- Done Depth (m) = 10 in \ 103 pst.
- slab thickness = Ain
Lo Table H-1 CRSI Delign Handbook

	p1 = 0.7 Ce Ct Is p5 pf = Inaw load on flot roof
	POSULO Factor: (CE) -> Toble 7-2
	Viture Roughness B: Whom and suburbon areas (Figure 26.7)
	- Fully Exposed: roots exposed w/ no shelter afterded by terrain
	higher shuthers or terroline
39	7. Ce = 0.9
	ermed Factor = ((+) -> Tuble 7-3
	:. Ct = 1.0
· Ir	pertunia Factor (I): Toble 1.5-1
	Risk Category III
	1. Is = 1.10
· (-)	and snow boods: Ps (Figure 7-1)
	.   P1 = 50 pst
	P4 = 0.7 (0.4)(1.0)(1.10) (50 psf)
	p1 = 34.65   psf = 5
Dave	oads: (FM (Ldoo) Dota sheets)
ron I	(= 32 pif) -> (bs 1-54 Roof Loads to New Controction Da
1.1	SKeet 2,5,2,8)

# **Appendix C.2: Seismic Load Calculations**

SCI	
	seismic load library w/o green root
	Step 1: Rick - Turgeted Hax Consider Earthquete
	Ss: Fig 22-1 -> 18% MG3C 9+6 Edition S1: Fig 22-2 -> 7%
	Step 2: The structure being analyzed 15 exept from seismic
	Step 3: Seismic Design (ategory (sox)
	1. Soil (lambroton Toble 20.3-1 -> Site D (Still soil)
	Lo soil properties are ned known
	2. $S_{DS} = (2/3)(F_Q)(S_S)$
	Table 11.4.1-> fa = 1.6 Sms
	Sus = (2/3)(1.6)(0.18) => Sus = 0.192
	$S_{01} = \left(\frac{2}{3}\right) \left(\frac{F_{v}}{S_{1}}\right) \left(\frac{S_{1}}{S_{1}}\right)$
	Tobe 11,4-2 -> Fu = 2.4
	$Sb1 = (1/3)(0.07)(2.4) \Rightarrow Sb1 = 0.112$
	3. Risk (ategory III -> structures w/ large number of persons
	From Toble 11.6-1 ->   SDC = B ]
	and Tuble 14 6-2

Sc II	
	Step 4: Determine Analysis Pracedure
	Determining Period T of a structure (T= Ta)
	has structural height (vertical distance from base to highest level of the serious
	Lo confet moment resulting from force recenting system)
	hn = From grand Flow = (14-778' x 4) + (101/2") =>   nn = 59.5 ft
	Ct: 0016 14.656, 0.875.
	X= 0.9
	$Ta = (0.016) (59.5)^{3}$
	Detuminas To
	Lo Ts = 0.5
	Step 5: Determine R. Response Modification coefficient
	Toble 12.2-1
	1 7. ordinary reinficod conceta nument frame
	↑ <del>+ 3</del>
	Step 6: Seinnic Impertence Factor (I.)
	Risk Calegory III
	LD [Ie = 1,25]
	No.

here it changes for Green Roof Design  account for 100% of weight of landscapind and other motoriols
Step 7: Seismic Base Shear (V) -> W/o Green Roof Weight.
V= C= W ; W= Weight of structure
Co: science response coefficiens
include in reamic weight = where Mot rout snow loads are greater than 3 upit
20 % of the days snow load, regardless root slope
$\frac{C_{5}}{\left(\frac{R}{I_e}\right)} \Rightarrow C_{5} = \frac{0.192}{\left(\frac{3}{1.25}\right)} \Rightarrow C_{5} = 0.08$
Cs shall not be less than: Cs = 0.044 sou Te ≥ 0.01
$C_{S} = \frac{S_{DL}}{T\left(\frac{R}{L}\right)}  for  T \leq T_{L}$
16)
$C_{S} = \frac{Sb_{1}T_{L}}{T^{2}\left(\frac{R}{Te}\right)} + c_{Y} = T > T_{L}$
True 6 -> Figure 22-12 Transition Period
W= 20% of snow lood + effective weight of library (excel spreadment)
W= 6.73 psf + 13,629.71 Kips
W= 6.93 (A811 x 92.87) + 13,629 71 Kips
W= 114.559 kips + 13,629.71 kir => W= 13,744.269 kips

2 C III	
	Weight of structure: (from commentary (.12,72)
	e calculations done in excel spreadsheet
	· Ellective seismic weight only portion of mass tred to
	the structure. Hence, live loads such as Loose furniture, Loose equip, and human
	occupants are not included.
	* (extram types of the loads such as storage loads are included
	· Other contributing to effective weight are:
	- All permanent equip. Can conditioners, elevator equip, mechanical systems)
	- 20% of man load (Pr > 30 psf)
	- weight of londinging and similar meterials.
	- Partitions to be exected as reavonged as specified in letter 4.3.2
*	Step 8: Distribute V, over height et structure
	Fx = Cvx V
	Wi and whe = portion of total effective
P	with Cox= Wx hx sellmic weight assigned to level or x
/	S Wihi i a x
-	Kill he and he = height from bose to level (or x
	Assume k= 2 as 0.5 sec < Ta = 2.5 sec
	CVX = (Wa-root ha-root)2
	(MO-14 x pt - 11) + (MT-24 x pm-24) + (M3-24x px-34) + (Mm mt, pm m)
	810 CVX (165, 242 15)2
	70 00 (82.096.26 K H)2+ (B1,869 K H)2+ (188,481.55 KH)2+ (165,242.15)2

C	
	Stop 9: Rodundary lactor (p)  [p=1.0] -> SDC A, B, or C
	Step 10. Jellanic Load Effects E and Em  Enomina Evinant SDS = 0.192 -> Step 3  E = PQE ± 0.250s D D= dead load QE= Fx
	$E = P Q_E \pm 0.2 S_{DS} D$ $E = (1.0)( ) + 0.2(0.172)($ $E = (1.0)( ) + 0.2(0.172)($
	Reput from Hep 7: ausuming Green Roof system
	V= (s W => ) (s=0.08) W= 13,744 27 K'ps + 375.66 K => W= 14,119.93 Kips
	V= 1,129.59 kip + 114.559 kp  [V= 1,244.15 kip ]  Green Root weight doesn't account for 25% or more of whole
	Stop 8: Distribute V, over height of structure

## **Appendix C.3: Wind Load Calculations**

MI		
	Wind load Analysis (see also ch. 29.5 ASCE =-10)	
	Step 2: Wind Speed	
	Lo JBC Figure 1609B or ASCF7-10 Figure 26.5-18	
	V= 134 mph) (Check MIBC 9th Edition)	
	Lo stare code governs this volve	
	Stop 3: Mean Rand Height	
	- Some as height above grand	
	Stor4. Exposure (otegory -> may change my green roof	
	Exposure B	
	Lo check commentery.	
	Step 5: Enclarus clarification	
	Lo enclosed building	
	Step 6: Wind Directionality (kd), Toposrophie Tactor (kgt), but Elliot (b)	
	Kd = 0.85 -> always for buildings.	
	KAL = 1.0 -> NO topographic effects on building	
	G= 085 -> Low rise building (rigid)	
	Step 7: Wind Deign MWFRS	
	· Methoid 1 -> Chapter 27 Par 1	
	Lo to analyze HWFRS.	
	Step 8: Determing Wind Design Hethol for C&C	
	· Hethod 3 D Chapter 30 Por 1	

N.M.	wind look shall not be less than 16 pit multiplied by the wall area of the building and 8 pit multiplied by the root area of the building
	** MWFRC Wind loads  • Velocity Pressure (extracent  12 = 0.00256 K2 K2+ K2 V2 (E9 273-2)
	For Expose B Building  Lo height above growd = [kg = 0.85]
	92= 0.00256 (0.85)(1.0) (0.85)(134 mph) <sup>2</sup> [72= 33.21 pst] [9h= 33.21 pst] → some as  12 b/c mean  height is the some
	• External pressure (officient (CP) - Flat roof (L= 16714, B= 1031+, h= 59.51+)
	-Wall prosino (afferent (cp) Figur 27-4-1 . Windwood (cp = 0.8) -) for 4.
	· leeward woll [cp= - 0.38] -> Par gh
	- PLANT PIEMER COOFFICENTS, (CP)
	P= 96CP - 9. (GCP;) [pst] buildings.
	- From Table 26.9-1 La GCPi= +0.18, -0.18 -s enclosed building.
	bust Effect Factor (6)  bust Effect Factor (6)  bust Effect Factor (6)  bust Effect Factor (6)

MIL	·J
	Wind calculations done at top of building assuming In= 92
	Fa wood wolls:
	p= (33.21 ps+)(0.85)(0.8) - (33.21 psF)(0.18)
	[P= 16.61 pst] [P= 28.56 pst] = assuming (-cpi to
	For Lesward wealts
	p= (33.21 p+ ) (0.85) (-0.38) - (33.21 p+) (0.18)
	1P= -16.70 P+ 1 P= -4.75 PSF
	Fer cide walls.
	p= (88.21ps) (0.85) (-0.7) - (33.21pst) (0.18)
	p= -25.73 psf   p= -13.78 esf
	C&C Wmol Lood (shall not be 1811 than 16 pst)
	o velocity Pressure (definion (kr)
	Lp From Toldy 30.3-1 [k2-0.85]
	o wind pressive
	p = gh [ (6Cp) - (6Cp))
	GCPI = 0.18, -0.18 -> TOOK 26.11-1
	· External Adyun continuent (GCP)
	Walls -> Figure 30.4-1 as not of least household Imagin = 9.87f
	(A) and (S) → (-Cp = +0.8)
	Good 6) effective who ever a toute => [GCP = 0.7]
	Roof -> Tigure 30-4-2
	a= 10 % of kent however dimension = 9.87 ft
	3) effective wind area 1 40+12 > 6Cp = -1.1
	(2) elective word area = 150+12->[GCp=-1.1]
	2) effective wind area = 150 ft2 -> [GCP = -1.1]

MR	
	(1),(2) &(3) effective wind one = 1000ft2 -> [GCp = 0.2]
	Design wind Pressives
	P= 9h [ (6Cp) - (6Cpi)]
	For Floor poor
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	For individual zones (Figure 30.4-2A)
	Zore 3) P= 31.26 psf [ (-1.6) - (0.8)] = [-40.01 psf
	72 P= 31.26 psf [(-1.1) - (0.1)] = [-40.01 pf]
	Zone () p= 31,26 psf [(=09-(018)]=[-83,76 psf]
	GCp for Zone (2) and (3) are the same as percepet
	15 higher then 3 ft.
	Zone (3) and (2) P= 31.26 psf [(-1.1) - (-0.12)] => [P= -28.75 psf]
	Zone 1) p = 31 26 psf [(-0.9) - (-0.12)] => [p= -22.50 psf]
	for walls
	Zone (4 ond) p= 31.26 p+ [ (0.8) - (0 18)] => [p= -30.63 p+ ]
	Love (a) and (5) => p= 31.26 pif [ (0.7) - (0.18)] => [p= 16.26 pif
	P= 31.26 psf [(0.7) - (-0.18)] => [p= 27.51 psf]
	p = 31.21 psf [(0.8) - (-0.18)] => [p=-19.38 psf]

Wind Load Distribution	
East Mes + 172'0"	
82.83 36.44 (0.876*	Poropel 1 10.5" 2 Root
36.177	
	14.66′
24.30	3rd Floor
33.45	PLCE
31.85 b	2nd floor
3/126	[4,66*
29.86	J N <sup>2</sup> Floor
26.10	14 66
2416	PROVIND
Chicult Other ve*	
CALCULATONS:	/ main = 222h)
Rat: 82.83 pit (172 ft x 0.875 ft ) + 38.44	2
	2
Rat: 82.83 pit (172 ft x 0.875 ft ) + 36.44	Rout level = 57.93 K
Rat: 82.83 pit (172 ft x 0.875 ft ) + 38.44	Rout level = 57.93 K
Rat: 82.83 pit (172 ft x 0.875 ft ) + 36.44	Rout level = 57.93 K
Raf: 82.83 pif (172 ft x 0.875 ft) + 36.44 Poof lovel = 12.47 x 1ps + 45.46 kip => 1 34 Place: 34.71 psf (172 ft x 14.66) =>	
Rat: 82.83 pit (172 ft x 0.875 ft ) + 36.44	
Raf: 82.83 psf (172 ft x 0.875 ft) + 36.44 Poof 18001 = 12.47 x 1ps + 45.46 k/p =>  3 <sup>12</sup> Place: 34.71 psf (172 ft x 14.661) =>  2 <sup>12</sup> Flace: 32.45 psf (172 ft x 14.661) =>	
ROOF 10001 = 12.47 x 1ps + 45.46 k/p => 1  300 Place: 34.71 psf (172 ft x 14.661) =>  200 Place: 32.45 psf (172 ft x 14.661) =>  144 Flore: 2016 psf (172 ft x 7.67 ft) +29.8	
Raf: 82.83 psf (172 ft x 0.875 ft) + 36.44 Poof 18001 = 12.47 x 1ps + 45.46 k/p =>  3 <sup>12</sup> Place: 34.71 psf (172 ft x 14.661) =>  2 <sup>12</sup> Flace: 32.45 psf (172 ft x 14.661) =>	
ROOF 10001 = 12.47 x 1ps + 45.46 k/p => 1  300 Place: 34.71 psf (172 ft x 14.661) =>  200 Place: 32.45 psf (172 ft x 14.661) =>  144 Flore: 2016 psf (172 ft x 7.67 ft) +29.8	2001 level = 57.93 & ]  2001 level = 57.93 & ]  2001 level = 87.52 kips ]  2004 Floor = 87.52 kips ]  10126 (172 le x 6.99 ft)  2

89	me shear(A):		
	Estory Forces => V	1= 57 93x + 87.52 K	181.82 K + 7479k
	4	+ 36 76 K	
	V= 338.82 Kips		
CN	porturing Homent (H	; (0	
	MG= (57.93 K x 58.634+		+ (81.82 k x 29.31 ft)
	+ ( 71.79 K X H.	66/4)	
7		7	
	Mo= 10,739,26 K. H		
		1	
	Overturning will not		V
0.5	the extra load that	the system impos	e on the building
0.5	2	the system impos	e on the building
0.5	the extra load that	the system imposed to resist the over	e on the building turning moment.
0.5	the extra load that	the system imposed to resist the over	e on the building turning moment.
0.5	the extra load that going to be used	the system imposed to resist the over	turning moment.
0.5	the extra load that going to be used	the system imposed to resist the over	e on the building turning moment.
0.5	the extra load that going to be used  57.93K  87.52K	the system imposed to resist the over	turning moment.
0.5	the extra load that going to be used  57.93K  87.52K	the system imposed to resist the over	turning moment.
0.5	the extra load that going to be used  57.93K  87.52K	the system imposed to resist the over	turning moment.  102.  14.66.
0.5	the extra load that going to be used  57.93K  87.52K	the system imposed to resist the over	turning moment.
0.5	going to be used  57.93K  87.52K  81.82K	the system impose to resist the over  Printil Root  200	turning moment.  102.  14.66.

MAIG	
	Wind Load Distribution
	(ps) Nov th - South Direction
	31.67 0
	3070 6
	29.95
	28 59
	26 49 <b>b</b>
	2439
	2/1 3/1
	2439 D
	CALCULATIONS:
	Roct : 82.8> pst (92.87 x 0.875) + 31.67 pst +3090 (92.678 x 7.33 ft)
	Roof level = 6.73 kips + 21.30 kips -> [Roof = 28.03 kips]
	3rd Floor : 29 95 pot (92.87 × 14.66") -> [3rd Floor = 40.78 kips]
	2nd Floor: 27.69 psf (92.871 x 14.661) => 2nd Floor= 37.70 Kips
	15th Flow , 2439 pot (9287' x 7.67') + 2439 + 26.40 (9287' x 6.90')
	15t Floor = 13.37 kips + 16.51 kips => [1tt Floor = 83.88 kips]
	Crownol Flow 221.39 put (92.82 x 7.33") => [Grounol Flow = 16.60 Kips]

XIW			
	Bajo Theor (V):		
	Estery Perces => V=		1 + 37,30 % + 35,80 K
	V= 156.99 KIPE	+ 16 60 K	
	Overturning Homens (H		v 43 Maft ) + ( 32.70KX 29.311t)
	+ (33 80K × 14 66		
	Ma= 5,036.99 K. F4	]	
	· Overturning moment in	North-south	direction is almost
	half of East-Wost		
		PARAPET	
	28.00 K	200 F	10.1/2.1/2
			14.66
	40.38×	3.60	/
			14:64
	33 dok b	2 160	/
			14 66'
	33.854	42	/
			141.66
	6,60 <sup>×</sup>	₩R.	

## **Appendix C.4: Factored Design Load (Pu) Calculations**

PuI	
	Column load Calculations
	Load combinations are the same as for stabs.
	© ©
	25° (B)
	Typical interior section for column
	AT= Tributory Area of column
THE .	Roof Floor:
	Column, B5
	AT = 25 14 × 20 14 => AT = 500 H2 } AT Drop PONO1 = 8.5'x 8.5' = 77,25 ft
	Dead Load:
	*MEP= 5 pst * Green Root = 35 pst -> mag not apply for this section.
	* Two_way dome flab = 91 psf * Ponthouse = 58.37 psf
	* solid head = 71 pst
	Dead load = (5pit + 35 pit + 91 pit + 58.37 pit + 4.20 pit) x(500 ft2) + (71 pit x 72.25 ft2)
	Dead load = 101.91 Kips
	Live Load: live loads are based on occupancy areas based on the

RI	
	Live load = 20 psf for entire roof  Live load = (20 psf) (500 ft2)/1000 => [Live load = 10 kips]  Show load = (34.65 psf x 500 ft2) => [Snow load = 17.33 kips]
	Load combinations (olum . 85  (1) Pu, = 1.40 => Pu= 1.4 (101.91 xips) => [Pu= 142.67 kips]
	② $Pu_2 = 1.2D + 1.6L + 655 = 9$ $Pu_2 = 1.2(101.91 \text{ K}) + 1.6(10) + 0.5(13.33 \text{ K})$ $Pu_2 = 146.96 \text{ K}$
	(3) $Pa_3 = 1.2D + 1.65 + L = Pa_3 = 1.2(101.91 k) + 1.6(17.23 k) + 10 k$ $Pa_3 = 160.02 \text{ Kips}$
	In this case column BS, B6, C5 and C6 will have the same as all their tributary areas, and loads are exactly the same, only for the Roof Floor.

PUILL	
	3rd Floor
	Column, B5 -> AT = 500 H2   AT Drop Panel = 72,25 F42
	Dead load:
	* Root combined = 193.59 pst + MEP = 5 pst
	* Rock Solid head = 71 psf * Two way Dome Slab = 403 psf
	* 2019 years 350 flan = 20 bit * Monte / bar prom / (aprimo = 102.25 bit
	Dead load = (193.57 pit + 5 pit + 103 pit + 105.52 pit) (500 ft2)
	+ (71 psf +59 psf) (72.75 ft2)
	Dead load = 213.00 Kips
	Live toad:
	* Live locals acting on tributory crea of column are.
	· corridor · mechanical room · meeting room.
	Live local = (80 psf) x (20' x 10') + (100 psf) x (20' x 12.5') + (40 psf) (20' x25)
	Live load = 16,000 lbs + 25000 lbs + 2000 lbs =5 [LL = 43 xips]
	Load Combination Colomn BS
	1) Pun = 1.40 => Pun = 1.4(213 x) => [Pun = 2982 Kips.]
	(2) Puz = 1.20 +1.62 + 0.55 => Puz = 1.2(213 K)+ 1.6(45K)+0.5(17 550)
	B) Pas= 1.20+ 1.65 + L=5 Pas= 1.2(215x) + 1.6(1733x) + 43x

(0)	ima C5
6	Dead load is the same
·	Live load counts of:
	ecornida . memorial room . meeting room.
1	Ive Load = (80 pit) (10'x275) + (80 pit) (10'x10") + (40pit) (2-5'x20)
	+ (100 by) (15 21 × 10.)
1	Live load = 40.5 kips
100	1 combination culum cs
	) Pu,= 1.40 => \Pu, = 298.2 mp
(2)	PMz = 329.07 KIP
(3)	) PUS = 323.83 KIPE
Co	Juma B6 and Column C6
	· Dead load is the some
	· Live lood consists of:
	e meeting room
	Live load = (40 pit) (500 ft2) => [LL = 20 Kipi]
Loo	a combinations Column 86 and 66
0 F	01 = 1.40 => \Pu1 = 298.2 kip)
2	Pur = 296.27 Kips
3	Pres = 308, 33 x 1 p)

PUIL	
	2nd +1001
	(alumn B5 -> [A7 = SOOFE ] A7 Droppose = 72 25Fez
	Deag Oag :
	* Reaf and 3rd floor combined = 407.09 pof + HEP = spot
	* Real and 3rd floor solid head = 130 pit * Two-way dome ilob = 102 pit
	* Salid hard = 59 pst + world / columns = 113.68 psf
	Dead load = (407.09 pit + 5 pit +105 pit + 11368 pit) (500ft2) + (130 pit +59pit) (72.25 ft2)
	Dead [gad = 328.04 kips]
	Live 1001d:
	* Live load acting on AT of column BS
	* Corridor * mechanical rum * meeting room.
	Live (and = (80 pst) x (20'x10') + (101 pst)(12.51 x10') + (10'x12.5')(40pst)
	+ (40 psf)(zo' x25)
	Live 1600 = 16,000 K + 12500 K + 5000 K + 224016
	LNO 1000 = 35.74 K
	Load combinations Column B5
	() Pu, = 1.40 => Pu, = 1.4 (828.04 K) =>   Pu, = 459.26 Kips)
	(2) Puz = 1.20 + 1.61+0.51 => Puz = 1.2(32104 R) + 1.6(35.44 K) + 0.5(17 33 K)
	Puz = 459,50 Kipi)
	(3) Pas = 1.20 + 1.65 + 1 => Pas = 1.2(32) 09x) + 1.6(17336) + 35.748

Pusi	
	(alumn C5
	Dead load 11 the care as the column 35
	· Live loods combus of:
	· (orrider - machas room.
	Time 1000 = (80 bit )(50 x10,) + (80 bit)(10.x15.2,) + (40 bit)(10.x15.2,)+(40t)
	(20° ×7 5°)
	Live 1000 = 33 Kips
	Land combinations Calume C5
	1) Par = 140 => Par = 14 (328.04 x) =>   Par = 431,26 x
	(2) Puz = 120 + 166 + 0.55 => \Puz= 455    KIPI
	3 Pus = 1.20 + 1.65 + L -> [Pus = 454,38 kip)
	Column B6  Live 1000 = (40 pst) (500 Ft2) = [20 kips]
	Load combination Colonia B6
	1) Pu = 14p => [Pu = 459.26 kip.]
	2) Puz = 1.20 + 1.61 + 0.53 => Puz = 434,31 K
	(3) Plus = 1.20 + 1.63 + k => Plus = 441.38 K
	Column CE
	Live load = (40 psf) (20 x17.5") + (40 psf) (7.5" 15") + (sopt) (5'x7.5")
	Live 10ad = 20.38 K
	Load combination Column C6
	1 Plus 1.40 => (AL = 459.26K)
	2) Puz = 1,20+1.6L+4.53 +5 (Puz = 434.92 x)
	(3) Pus = 1.20 +165 + L => Puz = 441.76x

Pu VII	
	1st Flow
	(0/0m n B5,C5 AT = 500 ft2 AT PANEL = 72.25 ft2
	& Roof, 3rd and 2nd floor combined = 628.77 pd * MEP = 5 plf
	* Runf, 3151 and 250 flow solid head = 189 pif * Domo slob = 103 pif
	* CORD head = 59 pst * WOIL / COLYANI = 121.94 pst
	Dead load = (628 97 psf + 5 psf + 102 psf + 121-94 psf) (500 ft2) +
	(189 pst + 59 pst) (72.25 ft=)
	Dead 1000 = 447.27 KIPI
	Live load:
	"Live local acting on column BS and as contit of:
	. library stucks
	LIVE LOUD = (500H2) ( 150 PS) => [LL= 75 KIP]
	load combinations Column B5 and C5
	1) Pui = 1.40 => Pui = 1.4 (447.27 K)=>   Pui = 626.18 Kips
	(2) Paz = 7.20+1.61+0.51 => Paz = 665,39 Kips
	(3) Pus = 1.20 + 1.65 + L => Pus = 1.2(447.27+)+(1.6)(14.35)+75K

Pu SIII	
	Column B6 and C6 Live load consist of:  . Isbrary stucks . Weeting room
	Live load = (150 pif) (20' x12.5') + (40 pif) (20 x12.5')  [LL = 47.5 K]
	Dod combination to column 66 and B6  Dec = 1.40 => Pu, = 1.4 (447.27 K) => Pu, = 626.18 K)
(	2) $Pu = 1.20 + 1.61 + 0.55 \Rightarrow Pu = 1.2(449.276) + 1.6(49.56)$ + 0.5(17.236)
(	3) Pus = 1.20 + 1.65 + L => Pus=12(447.2+8) + 1.6(17.25*) + (47.5 K)

Column Dimensions - Axial Load
· An analysis of the strength capacity of interior and edge
columns was developed. All calculations were based on column
dimensions per each floor and reintogred steel bars.
· All calumns are assumed to be circular concrete with spiral reinforcement.
First Floor Internal columns (23"x22") -> (5) in S-14 sheet
Nominal Axial load (opacity:
Pr.max = [As Ig + 0.85 f2 (As+ A)] 0.85
Ag= gross section area (in)
As= Area of steel reinforcement bars (in2)
Jy = Strongth of steel
J'c = strength of concrete
P= axio 0 force of column
Q = 6,75 for spiral columns
(BPn, max = 0.85 to (0.85 pc (As : Ast) + Asy fg)
Rolerence: ACI 318-14
From structural drawings:
8 No. 11 bors -on a 23" x 23" concrete column.
de- diameter of bar = 1.41 in A.t. 1.56 in2
I'c = assuming 5000 psi for columns
fg = 50,000 psi -> assymption
Ag = 23" x 23" => 1 Ag = 529 in2
Art = 8 x 1.56 in2 => [ Art = 12.48 in2 ]

IIXA	
	OPO. MOX = 0.85 (0.75) [0.85 (500 ps;) (529 in2-12 48 in2) + 50,000 psi (12 48 in2)]
	OPn. mox = 1,797.25 kips

## **Appendix C.5: Factored Design Load (Wu) Calculations**

Mul	1.20 + 10000 K/C+ 10000 K/C+ 10000 K/C+ 1
	Load (ombinations
	1. 1.40 2. 1.20 + 1.6L + 0.53 Growing Load Combinations
	1. 1.20 + 1.65 + L 4. 1.20 + 1.00 + L + 0.55 30: 1.20 + 1.65 + 0.50
	5. 1.20 + 1.0E + L + 0.25
	6. 6.90 + 1.00
	1. 0.9 D + 1.0 E
	Load (ambinations (alculations for stabs
	Root: (Gravity Lood Combination only)
	Dead load: Green roof = 35 pst
	Two-way dome slab = 10" +3"slab = 71 psf -> Table 11.1 (PS)
	Penthane and walls / area of roof = 932370.21 lbs/ (172" x 92.87")
	Penthuse = 58.37 ps 1
	MEP = 5 psf (assumption)
	solid hood = (13 in /12 m/te) x150 pcf = 162 pcf
	solid head = (162p+f-91 p+f) x 8.5ft = 603.5 ll/ft
	columns = 4.20 psf.
	h = 25' h = 20'
	4839.25 16/14
(	1) Mu = 1.40 => Wh = 1.4 (35 psf + 5 psf + 62 52 psf + 91 psf) (25") + 1.4  (603.5 26/ft)
	[Wuz= 7.62 K/ft]

```
2.) Ww = 1.2 D + 1.6 L + 0.55
     snow load = 34.65 pst
    Live 10001= 20 pot
    Wu = 1.2 (4839. 25 10/1+ + 603.5 86/1+ )+ 1.6 (20pit x25') + 0.5 (34.45 pot)
      Wu = 6,581.3 lb/1+ + 800 lb/1+ + 43213 lb/1+
      Wu = 7764.43 /4 => Wuz= 7.76 * / P+
   (3.) Wu= 1.20+ 1.65+ L
     Nu = 6531.3 865/ ++ + 1.6 (34.65 p) + (20 p) + x25')
     Wu = 6531.3 lbs/ft + 1386 lbs/ft + 500 lbs/ft
        Wu= 8417.3 lbs/H -> Twu= 8.41 k/ft
   3rd Floor
     Decret locate
                  Roof need lood = 193.57 pot
                  Pust sold head = 71 pst
                  HEP = 5 pst
                   Dome slob = 103 pct
                   30/10 head 31 From = 162 pit - 103 pit = 59 pit
                   moth and partitions = 1996466.34/(172729272)
                                  2 94 pit.
                   columns = 11.52 pst
                                         10,199-25 16/7
(I) Whe 1.40 => Whe 1.41 (193.57 pst + 5 pst + 103 pst + 941 pst + 11 52 pst) (25)
                          + 14 (56 fif + 71 fif) (8.5)
    Wag: 14,248,15 lbs/H + 1511.3 lb/H => Wag = 15.76 ×/ft
```

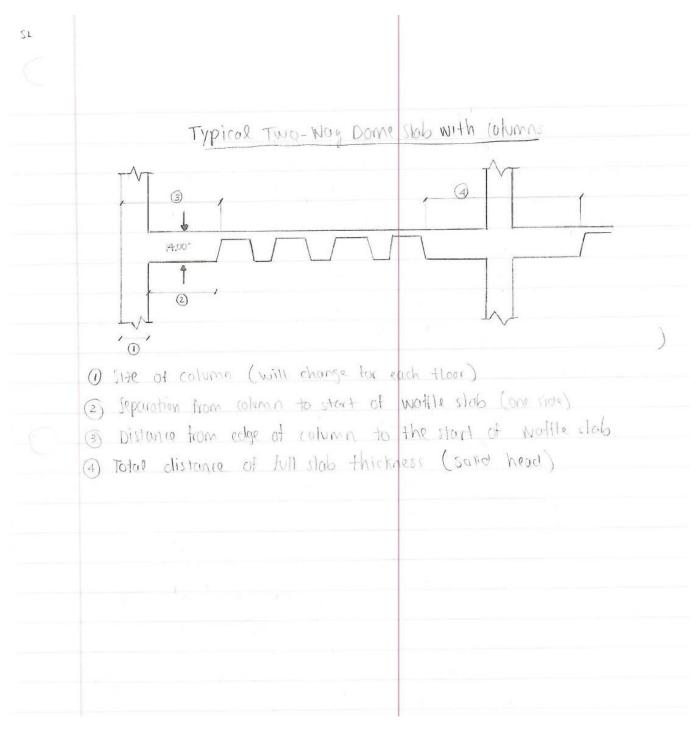
MIII	
(2.)	Wu = 1,20+1.6 L +0.55
	Snow load = 3463 pst
	Ivo 1000 = A 3741.80 Hz + 907 61 Hz - 40 yit -> meeting over
	8. 1752 o file = 150 pst -> librory stocks.
	c. 4299.42 = 50 pst -> office rum
	0. 3124.5 112 = 80 pit -> contider 3rd + coor
	E. 1786.07 1/2 = 100 pst -> mechanical room
	T. 561.0 ft+ + 2 x 281.75 ft2 = 100 pst -> stairs.
	Total Are 11 Few = 172 Ft x 92 82 Ft = 15,973.64 Ft2
	A.= 24.40% B= 10.97 % ] 0.26.92 % ] D= 19.87 y.
	[E = 11.18 % ] [7 = 6.66. ] -> Percentages based on live load occupancy
	Average tive lood = 73.0 pst.
	Win = 1,2 (10,177.75 16)/ft + 1079 5 lb/ft) + 1.6 (73 p.F)(25")
	+ 0.5 (34.65 psf) (251)
	Wuz = 13,508.1 lbs/f4 + 2,920 lbs/f4 + 4133.12 lbs/f4
	Wes. = 16,861.23 lbs/ft => Waz= 16,86 K/Ft
3)	Wus = 1.20 + 1.65 + L
	Was = 13,508. 1 lb./ft + 1.6 (34.65 p.F)(25.) + (75 p.F x 25.)
	Was = 13,508.1 161/14 + 1386 lbs/ft + 1825 lbs/ft
	Was = 16,719.7 lb/14 => [Wus = 16.72 k/ft]

II	
	2nd Floor
	Dead   was = - Root + 3x2 France = 407.04 pst
	- Roof + 3rd Figur solid head = 130 pst
	- MEP = 5 PST
	- Dome slab = 100 pst
	- solid head and flow = sapet
	- Walls / pertitions / columns = 113.68 pst
(L)	Wa = 1.40 => Wa = 1.41 (407.09 pst + 5 pst + 103 pst = 113.68 psf) (25"
	+ 1.21 (59 pst + 130 pst) (8.51)
	Wus = 1.4 (15,719.25 lb/1+)+1.4 (1606.5 lb/1+)
	Wuz= 24,256.05 lbs/ft => [Wu, = 24.26 k/ft]
2	Wu, = 1.20 + 1.6 L + 0.5 S
	Snow load = 34.65 psf
	Live local = A 201678H2 + 2720,51H2 = 50 pt -> office room.
	B. 31+2-77 Hz + 500 Hz + 685.50 Hz = 40 pit -> meeting room
	c. 1013. 87 /2 = 100 pst -> mechanical room
	0 50 H2 + 2 (81.75 H2) = 100 pH -> stains
	E. A099.42 H2 + 814, 58 H2 = 80 pt -> corrictor
	Total area of Flour = 172'x 92.87 = [15, 973 64 1/2]
	Porcen fuges based on accupancy = S A = 29.89 % B= 27.73 %
	C= 6.347 D= 6.66 % E= 30.76 %
	Average Live load = 63.10 pif

MaI	
	Was = 1.2 (15,719.25 lbs/f4 + 1606.5 lbs/f4) + 1.6 (63,10 psf)(251) + 0.5 (34.65 psf)(251)
	Wuz = 20,990.9 lbi/ft + 2524 lbi/ft + 433 13 lbi/ft
	Wuz = 28,748.03 lbs/At => Wuz = 23.75 K/At
(3	) Wu = 1,20 + 1,65 + L
	Wa = 20,790,9 + 1.6 (34.65 p) (25') + (63 10 p) (25')
	Waz = 23,754,4 /b1/ft => [ Was = 23.75 K/Ft ]
	15+ Flour (Gravity Load Combinations) Dead load: Raf, 3rd Flour, 2001 Floor = 628,77 pot
	RUF, 314 224 SOTICH HEAD = 189 p.f
	Dome 5/ab= 103 psf
	solid head = 59 psf
	Walls / portitions / columns = 721. 94 put
4	Wu = 1.40 => Wu = 1.4 (628.97 pif + spif + to-pif +121.94 pif) (25.)
	+ 1.4 (189 psf + 59 psf) (8.5°)
	Wa = 1.4 (21,467 75 /6/14) + 1.4 (2108 66/14)
	Wa. = 33,006.05 lbs/ft => Wu. = 33.00 k/ft]

JZ <sub>u</sub>
② Wuz= 1.20 + 1.6 L + 0.55
8 now load = 34.65 psf
Dead Load = 21,467.75 + 2108 lbs/ 14
tive lood = (A) 4664-22 ft + 910,21ft = A0 pif -> morting room
(B) 3269 25 the 1 4022 19 the = 150 pt -> library strekt
(c) 946 46 Hz = 60 pst -> reading your
€ 522 25 f-12 = 160 psf -> comov. 11± ficer
(E) 1221 53 Pt2 = 100 ptf -> much room
( 501. 0 + 2 (281.76 Fer) = 100 pit -> stuire
Total Are 15t +(00) = 172 ft x 92.87+ = [15, 923.64ft2]
A= 30.89 %   B = 45.65 %   C = 5.93 %   D = 3.24 %
t = 265 y   F = 6.66 y
Average hup load 1st floor = 102.20 psf
Nu2 = 1.2 (21,469.95 lb/ft + 2108 lb/ft) + 1,6 (102.20 pit)(251) + 0.5 (34.65 pit) (251)
Wu, = 28,290.9 865/H + 4088 lbs/H + 433.13 lbs/H
Wuz = 32,812.03 lb./ 1+ => [Wuz = 32.81 x/ ]
3) Mus= 1.20 + 1.65 + L
Was = 28,290.9 (b) /ft + 1.6 (34.65 pst)(25) + (102.20 pst) (25)
Whis = 32,231.9 (6)/1t => [Was = 32.23 k/f+]

## **Appendix C.6: Two-Way Dome Slab Calculations**



SLI	
	te = aug. equivalent America.
	Jee Example 1 Chapter H-10 and Ex 2.
	(te) 10 [2 (ts) + 8 (tr)] where, the thickness of ribbed area to thickness of ribbed area
	o drop panel in conventional flat slob construction (CRS) (h 11-16
	. Ribs are designed as joists (each rib contains (2) two bottom bar straight top bars are used and are of two lengths in the
	Column stop to account for the negotive moment conferences.
	Center-to-center span li= 20' li= 25' (interior columns)
	71: 20:00.
	le= 25°0°
	solid head; shop extend in each direction from the centerline of support a distance not less than 1/6 the span length measured from center to center of supports in that direction
	Minimum solid head = 1 & 1 + 1 &
	MINIMUM Solid head = 1 (25) + 1 (20) => 4.17' + 3,33'
	min solid head = 7.50"

Structure And	ysis Two-Way Dome s	stab	
Le This on	algsis works for the	1st, 2nd and third floor	
of the Gord	on Library Building A	separate analysis will be n	naok.
	-way Dome slob for		
Width of ribs	of Dome slab:		
		S-H Structural Drawings	
Overall dopth o			
	iches for overon depth		
	between ribs:		
	inches as a clear space	ng between 1165	
Slab Thicknes	Vd		
used 4	nches for slab thickness		
J-	1		
7	A"		
		10"	
		1	
	/ 18" / 5" /		
	N9 5(5).		
The Two-W	109 slob is the some	for each floor described	
aporo puna	100 the 5170 of th	for each floor described as columns will differ	
1001 park 11	out A separate and	lysis is necessory for	
each floor.	and the second	J. Comment	
ANCH LINGA.		Ŧ	

SLTL	See pg 248 ACI
	Bosed on structural drawings of Godon Library  a Assume a squere drap pand or salid head  be Assume a 816" solid section for drap panel boused  on dimension given in S-14 sheet structural prowing  gordan Library. This includes the dimensions of the column  till drap panel will have some alimensions for ease of  construction and for colculations.
	Two-way Damo slab (oparity (End span)  Total static Mannent (Ma):  Mo. (outside head) = No Li/8  Li= (alumn to column distance.  Mo. (head) = (wasona-Wa)(L2)2/2 Lzz column to end of salid head  Total Ma = Mo. + Mo.  23",
	$\frac{1}{1000 \text{ Ho}} = \frac{1}{28.19 \text{ K/H}} \left( \frac{19.08 \text{ Ho}}{14.329} \right)$ $\frac{1}{1000 \text{ Ho}} = \frac{1282.81 \text{ K/H}}{1000 \text{ Ho}} = \frac{1282.81 \text{ K/H}}{1000 \text{ Ho}}$

Exterior	Column (Negotive	Momona) (ACI B.6.4.2)
Mu =	= 0,26 Mo =>	Ma = 333.53 -F+
(Glumn	strip restist 100 %	of Mu, therefore 1.0 Mu
Battom	( Pasitvo Mamon	(ACI 15.6,4.4)
Mu	= 0.52 Mo =>	Mu = 052 (1282.81) =>  Mu = 66706 K
(a)um	strip (clists 603)	K++
Middle	Hu= 266.82 K.	of Ma, therefore 0,40Ma
		(1.4.1) (ACI 13.6.4.1)
		of Ma, Herefire 0.75 Mu
		=> Mu = 673,48 K.1+
Middle	strip ratios 25	V. of Hy, 0.25Mu
	Mu = 224.49	k. it

SLI			
	Theor at External column		
	d= (4+10) - (oncasto covor - do		
	$b^2=23+c1$ where $d_0=d_0$ do $b_0$		
	d- 14 A 75 - A50		
	Cco Cnc   d= 12 75 in		
	b1 = 23 + 12 75/2 => (b1 = 29.38in)		
	$b^2 = 23 + 1295in =  b_2 = 35.75in$ $b_0 = 2xb_1 + b_2 =  b_0 = 945in$		
	Ace box d - 1205.0 in2		
	Fortoled Shear (Mr) at centerline of exterior column:		
	Vu = Wu L/2 - (Man - Main)		
	" Nu = (2819 K/FF)(19.08 H)/2-[(897.97 - 333.53 KF)		
	Vu = 868.93 k - 29.58 K		
	Vu = 239.35 Kip		

ST. III	
	Their Check of Externa Column
	11c = (xsd/bo+2) \( \text{Trc}  \( \text{ACI Eq 11-32} \)
	Vc= ([30 x 12.75 / 94.51]+2) Vic => 6.05 (FC = [382.64 psi)
	A: 382.64 pri > 4 (4004pri = 253 pri We need to use 253 pri Le ACI Eq 11-35
	OVC = 0.75 (253) => OVC = 190 PSi 01 OVC = 0.191 KTI
	Mu = Vu + WMucas
	where $\gamma_0 = (1-\gamma_f)$ (ACT Eq. 11-37) $Y_f = 1/(1+(2/3)\sqrt{61/62})$ (ACT Eq. 13-1) $= 1/(1+(2/3)\sqrt{2738/3545} = \boxed{0.623}$ $V_0 = (1-0.623) = 2 \qquad \boxed{Y_0 = 0.38}$
	Mu = 03mo (ACI 18.6.36) Mu = 03 (1282.81 K.H)=> [Mu = 384.84 K.Ft]
	$T_c = \frac{b_1 d^3}{6} + \frac{2d \Gamma((a_0)^3 + (c_{10})^3)}{3} + b_2 d(c_{a_0})^2$
	$\overline{\sqrt{3}} = \frac{(29.38)(12.75)^3}{6} + \frac{2(12.75)}{3} \left[ \frac{(902)^5 + (2031)^3}{3} \right] + \frac{(35.75)(12.75)(102)^5}{3}$

SL <b>VII</b>	
	Je= 10149-18 + 77555,48 + 37497 37
	Va = 275.99k + (0.38)(364.84) (9.03m) 1205.01m2 125,200 1m4
	Vu = 0.245 + 0 0106 [Nu = 0.255 Ksi]
	Delign Homent Strendth (641n)
	As = # of bon in Column strip x Nominal Area of boxs  As = (33) x (0 z jn2) =>   As = 6.6 in2
	a= Asly , a= (66 in+)(60 ks) , a= 2.28 in \ 0.85 feb 0.85 (4ks)(51in)
	where b= effective width = helf the width of the pone = 51 in
	QMn = QAs & (d-a/2) => OPEN = 090(6.6 in2)(60K)(1275-2,28)
	TOM- 344.82 KILL : DIMN > MM /
	Mu = 0,26 H0 = 0.26 (1282.81) => Mu = 333.53 K F+  VIMU = 0.623 (333.53 K.Ft) => (207.49 K Ft)

- VIII	
	$p = A_3 \Rightarrow p = 6.6 m^2 \Rightarrow p = 0.010$
	- Pmax = 0.011 P = pmax /
	Interior Ipon
	44/164/17
	Panel Hamenas
	O Bottom (positive moment)
	Mu = 0.35 Mu = 0.35 (1282.81) => Mu = 448.98 K)+
	Colum strip resist 60% of Mu
	0.60MU => 06(448,98) => Mu= 269.39 = Ft
	Middle stap results 2007 it Ha
	0.40 Mu = 040 (448.98) = 5 Mu = 179.59 Kft
	• Top (nego time mamon+)
	Ma = 0.65 Ma = 0.65 (128281) = Mu = 833.83 KF
	Column Stop resist 75% of Ma
	0.75 Mu = 625.37 + Mu
	Hidele Stop ruist 25% of Ma
	0.25 Mu=> [Mu= 208 46 x Ft]
	Thear at Interior Columni
	,
	$b^2 = 23 + cL$
	Con Cao
	61

SL IX	
	$b_1 = b_2 = 23 + 12 + 9 = 8 = 35 + 95 \text{ in}$ $b_0 = 4 \times 35 \cdot 75 \cdot n \Rightarrow b_0 = 143 \cdot n$ $As = b_0 \times d \Rightarrow As = 1825 \cdot 25 \cdot n^{2}$ $Cho = Cob = 35 + 5/2 \Rightarrow Che = 17 + 88 \cdot n$ $J_C = (db_1/6) [d^2 + 4b_1^2]$ $J_C = (12.75 \times 35.75) [(12.75)^2 + 4(35.75)^2]$
	There (Va) of Interior (olumn  Vu = Wu L/2 + (Muxx - Muxx)  Vu = (28.10 x/ft) (19.08 H) + (897.97 - 333.53 x H)
	Va = 298.52 Kips    Then check  Ve = (xs d /bo + 2) The & AJire  Ve = (40 x 12 75/140 in +2) The  Ve = 5.56 The ye = 352 pc;    Dre = 264.04 pri

SLX.		
	Vo = Va => Va =  Ouc ≥ Va V	298.52 kips => [ Vac 0.164 ksi]
	factored Homeny at End	
	M 333.53 x.1+	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	FF. x 30. F36	
		×

SLX	
	Jlab (alculation Section 2 L= 25'; L= 23.08'  310b size = (20' × 25' c/c) = 23.08ft × 18.08ft
	Mo = Wal2/8 => Mo = (33.00 K/ft) (23.00 ft)2
	Mo = 2.197.33 k + H
	Interior Support  Min+ = 065M0 => 0.65 (2197.33) => [Min+ = 1428.26 k ft]
	M+ = 0.35M0 = 1 [M+ = 769 67 k.Ft]
	Total (olumn Strip Moments  Main = 0.75 Max = 0.75 (1428.26)=>   1071.19 k H
	Mc+ = 0.60M+ => Mc+ = 0.60 (76907) => [Mc+ = 461.44 K.H]
	Mcm= = 1071.19 K-Ft
	Total middle strip moments  Munt = 142826 - 1071.19 => [Munt = 357.09 k]{  Mmt = 769.07 k.ft - 46144 -> [Mmt = 307 64 k]{  Mmm = [357.09 k.ft]
	MMms - 1 354 Oct 18-11

## **Appendix C.7: Interaction Diagram Calculations**

IDI				
	(amputot	ion of Namina? Ax	10s and Nomina	Homent la
		#4spia		#4 spine
		74%	6	12275
		,		,
	fleunz	L: 6 bois	Frank	t 2: 8 bars
	Example: (olun	nn Type Figure		<i>y</i>
	. 1"/2" COURT		, 13.60°	,
	* 8 # 11 ba			•
	* 21/2" pitel			•
	· J'c = AKN			1 - di= 20.29*
	e fy = 60 Ks		741	2.91 in
	* Es = 29 000		Eg	0.003
	+ Diameter # 4 b		Ess   Ess.	eg f
	• Drawers # 11		, ai	1
	Ey = Fy /	Es	11 12 1	0.80%
		i)/29,000 kii	Ti Ta	Cs <sub>2</sub>
	Eg = 0.002	FO	X	

IOI	
	Location of NA:
	$dt = 23 in - \frac{11/2" - 0.50" - 1.41 in}{2} \Rightarrow dt = 20.29 in$ $6y = 0.00207$
	xb = 0.003 $x dt = 5$ $xb = 0.003$ $(2029')$ $0.003 + 63$ $0.003 + 0.00207$
	Xlo = 12.00 in \
	Depth of Whitney Stress black
	where, B1 = 0.85 for fic ≤ 4000 pi or 4 kii
	ab = 0.85 (12.00") => [ab = 10.2 in]
	Circultur compression Block Properties:
	$d = cos^{-1} \left( \frac{h/2 - ab}{h/2} \right) \Rightarrow cos^{-1} \left( \frac{23in}{2} - 10.2in \right) \Rightarrow cos^{-1} (0.113)$
	X= 83,51°
	Area of circular compression black
	$A = \frac{h^2}{2} \left( \frac{d \operatorname{rod}}{2} - \frac{1}{4} \operatorname{Sin} 2d \right)$
	$A = \frac{(23 \text{ in})^2}{2} \left( \frac{1.46}{2} - \frac{1}{4} \right) \sin 169.62^{\circ} $ $\Rightarrow A = 178.23 \text{ in } 2$

ID III	
	Location of control of compression block
	$\overline{X} = \frac{h^3}{4} \left( \frac{3 n^3 n^3}{3} \right) \implies \overline{X} = \frac{(23 n^3)^3}{4} \left( \frac{5 n^3}{3} \frac{83.51^n}{3} \right)$ $198.23 n^2$
	X = 5.581n
	Compressive force in compression Block (CE)
	Cc= 0.85 f'c A => Cc= 0.85 (4Ksi) (78.23102)
	strains and forces in tension and completion steel
	Est = 6.0023 (> Eq)
	Esz = 0.6012 ( Ey)
	εος = 0.00093 (4 6)) de-20.29 m
	2.410
	Linear Interpolation to
	get strain volves
	633 0 002 Era Esa
	Calculate forms in steet
	Tre Aig => Tr= 2(1.56 m2)(60 Ksi) => Tr= 187.2X
	Tz= As Es Es => Tz= 2 (1.56 m2) (0.00097) (29000 Ks)
	Tz = 87 77 Kips

ID M	
	$C_{51} = A_5 (f_y - 0.85 f_c) = C_{51} = 2(1.56 in^2)(60 ksi - 0.85 (4ksi))$ $C_{51} = 176.59 kips$
	Cs2 = As (Es2 Es - 0.85 (c) => Cs2 = 2(1.56 in2)(0.0012 x 29000 Kci - 0.85 (c)
	Nominal axial compression strength. Pro = Ca + Cs, + Csz - Ti - Tz
	Pn= 605.57 kips
	Harmood moment strength
	Mn= [ (c x x + (T1+Cs1) (0) + (T2+Cs2) (D1)]
	De disting from PNA to Cos
	Di = distres from PNA to Co2
	Mn= [(606.98 K)(5.581)+ (176 59 K+187 ZK)(8.8010)+(97.97 K+87.77 K)
	(4.40.0)
	Mn = 3381.37 k in + 3201.35 k · in + 817.26 k · in
	Mn = 7399.99 Kin or Mn = 616.66 K. HT

Eal	
	Nominge Axios and Manard strength (Full Axios)
	Lo assuming different "a" valve for interaction diagram proposes
	Oppth of thirting Ities Block  Obs 23 in
	Circular Compilation Block Properties
	$\alpha = \cos^{-1}\left(\frac{h/2 - \alpha_b}{h/2}\right) = 5 \cos^{-1}\left(\frac{23/2 - 23 \ln}{23/2}\right) = 5 \cos^{-1}\left(-1\right)$
	d= 180°   1x= 3 1415
	Area of compression Block
	$A = \frac{1}{2} \left( \frac{3 \cdot 146}{2} - \frac{1}{4} \sin 2\alpha \right) = 1$ $A = \left( \frac{23}{2} \right) \left( \frac{3 \cdot 146}{2} - \frac{1}{4} \sin 360 \right)$
	A: 415.46 in2
	location of contraid of compression black
	$\overline{X} = \frac{h^3/4 \left(\frac{\sin^3\alpha}{3}\right)}{h} \rightarrow \left[\overline{X} = 0\right]$
	(simplement torce (c)
	CC = 0.45)10 A => [Cc = 14112.56 xips]
	Strain Values (E)
	strains will have a valve of E= 0000 all arrow the
	whitey stren place
	Cin= 4 As ( 1g - 0.85 fe) => (Cin= 353.18 K)
	(52 = A3 (EEs - 0.85 Ja) 55 Cm = 4(1.56 in) (0.003 x29 000 + 51 - 0 \$5 (4h))
	C12 : 521.66 K

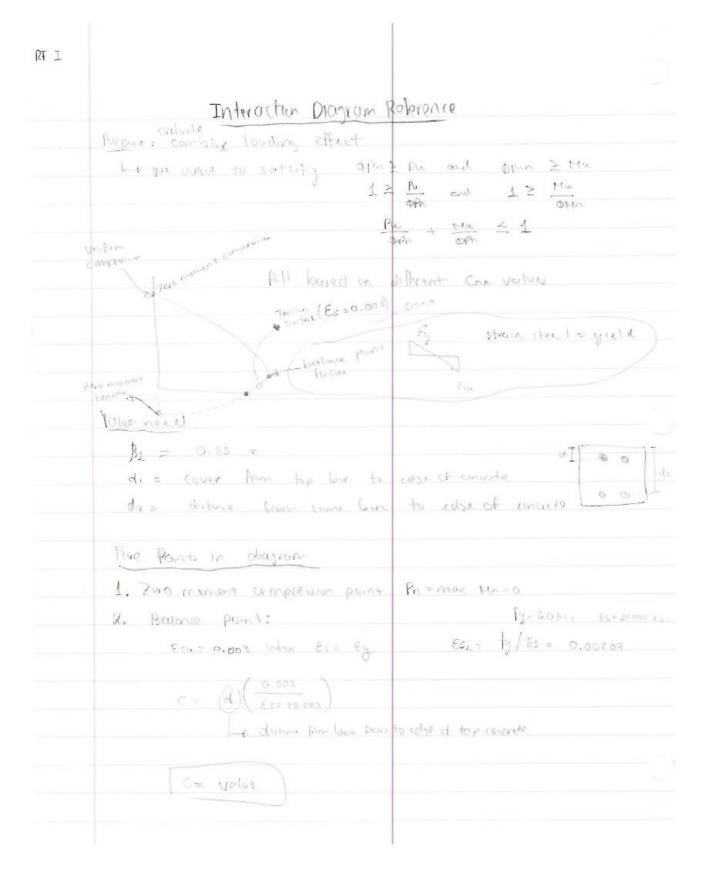
IDAI	
	Primer = Cr + Csr + Csz Primer = 1412 56 K + 353.18 K + 521.66 K
	1 Pr., Max = 2287.40 Kpl
	$M_{n}=0$
	Nominal Axias and Moment strongth (pure Flexive Part Pau)
	$P = Cs_1 + Cs_2 + Cc_3 - 7_1 - 7_2 = 0$ $O = As_3 (Fy - 0.85 fre) + As_3 (0.003 (x5 - 0.85) + 0.85) $
	- Aity - 0.00017As (d1-x0)-d1) Es
	$A = \frac{h^2}{2} \left( \frac{\alpha \tan \theta}{2} - \frac{1}{4} \sin 2\alpha \right) \Rightarrow A = \frac{h^2}{2} \left( \frac{\cos^{-1} \left( \frac{n}{2} - B_1 x_0}{n/2} \right) - \frac{1}{4} \sin 2 \left( \frac{hh}{n/2} \right) \right)$
	$A = \frac{(23)^2}{2} \left( \cos^{-1} \left( \frac{\frac{23}{2} - 0.85 \times b}{23/2} \right) - \frac{1}{4} \sin 2 \left( \cos^{-1} \left( \frac{\frac{23}{2} - 0.85 \times b}{23/2} \right) \right)$
	$A = 264.5 \left( \frac{11.5 - 0.85 \times 6}{11.5} \right) = 0.255102 \left( \frac{11.5 - 0.85 \times 5}{11.5} \right)$

TTYON	
	$A = 2645 \left( \frac{\cos^{-1} \left( 1 - 0.0739 \times b^{-1} \right)}{2} - 0.25 \sin 2 \left( \cos^{-1} \left( 1 - 0.0739 \times b^{-1} \right) \right) \right)$
	$0 = z(1.56)(60 - 0.85(4)) + z(1.56)(0.003(\frac{x_6 - 271}{x_6})29000 - 0.85(4))$
	+ 0 85 (4) A - 2 (1.56) (60) - 6-COM (2 x1.56) (20.20-44) 29000
	$O = 176.59 + 3.12 \left( 87 \left( \frac{x_{b-2.71}}{x_{b}} - 3.4 \right) + 3.4 A - 187.2 \right)$
	$-187.3\left(\frac{(20.29-4.4)}{(20.29-4.5)}\right)$
	$O = 176.59 + 312 \left( 87 - \frac{235}{xb} + \frac{3}{xb} - \frac{3}{4} \right) + 3.44 - 1892 - 1873 \left( \frac{(26.24 - x5) - 4.26}{(26.29 - xb)} \right)$
	$0 = 3.12 \left(83.6 - \frac{235.77}{10.61} + 3.44 - 10.61 - 187.3 \left(\frac{(20.29 - 10.6) - 44}{(20.29 - 10.6)}\right)\right)$
	0= 260.83 - 735.60 + 3.4 A - 10.61 - 1573 ((20.29 - xb) - 44)
	0= 250.22 - 335.60 + 899.3 (05-1 (1-0.0739 xb) - 6.25 5102 (05-1 (1-0.0739 xb))
	$-187.3 \left( \frac{(20.29-x5)-44}{(20.29-x5)} \right)$
	*

10 VIII	
	0= 250.22 755.60 (3800.32 + 197.3 xb) ((20.29-x5)-44) 4
	0-250.22 - 735.6 - (3600.32 + 87.5xb) (15.89-xb) +
	0 = 250.22+ 735.6 _ 60387.08 + 3800.32 Xb - 2976.2 Xb + 183.3 X62 +
	O= 187.3 xb2 - 60136.86 + 735.6 + 824.12 xb +
	see spreadsheet for completion

ID TX	
	Tension (entred Point (Ec: 0.003 and Ec: 0.005)
	Xp= 0003 × 01+ =>   Xp= 160:0
	ab = B1 x6 +5 06 = 0-83 (760m) => [06= 647 in]
	$A = \cos^{-1}\left(\frac{h/_2 - \cos}{h/_2}\right) = 5 \cos^{-1}\left(\frac{23/_2 - 643}{23/_2}\right) \Rightarrow \cos^{-1}\left(0.449\right)$
	d = 63 620 or d = 121 roll
	Are of composition Block  A = $\frac{h^2}{2} \left( \frac{2 \log 1}{2} - \frac{1}{4} \sin 2\alpha \right)$ . A = $\frac{(23)^2}{2} \left( \frac{1.11}{2} - \frac{1}{4} \sin 1273\% \right)$
	A = 94 22 in2
	loretran of comparison block
	$\bar{X} = \frac{h^3}{4} \left( \frac{\sin^3 \alpha}{3} \right) \Rightarrow \bar{X} = \frac{(23)^3}{4} \left( \frac{\sin^3 6363^2}{3} \right)$ $= \frac{h^3}{4} \left( \frac{\sin^3 \alpha}{3} \right) \Rightarrow \frac{1}{4} \left( \frac{\sin^3 6363^2}{3} \right)$
	又 <sub>2</sub> 7.74 in 7

XOI	
	(Ompression there in Diese (Co)
	(c = 0.85 ) c A => (c = 0.85 (4 ksi) (94.22 in)
	Strains and force in tension and compression
	En = 0.0019
	Ecz = 0.00019
	8.5 - 0.0033
	0.005
	0.003
	Figres in Steel
	T1 = Adg = T1 = 2 (1.56 in) (60 km) = 187.2 kl
	Tz = A: Ess Es => Tz = Z(1 56 m2) (0.0003) (2 m000 m3)
	T2 = 298.58 K
	Cs. = As (1g - 0.85)=> Csi = 2(156in2)(60 ksi - 0.85(476))
	(Cs) = 176,59 k
	Cs2 = As (Es2 Es = 0.85 Ne) = 5 Cs2 = 2(1.56 in+) (0 00019 x 29000 - 0.85 (4)
	) Cs2 = 6.58 K
	Pn= Cc+ (s1 + Cs2 - T1 - 72 -) Pn=320,35 K+176 59 K+658K-1977K-298.6K
	Pn= 17.74 Kips



&E II	
	a=FLC
	a=Bic a=
	Esn - 0.003 ( c-d1 ) = yolve
	a= B, c = 0.515(c) Are = over of top steel  Are = over of top steel
	Congression Heel = Asiles = Asi (60Hi)
	Total force = Csi + Cc + Tiz, bolonce pont
	Ysi - distance from Prise to edge - de =
	Yes = distance from PNA to estage - a = Ys: = distance from bottom box to edgs - distance from PNA treetige =
	Mn= (Co1 x ys) + ( yee y Ce) + ( yez x Tse)
	C= occount of = M

RF III	
	Point 3: Pure tlexux Point (P-0)
	P= 0 003 AsiEs (C-di) + 0 xs fic B1 cb - Asifg = 0  Csi  Csi
	Le [0.88] CZ + [0.003 As, Es - As Fg] C - 0.003 As Esd = 0
	Get (c) your and bosed on that (a) > a = Bic
	Cs: $c = 0.000 A_{11} Fs \left(\frac{c - \sigma_{1}}{c}\right)$ $cc = 0.85 f'c B_{1} cb$
	Ts. = Asz fg that Levet arm
	The other eves are sains to be the same as previous it and the
	Mx = (4c x cc) + (co x yo) + (Toz x ysz)
	Part 4 Pura Tension
	P= ( As, + As, ) by
	$M_{\rm N} = 0$

K= II		
	Point 5: Tension - Controlled (Eco: 0.003 and Ess 0.005)	
	C= d (0,003)	
	$e_{s,c} = 0.005 \left( \frac{c - d_s}{c} \right)$ strain on top stars	
	a= p, e => [0= 0.85c]	
	Co = Par In Co = 0.88 Fe a b   P = Co + 752	
	Lever aim  Yee = PNA to edge - a  Other ones we the some.  [Na = (Yee x ce) + (Yrix csi) + (712 x /si)]	

# APPENDIX D: SOLAR COLLECTOR CALCULATIONS

### **Appendix D.1: Solar Evacuated Tube Load Calculations**

Tippenum 211 Solul Liucultu luse Loud Guicultulons		
	Solar Evacuated Collectors Info	
	O O UNIC O CONTINUE DE SANTAS, MINISTERIO	
۰	Dimensions: 78,9" x 86,4" x 5,3"	
	Weight: 209 lbs (dry)	
	angle: 40° south	
4	Number of collectors: 31, 16 on one side, 15 on another	
	Third Capaity: 0,2 gal- = (0,2 gal) (8,34 lgal)=1,67 lb (30 tubes)=50,1 lb	
	Smar low capacity: 60 /t2. angl = 45° or higher	
	1. 1. 1	
	Wind lood capacity: Up to winds of 196 mph	

_	Dead Load D
	40 One collector = 209 lb + 50,1 lbs = 259,1 lbs (16) = 4145,6 lbs (one side)
	Lo ana = (78,9"/12')(86,4"/12) = 47,34/f2
	D= 259, 165 = 5,47 psf one collector
	47,34/42
.50	
-	Smou Load S
	Flat roof snow load (section 7.3)  * PF= OF Ce Ct IF Pg *
	* PF= OF Ce Ct IF Pg *
	Lo Esposure factor (Ce) (table 7-2)
	Terrain Category B (Section 26,7); fully exposed woof
	Ce = 0,9
	Lo Ground Smou Lour (Pg) (Figure 7-1)
	. Worketer = 50 psf
	Lo Thumal factor (Ct) (table 7-3)
	(t=1.0
	Lo Importance Factor (15) (table 1.5-2)
-	Risk category III
_	16= 1.10
	Lo Flat Roof Smou Lond
	PF=0,7 Ce Ct IF Pg
	PF=0,7(09)(1,0)(50 psF)
	PF= 34,65 psF
	5= 34, 65 psf
	2

1	
ı	
1	
	11: 1 food 11 Boot ton Solve Crossy Libbines ext.)
	Ulinch Load W (Proof top Solar arrays buildings @ 7)
1	1) Rish Category (table 1.5-1)
+	nish category III
+	2) Basic Wind Speed (Fig 26,5-1B)
4	Workester, Ma - DV= 135 mph
4	3) Wind directionality factor (Fig 26,6-1)
4	40Structure type: Guilding
	Kd=0,85
	Lo Exposure Category (26,7 Section)
	Exposure B
	Lo Topographic Effects (Section 26,8)
1	ma topographic factor
	Rzt = 1.0
	4 Gust Effect factor (Section 26, 9)
	Rigid building
	G=0,35
	4) Velocity Pressure Exposure Coefficient (table 29.3-1)
	Height above ground level = 26 ft : Exposure B
	1/2= 0,668
	5) Velocity Pressure (Section 29,3,2)
	9z=0,00256 Kz Kzt Kd V2
	9z=0,00256 (0,668)(1.0)(0,85) (135 mph)2
	9z=26,49 psf °
	16- 000 11 100

ı	
Ĭ	
4	From wind design for low profile solar photorottaic arrays on flat roofs
	1) Compute Apr
	Apr=0,5 Th We har building hight
	Apr-0,5 Table (43') We building with on longest side
	Apr- 17,66 /t
	* Apv≤h. if Apv>h, then Apv=h
	2) Normalized Wind Ones An
	$A_{Q} = \begin{pmatrix} 1000 & A \end{pmatrix}$
	(max (17,66: 156t))2) A-
	An= / 1000 \ (148/)(48.1)
	An= ( 1000 ) (148/)(48 D)
	An = 7887.56
	3) Normalized Net pressure (Figure 29,9-1)
	15° = W= 35° * 5000 is max An
	107 An=0,30 -> 6-C10 1000-0,42
	4) Cary Length Charle Length fractor
	4) Pand length Chard Length factor  8c= 0,6 + 0.6 1p lp chard length of system = 7,2 ft
	Xc=0,6+0,6(7,2')
	8c = 4,92
	5) Parapet Heigth footor
	hpt < 4 ft
	Xp=1.0
	6) Determine Characteristic Height
	he= min (h, 1/t) + lp sin w hi= solar panel height above
	he-min (53", 1/1) + (72") sin (40°) roof at low edge
	hc=6,316t

×

- 1		
- 1		
- 1		
- 1		
1	7) 7) 1	F 1 (F)
-	+) Vetermine array Edg	dx = horizontal distance from algo of
1	0x 36+ 0	dx = horzontal distance from algo of fond to edge of earl or other fond
	6.3/4	
-	120	ford to edge of logger other flore
_	1/hc- 0,5	
	• E=1.0	
1		
$\dashv$	8) Not Pressure Coeffici	av
	(b (m)- YpE [ (bo	(n) non (ye)
	(b(in) = 1.0(1.0)[	
-	(6(m)=4470	
	9) Design Wind Passe	in0
	(p= 9z (6Cm)	
7		
-	P= 26,49(1,446	
	p. 39,09psf	
		No. of the control of
-		
-		· ·
-		
_		
		5
Ш	II.	3

-	
ı	
-	Seismir Load E
	· Ss: (Figure 22-1)
	Worker, Ma: MCER-18/2
	· 5.: (Figure 22-2)
	Worcester, Ma: MCER = 7/2
	Lo Seirmic Design Category
	Soil darification (Section 20)
	Site D - Unknown details
	Lo Design spectral acceleration Paramiters (Section 11.4.4)
	Sps= 2 SM5
	501 = 3 5MI
	· Spectral response audination Parameter (Section 11.4.3)
	SMS= Fo Ss
	SMI= FV SI
	· Site Coefficients
	For sit D & So < 0,25 (table 11.4-1) & S, < 0,1 (table 11.4-2)
	Fa=1,6 Fy=2,4
	- SMS=1,6(0,18) - SMI=2,4(0,07)
	SHS = 0,288 SHI = 0,168
	$-S_{DS} = \frac{2}{3}(0.288)$ $-S_{DI} = \frac{2}{3}(0.168)$
	Sps=0,192 Sp.=0,112
	Lo Bisk Category (table 1.5-1)
	Rich Category III
	Lo Seismic Derigo Cotegory (table 11.6-1)
	For 0,167 5 Sps 50,33 & risk category III
	SDC=B

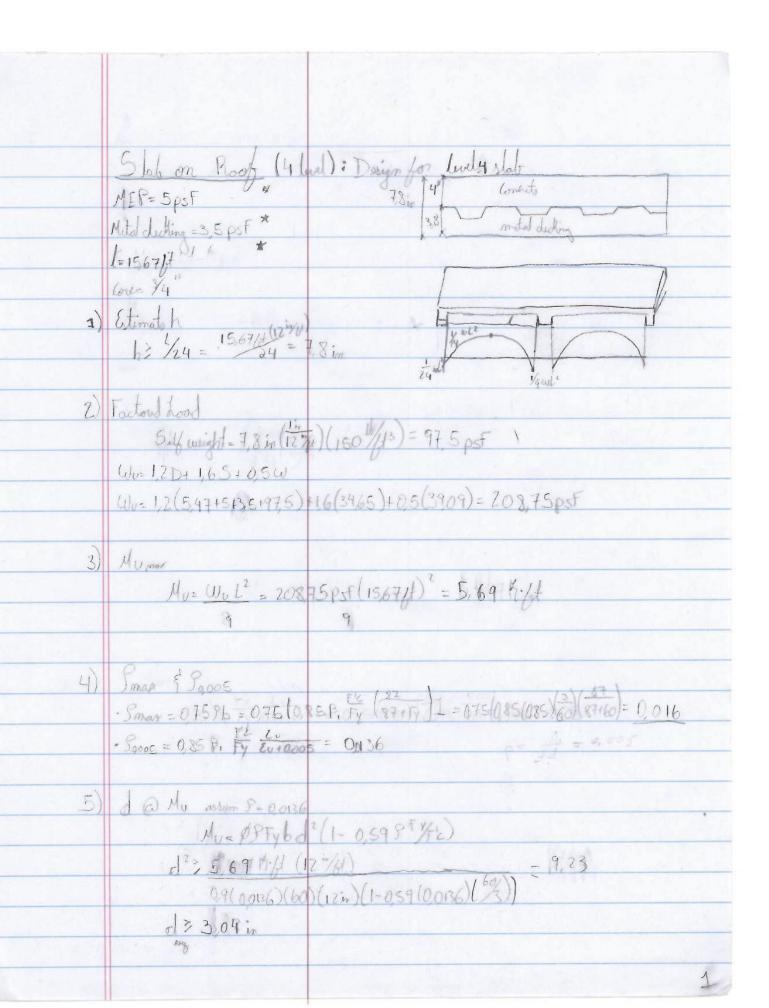
н	
1.	C 1 + . + + (111 1 - 2)
	Sairmie Amportono Factor (table 1.5-2)
	Pish citegory III
1.	le=1.25
LD	Saismic Prosponse Coefficient (Section 12.8.1.1)
	$C_{5} = \frac{S_{DS}}{(R)} = \frac{0.192}{31.35} = 0.8$
1.	
-0	Response modification factor (R) (table 12.2-1)
1.	Seismic bare shear (V) (Section 12,8,1)
M .	
Н	-
	Ta= Q1(3)
1.	Ta= 0,3=T Vertical Distribution Factor (Cvx) (Section 12.8.3)
L-D	
	Cvx = Wx hx h h=1 since T=0,5  Z Wih:h Wx= 124psF
	154
	Cvx = (12485)(26ft) hx=26ft (12485)(26ft)
l.	Cyx = 1,0 psf
-D	Latinal Spirmic force (Fx) (Section 12.8.3) Fx-Cvx V
Ì	Fx=1,0(9,92psf)
	Fx= 9,92 psf
	11- 116 PS)

	4 Soismic Lord Effect (Section 17.4.2)
	E = Eh + Ev
	· Horizontal Laismic Load Effect (Eh) (Section 12.4.2.1)
	Eh= Pae P=1.0 because SDCB
	Eh= 1.0(9,92psf) Que= Fx
	Eh= 9,92pst
	· Vertical leismic Load Effect (Ex) (Section 12.4.2.2)
	Ev=0,2 Sps D
	Ev = 0,2 (0,192) (5,47psf)
4	Ev=0,210pst
	E = 10,13 psf
4	Summery
4	D= 5,47psf + self weight = 55,47psf E= 10,13psf
-	S= 34,65 psf L= 0
-	W= 39,09psf R= D
-	Building L=10PSF
-	Lood Confinations
-	1. 1,4D = // (C D)
-	2.1.2D+1.61+0.5(lraSorR)
-	3.1,20 + 1,6 (L, or Son R) + (L on 0,5 w)
	4. 12D+10W+1+05 (Lon Sor R)
-	5.1,2D+1,0E+L+0,2S
	6. 09D+1,0W
	7. 09D+10E =

Load Combinations	
1. 1,4 D = 1,4(5,47	oef) - 7660sf
	1/5/R)=1,2(5,47)4,610+0,5(34,65)=39,89psf
3.12D+16(L/S/R)+	(1/0,5W)=1,2(5,47)+1,6(34,65)+0,5(39,09)=81,55psf
4 120 +10011-1+05/10	(5/R)=1,2(5,47)+1,0(39,09)+10+0,5(34,65)=70,98psf
	2(5,47)+10(00+1)+10+07(3465)=23,704 +
	47psf)+1,0(39,09)=44,013psf
t. 0,9D+1,0Eh= 0,9(5,4	17)+1,0(9.93)= 14,843 psf
Governing load = 81,55	osf
0 0000000000000000000000000000000000000	
+ cuth lot 114 1	
	9

## **Appendix D.2: Member Design Calculations**

- Slob: one way continous the with inner support  . Metal Deck - 3 spst  . Mer = 3pst  . Oll boks on the some except for the roof's  - Column: . 12" x12" ( extinated by measuring) & #3 stimups  . Column placement & number of columns structed as for  as possible giver the amount of information  . Eoverned by axial force and a  - Beam: . 8 x10" ( extinated by eye)  . Language extinated as his as possible  . As made to be primited to the slob's  . Personch  . 1 = 3 x5;  . 2 = 3 x5;  . 3 = 4 x5 x5;  . 3 = 5 x5 x5;  . 4 = 5 x5 x5;  . 5 = 5 x5 x5;  . 5 = 5 x5 x5;  . 6 = 5 x5 x5;  . 7 = 60 x5;		
- Slab: one way continous slob with imm supplot  . Mital Deck = 3,555  . MEP = 3pst  . Oll slob on the some except for the roof's  - Column: 12" x12" ( stimated by measuring) & #3 strongs  . Column placement & number of columns estimated as but  as possible given the amount of information  . Coverned by axial forces and  - Beam: . 8" x10" ( estimated by eye)  . Layout estimated as but as partifle  . As needs to be similar to the slob's  . Personch  . I'z= 3 Ksi  . Als stul & 1432 stul - > Ty=60 hsi		
- Slab: one way continous slob with imm supplot  . Mital Deck = 3,555  . MEP = 3pst  . Oll slob on the some except for the roof's  - Column: 12" x12" ( stimated by measuring) & #3 strongs  . Column placement & number of columns estimated as but  as possible given the amount of information  . Coverned by axial forces and  - Beam: . 8" x10" ( estimated by eye)  . Layout estimated as but as partifle  . As needs to be similar to the slob's  . Personch  . I'z= 3 Ksi  . Als stul & 1432 stul - > Ty=60 hsi		
- Slab: one way continous slob with imm supplot  . Mital Deck = 3,555  . MEP = 3pst  . Oll slob on the some except for the roof's  - Column: 12" x12" ( stimated by measuring) & #3 strongs  . Column placement & number of columns estimated as but  as possible given the amount of information  . Coverned by axial forces and  - Beam: . 8" x10" ( estimated by eye)  . Layout estimated as but as partifle  . As needs to be similar to the slob's  . Personch  . I'z= 3 Ksi  . Als stul & 1432 stul - > Ty=60 hsi		
- Slab: one way continous Job with imm supplat  . Mtal Deck = 3,555  . MEP = 3pst  . Oll slabs are the same except for the roof's  - Column: . 12" x12" ( intinated by measuring) & #3 strongs  . Column placement & number of columns estimated as but  as jossible given the amount of information  . Coverned by axial force and  - Beam: . 8"x10" ( intinated by eye)  . Law out estimated as but are passible  . As needs to be similar to the slab's  . Research  . I'z= 3 Ksi  . Als itel A432 stal - > Ty=60 Ksi	0	Assumptions
MER = 5 psf  Coll slots are the same except for the roof s  - Column: 12" x12" ( intinated by measuring) & # 3 stimus  Column placement & number of columns atended as but  as possible given the amount of information  Economy by axial forces only  - Boam: . B"x10" ( intinated by eye)  Town at estimated as but are possible  As needs to be similar to the slab's  Personch  T'e= 3 hs:  A15 ited & 1432 ited - > Ty=60hs;		- Slat: one way continous dat with imm support
· MER = 3 psf  · Column: · 12" × 12" ( intinated by measuring) & #3 strongs  · Column placement & number of columns streated as but  as possible given the amount of information  · Covered by axial forces only  - Boam: · \$"×10" ( extinated by eye)  · Jayout estimated as but as passible  · As needs to be similar to the slab's  · Presearch  · t'z= 3 ksi  · Als stul & 1432 stul - > Ty=60 hsi		. Ntl Dakes cost
· Column: 12" x12" ( extinated by measuring) & # 3 stimups · Column placement & number of columns stimuted as but  as possible given the amount of information · Coverned by axial forces only  - Boam: · B" x10" ( extinated by eye) · Loyout estimated as but as possible · As mosts to be similar to the slab's  • Presearch • I'c= 3 Ks; • A15 ited & 1432 ited - to Fy=60 Ks;		
- Column: 12" x12" ( extinated by measuring) & # 3 strongs  · Column placement & number of columns streated as but  as possible given the remount of information  · Coverned by axial forces only  - Beam: . B" x10" ( extinated by eye)  · Layout extinated as bust as possible  · As needs to be similar to the slab's  · Persearch  · t'= 3 hs;  · As stud & 1432 stud - > Fy=60hs;		
· Column placement & number of columns stimated as but  as possible given the remount of information  · Conserved by axial forces only  - Boam: · B'x10" (extinated by eye)  · Layout estimated as but as possible  · As needs to be similar to the slab's  · Perearch  · I'z= 3 hs;  · As stul & 1432 stul - > Ty=60 hs;		· (Il slots on the same except for the roof 1
es possible giver the remount of information  · Coverned by axial forces only  - Beam: · B'x10" (extincted by eye)  · Layout estimated as best as possible  · As needs to be similar to the slab's  · Plesearch  · I'e=3 Ks;  · A15 stul & 1432 stul -> Fy=60Ks;		- Column: . 12" x12" ( estimated by measuring ) & # 3 stirrups
es possible giver the remount of information  · Coverned by axial forces only  - Beam: · B'x10" (extincted by eye)  · Layout estimated as best as possible  · As needs to be similar to the slab's  · Plesearch  · I'e=3 Ks;  · A15 stul & 1432 stul -> Fy=60Ks;		· Column placement & number of columns extended as best
· Boam: · B'x10" (extincted by eye)  · Jayout extincted as hist as passifle  · As needs to be similar to the slab's  · Persearch  · T'e= 3 hs:  · As stul & 1432 stul - > Fy=60hs:		as jossible given the semount of information
Beam: . B'x10" (attracted by eye)  · Jayout estimated as but as passifle  · As needs to be similar to the slab's  · Personah  · t'a= 3 hs:  · As stul & 1432 stul - > Fy=60hs:		· Corporal by axial Louis only
· As needs to be similar to the slab's  · Research · t'e= 3 ks: · As stul & 1432 stul - > Fy=60ks:		- Boom: . 5" × 10" ( attracted by one)
· Perearch · t'e= 3 ks: · Ais stul = 1432 stul - 15 Fy=60ks:	14 1 1 1 1 1	to the that had as willing
· Perearch · t'e= 3 ks: · Ais stul = 1432 stul - 15 Fy=60ks:		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
· t'e= 3 ks; · Ais stul = 1432 stul -> Fy=60hs;		AS needs to be survey to the state 2
· t'e= 3 ks; · Ais stul = 1432 stul -> Fy=60hs;		
· A15 stul = 1432 stul - > Fy=60451	•	Research
	el Valle	· t'e= 3 Ksi
		· A15 stul = 1432 stul - 15 Fy= 60 hsi
	THE G	1 Je go go sans
A		A



	· du = h - core - 0,25	
	= 1,8 - 0,75" - 8,25	
	= 6,8	
	do & day (Snot officient)	
6)	As pri unit width	
	@ intrior support	
	ossum a=1	
J. V. S. B. T. B.	As = Mu = 569 (12) = 0.20 1 in 2	
	\$\frac{1}{2}\ \(\text{O}\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	
	$a = Asfy = 0.001(60) = 0.39 in^2$	
	08572 b 085(3)(12)	
	@ Midsgan ( Satisfactory to use some "a" for other locations)	
	Mu= 1 Wul2 = 20875 (15.67)2 = 3,66 kgt	
	As= 3.66 (12) - 1012 in2	
	$As = \frac{3.66(12)}{0.9(60)(68 - \frac{0.39}{2})} - 0.12 \text{ in}^2$	
	@ Exterior	
	Mu= 1 Wul2 = 20875(15,67)2 = 2,14/hft	
	24 24	
	As-214:17 0072:21	
	As= 2,14.17 - 0.072 in 2	
	71 (80)(8)	
7)	8 > Smin = 00018	
1/	Pro 10012 A - 1 0012 (12) (78) - 1011.2	
	Smin=00018 = As -15 As min-00018 (12) (7,8) = 0,17 in2	
		2

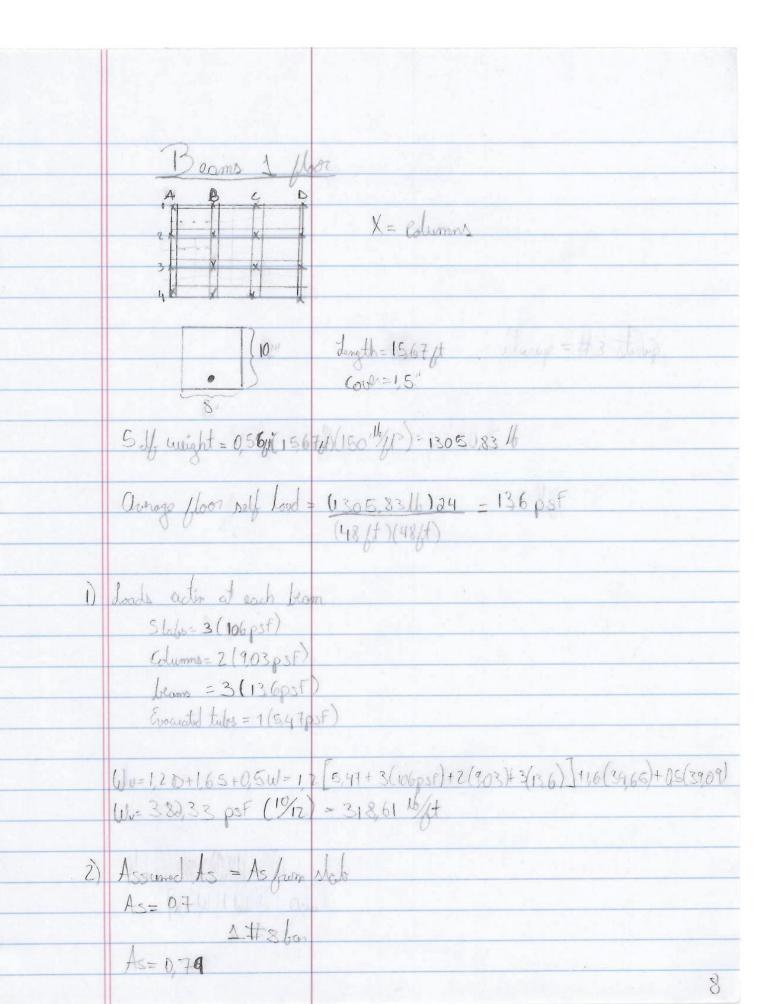
8)	Shan $V_{0}=1.15 \frac{W_{0}L}{2} - W_{0}d = 1.18 \left(\frac{0.20815}{2}.15,67\right) - 0.20875 \left(\frac{6.8}{12}\right)$ $V_{0}=1.76 \text{ Mips}$
	QVC=02 Tre bd=0.75(2)(\frac{\squares 0.000}{1000})(12)(6.8)=6,7 kgs
9)	A. 70136/4 A. 70136/4
	6,5"; As=020:n2
10)	New d  d du = h - cours - holf by Liambs  = 7.8-0.75 - 0.375/2  dds = 6.86" * Doesn't change
11)	actual 8  S=As = 620 [0,0024]  bd 12(6,86)
	$S_{max} > S > S_{min}$
	3

12)	Mn det	
10)	a. Asty = a	70(60) -030"
	0.85166	20(60) = 039" 85(3)(17)
	& Mn= & As fy (d- &	) = 0,9 (60) (0,20) (6,86 - 0,39) =71,9in-kips
	grn=6,0 ng 2M	<i>y</i> √
	7.4	
		4

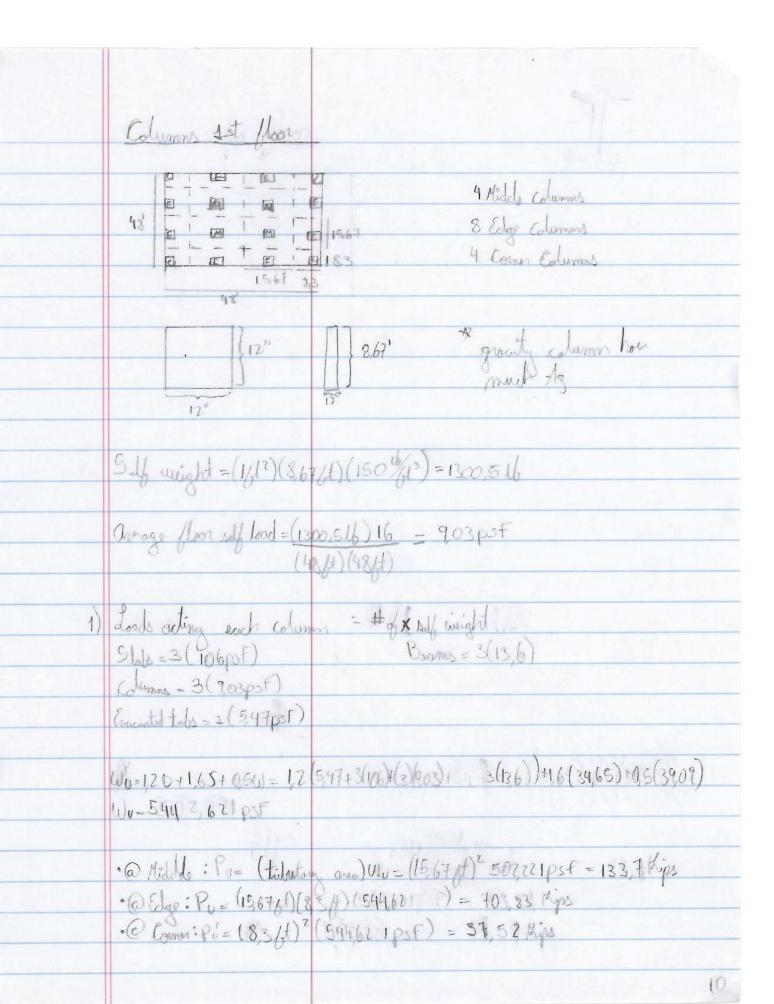
	Slat on 1 st floor: Design for levels 1-3 slate	
	MEP=5psf 4th-2nd Lud Mab=318psf	
	Metal Dech = 35 psf 3rd - 1st level columns = 27,09psf	
	1=1567' h=7x" d=6x"	
	3rd-1st level bears = 40.8	
1)	Fotord lood	
-1./	Self Weight = 106 PSF "including NES & notal Dech	
	Wu= 1,2D +1,65+0,5W	
	W=1,2(106+547+318psf+2769440,8)+1,6(34,65)+\frac{1}{2}(3909)	
	Wo-671,82psf	
	.1	
(2)	Mu:	
	@ Vatrior support: Nv = - = (64.82)(15.672) - 18,33 h./	
-	@ Hidspan: Hu= 19(67, 2) (1567°) = 11,82 h-ft	
	@ Exterior : Ao = = = = (67/2)(19.672) = 697 K-ft	
3)	Smax & Swos	
	· Smar= 0,75 Sb=0,75 (0,85 S, Ty (87+Ty)] = 0,016 · So003= 0.85 S. (Ty) Eu+0005 = 00136	
	· Socos= 085 8. (Fy) Europos = 00136	
4)	dry > d des	
	dry? Mu	
	\$ Secos Fy L (1-059 Secos Fc)	
	dry 2, 5,5" d>dry	
	D	
		5

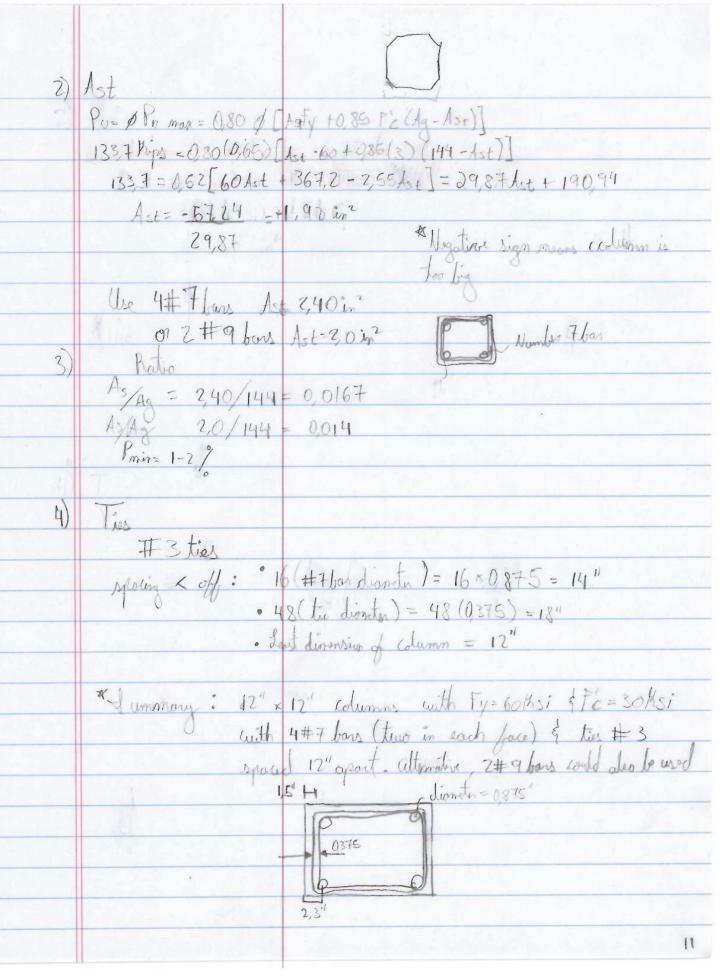
5)	As per unit width	
	@ interior : a=1	
	As= 1833(12) = 0646in2	
	$0.9(60)(68-\frac{1}{2})$	
	a = 0646(60) = 1.27	
	0.85(3)(12)	
	(a) Mideran	
	As= 11 & (12) = 038in2	
	09(60)(68-1,3)	
	(a) Exterior	
	As = 6,97 (12) . 0,25 in <sup>2</sup> 09(60)(68-\frac{13}{2})	
	0,1400,1000 0	
6)	8>8-min = 0,0018	
97	Asmir - 00018 bh = 0.17in	
	7 - 1000 DIL 0,1100	
4)	Shen	
	Vu=1.15(=) Wu1-dWu=45(=)(067182)(1567)-68(=)(067182)	
	Vu= 5,67 K	
	00- 2,01110	
110	PVc= 02 Tre bd	
	PVC= 67 K	
	: Ø Ve >V	
	. • 9 ° C > VI	
1112		
		6
	2021 CP (VXSCZ)(1()	

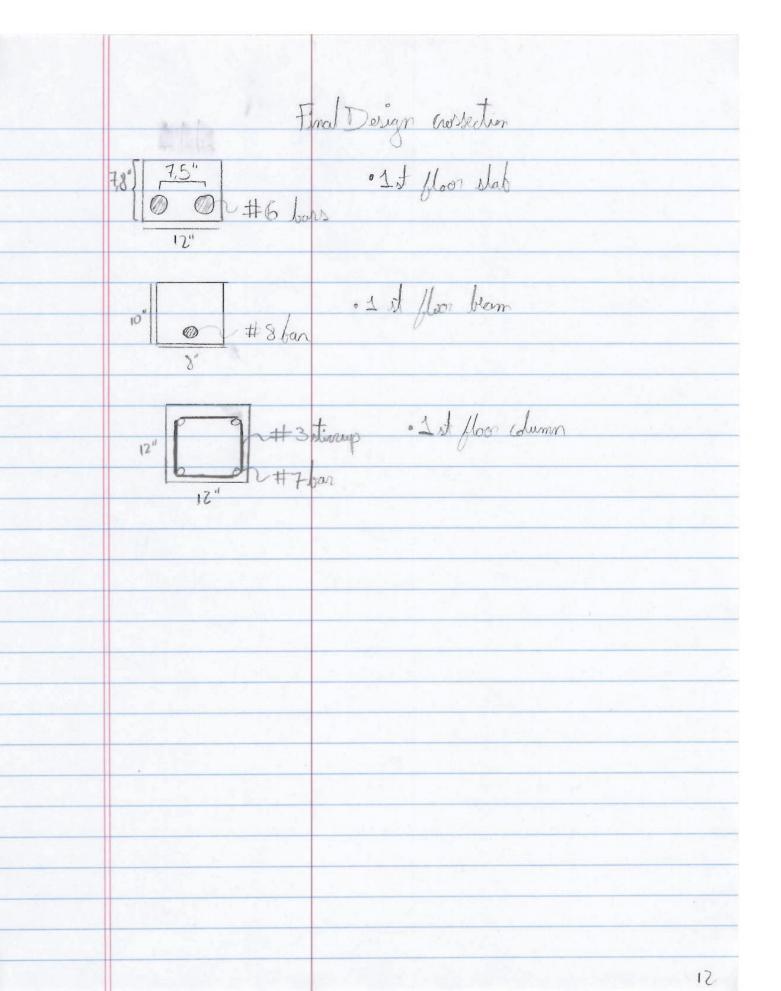
8)	(50) # 6 ban spood every 7,5 inches  As=0,7 in
9)	Actual d
	$d = h - \cos \theta - hd  \text{for dyanter}$ $d = \frac{1}{8} - \frac{0.75}{2} - \frac{0.75}{2}$ $d = 6.67''$
10	Octual 8  S= As = 0.76 in = 0.009!  bd 12in (667)
	Smap > 9 > Smin
10)	gMn cheX $a = Asfy = 0.7(60) = 1.37''$ $985fcL = 0.85(3)(17)$
	ØMn=Ølsty(d-2)=09(076)(60)(66)-637)=226,2 Hip.in ØMn-18,9 Hips.fl > Mu
	7



3)		
	$=10-1.5-1.0/2=8^{\circ}$	
4)	-   a # fs= Fy (P <pb)< th=""><th></th></pb)<>	
1)	a=Asfy = 079 (60) = 2,3"	
	0,85726 0,86(3)(8)	
<b>-</b>		
5)	Et 1/d tons lestoin C= 3/3, = 2, 85= 2,71	
	Et= (de-C) 103= (8-2,3) 0,003+0,0074 ~ 4) of tensil trus	
	Z900000 - 0,0007 7 geld strain in tension	
	Et > Ey Hon Fs-Fy	
	Ø=09	
6)	allowed Homer	
	$\phi_{Mn} = \phi \text{ As fy } (d - \frac{\alpha}{2})$ $= 0.9 (0.71 \text{m}) (60 \text{Msi}) (8" - \frac{33}{2})$	
	$=0.9(0.7h)(60\%si)(8-\frac{1}{2})$	
	= 292,27 Air = 24,3 thips ft > Mu	
7)	No= Wol2 = 318,61 (15,67)2 = 9,78 K. H	
	8 8	_
8	$S = \frac{As}{bcl} = \frac{0.79 \text{ in}^2}{8(8)} = 0.0123$	
2	9	







## **Appendix D.3: Economic Analysis**

	Economic Jeasibility
1-11	The state of the s
	1) Fired cart = Pice of tech + Installation Cost
	= (2080) 31 +1000 +70 (80)
	= 102080
	2) Savings Ren year
	Corner spending = 35 \$ 92 \$ per year
	ted soving = 613.70(31) = 19009 7
3. 75	Et = 0.0003 10 0007 100 1/633 8
	Futur = 35592-190097 +60=16632,8
	Saving por year= 355 92-16632,8= 18959,2
	3) Paybach
	X= Fixedort - 102080 = 5,382 5,4 years Saving per year 18959,7
	(= 102080 = 3,00° 3,4 Geors
	Javias Pen year 18459, 2
114	